

# Managing energy-water-carbon-food nexus for cleaner agricultural greenhouse production: A control system approach

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## Abstract

Poverty, food insecurity and climate change are global issues facing humanity, threatening social, economic and environmental sustainability. Greenhouse cultivation provides a potential solution to these challenges. However, some greenhouses operate inefficiently and need to be optimized for more economical and cleaner crop production. In this paper, an economic model predictive control (EMPC) method for a greenhouse is proposed. The goal is to manage the energy-water-carbon-food nexus for cleaner production and sustainable development. First, an optimization model that minimizes the greenhouse's operating costs, including costs associated with greenhouse heating/cooling, ventilation, irrigation, carbon dioxide (CO<sub>2</sub>) supply and carbon emissions taking into account both the CO<sub>2</sub> equivalent (CO<sub>2</sub>-eq) emissions caused by electrical energy consumption and the negative emissions caused by crop photosynthesis, is developed and solved. Then, a sensitivity analysis is carried out to study the impact of electricity price, supplied CO<sub>2</sub> price and social cost of carbon (SCC) on the optimization results. Finally, a model predictive control (MPC) controller is designed to track the optimal temperature, relative humidity, CO<sub>2</sub> concentration and incoming radiation power in presence of system disturbances. Simulation results show that the proposed approach increases the operating costs by R186 (R denotes the South African currency, Rand) but reduces the total cost by R827 and the carbon emissions by 1.16 tons when compared with a baseline method that minimizes operating costs only. The total cost is more sensitive to changes in SCC than that in electricity price and supplied CO<sub>2</sub> price. The MPC controller has good tracking performance under different levels of system disturbances. Greenhouse environmental factors are kept within specified ranges suitable for crop growth, which increases crop yields. This study can provide effective guidance for growers' decision-making to achieve sustainable development goals.

*Keywords:* Greenhouse, energy-water-carbon-food nexus, carbon emissions, social cost of carbon, sensitivity analysis

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## 1. Introduction

Global issues such as poverty, energy crisis, food insecurity, climate change and global warming affect social, economic and environmental sustainability [1]. During the COVID-19 epidemic, the impact of these issues is increasing, especially in some low-income countries [2]. Agricultural production is critical to deal with these issues [3]. According to the World Bank, agriculture can help 80% of the world's poor

reduce poverty, increase incomes and improve food security [4]. However, the growth of crops is greatly affected by the weather under the traditional open-field cultivation mode. Crops cultivated with this mode have low yields [5]. In recent years, with a growing population and decreasing arable land, the traditional open-field cultivation mode is facing many challenges in providing sufficient food [6]. Moreover, some cultivation modes cause problems such as soil erosion, land degradation and pesticide residues, which restrict the sustainable development of agriculture [7]. Compared with traditional open-field cultivation, modern precision agriculture has many advantages, such

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as environmentally friendly and high crop yields, which can help to achieve cleaner production and sustainable development [8].

Greenhouse cultivation is one of the most popular modern agricultural technologies [9]. A greenhouse is an enclosed agricultural building covered with transparent materials such as plastic or glass to allow sunlight to pass through. Greenhouses can provide a suitable environment for crops and protect them from adverse external environmental conditions such as extreme temperatures, heavy rain and hail, etc [10]. Therefore, the crops under greenhouse planting mode can obtain higher yield and better quality than those under traditional outdoor planting mode [11].

Greenhouses consume a lot of resources, which leads to high operating costs and adverse environmental impacts [12]. Firstly, greenhouses consume a lot of energy and the energy efficiency of greenhouse systems under some traditional operation modes is low [13]. About 65% to 85% of the energy consumed by greenhouses is used for heating [14]. Greenhouse heating is generally done by using electric heaters or burning fossil fuels, which will increase carbon dioxide ( $\text{CO}_2$ ) emissions [15]. The increasing  $\text{CO}_2$  emissions contribute to global warming, which has a great impact on environmental sustainability [16]. Secondly, the greenhouse irrigation process needs to be optimized to reduce water consumption while meeting the water demand for crop growth [17]. Thirdly, greenhouse  $\text{CO}_2$  supply and shading control also should be considered in the optimization of greenhouse operations to reduce operating costs [18].

Some studies focus on reducing greenhouse energy consumption or costs. In [19], a model predictive control (MPC) method is proposed to improve the energy efficiency of the greenhouse heating system. A simplified linearized model of the system around the predefined set points is adopted. The designed controller tracks the optimized reference trajectory to reduce energy consumption. The results show that the proposed method can improve the system performance without modifying the system. In [20], the use of a solar soil heat storage system for greenhouse heating is studied. The solar energy stored in the soil under the greenhouse can be used to reduce the energy demand of extreme cold and continuous overcast days in winter. Results reveal that 27.8 kWh of electricity can be saved per square meter of greenhouse per year. In [21], an optimal control method for the energy utilization of a semi-closed greenhouse is proposed. All

available equipment is used under optimal conditions. The energy cost is reduced by 29% compared with the grower's situation. In [22], the use of ground thermal energy for greenhouse heating is studied. During the day, the air suspension exchanger recovers excess solar energy. At night, excess energy stored in storage tanks is used to heat the greenhouse air. The obtained results indicate that the energy stored in the ground can increase the temperature by 6 °C at night.

Some studies focus on reducing greenhouse water consumption. Water is critical for agricultural crop production [23]. Methods to reduce water consumption by improving water efficiency have been discussed in many studies. A predictive control approach for reducing greenhouse energy and water consumption is presented in [24]. In [25], a method of reducing water use for evaporative cooling is studied. Results reveal that increasing the temperature of the extracted air can effectively reduce water consumption. In [26], the irrigation of a rooftop greenhouse is optimized to reduce water consumption and environmental impact while maintaining the water requirements of the grown tomatoes.

Some studies focus on the optimization of the greenhouse  $\text{CO}_2$  supply. Using  $\text{CO}_2$  as fertilizer for crops in greenhouses can not only improve crop yields but also increase  $\text{CO}_2$  sink [27]. This technology has been widely used in greenhouse production and achieved good economic benefits. In [28], two optimal control methods of  $\text{CO}_2$  supply for greenhouse tomato planting are proposed. In [29], the technology of  $\text{CO}_2$  by-product applied to tomato production in an agricultural greenhouse is evaluated. Results show that  $\text{CO}_2$  utilization technology has better economic benefits than  $\text{CO}_2$  storage.

