

# Improvement of the energy and exergy efficiencies of the parabolic solar collector equipped with a twisted turbulator using SWCNT-Cu/water two-phase hybrid nanofluid

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## ABSTRACT

In the present numerical study, the effect of twisted turbulator on the improvement of energy and exergy efficiencies and hydraulic performance of SWCNT-Cu/water hybrid nanofluid in a solar collector is evaluated using computational fluid dynamics and ANSYS-FLUENT software. In this study, SOLIDWORKS software is employed to draw the geometry of the solar collector. Since the fluid flow in the solar collector is turbulent, the SST  $k-\omega$  turbulence model is used. In addition, a mixed two-phase model is employed to model the hybrid nanofluid. The study is performed for Reynolds numbers (Re) in the range of 9000 to 36000, volume fractions ( $\varphi$ ) of 1 to 3%, and turbulator pitch ratios (PR) of 1, 2, 3, and 4. It can be concluded that the average Nusselt number and the pressure drop are ascending functions of  $\varphi$  and Re. Also, the amount of pressure drop and the average Nusselt number is enhanced with the PR. At  $\varphi = 3\%$  and  $Re = 36,000$ , the twisted turbulator with  $PR = 4$  intensifies the average Nusselt number by 74.95% compared to the solar collector without turbulator. At  $\varphi = 3\%$  and  $Re = 36,000$ , the twisted turbulator with  $PR = 4$  enhances the pressure drop by 429.31% compared to the solar collector without turbulator. In a solar collector with a twisted turbulator with  $PR = 4$  and  $\varphi = 3\%$ , the amount of energy efficiency is enhanced by 41.75% by enhancing the Re from 9000 to 36000. In a solar collector with a turbulator with  $PR = 1$  and  $\varphi = 3\%$ , the amount of exergy efficiency is enhanced by 33.09% by intensifying the Re from 9000 to 36000.

## Introduction

Today, the optimal use of energy [1–7], especially renewable energy [8–10], is an important issue due to the energy management demand [11,12,53] and increasing energy consumption. Improvement of the solar collector (SC) performance can be helpful in encouraging people to use them. In recent decades, several methods have been developed to improve heat transfer in various systems, such as microchannel [13–15],

and many researchers have used these methods to improve their performance and enhance their efficiency. According to open literature, nanofluids may enhance heat transfer [16–23,55] because of their superior thermal properties to the base fluids [24–30,54,56]. Hong et al. [31] numerically examined the impact of water-copper nanofluid on the thermal performance of a parabolic SC using the finite volume method and FLUENT software. They used SOLIDWORKS software to design the geometry of PSC. They also used the SIMPLE algorithm to discretize the

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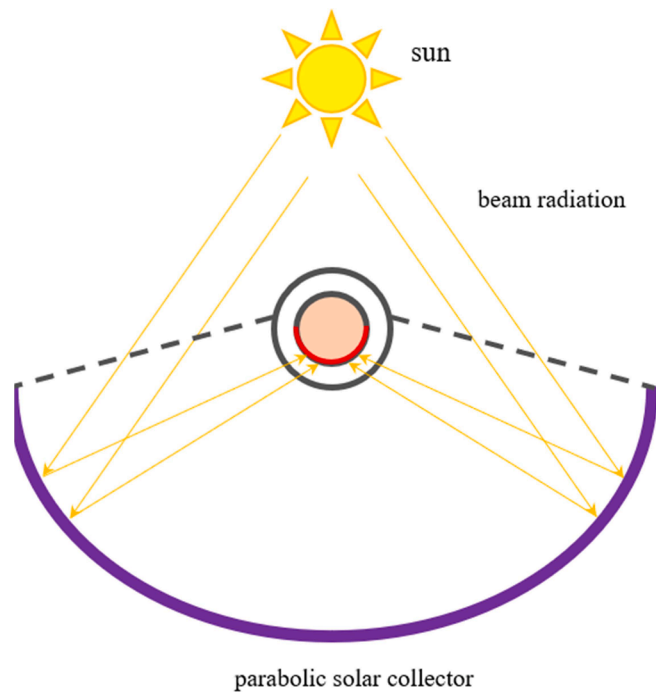


Fig. 1. Schematic of SC.

governing equations. The results demonstrated that the use of water-copper nanofluid significantly improves PSC effectiveness. Also, the thermal performance of SC is enhanced significantly by intensifying the  $\phi$ .

Alimoradi et al. [32] inspected SC thermal response in the presence of turbulent channel under constant heat flux experimentally and numerically using FLUENT software for numerical simulations. They

employed modeler design software to design the geometry. Based on the results reported by the authors, the experimental and numerical data were in good agreement with each other. An increment in the Re and the PR of the twisted turbulator (TT) resulted in an improvement in heat transfer. In addition, the use of holes in TTs enhances heat transfer and reduces pressure drop in the cavity.

Dezfulzadeh et al. [33] used the finite volume method and FLUENT

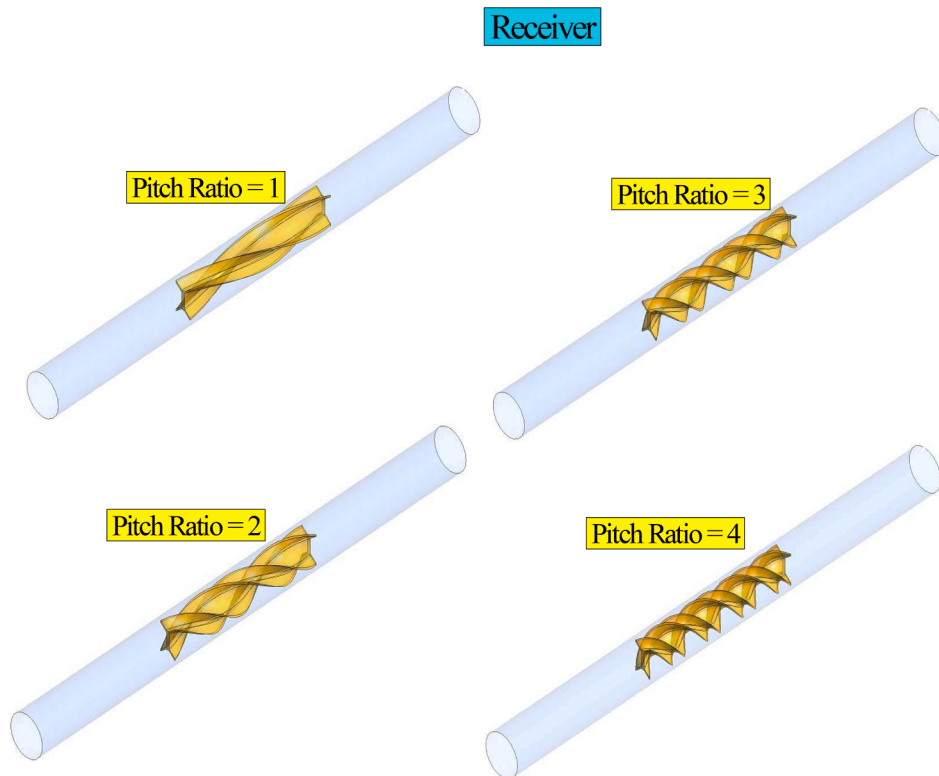
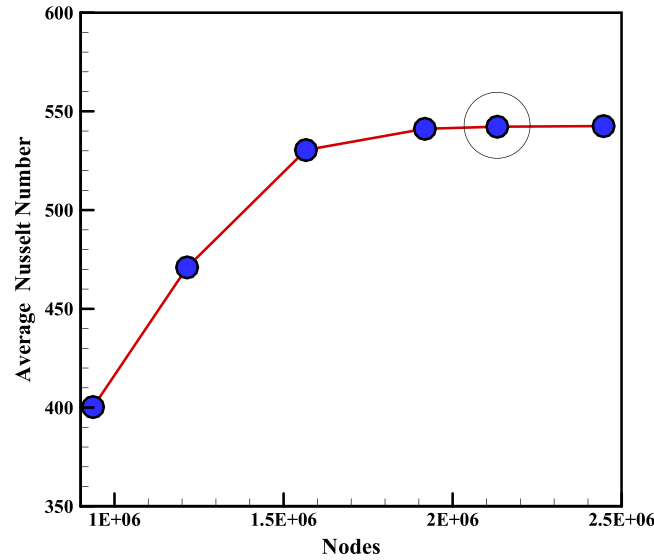


Fig. 2. Schematic of the receiver tube equipped with a TT with different values of PR.

**Table 1**

Thermophysical properties of base fluid and nanoparticles (298 K) [33,47].

