# THE EFFECTS OF THE M-CYCLE ON THE PERFORMANCE OF A GAS TURBINE

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#### **ABSTRACT**

The M-Cycle represents one of the best heat recovery technologies known today. Technically, it can be incorporated into the Brayton cycle by replacing the heat recuperator with a recuperator-humidifier and directing high humidity compressed air into the combustion chamber. This provides a large increase in the cycle efficiency due to the reduction of the ambient temperature (from dry bulb to the dew point temperature), a reduction in compressor work, an increase in the volumetric flow, increase in combustion efficiency (increased fuel economy), and a large reduction in NO<sub>x</sub>. These combined improvements provide an improved Brayton cycle efficiency.

By adding steam to the fuel gas stream in the combustion chamber of a Brayton cycle turbine the operating power will increase substantially. Experiments with innovative gas turbine cycles like Evaporative Gas Turbine (EvGT)[1], the Humid Air Turbines (HAT)[2], or the Cascade Humidified Advanced Turbine (CHAT) cycle[3], where instead of steam an equivalent amount of water vapor is created from waste heat from stack gases, and in some cases intercompressor coolers, have shown improvements in efficiency. Using reduced compressor power for the same mass flow rate causes the largest efficiency gain. However, efforts to commercialize these advanced turbine cycles have been stymied by the difficulty in maintaining the air to humidity ratio, and the added capital equipment cost such as the saturating tower, boilers and numerous heat exchangers. The development of the M-Cycle offers a cost-effective solution to these issues by presenting the opportunity to realize the thermodynamic advantages of these high performance cycles [4].

This paper analyzes the performance of the M-Cycle when operating with a Rolls-Royce 250 gas turbine and compares the output to the standard Brayton Cycle while varying the inlet humidity, temperature and air and fuel flow rates.

#### **NOMENCLATURE**

[Btu/lb]

	[ ]	
m	[lb/sec]	Mass Flow Rate
p	[psia]	Pressure
$r_p$	-	Pressure Ratio
ť	[°F]	Dry-bulb Temperature
$t_d$	[°F]	Dew-point Temperature
v	$[ft^3/lbm]$	Specific Volume
C		Constant
P		Pressure
R	$[ft*lb_f/lb_m*^{\circ}R]$	Specific Gas Constant
Subsc	ripts	
1,2	•	Subscripts indicating state
F		Fuel
W	[psia]	Water Vapor Partial Pressure
Ws	[psia]	Saturation Pressure

Enthalpy

## **BACKGROUND**

The M-Cycle [5] applied to gas turbines is a three step process. After the compressor, the hot, compressed gas enters the M-Cycle heat exchanger and is divided into many small channels in a plate and frame arrangement. The hot gas travels the length of the exchanger, losing heat through the plates to the wet side. The gas is cooled down to the dew-point of the gas at that pressure. The second step has the gas passing through the wet side channels. The heat from the incoming gas, as well as the heat from the exhaust gas heats the liquid water and produces steam. This steam adds mass flow and energy to the gas stream and it exits the exchanger for the combustion chamber. The third step comes after expansion, as the hot exhaust gas passes through the exchanger to boil water for the entering gas stream. The M-Cycle details are outlined in the section below.

#### **PSYCHROMETRICS**

Psychometrics in this report are based on the ASHRAE 1992 Fundamentals book. The equations are processed into a spreadsheet and analyzed based on each point in the Brayton cycle and are presented here as a reference for the later discussion of the M-Cycle.

## **Psychrometric Equations**

Saturation Pressure given over liquid water:

$$\ln(p_{ws}) = \frac{c_8}{T} + C_9 + C_{10}T + C_{11}T^2 + C_{12}T^3 + C_{13}\ln T \quad (1)$$

Where:  $C_8 = -1.0440397E+04$ 

 $C_9 = -1.1294650E + 01$ 

 $C_{10} = -2.7022355E-02$ 

 $C_{11} = 1.2890.360E-05$ 

 $C_{12} = -2.4780681E-09$ 

 $C_{13} = 6.5459673E+00$ 

Humidity Ratio is given by:

$$W = 0.62198 \frac{p_W}{p - p_W} \quad (2)$$

Enthalpy of the mixture is given by:

$$h = 0.240t + W(1061 + 0.444t)$$
 (3)

Where the first term represents the enthalpy of the dry air, the second represents the enthalpy of the saturated water vapor.