For the greenhouse production, energy, water, carbon emissions and food are highly inter-connected, which is called the energy-water-carbon-food (EWCF) nexus. Energy, water and food are essential for human well-being, poverty reduction and sustainable development [30]. The management of the EWCF nexus helps to achieve social, economic and environmental objectives with limited resources [31]. However, the EWCF nexus approach has been rarely discussed in previous studies on greenhouse operation optimization. Most previous studies focus on resource utilization such as reducing energy and water consumption, or economic aspects, such as reducing greenhouse operating costs or increasing greenhouse production profits, while few studies consider the envi-

ronmental impact of carbon emissions. To fill these gaps, an optimization method that takes into consideration both economic costs and carbon emissions of greenhouse systems is studied in this paper. The proposed method is studied based on meteorological data from South Africa. South Africa is a country short of electricity [32]. The vast majority of electricity in South Africa is generated by burning coal. Figure 1 shows the energy mix of South Africa from 1990 to 2018. It can be observed that coal accounts for more than 80% of South Africa’s total energy, while renewable energy accounts for a small part of the overall mix. Due to its heavy reliance on coal, South Africa has become the 14th largest carbon emitter in the world and the largest carbon emitter in Africa.

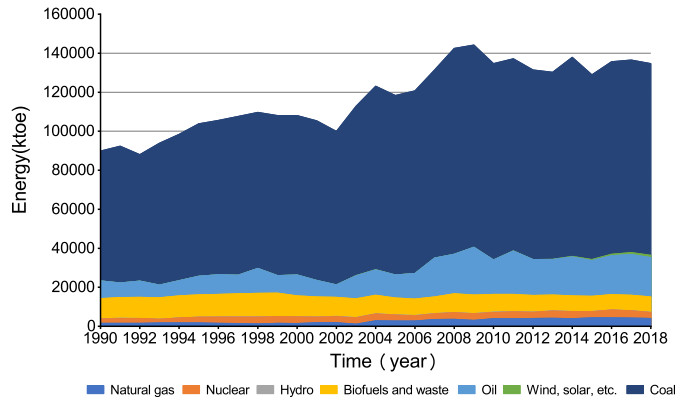


Figure 1: Energy mix of South Africa

In this study, an economic model predictive control (EMPC) method for a greenhouse under the climate of South Africa is proposed. The objective is to manage the EWCF nexus for low-cost and cleaner crop production. The proposed method has a two-layer structure consisting of an optimization layer and a control layer. At the optimization layer, an optimization method is adopted to minimize the total cost including the operating costs and the cost of carbon emissions while keeping greenhouse environmental factors including temperature, relative humidity, CO<sub>2</sub> concentration and incoming solar radiation power within required ranges. The calculation of operating costs takes into account heating/cooling, ventilation, CO<sub>2</sub> supply and irrigation. The carbon emissions include the CO<sub>2</sub> equivalent (CO<sub>2</sub>-eq) emissions from electricity consumed by greenhouse operation and the negative emissions from crop photosynthesis. The cost of carbon emissions is determined by the amount of CO<sub>2</sub>-eq emissions and the social cost of carbon (SCC) which is a commonly used indica-

tor to measure the expected economic loss caused by one ton of CO<sub>2</sub> emissions [33]. Moreover, a sensitivity analysis is carried out to study the impact of the electricity price, supplied CO<sub>2</sub> price and SCC on the total cost. At the control layer, an MPC approach is used to deal with system disturbances. The control performance of the designed controller is analyzed.

The main contributions of this study can be summarized as: 1) Most studies on greenhouse operation optimization consider energy consumption or economic costs but ignore the environmental impacts of carbon emissions. In this paper, both operating costs and carbon emissions are considered. The proposed method helps to achieve cleaner crop production and sustainable development. 2) Most previous studies on the optimization of greenhouse operation only considered one or some of the environmental factors (temperature, relative humidity, CO<sub>2</sub> concentration and incoming solar radiation power), while this study considered all of them. Compared with previous studies, this study can provide a better environment for crop growth and obtain a higher crop yield. 3) The impact of climatic factors on the CO<sub>2</sub> absorption rate of crop photosynthesis is analyzed. The feasibility of reducing the CO<sub>2</sub> emission of the greenhouse system by adjusting the climate environment inside the greenhouse is studied. 4) The SCC and the grid emission factor are introduced to calculate the cost of carbon emissions. The multi-objective optimization problem considering two conflicting objectives of greenhouse operating costs and CO<sub>2</sub> emissions is transformed into a single-objective optimization problem that minimizes the total cost of operating costs and carbon emissions costs. The computational complexity of the greenhouse operation optimization problem is reduced. 5) A sensitivity analysis of the electricity price, supplied CO<sub>2</sub> price and SCC is conducted. A deeper insight into the effects of uncertainty in model parameters on the optimization results is obtained. 6) An MPC method is introduced to deal with system disturbances and the complex interactions between different environmental factors.

The rest of this paper is organized as follows. Section 2 presents the greenhouse system model. Section 3 discusses the proposed optimization methods. Section 4 designs the EMPC controller. Simulation results are shown in Section 5. Section 6 concludes this paper and gives future work.

## 2. System description

### 2.1. Greenhouse system

The growth of crops in the greenhouse requires suitable temperature, relative humidity, CO<sub>2</sub> concentration and light intensity, which needs to be achieved through the cooperation of multiple systems including a power supply system, ventilation system, carbon supply system and irrigation system [34].

Figure 2 is the schematic diagram of greenhouse production. The production process can be summarized as follows: First, farmers set optimization goals and system constraints based on their own experience and needs. Then, the controller, that is, the control centre, gives corresponding instructions to each system based on the received information. Finally, each system operates based on the control signal received from the control centre.