Property	Water	Cu	SWCNT
$\rho(\text{kg.m}^{-3})$	998.2	8954	1047
$c_p(\text{J.kg}^{-1}.K^{-1})$	4182	383	3428
$k(\text{W.m}^{-1}.K^{-1})$	0.6	400	0.6833
$\mu(\text{kg.m}^{-1}.s^{-1})$	0.001003	-	-

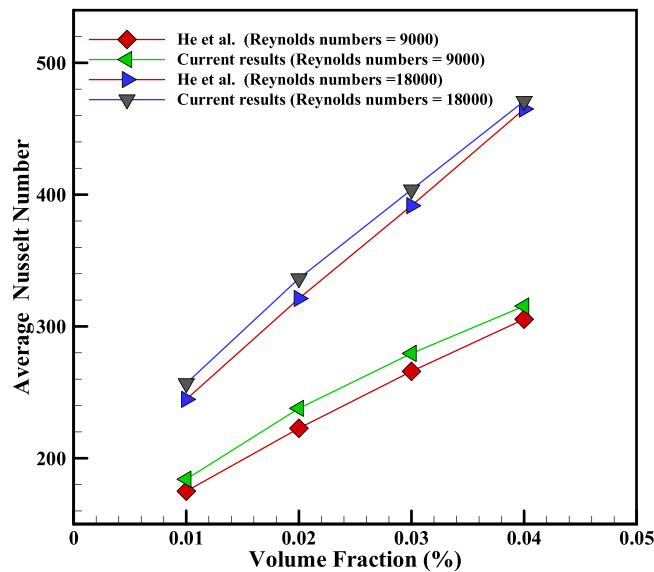
**Fig. 3.** Grid independence results in terms of the  $\overline{Nu}$  for SWCNT-Cu/water two-phase hybrid nanofluid in SC with TT for  $Re = 36000$ ,  $\phi = 3\%$ , and  $PR = 4$ .

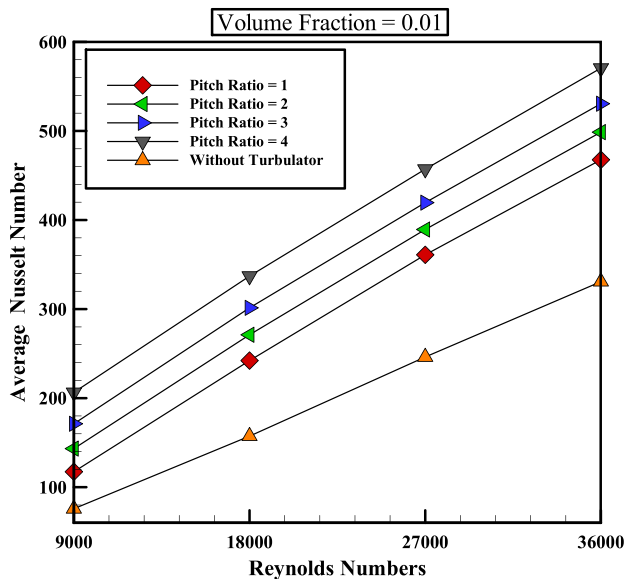
software to examine the effect of grooved turbulators under the influence of a magnetic field on the exergy efficiency of a heat exchanger. They used a hybrid nanofluid combined with three nanoparticles and demonstrated that the exergy efficiency is enhanced by enhancing the  $\phi$  and  $Re$ .

Wu et al. [34] numerically examined the effect of absorbent tubes

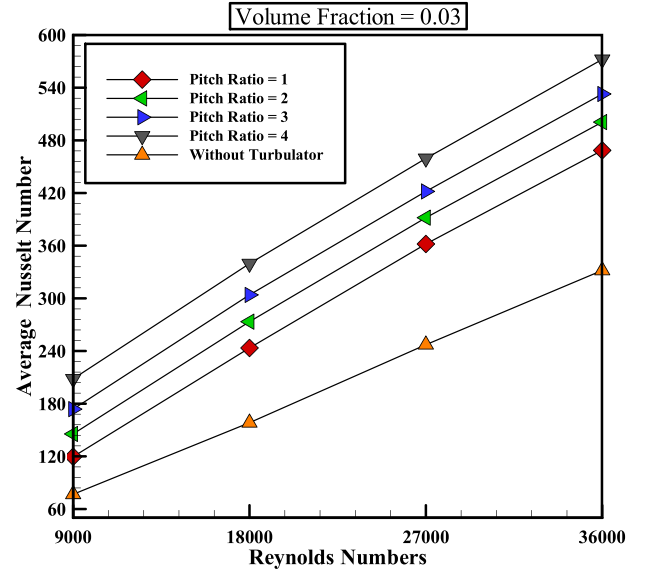
and different directions within the parabolic SC using the finite volume method and FLUENT software. They employed the SIMPLE algorithm to discretize the equations. It was found that the use of absorber tubes with a slope of  $3^\circ$  leads to the maximum thermal performance of the parabolic solar collector (PSC).

Ebrahimipour and Sheikholeslami [35] numerically studied the effect

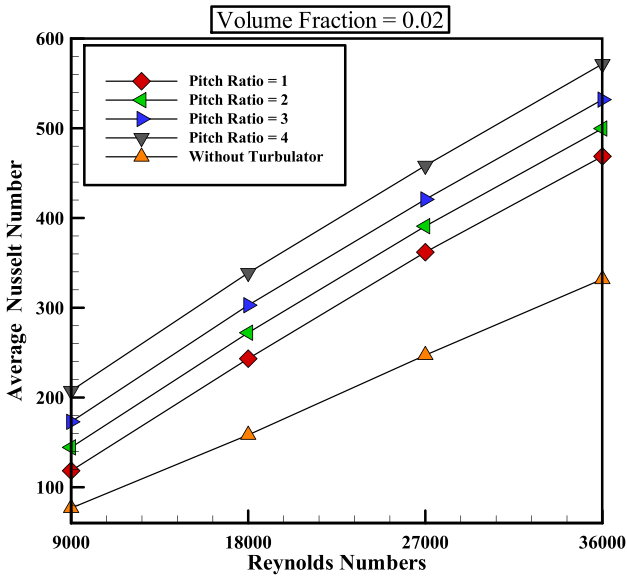
**Fig. 4.** Validation of the present numerical simulation with the results of He et al. [52]



(a)



(c)



(b)

Fig. 5. The  $\overline{Nu}$  versus Re in a SC equipped with a TT with different values of PR for (a)  $\phi = 1\%$ , (b)  $\phi = 2\%$ , and (c)  $\phi = 3\%$ .

of different angles of a SC mirror filled with nanofluid. They also used the finite volume method and FLUENT software for the simulations. The results revealed that an increment in the angle of the SC mirrors and an enhancement in the Re intensify SC thermal response. The SC usefulness was improved up to 65.23% by changing the angle of the mirrors.

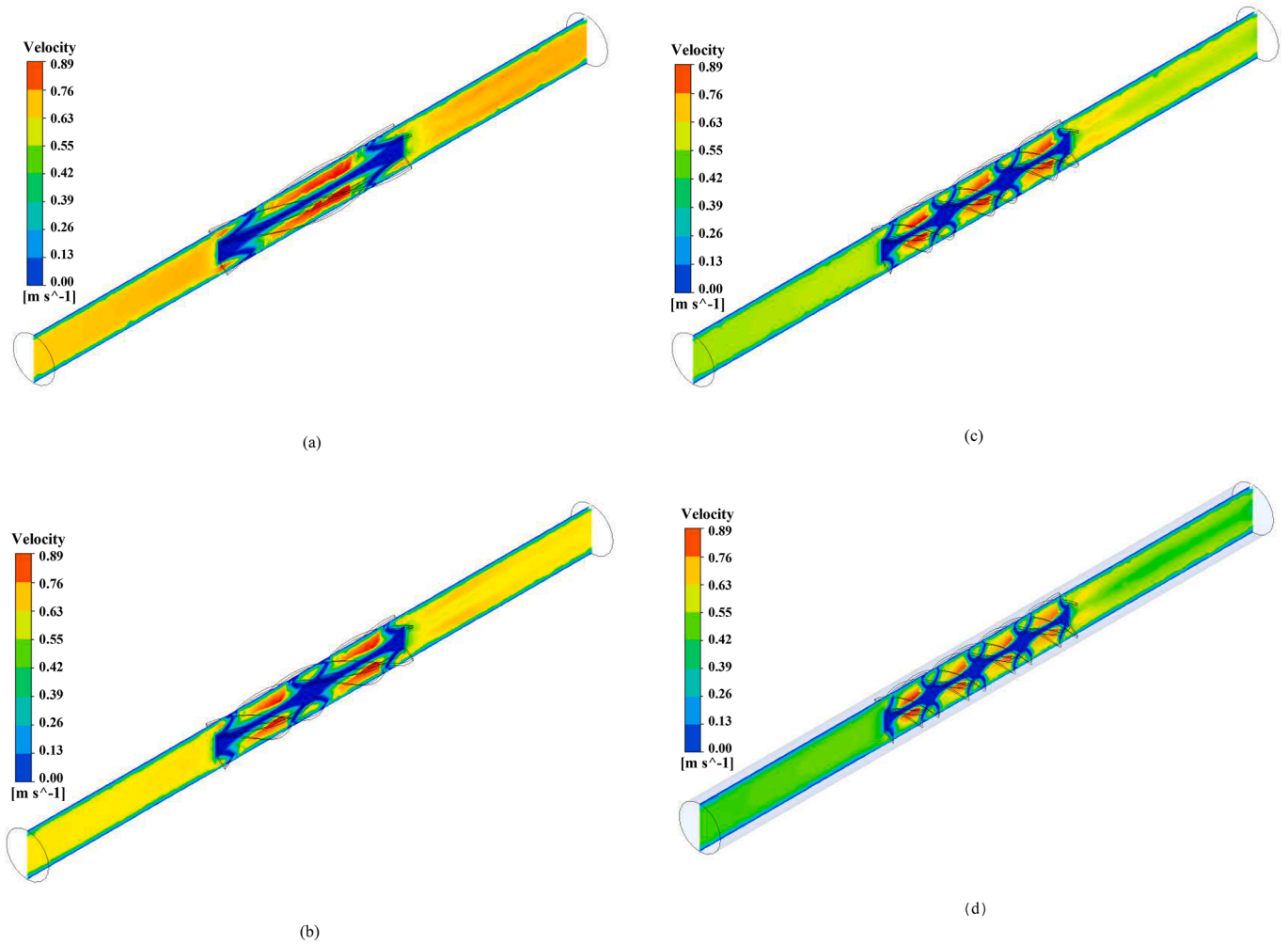
The exergy analysis was also used in many studies [36,37]. Nazir et al. [38] investigated the effect of  $Al_2O_3$ /water on the exergy and energy efficiency of a SC in a laminar flow regime. They also evaluated the effect of  $\phi$  and demonstrated that there is a linear relationship between exergy and energy efficiency with the  $\phi$  so that the exergy and energy efficiency is improved with the  $\phi$ .