Dew Point is given by:

$$t_d = C_{14} + C_{15}\alpha + C_{16}\alpha^2 + C_{17}\alpha^3 + C_{18}(p_w)^{0.1984}$$
 (4)  
Where:  $C_{14} = 100.45$   $C_{15} = 33.193$   $C_{16} = 2.319$ 

 $C_{17} = 0.17074$ 

 $C_{18} = 1.2063$ 

### **PSYCHROMETRIC CHARTS**

The Psychrometric Charts provide the user with a quick way to determine property states of a given air-vapor mixture given any two conditions. An example chart is given in the following for condition of 1 atmosphere.

The graph layout is given with dry bulb temperature (°F) versus humidity ratio given in pounds of water vapor per pound of dry air. The curved lines represent lines of relative humidity, given in 10% increments. The diagonal lines are lines of constant enthalpy given in Btu per pound.

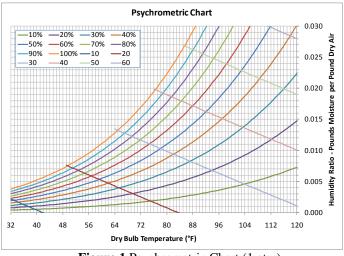


Figure 1 Psychrometric Chart (1 atm)

#### **BRAYTON CYCLE**

The Brayton Cycle is the fundamental thermodynamics cycle for modeling the performance of gas turbines. The combustion occurs at a constant pressure state, and the inlet and exhaust are at the same pressures. Again, as a reference for the understanding of the M-Cycle, the Brayton Cycle is described in four steps, as shown below:

### **Process 1-2: Isentropic Compression**

The equations relating these two states can be seen below. This assumes a given pressure ratio, humidity ratio, standard atmospheric conditions at inlet, and air and water vapor as an ideal gas.

$$\begin{split} \dot{m}_1 &= \dot{m}_2 \ \, (5) \\ P_2 &= P_1 * r_p \ \, (6) \\ v_2 &= v_1/r_p^{\left(\frac{1}{\gamma-1}\right)} \ \, (7) \\ T_2 &= \frac{P_1 v_1}{R} \ \, (8) \\ h_2 &= 0.240 T_2 + W (1061 + 0.444 T_2) \ \, (9) \end{split}$$

## **Process 2-3: Isobaric Combustion**

In the next step, the mass of the fuel adds to the total mixture, the pressure is stable, and the energy of the burned fuel is added to the enthalpy exiting the combustor.

$$\dot{m}_3 = \dot{m}_2 + \dot{m}_f \quad (10)$$

$$P_3 = P_2 \quad (11)$$

$$v_3 = v_2 \quad (12)$$

$$T_3 = T_2 + \frac{h_3 - h_2}{c_p} \quad (13)$$

$$h_3 = h_2 + \frac{\dot{m}_f Q_{LHV}}{\dot{m}_3} \quad (14)$$

## **Process 3-4: Isentropic Expansion**

The hot gas passes from the combustion chamber and expands through the power turbine.

$$\dot{m}_4 = \dot{m}_3 \quad (15)$$

$$P_4 = P_1 \quad (16)$$

$$v_4 = \frac{RT_4}{P_4} \quad (17)$$

$$T_4 = T_3/r_p^{(\frac{V-1}{\gamma})} \quad (18)$$

$$h_4 = 0.240T_4 + W(1061 + 0.444T_4) \quad (19)$$

## **Process 4-1: Isobaric Heat Rejection**

This is not an actual process, since the Brayton cycle is an open cycle. The exhaust gases are dumped to atmosphere while the fresh air begins the cycle again. Several processes, including the M-Cycle, rely on this "waste" heat for higher efficiencies in their modified cycles.

The figure below demonstrates the basic Brayton cycle on a P-v and T-s diagram.