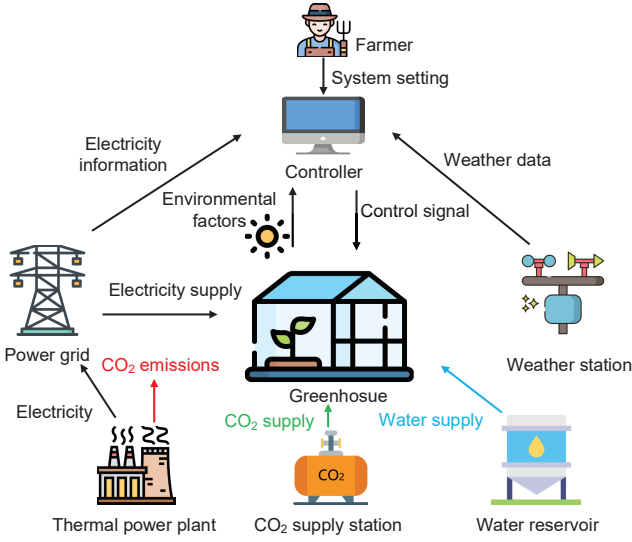


Figure 2: Schematic diagram of greenhouse production

### 2.2. Greenhouse environmental factors model

In this study, four environmental factors (temperature, relative humidity, CO<sub>2</sub> concentration and incoming radiation power) affecting crop growth are considered. The model adopted is derived from [35] and [36] and has been verified to have good prediction performance.

#### 2.2.1. Temperature

The temperature is determined by the energy balance of the system. Figure 3 shows the energy, water and CO<sub>2</sub> flow. It can be seen that the energy

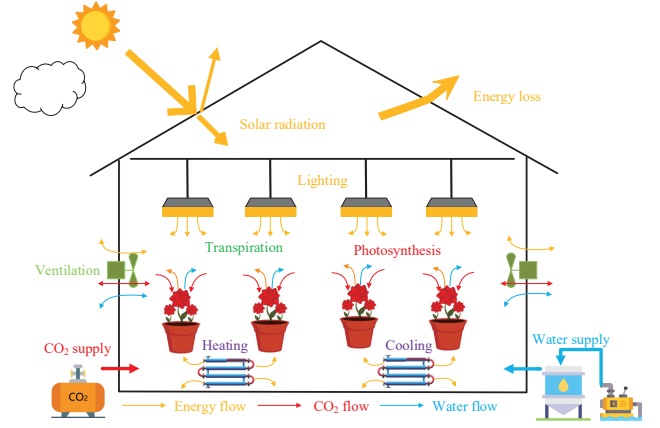


Figure 3: Energy, water and CO<sub>2</sub> flow

mainly comes from solar radiation and heating. The energy loss is caused by greenhouse ventilation, heat exchange with outdoor air, crop transpiration and greenhouse cooling. Therefore, the temperature can be calculated by:

$$\frac{dT_{air}}{dt} = \frac{1}{C_{cap}}(Q_{sun} + Q_{lamp} - Q_{cov} - Q_{trans} - Q_{vent} + Q_c), \quad (1)$$

where  $T_{air}$  is the greenhouse temperature,  $C_{cap}$  is the greenhouse heat capacity,  $Q_{sun}$  is the incoming radiation power, and  $Q_{lamp}$  is the lamp heating power.  $Q_{cov}$  is the heat loss through the cover,  $Q_{trans}$  is the energy absorbed by crop transpiration.  $Q_{vent}$  represents the energy loss through ventilation.  $Q_c$  represents the heating or cooling power. When the value of  $Q_c$  is positive, the greenhouse is being heated, and the heating power is  $Q_c$ . When the value of  $Q_c$  is negative, the greenhouse is being cooled, and the value of cooling power is the absolute value of  $Q_c$ .

$Q_{sun}$  is determined by:

$$Q_{sun} = \alpha_1(1 - s_r)Q_{rad}, \quad (2)$$

where  $\alpha_1$  represents the transmission coefficient of the cover,  $s_r$  is the shading rate,  $Q_{rad}$  represents the solar radiation power.

$Q_{cov}$  can be calculated by:

$$Q_{cov} = \alpha_2(T_{air} - T_{out}), \quad (3)$$

where  $\alpha_2$  is the cover heat transfer coefficient,  $T_{out}$  is the outdoor temperature.

$Q_{trans}$  can be obtained by:

$$Q_{trans} = g_e L(H_{crop} - H_{air}), \quad (4)$$

Nomenclature			
$T_{air}$	greenhouse temperature, °C	$RH_{air}$	greenhouse relative humidity, %
$T_{out}$	outdoor temperature, °C	$SCC$	social cost of carbon, \$/ton
$Q_c$	controlled heating or cooling power, W/m <sup>2</sup>	$s_r$	shading rate
$Q_{sun}$	incoming radiation power, W/m <sup>2</sup>	$\alpha_1$	transmission coefficient
$Q_{lamp}$	lamp heating power, W/m <sup>2</sup>	$\alpha_2$	heat transfer coefficient, W/°Cm <sup>2</sup>
$Q_{cov}$	heat transfer through the cover, W/m <sup>2</sup>	$g_e$	transpiration conductance, m/s
$Q_{rad}$	solar radiation power, W/m <sup>2</sup>	$LAI$	leaf area index
$Q_{trans}$	transpiration endothermic power, W/m <sup>2</sup>	$L$	energy needed to evaporate water from a leaf, J/g
$Q_{vent}$	heat loss through ventilation power, W/m <sup>2</sup>	$\epsilon$	ratio of latent to sensible heat content of saturated air
$H_{air}$	greenhouse humidity, g/m <sup>3</sup>	$r_b$	boundary layer resistance parameter, s/m
$H_{trans}$	vapour evaporated by the crop, g/m <sup>2</sup> s	$r_s$	stomatal resistance, s/m
$H_{cov}$	vapour condensation to the cover, g/m <sup>2</sup> s	$\gamma$	crop specific parameter
$H_{crop}$	vapour concentration at crop level, g/m <sup>3</sup>	$P_E$	artificial lighting power, W/m <sup>2</sup>
$H_{out}$	humidity outside the greenhouse, g/m <sup>3</sup>	$\eta$	lighting thermal conversion coefficient
$H_{vent}$	vapour flux due to ventilation, g/m <sup>2</sup> s	$g_v$	ventilation rate, m/s
$RH_{air}$	greenhouse relative humidity, %	$s$	the greenhouse area, m <sup>2</sup>
$C_{air}$	greenhouse CO <sub>2</sub> concentration, g/m <sup>3</sup>	$\rho_{air}$	density of air, kg/m <sup>3</sup>
$C_{out}$	CO <sub>2</sub> concentration outside the greenhouse, g/m <sup>3</sup>	$h$	average height of greenhouse, m
$C_{inj}$	CO <sub>2</sub> injection into the greenhouse, g/m <sup>2</sup> s	$g_c$	the condensation conductance, m/s
$C_{assi}$	CO <sub>2</sub> assimilation by the crop, g/m <sup>2</sup> s	$p_{gc}$	parameter related to the properties of the condensation surface, m°C <sup>-1/3</sup> s <sup>-1</sup>
$C_{vent}$	effect of ventilation on CO <sub>2</sub> concentration, g/m <sup>2</sup> s	$p_o$	off-peak electricity price, R/kWh
$C_{cap}$	greenhouse heat capacity, J/°Cm <sup>2</sup>	$p_s$	standard electricity price, R/kWh
$C_{p,air}$	air heat capacity, J/kg°C	$p_p$	peak electricity price, R/kWh
$C_{oper}$	operating costs, R	$p_c$	supplied CO <sub>2</sub> price, R/ton
$C_{elec}$	electricity cost, R		
$C_{carb}$	cost of supplemental CO <sub>2</sub> , R		
$C_{equi}$	equivalent carbon emissions of energy consumed, ton		