Akbarzadeh and Valipour [39] inspected the first/second laws sensitivity to helical turbulator using the finite volume method and ANSYS FLUENT software. They focused on the effect of different values

of PR in the helical turbulator on the energy and exergy efficiencies of the SC. It was found that the use of a helical turbulator significantly enhances the exergy and energy efficiency compared to a simple SC. In addition, the exergy efficiency was reduced with the PR.

Ma et al. [40] inspected TTs efficacy in the space between a cylinder filled with copper/water-EG. The flow regime was turbulent, and the  $k-\epsilon$  turbulence was employed along with SIMPLE approaches. According to the results reported by the authors, due to the nanofluid flow through the twisted tubes, the disturbance is generated in the viscous sublayer, resulting in an enhancement in the average Nusselt number ( $\overline{Nu}$ ).

Chang et al. [41] investigated the effect of twisted tapes on the thermal performance of PSCs. Their study was performed for different values of Re 7000 to 30,000 in. They used the standard  $k-\epsilon$  turbulence.



**Fig. 6.** 6. Velocity contours for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a) PR = 1, (b) PR = 2, (c) PR = 3, and (d) PR = 4.

Their results demonstrated that placing the twisted tape and enhancing its PR results in an improvement in heat transfer (HT) in the PSC. Also, the maximum HT rate in the PSC was improved by 187.90% at  $Re = 30,000$ .

Mashayekhi et al. [42] used the finite volume method and FLUENT software to evaluate the effect of different values of PR of spiral turbulator on thermal-hydraulic performance (THP) of two-phase water-silver nanofluid in a channel. They considered  $\phi =$  zero to 4% and the different values of PR of the helical turbulator in the range of  $Re$  from 100 to 1500. It can be concluded that the placement of the helical turbulator and enhancement of its pitch ratio enhances the THP of the channel. In addition, the amount of HT is enhanced with the  $\phi$  in a water/silver nanofluid.

Siavashi et al. [43] inspected the THP sensitivity of two-phase water-aluminum nanofluid in a channel by utilizing  $k-\omega$  turbulence two-phase model. The results revealed that the placement of porous ribs and an increment in their height have a significant effect on enhancing the rate of HT. Also, the use of two-phase water-aluminum oxide nanofluid experienced better THP than water-based fluid.

Goldanlou et al. [44] examined PSC effectiveness filled with hybrid nanofluid using the finite volume method and FLUENT software. They used design modeler software to model the geometry of the PSC. They employed the  $k-\epsilon$  turbulence model for their simulations. It was shown that the use of a hybrid nanofluid improves the thermal performance of the PSC compared to the base fluid.

Abbasi Varzaneh et al. [45] employed computational fluid dynamics to examine the effect of rib height on the THP of water/aluminum oxide

nanofluid in a heat exchanger. The aim of this study was to investigate the impact of different heights of triangular ribs in the turbulent flow regime at  $Re = 5000-20,000$ . They demonstrated that an increment in the height of the triangular ribs enhances the  $\overline{Nu}$  and reduces the pressure drop. In addition, the maximum improvement of 67.21% in thermal performance of the heat exchanger corresponded to the rib with a height of 12 mm and  $Re = 20,000$ .

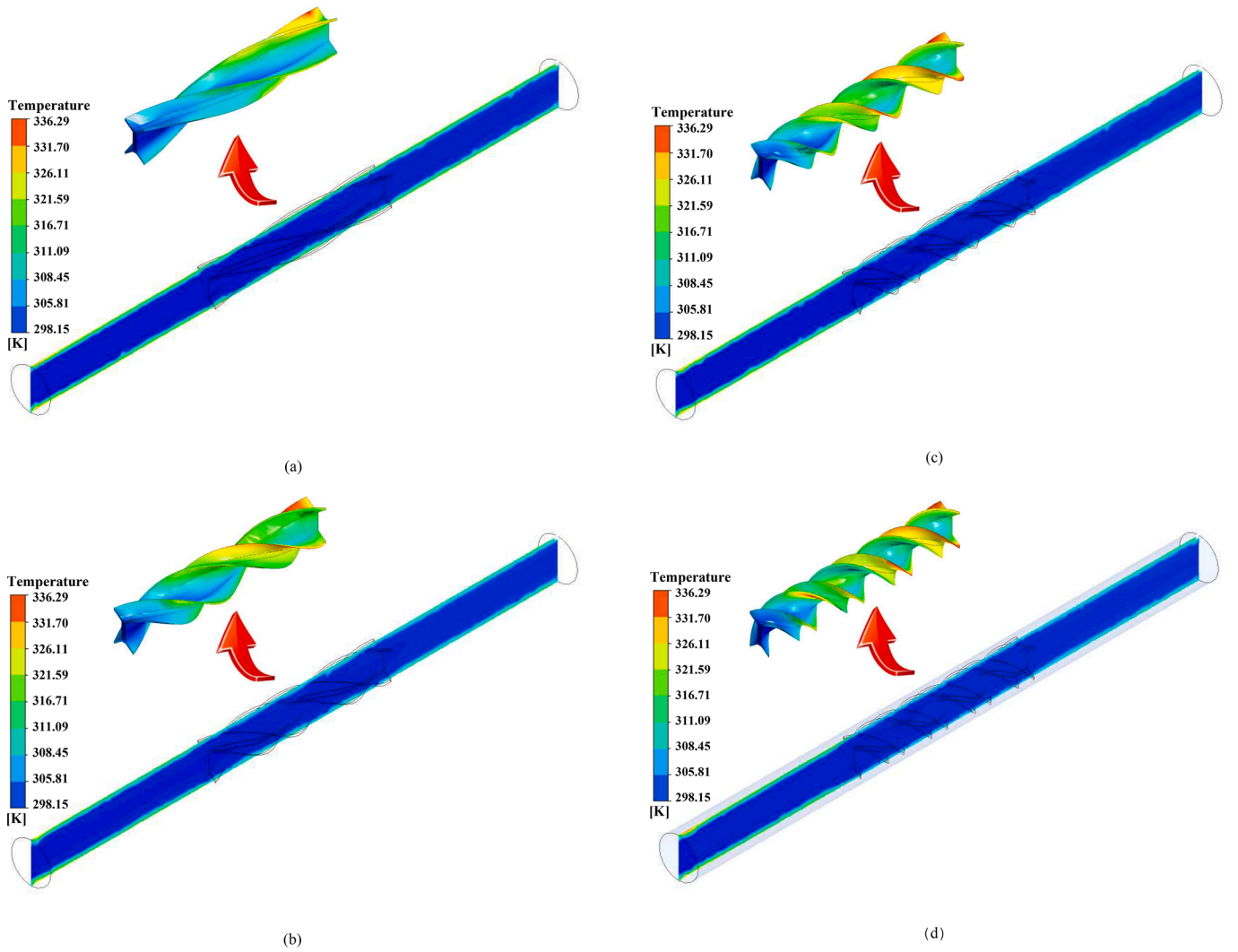
Rostami et al. [46] added elliptical tubes to a SC filled with nanofluid. They used water/multi-walled carbon nanotubes as working fluid. They inspected the impact of the  $\phi$  and  $Re$  on SC performance. The authors showed that the exergy efficiency is an ascending function with  $Re$  and  $\phi$ .

According to the studies performed so far, the effect of a TT on THP, exergy and energy efficiency of two-phase SWCNT-Cu/water hybrid nanofluid inside a SC was not examined. Hence, in this numerical study, the effect of two-phase SWCNT-Cu/water hybrid nanofluid at  $\phi = 1$  to 3%,  $Re = 9000-36000$ , and PR = 1, 2, 3, and 4 are examined. The use of new geometry in turbulator design is the most important innovation of this study. On the other hand, the use of polymer hybrid nanofluids in parabolic collectors is another innovation of this research.

### Geometric model and formulation

The geometry of the SC is shown schematically in Fig. 1.

Figure 2 illustrates a schematic of a receiver tube equipped with a TT at different values of PR. The length of the absorber tube is 900 mm and the length of the TT is 350 mm. Also, the distance between the turbulator



**Fig. 7.** Temperature contours for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a) PR = 1, (b) PR = 2, (c) PR = 3, and (d) PR = 4.

and inlet and outlet is 250 mm. In this study, in order to model radiation, FLUENT software and surface-to-surface radiation model are used. The SST  $k-\omega$  turbulence model is employed which means that the flow conforms to turbulent.