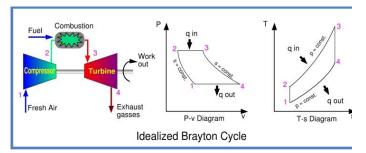


Figure 2 Basic Brayton Cycle

## M- CYCLE

The M-Cycle is a modification of the state of the gas after compression to before combustion. The diagram below shows the flow path of the compressed gas as it flows from compressor to combustor. The gas passes through the dry side of the heat exchanger, then to the wet side, causing the flow to cool to saturation and then adding energy from the steam. The exhaust gas stream adds more energy to the incoming flow, as it passes heat through the liquid water in the exchanger.

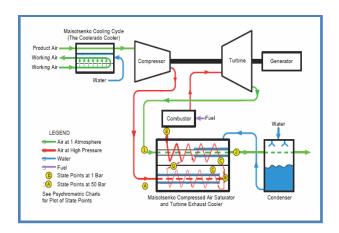


Figure 3 M-Cycle Diagram

# M-Cycle Illustration on a Psychrometric Chart

The M-Cycle is described in three steps:

State A to B: Cooling of the flow down to the dew point

State C to D: Addition of saturated water vapor

State C to E: Heating of the combined Gas Stream

This can be shown on a Psychrometric chart as follows: (example at 7 atm compression)

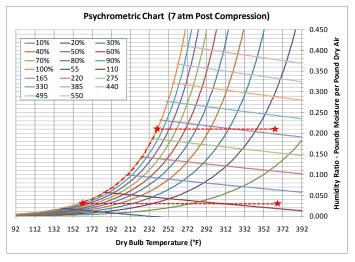


Figure 4 Compressor Psychrometric Chart

## **M-Cycle Equations**

To solve for the M-Cycle states, we assume any extra energy is transferred at 100% efficiency and compare it to the unmodified cycle.

**State A to B:** Cooling of the compressed flow down to the dew point.

To calculate this temperature, we use the saturated vapor line at the specific humidity ratio coming into the cycle. The enthalpy difference is assumed to be transferred into the water on the wet side of the exchanger.

# State C to D: Addition of Saturated Water Vapor

By using an iterative process, the heat from the inlet stream and exhaust stream is used to transfer liquid water into steam. This mass flow is added to the gas stream.

## State C to E: Heating of Gas Stream

Using the last of the energy, the stream is heated back to near the original value of the inlet cycle. The iterative steps assume temperatures at D and E, then seek agreement at the end of the cycle by exhaust heat return.

**ROLLS ROYCE ALLISON 250** The following spreadsheets outline the effects of the M-Cycl on a given gas turbine.

The **BASIC BRAYTON CYCLE** gives the basic operating parameters of the cycle. The data presented is for the operation of the Allison 250 using the Brayton Cycle.

#### **BASIC BRAYTON CYCLE**

Constants			State 3 - Combustion			
R	53.353	lbf*ft/lbm-*R	T3	972	"F	
Ratio Specific Heats	1.3		P3	102.872	psia	
Pressure Ratio	7		Humidity Ratio	0.0086%		
Compression Ratio	4.468		Mass Flow	3.600	lb/sec	
Fuel Flow	0.05	lb/sec	v3A	3.500	ft^3/1b	
Fuel LHV	18300	Btu/lb	Saturation Pressure	12594	psia	
c p @ 2000°F	0.410	Btu/Ib-*F	w	0.006604	lb water/lb dryair	
			Dew Point	710.490	"F	
			Enthalpy	346.1	Btu/lb	
State 1	- Compress	oriniet		State 4 - Turbine Exhaus	:	
T1	60	*F	T4	454	"F	
P1	14.696	psia	P4	14.696	psia	
Humidity Ratio	60%		Humidity Ratio	0.0351%		
Inlet Mass Flow	3.55	lb/sec	Mass Flow	3.600	lb/sec	
v1	13.102	ft^3/lb	v3A	11.444	ft^3/1b	
Saturation Pressure	0.25634	psia	Saturation Pressure	440	psia	
W	0.006604	lb water / lb dry air	W	0.006604	lb water/lb dryair	
Dew Point	46.150	*F	Dew Point	390.798	*F	
Enthalpy	21.583	Btu/lb	Enthalpy	117.277	Btu/lb	
				*****		
T2	- Compresso	r Outlet	Thermal Efficiency	36.13%		
P2	355					
	102.872 0.7527%	psia	- 8	ficiency: 1-(T4-T1)/T3-T	2)	
Humidity Ratio	3.55					
Mass Flow		lb/sec	D	224.45	kW	
	2.933	ft^3/lb	PowerOutput	231.15	kW	
Saturation Pressure W	143.605	psia				
	0.006604	Ib water / Ib dry air	Power Output	Power Output 0.87*m3*(T3-T4)-m2*(T2-T1)/0.78/0.81		
Dew Point	207.356	*F				
Enthalpy	93.248	Btu/lb				