where  $g_e$  is the transpiration conductance, and  $L$  is the energy consumed to evaporate water from a leaf.  $H_{crop}$  is the absolute water vapour concentration at the crop level.  $H_{air}$  is the absolute water vapour concentration.

$g_e$  is obtained by:

$$g_e = \frac{2LAI}{(1 + \epsilon)r_b + r_s}, \quad (5)$$

where  $LAI$  is the leaf area index,  $\epsilon$  is the ratio of latent to sensible heat content of saturated air,  $r_b$  is the boundary layer resistance and  $r_s$  is the stomatal resistance.

$H_{crop}$  is given by:

$$H_{crop} = H_{air,sat} + \epsilon \frac{r_b}{2LAI} \frac{R_n}{L}, \quad (6)$$

where  $H_{air,sat}$  is the saturated vapour concentration.  $H_{air,sat}$  is determined by:

$$H_{air,sat} = 5.5638e^{0.0572T_{air}}. \quad (7)$$

$\epsilon$  and  $r_s$  can be obtained by:

$$\epsilon = 0.7584e^{0.0518T_{air}}, \quad (8)$$

$$r_s = (82 + 570e^{-\gamma \frac{R_n}{LAI}})(1 + 0.023(T_{air} - 20)^2), \quad (9)$$

where  $\gamma$  is a crop parameter,  $R_n$  represents the net radiation at crop level.

$$R_n = 0.86(1 - e^{-0.7LAI})(Q_{sun} + P_E), \quad (10)$$

where  $P_E$  is the power of lighting.

$$Q_{lamp} = \eta P_E, \quad (11)$$

where  $\eta$  is the lamp heating coefficient.

$$Q_{vent} = g_v \rho_{air} C_{p,air} (T_{air} - T_{out}), \quad (12)$$

where  $g_v$  represents the ventilation rate,  $\rho_{air}$  represents the air density,  $C_{p,air}$  represents the air heat capacity.

### 2.2.2. Relative humidity

The relative humidity  $RH_{air}$  is determined as follows:

$$RH_{air} = H_{air}/H_{air,sat}, \quad (13)$$

where  $H_{air}$  is the air vapour concentration and can be calculated by:

$$\frac{dH_{air}}{dt} = \frac{1}{h}(H_{trans} - H_{cov} - H_{vent}), \quad (14)$$

where  $H_{trans}$  is the vapour produced by plant transpiration,  $H_{cov}$  is the vapour condensation to the cover and  $H_{vent}$  is the vapour flux caused by ventilation.  $h$  is the greenhouse height.

$H_{trans}$  can be described by:

$$H_{trans} = g_e(H_{crop} - H_{air}). \quad (15)$$

$H_{cov}$  can be obtained by:

$$H_{cov} = g_c \left[ 0.2522e^{0.0485T_{air}}(T_{air} - T_{out}) - (H_{air,sat} - H_{air}) \right], \quad (16)$$

where  $g_c$  is the condensation.  $g_c$  can be obtained by:

$$g_c = \begin{cases} 0 & \text{if } T_{air} \leq T_{out} \\ p_{gc}(T_{air} - T_{cov})^{1/3} & \text{if } T_{air} > T_{out}, \end{cases} \quad (17)$$

where  $p_{gc}$  is a coefficient determined surface characteristics.

$H_{vent}$  can be obtained by:

$$H_{vent} = g_v(H_{air} - H_{out}), \quad (18)$$

where  $g_v$  is the ventilation rate.

### 2.2.3. CO<sub>2</sub> concentration

For the greenhouse system, CO<sub>2</sub> supplement is through greenhouse ventilation and CO<sub>2</sub> injection. CO<sub>2</sub> loss is due to the assimilation of crops. The CO<sub>2</sub> concentration model is given by:

$$\frac{dC_{air}}{dt} = \frac{1}{h}(C_{inj} - C_{ass} - C_{vent}), \quad (19)$$

where  $C_{air}$  is the CO<sub>2</sub> concentration inside the greenhouse,  $C_{inj}$  is the CO<sub>2</sub> injection rate,  $C_{ass}$  is the CO<sub>2</sub> assimilation,  $C_{vent}$  is the changes in CO<sub>2</sub> concentration due to ventilation.

$C_{ass}$  and  $C_{vent}$  can be obtained by:

$$C_{ass} = 2.2 \times 10^{-3} \frac{1}{1 + \frac{0.42}{C_{air}}} (1 - e^{-0.003(Q_{sun} + P_E)}), \quad (20)$$

$$C_{vent} = g_v(C_{air} - C_{out}). \quad (21)$$

### 2.2.4. Incoming radiation power

Solar radiation power is an important environmental factor affecting crop growth. The calculation of incoming radiation power  $Q_{sun}$  can be found in Equation (2) and will not be repeated in this section.