As reported in Table 1, SWCNT-Cu/water is used in this study.

In order to numerically simulate the SWCNT-Cu/water nanofluid flow inside the SC, the two-phase mixed method is used. The governing equations are as follows:

Continuity equation:

$$\frac{\partial}{\partial x_i} (\rho u_i) = 0 \quad (1)$$

Momentum equation:

$$\frac{\partial}{\partial x_i} (\rho u_i u_j) = -\frac{\partial p}{\partial x_i} + \frac{\partial \tau_{ij}}{\partial x_j} + \rho g_i \quad (2)$$

$$\tau_{ij} = \frac{\mu^* \partial u_i}{\partial x_j} \quad (3)$$

$$\mu^* = \mu + \mu_t \quad (4)$$

Energy equation:

$$\frac{\partial}{\partial x_i} (\rho c_p u_i T) = \frac{\partial}{\partial x_i} \left( \lambda^* \frac{\partial T}{\partial x_i} \right) \quad (5)$$

$$\lambda^* = \lambda + \lambda_t \quad (6)$$

$$\lambda_t = \frac{c_p \mu_t}{\sigma_t} \quad (7)$$

In this study, the  $k-\omega$  turbulence model is used. This model has the capabilities of the  $k-\varepsilon$  model and also covers the weaknesses of that model. In fact,  $k-\omega$  model has been used due to the higher accuracy and speed of convergence.

Similar to references of [48–50], the following turbulent formulations are utilized:

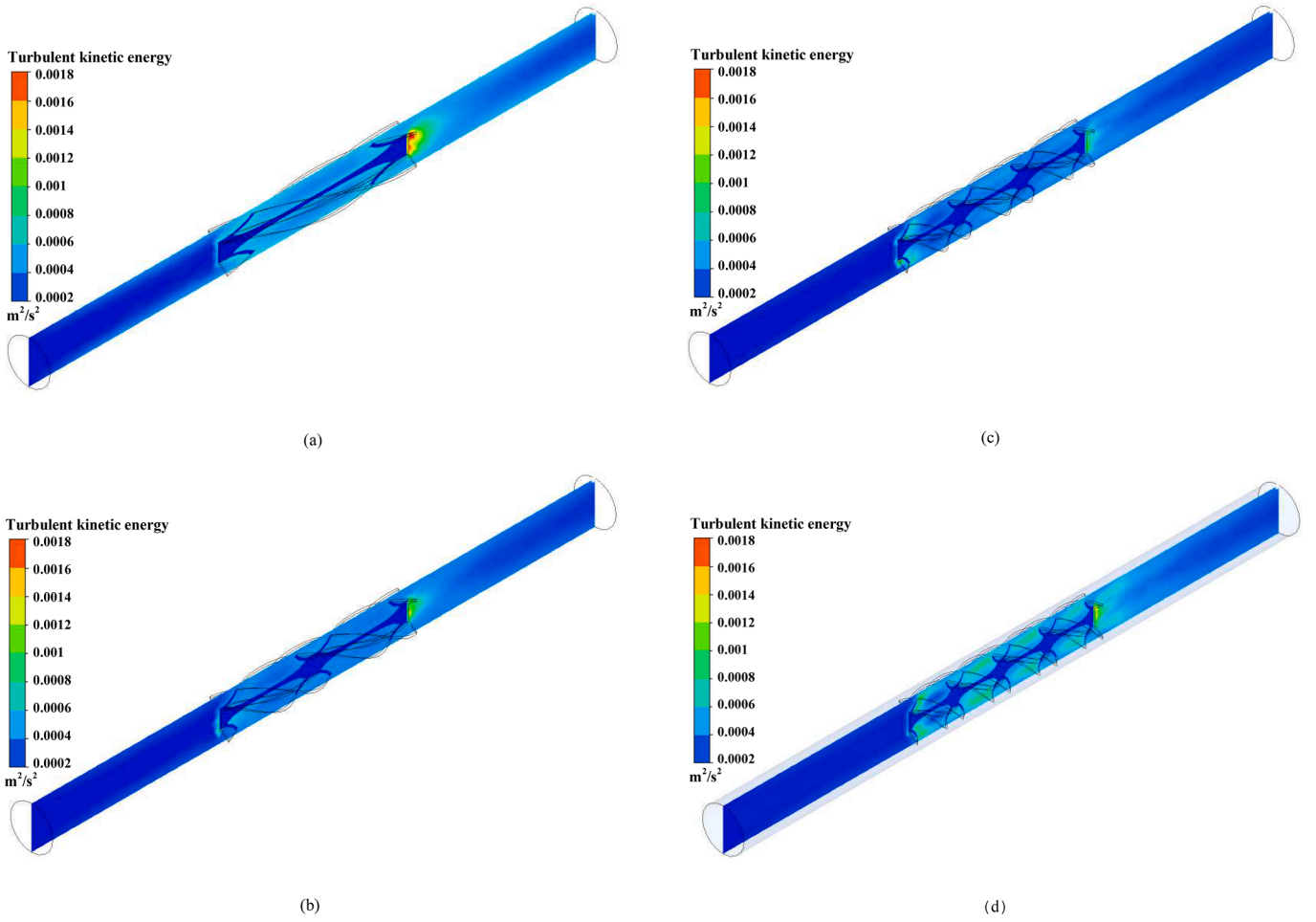
$$\frac{\partial}{\partial x_i} (\rho u_i k) = \frac{\partial}{\partial x_i} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_i} \right] + G_k - Y_k \quad (8)$$

$$\frac{\partial}{\partial x_i} (\rho u_i \omega) = \frac{\partial}{\partial x_i} \left[ \left( \mu + \frac{\mu_t}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_i} \right] + G_\omega - Y_\omega + D_\omega \quad (9)$$

$$\mu_t = \frac{\rho k}{\omega} \frac{1}{\max \left\{ \frac{1}{\alpha^*}, \frac{\Omega F_2}{\sigma_1 \omega} \right\}} \quad (10)$$

$$\Omega = \sqrt{2 \Omega_{ij} \Omega_{ij}} \quad (11)$$

where  $\Omega_{ij}$  is the mean rate of rotation tensor and defined as follow [51]:



**Fig. 8.** Turbulence kinetic energy contours the temperature contours are plotted for two –phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ .

$$\Omega_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right) \quad (12)$$

The other notations in Eqs. 8–10 are defined as follows [50]:

$$\sigma_k = \frac{1}{\frac{F_1}{\sigma_{k,1}} + \frac{1-F_1}{\sigma_{k,2}}} \quad (13)$$

$$\sigma_\omega = \frac{1}{\frac{F_1}{\sigma_{\omega,1}} + \frac{1-F_1}{\sigma_{\omega,2}}} \quad (14)$$

$$F_1 = \tanh(\Phi_1^4) \quad (15)$$

$$F_2 = \tanh(\Phi_2^2) \quad (16)$$

$$\Phi_1 = \min \left\{ \max \left\{ \frac{\sqrt{k}}{0.09\omega y}, \frac{500\mu}{\rho y^2 \omega} \right\}, \frac{4\rho k}{\sigma_{\omega,2} D_\omega^+ y^2} \right\} \quad (17)$$

$$\Phi_2 = \max \left\{ \frac{2\sqrt{k}}{0.09\omega y}, \frac{500\mu}{\rho y^2 \omega} \right\} \quad (18)$$

$$D_\omega^+ = \max \left\{ \frac{2\rho}{\omega \rho_{\omega,2}} \frac{\partial k}{\partial x_i} \frac{\partial \omega}{\partial x_i}, 10^{-20} \right\} \quad (19)$$

$$\alpha^* = \alpha_\infty^* \left( \frac{\alpha_0^* + \frac{Re_t}{R_k}}{1 + \frac{Re_t}{R_k}} \right), \alpha_0^* = \frac{\beta_i}{3}, Re_t = \frac{\rho k}{\mu \omega}, \beta_i = F_1 \beta_{i,1} + (1 - F_1) \beta_{i,2} \quad (20)$$

$$G_k = \tau_{i,j} \frac{\partial u_i}{\partial x_j}, \tau_{i,j} = \mu_t \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \rho k \delta_{ij} \quad (21)$$

$$Y_k = \rho \beta^* k \omega, G_\omega = \frac{\rho \alpha}{\mu_t} G_k, Y_\infty = \rho \beta_i \omega^2 \quad (22)$$