# **EXAMPLE 1: M-CYCLE EXAMPLE (IDENTICAL FUEL FLOW RATE)**

State 2A - M-Cycle Cooling			State 3 - Combustion		
T2A	103	°F	T3 972 °F		
P2A	102.872	psia	P3 102.872 psia		
Humidity Ratio	0.7527%		Humidity Ratio 0.3465%		
Mass Flow	2.92875	lb/sec	Mass Flow 3.607 lb/sec		
v2A	2.027	ft^3/lb	v3 6.760 ft^3/lb		
Saturation Pressure	1.040	psia	Saturation Pressure 7740 psia		
W	0.006604	lb water / lbdry air	W 0.219 Ib water / Ib dryai		
Dew Point	86.379	*F	DewPoint 655.250 °F		
Enthalpy	32.0293	Btu/lb	Enthalpy 612.7 Btu/lb		
Mass Flow Modifier	0.8250		FuelTotal 117.8%		
State2B - M-Cycle Saturation			State 4 - Turbine Expansion		
T2B*	242	°F	T4 454 °F		
P2B	102.872	psia	P4 14.696 psia		
Humidity Ratio	100%		Humidity Ratio 1.8038%		
Mass Flow	3.548	lb/sec	Mass Flow 3.607 lb/sec		
v3B	2.527	ft^3/lb	v4 22.107 ft^3/lb		
Saturation Pressure	25.903	psia	SaturationPressure 212 psia		
W	0.219	lb water / lbdry air	W 0.219 Ib water / Ib dryai		
Dew Point	214.576	°F	DewPoint 338.455 °F		
Enthalpy	314.335	Btu/lb	Enthalpy 385.931 Btu/lb		
	State 2E - M-Cycle Heating		ThermalEfficiency 57.09%		
T2E**	256	*F			
	Energy Balance (100% Transfer T4-T1)				
Exhaust Heat Remain 194.22 Btu/lb			Efficiency: [(h3-h4)-(h2-h1)]/(h3-h2)		
Vapor h at T2B	1140.378	Btu/lb			
Vapor Mass Rate	0.619	lb/sec	PowerOutput 400.25 kW		
Energy Left	-1.473	Btu/lb			
W	0.219	lb water / lbdry air	Power Output: 0.87*m3*(h3-h4)-m2*(h2-h1)/0.78/0.81		
Dew Point	227.130	*F			
Enthalpy	319.059	Btu/lb			

# EXAMPLE 2: M-CYCLE EXAMPLE (IDENTICAL AIR FLOW RATE)

	State 2A - M-Cycle Cooling		St	ate 3 - Combust	ion	
T2A	103	*F	T3	867	*F	
P2A	102.872	psia	P3	102.872	psia	
Humidity Ratio	0.7527%		Humidity Ratio	0.2996%		
Mass Flow	3.55	lb/sec	Mass Flow	4.215	lb/sec	
v2A	2.027	ft^3/lb	v3	6.026	ft^3/lb	
Saturation Pressure	1.040	psia	Saturation Pressure	7740	psia	
w	0.006604	lb water / lb dry air	W	0.181	lb water / lb dry a	
Dew Point	86.379	*F	Dew Point	655.250	*F	
Enthalpy	32.0293	Btu/lb	Enthalpy	516.4	Btu/lb	
Mass Flow Modifier	1.0000		Fuel Total	100.0%		
	State2B - M-Cycle Saturation			4 - Turbine Expa		
T2B*	234	*F	T4	387	*F	
P2B	102.872	psia	P4	14.696	psia	
Humidity Ratio	100%		Humidity Ratio	1.5597%		
Mass Flow	4.165	lb/sec	Mass Flow	4.215	lb/sec	
v3B	2.498	ft^3/lb	ν4	18.829	ft^3/lb	
Saturation Pressure	22.397	psia	Saturation Pressure	212	psia	
W	0.181	lb water / lb dry air	W	0.181	lb water / lb dry a	
Dew Point	207.356	*F	Dew Point	338.455	*F	
Enthalpy	266.997	Btu/lb	Enthalpy	315.967	Btu/lb	
	State 2E - M-Cycle Heating		Thermal Efficiency	60.30%		
T2E**	346	*F				
	Energy Balance (100% Transfer T4-T1)		Efficiency: I	Efficiency: [(h3-h4)-(h2-h1)]/(h3-h2)		
Exhaust Heat Remain	165.93	Btu/lb	Efficiency.	Emclency. [(113-114)-(112-111)]/(113-112)		
Vapor hat T2B	1136.826	Btu/lb				
Vapor Mass Rate	0.615	lb/sec	Power Output	350.48	kW	
Energy Left	0.058	Btu/lb				
w	0.181	lb water / lb dry air	Power Output: 0.87*m3*(h3-h4)-m2*(h2-h1)/0.78/0.81			
Dew Point	304.967	*F				
Enthalpy	302.877	Btu/lb				