### 2.3. Greenhouse irrigation model

In this study, the drip irrigation method is used. The amount of water consumed for irrigation is equal to the evapotranspiration of crops. The dynamic model of the greenhouse irrigation can be expressed as:

$$\frac{dI_{con}}{dt} = ET, \quad (22)$$

where  $I_{con}$  represents the amount of water consumed for irrigation,  $ET$  represents the crop evapotranspiration.

$$ET = k_c \times \frac{0.408\Delta R_n + \gamma \frac{1713}{T_{air} + 273}(e_s - e_a)}{\Delta + 1.64\gamma}. \quad (23)$$

where  $k_c$  is the crop factor,  $\Delta$  is the slope of the vapor pressure curve,  $\gamma$  is the psychrometric constant,  $e_s$  is the saturation vapour pressure,  $e_a$  is the average vapour pressure.

$$\Delta = \frac{4098 \times e_s}{(T_{air} + 237.3)^2}, \quad (24)$$

$$e_a = e_s \times RH_{air}, \quad (25)$$

$$e_s = 0.6108 \times \exp\left(\frac{17.27 \times T_{air}}{T_{air} + 237.3}\right). \quad (26)$$

### 2.4. Model analysis

The validation of the greenhouse climate model used can be found in [35] and [36]. The performance analysis of the crop reference evapotranspiration model can be found in [37]. The authors collected data from greenhouses and compared it with the results predicted by the model. The results show that the predicted values can follow the actual values well. The model is verified to have good performance and can be used for optimization and control of greenhouse systems.

According to Equation (20), we can find that the CO<sub>2</sub> assimilation rate is related to the incoming solar radiation power and the CO<sub>2</sub> concentration. Figure 4 shows that the assimilation rate, i.e. crop CO<sub>2</sub> absorption rate, increases with the increase of temperature and radiation power. Therefore, the following methods can be used to increase the assimilation rate and reduce the CO<sub>2</sub> emissions of the greenhouse system: increasing the radiation power and CO<sub>2</sub> concentration. The incoming solar radiation power can be adjusted by controlling the greenhouse shading system. The CO<sub>2</sub> concentration can be adjusted by the CO<sub>2</sub> supply system. It should be noted that the effect of radiation power on the assimilation rate is greater than that of CO<sub>2</sub> concentration.

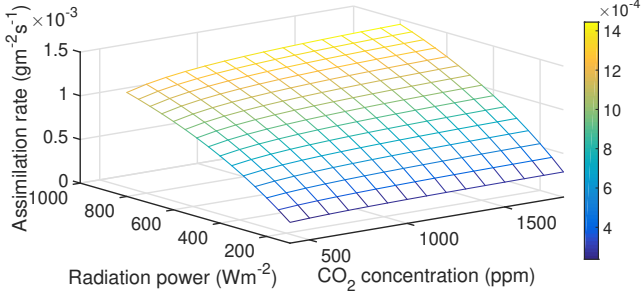


Figure 4: Crop assimilation rate

### 3. Optimization

The greenhouse operation optimization problem can be formulated as the optimization of greenhouse heating/cooling, ventilation, CO<sub>2</sub> supply and shading to achieve the set goals of reducing costs and carbon emissions while providing the desired environment for crop growth. The following will explain the optimization problem from four aspects: decision variables, objectives, constraints and optimization methods.

#### 3.1. Decision variables

This study takes into consideration the control of greenhouse heating, ventilation, CO<sub>2</sub> supply and shading systems. Decision variables include  $Q_c$ ,  $g_v$ ,  $C_{inj}$  and  $s_r$ .

#### 3.2. Objectives

The proposed optimization method considers economic costs and the environmental impact of greenhouse operation. Greenhouse operation planning considers two objectives: greenhouse operating costs and carbon emissions.

##### 3.2.1. Operating costs

The calculation of greenhouse operating costs  $C_{oper}$  takes into account greenhouse heating, ventilation, CO<sub>2</sub> supply and irrigation. These costs can be divided into two categories: the cost of electricity consumed and the cost of CO<sub>2</sub> supplied.  $C_{oper}$  can be calculated by:

$$C_{oper} = C_{elec} + C_{carb} \quad (27)$$

where  $C_{elec}$  is the cost of electricity consumed,  $C_{carb}$  is the cost of CO<sub>2</sub> supplied.  $C_{elec}$  can be calculated by:

$$C_{elec} = C_h + C_v + C_i, \quad (28)$$

where  $C_h$  is the cost of greenhouse heating and cooling,  $C_v$  is the cost of ventilation,  $C_i$  is the cost of irrigation.

$$C_h = \int_{t_i}^{t_f} Q_c(t)p(t)Sdt, \quad (29)$$

$$p(t) = \begin{cases} p_o & t \in [0, 6] \cup [22, 24] \\ p_s & t \in [9, 17] \cup [19, 22], \\ p_p & t \in [6, 9] \cup [17, 19] \end{cases} \quad (30)$$

where  $S$  is the greenhouse area,  $p$  is the electricity price. It should be pointed out that the time-of-use (TOU) tariff is used.  $p_o$ ,  $p_s$  and  $p_p$  represent electricity price during the off-peak, standard and peak period, respectively.

$$C_v = \int_{t_i}^{t_f} g_v(t)p(t)\frac{Q_f S}{V_f}dt, \quad (31)$$

where  $Q_f$  is the rated power of the ventilation fan,  $V_f$  is ventilation volume per hour at rated power.

In this study, the irrigation uses free groundwater. The irrigation cost refers to the operating cost of the water pump. As shown in Figure 3, the water pumped from the ground will first be stored in a reservoir and then supplied to the greenhouse according to the needs of the crops. It should be pointed out that the storage capacity of the reservoir can meet the water needs of the crops in the greenhouse for one day. Therefore, the water pumping is carried out during the off-peak period to reduce the irrigation cost.  $C_i$  can be calculated by:

$$C_i = p_o Q_p \frac{I_{con}}{V_p}, \quad (32)$$

$$I_{con} = \int_{t_i}^{t_f} ET(t)dt, \quad (33)$$

where  $Q_p$  is the rated power of the pump,  $V_p$  is the volume of water pumped by the pump per hour at rated power,  $I_{con}$  is the volume of water consumed by the greenhouse irrigation.