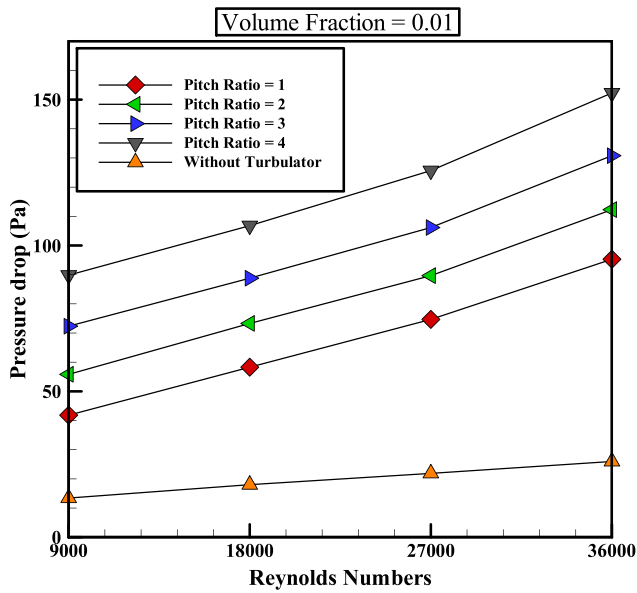
$$\alpha = \frac{\alpha_\infty}{\alpha^*} = \left( \frac{\alpha_0^* + \frac{Re_t}{R_k}}{1 + \frac{Re_t}{R_k}} \right), \alpha_\infty = F_1 \alpha_{\infty,1} + (1 - F_1) \alpha_{\infty,2} \quad (23)$$

$$\alpha_{\infty,1} = \frac{\beta_{i,1}}{\beta_\infty^*} - \frac{\kappa^2}{\sigma_{\omega,1} \sqrt{\beta_\infty^*}}, \alpha_{\infty,2} = \frac{\beta_{i,2}}{\beta_\infty^*} - \frac{\kappa^2}{\sigma_{\omega,2} \sqrt{\beta_\infty^*}} \quad (24)$$

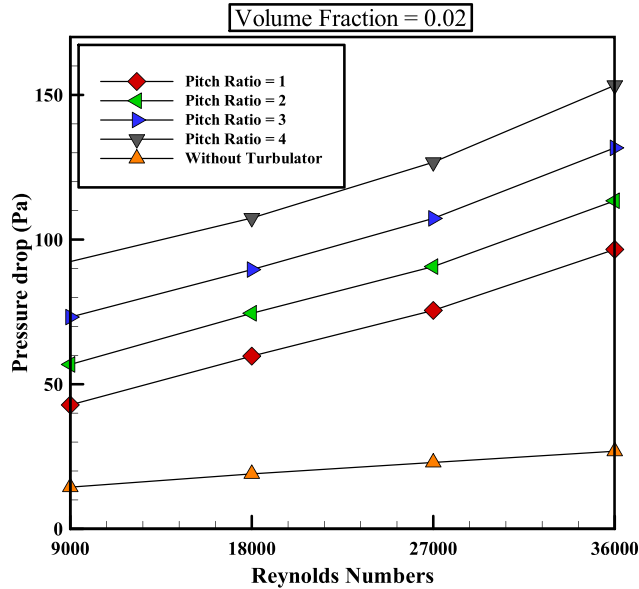
Finally, the energetic and exergetic efficiencies are defined as follows [31]:

$$\eta_n = \frac{E_n}{I \cdot A} = \frac{p_{fo} \cdot Q_{in} \cdot \rho_{in} \cdot c_{p,in} \cdot (T_{fo,out} - T_{in}) + (1 - p_{fo}) Q_{in} \cdot \rho_{in} \cdot c_{p,in} \cdot (T_{fi,out} - T_{in})}{6 \cdot 10^4 \cdot I \cdot A} \quad (25)$$

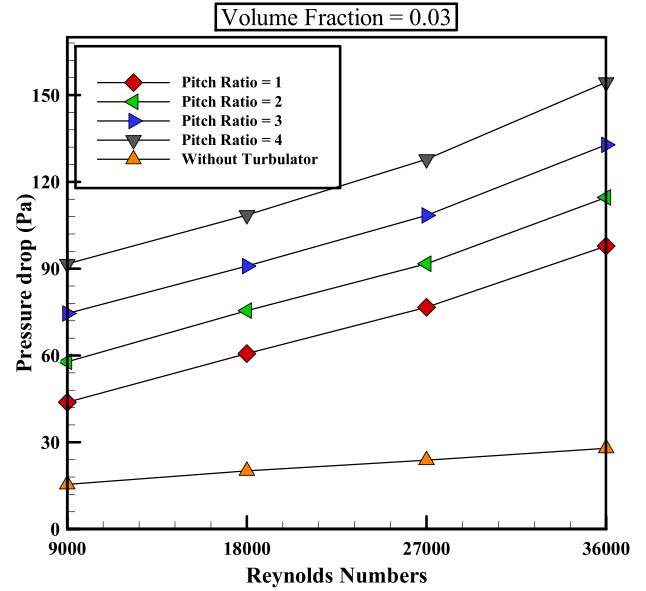
$$\eta_{ex} = \frac{\dot{Q}_{HTF} - \dot{m}_{HTF} c_{p,HTF} \ln \left( \frac{T_{\infty}}{T_{i,HTF}} \right)}{-\dot{Q}_{HTF} - \dot{m}_{CF} c_{p,CF} \ln \left( \frac{T_{o,CF}}{T_{i,CF}} \right) + VI \eta_P} \quad (26)$$



(a)



(b)



(c)

Fig. 9. Pressure drop in terms of Re in a SC equipped with a TT with different values of PR for (a)  $\phi = 1\%$ , (b)  $\phi = 2\%$ , and (c)  $\phi = 3\%$ .

## Numerical modeling

In the present study, the effect of TT on THP, exergy and energy efficiency is examined using computational fluid dynamics and FLUENT's software. In order to solve the problem, the SOLIDWORKS software is used to design the geometry. Since Re changes from 9000 to 36000, the SST  $k-\omega$  model is used to model turbulent flow. The solution is three-dimensional and steady. The SWCNT-Cu/water hybrid nanofluid is simulated using a two-phase mixed model. The first phase is the base fluid, and the second one is SWCNT and Cu nanoparticles. The coupled algorithm is used to couple the velocity and pressure equations. In order to spatially discretize gradients, the Green-Gauss Cell-Based model is employed.

## Grid independence test

In order to study the grid independence, the  $\overline{Nu}$  for SWCNT-Cu/water two-phase hybrid nanofluid flow inside the SC with TT is calculated for different grid points (Fig. 3). The figure demonstrates that the grid with 2,436,268 elements is sufficient for the simulations. Further increase in the number of elements does not change the Nu. Therefore, it is possible to ensure the accuracy of the computational grid for the SC with a TT.

## Verification

Verification of numerical results is performed based on the geometry



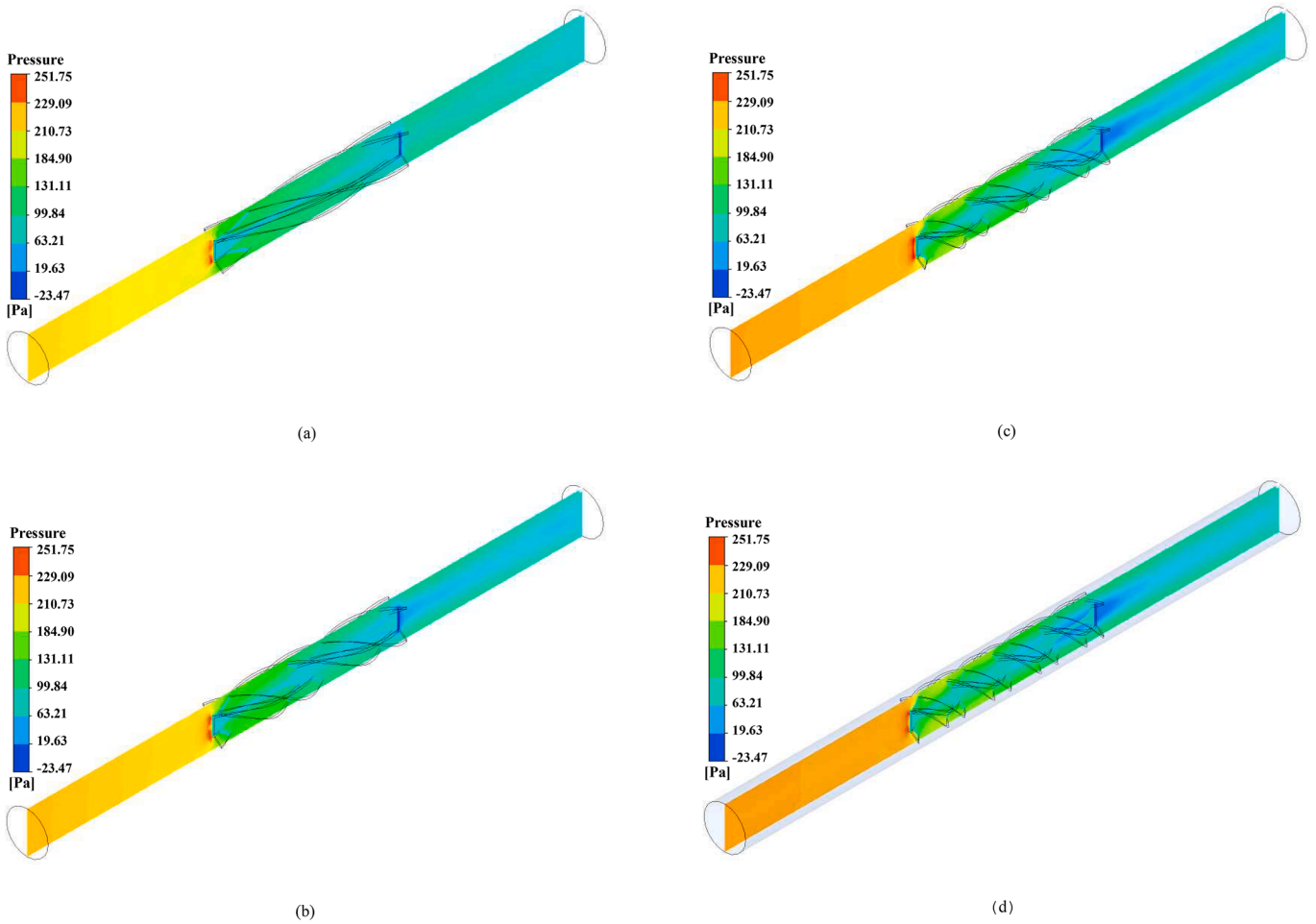


Fig. 10. Pressure contours for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ .

and boundary conditions of the study of He et al. [52]. The  $\overline{Nu}$  is calculated and compared with their research (Fig. 4). The error between the values of the  $\overline{Nu}$  obtained from the present simulations and the results of He et al. [52] is about 5.23%, indicating that the accuracy of the modeling results is ensured.