#### DISCUSSION

The **FIRST EXAMPLE** shows the M-Cycle with the fuel flow rates the same as in the Basic Brayton Cycle. This results in an increase in efficiency of 36.7% and a 42.2% increase in power over the Basic Brayton Cycle. These improvements result because of improved heat exchange process in the M-Cycle heat exchanger, lower compressor exit temperature (increase in compressor efficiency), and the lowering of the turbine exhaust temperature (larger expansion ratio).

The **SECOND EXAMPLE** shows the M-Cycle with identical inlet air flow rates compared to the Basic Brayton Cycle. This results in an increase in efficiency of 40% and an increase in power output of 34%. The increase in power results because of the increase in fuel flow, but the increase in efficiency results because of the better utilization of the heat transfer in the M-Cycle exchanger, and the lower compressor operating temperature.

#### **CONCLUSIONS**

The M-Cycle could be used for many applications in the power industry to increase the overall system efficiencies. There are several modes of operation of the cycle that can be considered. There are two evaluated in this paper, but several other are being evaluated and will be discussed in a later paper.

The Constant Air Flow (CAF) and the Constant Fuel Flow (CFF) modes of operation offer insight into the operating characteristics of the M-Cycle coupled to a gas turbine. Optimization techniques have been used to determine the most efficient operating points for the turbine-M-Cycle combination. In the CAF mode of operation, the combined system efficiency was 60.3%. This is a significant improvement over conventional gas turbine efficiencies. In the CFF mode of operation, the combined system efficiency was 57%.

The flexibility of the M-Cycle for use with gas turbines can be found in performance improving applications, such as, to cool compressor intercoolers, to saturate the compressed air while reducing the temperature of the exhaust gases toward the dew point temperature of the compressed air, and to saturate the fuel with water vapor while further cooling the turbine exhaust gases.

The M-Cycle is a thermodynamic development for energy recovery, which utilizes the an efficient heat (enthalpy) recovery process for any combustion engine. It is possible to significantly increase the thermal efficiency for the turbine (> 50%). The gas turbine, using humidified compressed air through the M-Cycle, becomes less than half the size of a standard turbine to generate the same amount of power. This is possible because much more of the power produced by the turbine goes to the drive train rather than to compress air as in a standard turbine because of the lower cycle operating temperatures. In addition and because of the higher efficiency in this M-Cycle turbine, pollution is dramatically reduced due to the water vapor creating a more even burning process during combustion. Additional water will not be needed because the

M-Cycle heat exchanger constantly recycles water in the exhaust gas.

The new M-Cycle gas turbine could provide the following improvements to a gas turbine sytem:

- 1. Approximately double fuel efficiency compared to a simple gas turbine.
- 2. Reduce the CO<sub>2</sub> by approx.half
- 3. Could reduce NOx related pollution by up to 90% (no hot spots).
- 4. Could reduce the size of the gas turbine by approx. half for the same usable shaft power out.
- 5. Require a recuperative plate heat exchanger.
- 6. Require an air-cooled condenser.
- 7. Creates a much wider power band.

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