$C_{carb}$  can be obtained by:

$$C_{carb} = \int_{t_i}^{t_f} p_c C_{inj}(t)Sdt, \quad (34)$$

where  $p_c$  is the price of supplied CO<sub>2</sub>.

##### 3.2.2. CO<sub>2</sub> emissions

This study focuses on carbon emissions caused by energy use in the greenhouse system, while other greenhouse gases such as N<sub>2</sub>O and CH<sub>4</sub> produced are

not considered. Carbon emissions are determined by the CO<sub>2</sub>-eq emissions from electricity consumed, negative emissions from CO<sub>2</sub> absorbed and soil respiration. The impact of soil respiration on carbon emissions is small compared to other factors considered. To simplify modeling, soil respiration is not included. The CO<sub>2</sub> emissions model can be expressed as:

$$C_{emis} = C_{equi} - C_{abso}, \quad (35)$$

$$C_{equi} = k_{eq}E_{elec}, \quad (36)$$

$$E_{elec} = \int_{t_i}^{t_f} (Q_c(t)S + Q_v(t)S + \frac{Q_p ET(t)}{V_p}) dt, \quad (37)$$

$$C_{abso} = \int_{t_i}^{t_f} C_{assi}(t)S dt, \quad (38)$$

where  $C_{equi}$  is the CO<sub>2</sub>-eq emissions of the consumed energy, which is determined by the electrical energy consumed  $E_{elec}$  and the grid emission factor  $k_{eq}$ .  $k_{eq}$  represents the CO<sub>2</sub> emissions per kilowatt-hour of electricity generated.

### 3.3. System constraints

For greenhouse cultivation, the greenhouse environmental factors (state variables) should be maintained within appropriate ranges, otherwise the yield of crops will decrease. For example, too high temperature will cause crop wilting or even death, and too low CO<sub>2</sub> concentration will reduce the rate of photosynthesis of crops. The constraints of these state variables can be set by growers according to their own experience, and can also be obtained through the optimization of greenhouse crop yields or profits.

#### 3.3.1. State constraints

The state constraints are as follows:

$$T_{air}^{min} \leq T_{air} \leq T_{air}^{max}, \quad (39)$$

$$RH_{air}^{min} \leq RH_{air} \leq RH_{air}^{max}, \quad (40)$$

$$C_{air}^{min} \leq C_{air} \leq C_{air}^{max}, \quad (41)$$

where  $T_{air}^{min}$ ,  $RH_{air}^{min}$  and  $C_{air}^{min}$  are the lower limits of temperature, relative humidity and CO<sub>2</sub> concentration, respectively.  $T_{air}^{max}$ ,  $RH_{air}^{max}$  and  $C_{air}^{max}$  are the upper limits of temperature, relative humidity and CO<sub>2</sub> concentration, respectively.

It should be pointed out that greenhouse shading is only carried out when the incoming solar radiation power is greater than the set lower limit value  $Q_{sun}^{min}$ . Moreover, the incoming solar radiation power value

after shading control should be greater than  $Q_{sun}^{min}$ . The constraints of the shading rate can be given by:

$$\begin{cases} s_r = 0 & \text{if } Q_{sun} \leq Q_{sun}^{min} \\ 0 < s_r \leq 1, Q_{sun}^{min} \leq Q_{sun}(1 - s_r) & \text{if } Q_{sun} > Q_{sun}^{min} \end{cases} \quad (42)$$

#### 3.3.2. Input constraints

The input constraints are as follows:

$$Q_c^{min} \leq Q_c \leq Q_c^{max}, \quad (43)$$

$$g_v^{min} \leq g_v \leq g_v^{max}, \quad (44)$$

$$C_{inj}^{min} \leq C_{inj} \leq C_{inj}^{max}, \quad (45)$$

$$s_r^{min} \leq s_r \leq s_r^{max}, \quad (46)$$

where  $Q_c^{min}$ ,  $g_v^{min}$ ,  $C_{inj}^{min}$  and  $s_r^{min}$  are the lower limits of heating/cooling power, ventilation rate, CO<sub>2</sub> supply rate and shading rate, respectively.  $Q_c^{max}$ ,  $g_v^{max}$ ,  $C_{inj}^{max}$  and  $s_r^{max}$  are the upper limits of heating/cooling power, ventilation rate, CO<sub>2</sub> supply rate and shading rate, respectively.  $k$  represents the  $k$ th sampling interval.

To reduce the actuator wear caused by frequent changes, the rate of change constraints should be considered.

$$\left| \frac{Q_c}{dt} \right| \leq k_1, \quad (47)$$

$$\left| \frac{g_v}{dt} \right| \leq k_2, \quad (48)$$

$$\left| \frac{C_{inj}}{dt} \right| \leq k_3, \quad (49)$$

$$\left| \frac{s_r}{dt} \right| \leq k_4, \quad (50)$$

where  $k_1$ ,  $k_2$ ,  $k_3$  and  $k_4$  are the maximum change rates of  $Q_c$ ,  $g_v$ ,  $C_{inj}$  and  $s_r$ , respectively.

### 3.4. Optimization methods

#### 3.4.1. Analysis of optimization methods

This study considers two conflicting objectives: operating costs and carbon emissions. Therefore, a multi-objective optimization method can be used. The multi-objective optimization problem is formulated as:

Minimize:

$$F(\vec{x}) = [f_1(\vec{x}), f_2(\vec{x})]^T, \quad (51)$$



subject to:

$$\begin{cases} g_i(\vec{x}) \leq 0, i = 1, 2, \dots, p \\ h_j(\vec{x}) = 0, j = 1, 2, \dots, q \end{cases}, \quad (52)$$

where  $\vec{x} = [x_1, x_2, \dots, x_n]^T$  represents the decision variables,  $f_1$  and  $f_2$  are objective functions,  $g_i$  is the function of the inequality constraint,  $h_j$  is the function of the equality constraint.

It should be pointed out that solving a multi-objective optimization problem could be computationally complex. If the multi-objective optimization method is adopted, the greenhouse should be equipped with a powerful control system that can deal with complex calculation problems. In addition, if the weighted sum method is used, growers will be required to have extensive experience in determining weight factors of different objectives.