## Results and discussion

In this section, the results of the present numerical simulations are presented. The effect of different values of  $PR$  of the TT on the  $\overline{Nu}$ , pressure drop, THP, and exergy and energy efficiency is investigated. Also, the contours of velocity, temperature, pressure, and streamlines inside the SC are provided for  $PR = 1, 2, 3$ , and  $4$ ,  $\phi = 3\%$ , and  $Re = 36000$ .

### Effect of pitch ratio on $\overline{Nu}$

Figure 5 shows the variations of the  $\overline{Nu}$  versus  $Re$  in a SC equipped with a TT with different values of  $PR$  for (a)  $\phi = 1\%$ , (b)  $\phi = 2\%$ , and (c)  $\phi = 3\%$ . According to the results, the  $\overline{Nu}$  has an increasing trend with the  $\phi$  and  $Re$ . For example, at  $Re = 36000$ , an increment in the  $PR$  enhances HT. Increasing the  $PR$  value has caused more fluctuation in the fluid flow, resulting in increased heat exchange, and therefore the average Nusselt number increases with increasing  $PR$ . For  $\phi = 1\%$  and  $Re = 36,000$ , the TT with  $PR = 4$  intensifies the  $\overline{Nu}$  by 71.45% compared to the SC without turbulator. At  $\phi = 2\%$  and  $Re = 36,000$ , the TT with  $PR = 4$  enhances the  $\overline{Nu}$  by 73.11% compared to the SC without turbulator.

At  $\phi = 3\%$  and  $Re = 36,000$ , the TT with  $PR = 4$  increases the average  $\overline{Nu}$  by 74.95% compared to the SC without turbulator. With the use of a turbulator, turbulence and oscillation in the flow increases and as a result, heat exchange between particles intensifies; thus, the average Nusselt number enhances.

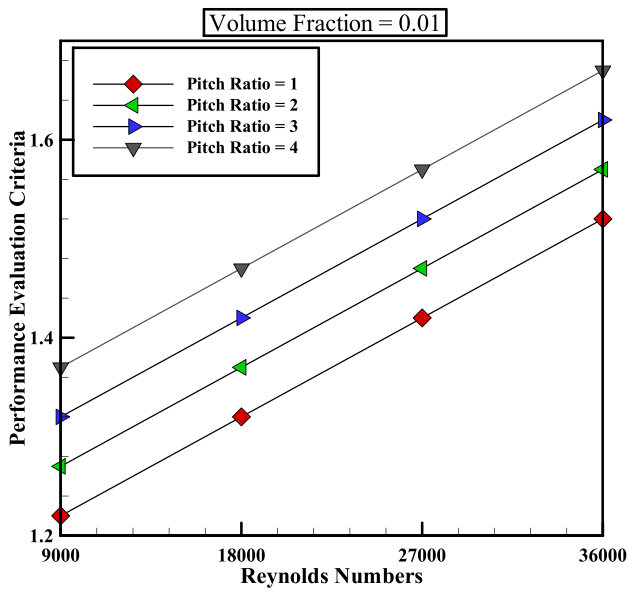
Contours of velocity for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . As can be seen in the figures, the velocity of the SWCNT-Cu/water nanofluid is zero close to the wall and has its maximum value in the middle of the SC. Also, the use of a TT causes the mixing and disturbance to be created in the viscous sublayer. Therefore, the vortices are formed and enhance the thermal performance of the SC.

Figure 7 demonstrates the temperature contours for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . As can be seen, an increment in the  $PR$  of the TT causes the temperature at the turbulator surface to rise.

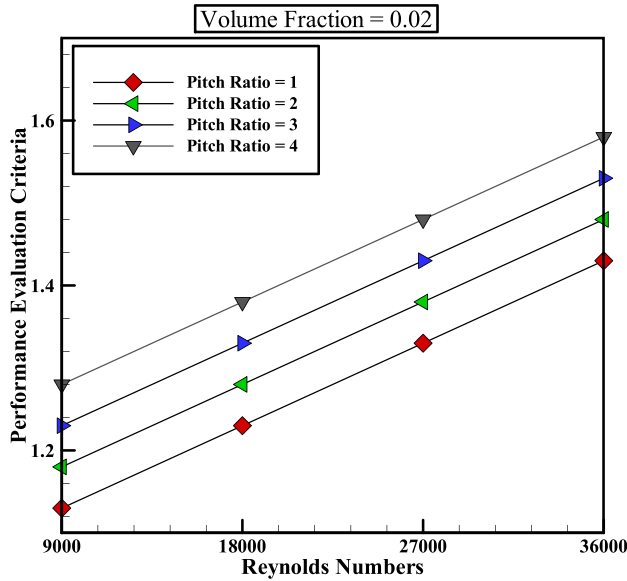
In Fig. 8, turbulent kinetic energy contours the temperature contours are plotted two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  are shown in Fig. 6 for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . Due to the oscillating nature of the turbulent flow and the type of geometry studied, the speed fluctuations behind the turbulator increase. Because kinetic energy is caused by speed fluctuations, the amount of kinetic energy increases in this area.

### Effect of pitch ratio on pressure drop

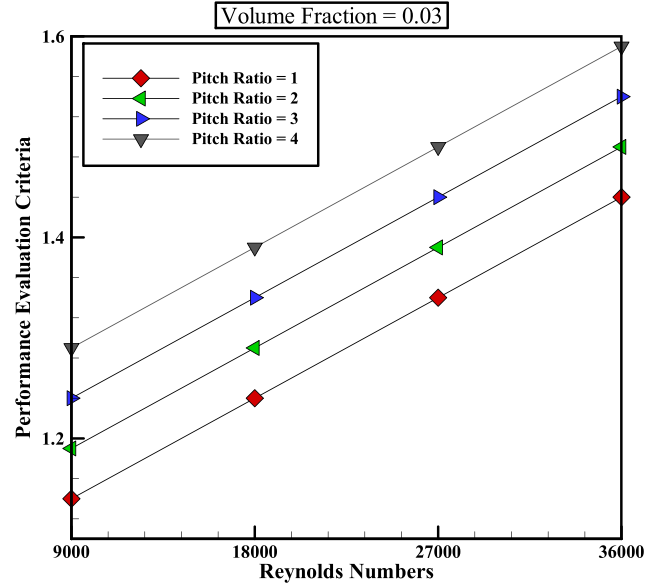
Figure 9 demonstrates the pressure drop in terms of  $Re$  in a SC



(a)



(b)



(c)

Fig. 11. Variations of THP in terms of Re for a SC equipped with a TT with different values of PR and (a)  $\phi = 1\%$ , (b)  $\phi = 2\%$ , and (c)  $\phi = 3\%$ .

equipped with a TT with different values of PR for (a)  $\phi = 1\%$ , (b)  $\phi = 2\%$ , and (c)  $\phi = 3\%$ . The pressure drop in the solar culture is an ascending function of the volume fraction of nanoparticles and Re. Increasing the volume fraction of nanoparticles intensifies the viscosity of hybrid nanofluid and as a result the amount of shear stresses rises. Also, an increment in the PR of the TT has a significant effect on pressure drop. As the PR value increases, the curvature in the turbulator rises and as a result, the flow lines become more curved. This event leads to more intense velocity gradients and augmented friction. This leads to an intensification in pressure drop.

At  $\phi = 1\%$  and  $Re = 36000$ , TTs with PR = 4 increase the pressure drop by 411.03% compared to the SC without turbulator. At  $\phi = 2\%$  and  $Re = 36,000$ , TTs with PR = 4 intensifies the pressure drop by 415.78% compared to the SC without turbulator. At  $\phi = 3\%$  and  $Re = 36,000$ , TTs

with PR = 4 increase the pressure drop by 429.31% compared to the SC without turbulator.

The pressure contours are shown in Fig. 10 for two -phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  for (a) PR = 1, (b) PR = 2, (c) PR = 3, and (d) PR = 4. As can be seen, the accumulation of SWCNT-Cu/water two -phase hybrid nanofluid flow is enhanced during the initial contact with the turbulator by intensifying the PR of the TT. Therefore, it can be concluded that an increment in the PR enhances the pressure drop.

#### Effect of pitch ratio on THP

Variations of THP in terms of Re are shown in Fig. 11 for a SC equipped with a TT with different values of PR and (a)  $\phi = 1\%$ , (b)  $\phi =$

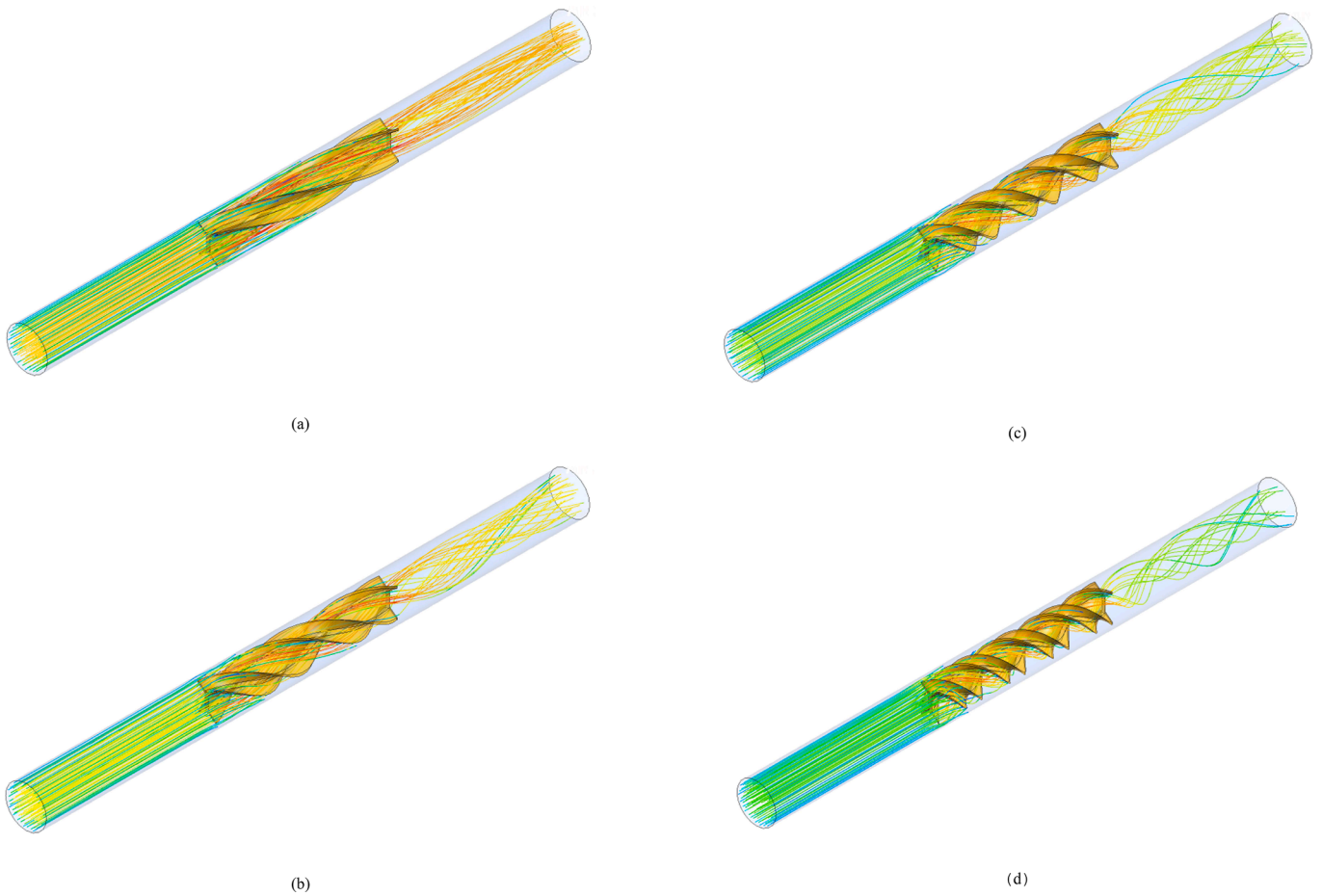


Fig. 12. Streamline contours for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ .

2%, and (c)  $\phi = 3\%$ . As can be seen, for all cases, the value of the THP is greater than 1. Therefore, the addition of a TT and an enhancement in its PR improve the THP. As the volume fraction of nanoparticles intensify, both the Nusselt number and the pressure drop augment. This augmentation is greater in the average Nusselt number compared to that in pressure drop. As a result, as the volume fraction of nanoparticles rises, the amount of PEC enhances.

Streamline contours are shown in Fig. 12 for two-phase hybrid nanofluid with  $\phi = 3\%$  and  $Re = 36000$  for (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . As can be seen, the density of the streamlines enhances with the PR.

#### Effect of pitch ratio on energy efficiency

Figure 13 illustrates the energy efficiency in terms of  $Re$  for a SC equipped with a TT with different volume fractions and (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . For all cases, the energy efficiency is an ascending function of the pitch ratio of the TT. In a SC with a TT with a pitch ratio of 1 and  $\phi = 3\%$ , the amount of energy efficiency is enhanced by 35.81% by increasing the  $Re$  from 7000 to 28000.

In a SC with a TT with  $PR = 2$  and  $\phi = 3\%$ , the amount of energy efficiency intensifies by 37.90% by enhancing the  $Re$  from 7000 to 28000. In a SC with a TT with  $PR = 3$  and  $\phi = 3\%$ , the amount of energy efficiency is enhanced by 39.07% by intensifying the  $Re$  from 7000 to 28000. In a SC with a TT with  $PR = 4$  and  $\phi = 3\%$ , the amount of energy efficiency is enhanced by 41.75% by increasing the  $Re$  from 7000 to 28000.

#### Effect of pitch ratio on exergy efficiency

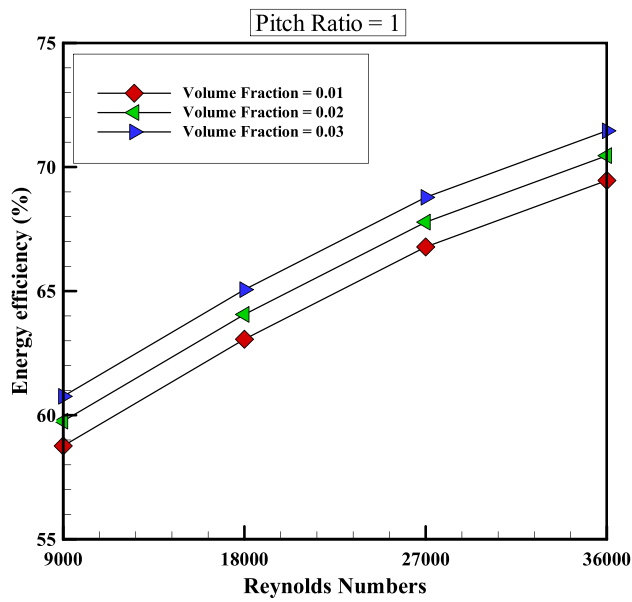
Exergy efficiency as a function of  $Re$  is presented in Fig. 14 for a SC equipped with a TT with different values of  $\phi$  and (a)  $PR = 1$ , (b)  $PR = 2$ , (c)  $PR = 3$ , and (d)  $PR = 4$ . The exergy efficiency is an ascending function of  $Re$  and  $\phi$ . In a SC with a TT with  $PR = 1$  and  $\phi = 3\%$ , the amount of exergy efficiency is enhanced by 33.09% by increasing the  $Re$  from 9000 to 36000. In a SC with a TT with  $PR = 2$  and  $\phi = 3\%$ , the amount of exergy efficiency enhances by 32.32% by intensifying the  $Re$  from 9000 to 36000. In a SC with a TT with  $PR = 3$  and  $\phi = 3\%$ , the amount of exergy efficiency is increased by 30.11% by enhancing the  $Re$  from 9000 to 36000. In a SC with a TT with  $PR = 4$  and  $\phi = 3\%$ , the amount of exergy efficiency enhances by 30.67% by increasing the  $Re$  from 9000 to 36000.

#### Conclusions

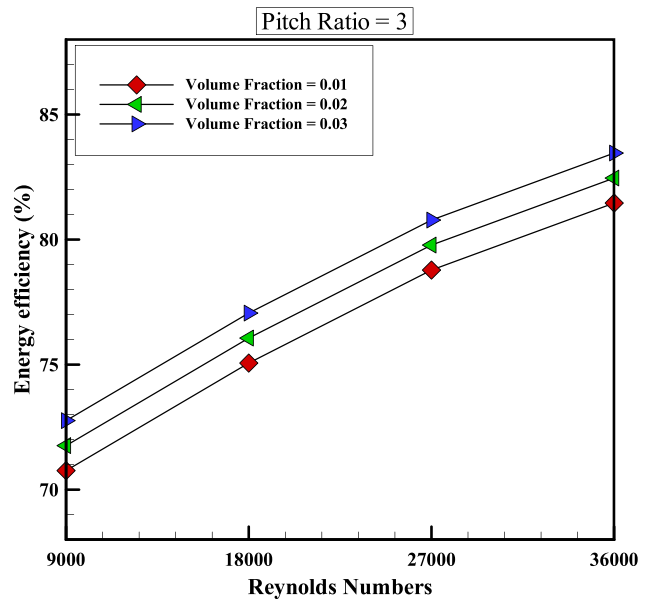
In the present numerical study, the impact of TT in a SC on energy and exergy efficiencies and THP of SWCNT-Cu/water hybrid nanofluid was evaluated. The study was performed for  $Re$  in the range of 9000 to 36000,  $\phi = 1$  to 3%, and  $PR = 1, 2, 3,$  and 4. Based on the results obtained from the numerical study, it can be concluded:

The pressure drop and the  $\bar{Nu}$  enhance by intensifying the PR of the TT.