#### 3.4.2. Single objective (total cost) optimization

In this study, a single objective optimization approach is proposed to reduce the total cost including the operating costs and the cost of carbon emissions. This method solves the problems of computationally intensive for obtaining the Pareto frontier of a multi-objective optimization problem and the difficulty of selecting weights for different objectives in the weighted sum method.

The grid emission factor is introduced to calculate the CO<sub>2</sub>-eq emissions of the electrical energy consumed by the greenhouse system. The SCC is used to quantify the impact of carbon emissions on the environment as cost. The objective function can be expressed as:

$$J = C_{oper} + C_{emis}SCC. \quad (53)$$

It should be pointed out that the calculation of SCC is not the focus of our research. In this paper, a value of \$50 per ton, which is very close to the value given by the US government (\$51 per ton), is adopted. The optimization problem can be formulated as: to minimize  $J$  and subject to constraints (39) to (50).

## 4. Economic model predictive control

In this paper, an EMPC method for greenhouse operation management is studied. The EMPC strategy is widely used in building energy management and has achieved good economic and control performance [38].

### 4.1. Hierarchical control structure

The proposed method consists of an optimization layer and a control layer. At the optimization layer, an optimization strategy is proposed to minimize the total cost including the operating costs and the cost of carbon emissions. The optimization results are taken as reference trajectories of the control layer. At the control layer, an MPC controller is designed to follow the reference trajectories obtained from the optimization layer.

### 4.2. Open loop controller

The state-space model can be expressed as:

$$x_o(k+1) = f_o(x_o(k), u_o(k)), \quad (54)$$

where  $x_o$  is the state variable,  $u_o$  is the input variable,  $u_o(k) = [Q_c(k), g_v(k), C_{inj}(k), s_r(k)]^T$ ,  $x_o(k) = [T_{air}(k), RH_{air}(k), C_{air}(k), Q_{sun}(k)]^T$ ,  $k$  represents the current time  $kT_o$ ,  $T_o$  is the optimization sampling interval,  $f_o(\cdot)$  is the nonlinear functions that represent the greenhouse system model obtained from Equations (1) to (26). The optimization objective function  $J_o$  is derived from Equation (53) and can be expressed as:

$$\begin{aligned} J_o = & \sum_{k=1}^{N_o} ( (|Q_c(k)| + \lambda_v g_v(k)) p(k) S + p_o Q_p \frac{ET(k)}{V_p} \\ & + C_{inj}(k) p_c S + SCC(k_{eq}(Q_c(k) S + \frac{Q_f}{V_f} g_v(k) S \\ & + \frac{Q_p ET(k)}{V_p}) - C_{assi}(k) S), \end{aligned} \quad (55)$$

where  $N_o$  is the total number of samples for the optimization. Please note that how  $ET$  is affected by the decision variable  $s_r$  can be found in Equations (2) and (23) to (26).

The rate of change constraints for the optimization can be given by:

$$\begin{cases} |Q_c(k+1) - Q_c(k)| \leq k_1 T_o \\ |g_v(k+1) - g_v(k)| \leq k_2 T_o \\ |C_{inj}(k+1) - C_{inj}(k)| \leq k_3 T_o \\ |s_r(k+1) - s_r(k)| \leq k_4 T_o \end{cases} \quad (56)$$

The total cost optimization controller solves the following problem:

$$u_o^* = \arg \min_{u_o} J_o, \quad (57)$$

subject to the constraints (39) to (46) and (56). It should be pointed out that the corresponding state

$x_o^*$  can be calculated according to the obtained input  $u_o^*$  and the model (54). The obtained  $x_o^*$  will be taken as the reference trajectories  $x_{ref}$  for the controller at the control layer.

### 4.3. MPC controller

The state-space model is given by:

$$x_m(m+1) = f_m(x_m(m), u_m(m)), \quad (58)$$

where  $x_m$  is the state variable,  $u_m$  is the input variable,  $x_m(m) = [T_{air}(m), RH_{air}(m), C_{air}(m), Q_{sun}(m)]^T$ ,  $u_m(m) = [Q_c(m), g_v(m), C_{inj}(m), s_r(m)]^T$ .  $m$  represents the current time  $mT_m$ ,  $T_m$  is the sampling interval for MPC.  $T_m = T_o/N_s$ ,  $N_s$  is a positive integer. The total number of samples  $N_m$  can be calculated by:  $N_m = N_s \times N_o$ .

For time  $t_m \in [m_1T + m_2T_m, m_1T + (m_2+1)T_m]$ ,  $m_1 = 0, 1, 2, \dots, N_o-1$ ,  $m_2 = 0, 1, 2, \dots, N_m-1$ , the MPC controller is to follow the reference trajectories  $x_{ref}(m_1+1)$ . The objective function can be expressed as:

$$J_m = \sum_{i=1}^{N_p} (\Delta x_m(k+i|k))^T Q (\Delta x_m(k+i|k)) + \sum_{i=0}^{N_c-1} (\Delta u_m(k+i|k))^T R (\Delta u_m(k+i|k)), \quad (59)$$

where  $N_p$  and  $N_c$  represent the prediction horizon and control horizon, respectively.  $|k$  means that the predicted value is based on the information up to time  $k$ .  $\Delta x_m$  represents the tracking error.  $\Delta u_m$  represents the control effort.  $Q$  and  $R$  are the weighting matrices that penalize the future tracking and control efforts, respectively [39].  $\Delta x_m(k+i|k)$  and  $\Delta u_m(k+i|k)$  can be calculated by:

$$\Delta x_m(k+i|k) = x_m(k+i|k) - x_{ref}(k+i), \quad (60)$$

where  $x_{ref}$  represents the reference trajectories.

$$\Delta u_m(k+i|k) = \begin{cases} u_m(k+i|k) - u_m(k-1), & i=0 \\ u_m(k+i|k) - u_m(k+i-1|k), & i=1, 2, \dots, N_c-1. \end{cases} \quad (61)$$

The rate of change constraints can be given by:

$$\begin{aligned} |Q_c(k+1) - Q_c(k)| &\leq k_1 T_m \\ |g_v(k+1) - g_v(k)| &\leq k_2 T_m \\ |C_{inj}(k+1) - C_{inj}(k)| &\leq k_3 T_m \\ |s_r(k+1) - s_r(k)| &\leq k_4 T_m \end{aligned} \quad (62)$$

Define vector

$U = [u_m(k|k), u_m(k+1|k), u_m(k+2|k), \dots, u_m(k+N_c-1|k)]^T$ . The MPC controller solves the following problem:

$$U^*(k) = \arg \min_U J_m(k), \quad (63)$$

subject to the constraints (39) to (46) and (62).