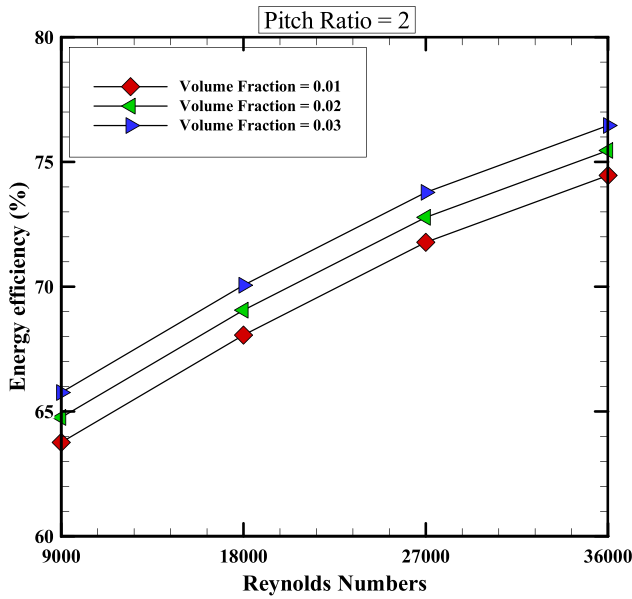
- At  $\phi = 3\%$  and  $Re = 36,000$ , the placement of TTs with  $PR = 4$  enhances the  $\bar{Nu}$  by 74.95% compared to the SC without turbulator.



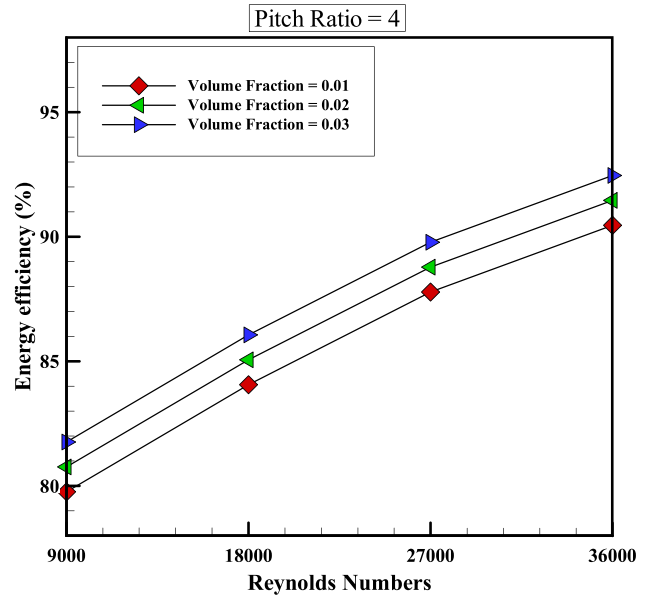
(a)



(c)



(b)



(d)

Fig. 13. Energy efficiency in terms of Re for a SC equipped with a TT with different values of  $\phi$  and (a) PR = 1, (b) PR = 2, (c) PR = 3, and (d) PR = 4.

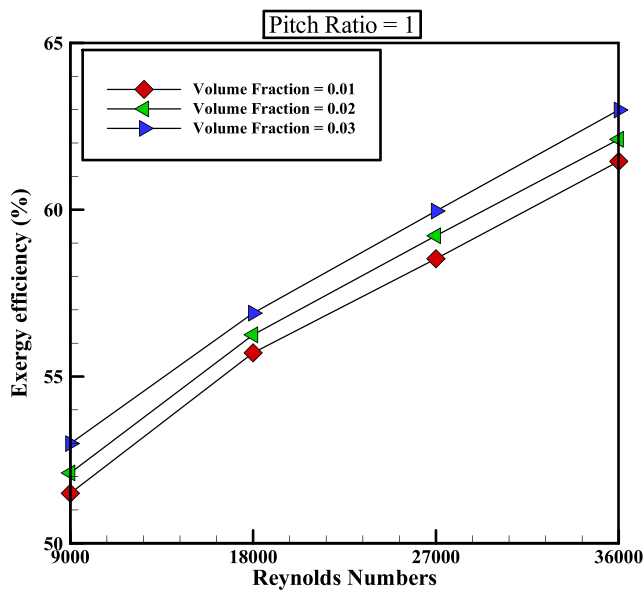
- For all cases, the values of the THP are greater than 1. Therefore, it can be concluded that the addition of a TT and an increment in its pitch ratio improve the THP.
- For all cases, the energy efficiency is an ascending function of the PR.
- In a SC with a TT with PR = 4 and  $\phi = 3\%$ , the amount of energy efficiency is enhanced by 41.75% by increasing the Reynolds number from 7000 to 28000.
- Exergy efficiency is an ascending function of Re and  $\phi$ .
- In a SC with a TT with PR = 1 and  $\phi = 3\%$ , the amount of exergy efficiency intensifies by 33.09% by enhancing the Re from 9000 to 36000.

*CRedit authorship contribution statement*

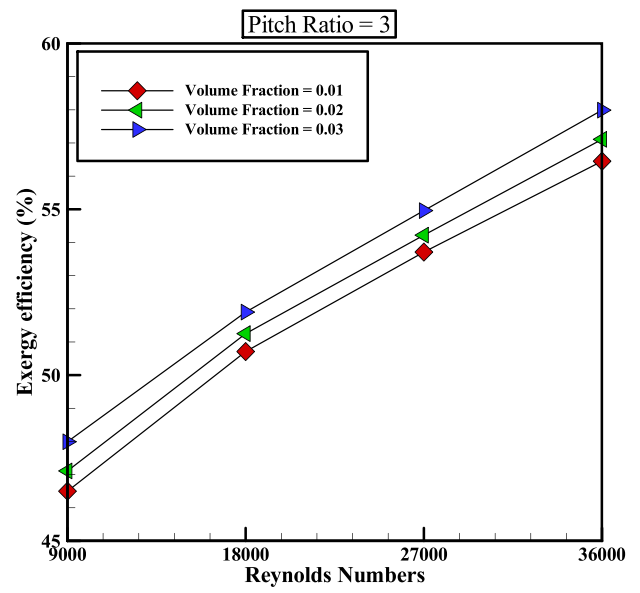
**Muhammad Ibrahim:** Funding acquisition, Writing – original draft. **Awatef Abidi:** Formal analysis, Writing – original draft. **Ebrahim A. Alghayne:** Writing – original draft. **Tareq Saed:** Writing – original draft. **Goshtasp Cheraghian:** Conceptualization, Writing – review & editing. **Mohsen Sharifpur:** Conceptualization.

**Declaration of Competing Interest**

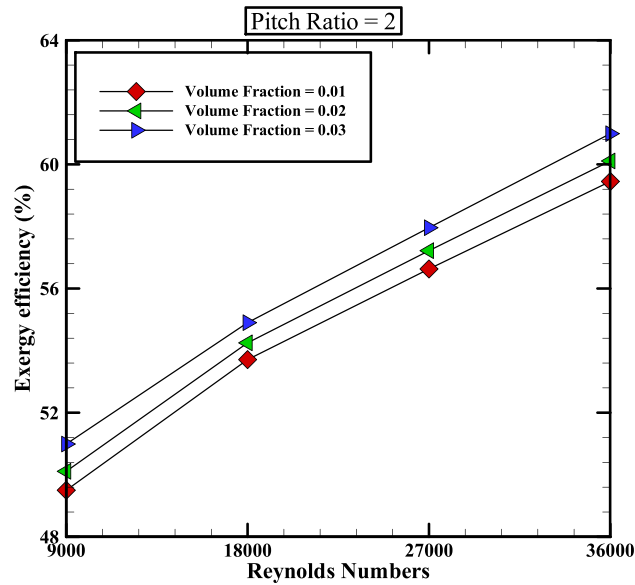
The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.



(a)



(c)



(b)

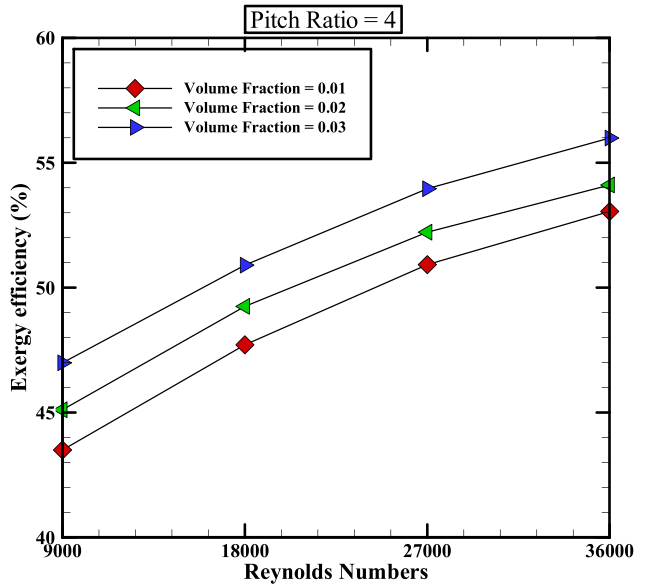


Fig. 14. Exergy efficiency as a function of Re for a SC equipped with a TT with different values of  $\phi$  and (a) PR = 1, (b) PR = 2, (c) PR = 3, and (d) PR = 4.

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