The greenhouse EMPC procedure can be described by the pseudo code of Algorithm 1.

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#### Algorithm 1: EMPC algorithm

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Solve the open loop optimization problem

formulated in Equation (57);

Take the optimization results as the reference trajectories of model predictive control;

**while**  $k \leq N_m - N_p$  **do**

    Calculate the value of  $U$  by solving the optimal problem (63);

    Implement the first element in  $U$  and ignore the rest;

    Calculate the state of next interval;

$k = k + 1$ ;

**end**

**while**  $k > N_m - N_p$  **do**

$N_p = N_p - 1$ ;

    Calculate the value of  $U$  by solving the optimal problem (63);

    Implement the first element in  $U$  and ignore the rest;

    Calculate the state of next interval;

$k = k + 1$ ;

**end**

---

## 5. Simulation

### 5.1. Simulation data

The meteorological data used comes from a weather station at the University of Pretoria. The weather data for July 1, 2020, is adopted and shown in Figure 5. The system constraints are listed in Table 1. The model parameters are listed in Table 2.

### 5.2. Optimization results

The optimization problems are solved by the ‘fmincon’ function with the ‘interior-point’ algorithm in the MATLAB environment.

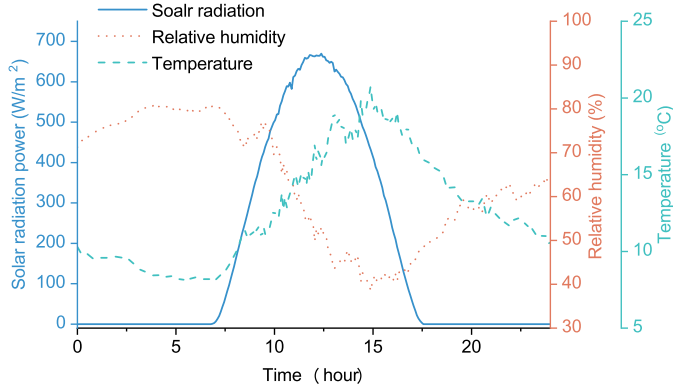


Figure 5: Meteorological data for July 1, 2020

Table 1: Greenhouse system constraints

Variable	Value	Unit
$T_{air}^{min}$	14	°C
$T_{air}^{max}$	26	°C
$RH_{air}^{min}$	0	%
$RH_{air}^{max}$	90	%
$C_{air}^{min}$	400	ppm
$C_{air}^{max}$	2000	ppm
$Q_c^{min}$	-200	$Wm^{-2}$
$Q_c^{max}$	200	$Wm^{-2}$
$g_v^{min}$	0	$ms^{-1}$
$g_v^{max}$	0.02	$ms^{-1}$
$C_{inj}^{min}$	0	$gm^{-2}s^{-1}$
$C_{inj}^{max}$	0.02	$gm^{-2}s^{-1}$
$k_1$	0.17	$Wm^{-2}s^{-1}$
$k_2$	$1.67 \times 10^{-5}$	$ms^{-2}$
$k_3$	$1.67 \times 10^{-5}$	$gm^{-2}s^{-2}$
$k_4$	$3.33 \times 10^{-4}$	$s^{-1}$

### 5.2.1. Optimization results of the proposed method

The optimization results of the proposed method are shown in Figure 6. Sub figures 1 to 4 show the heating/cooling power, ventilation rate, CO<sub>2</sub> injection rate and shading rate, respectively. Sub figures 5 to 8 show the temperature, relative humidity, CO<sub>2</sub> concentration and incoming solar radiation power, respectively.

From sub-figure 1, we can find that greenhouse heating mainly occurs in the morning when the greenhouse temperature has gradually decreased to the set lower limit and the solar radiation power during this period is low. Therefore, the greenhouse should be heated to maintain the temperature within the specified range (between 14 °C and 26 °C). From sub-figure 2, we can see that the ventilation mainly occurs at noon when the outdoor temperature is high. The energy loss caused by the ventilation process can be reduced. From sub-figure 3, we can see that the CO<sub>2</sub>

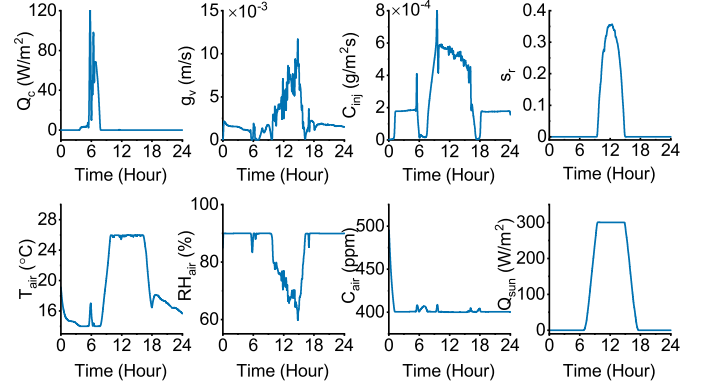


Figure 6: Optimization results of the proposed method

injection rate is low. The CO<sub>2</sub> concentration in the greenhouse is kept at a low level that is close to the lower limit of 400 ppm. The reason is that the low CO<sub>2</sub> supply rate helps achieve the goal of reducing operating costs. From sub-figure 4, we can find that the shading control is only performed when the solar radiation power is greater than 300 W/m<sup>2</sup>. From sub-figures 5 to 8, we can see that temperature, relative humidity, CO<sub>2</sub> concentration and incoming solar radiation power are kept within specified ranges.

### 5.2.2. Comparison between the proposed method and the baseline

In this study, a greenhouse operation method to minimize the operation cost, which is often used in greenhouse management, is taken as the baseline. The study of the baseline method can be found in [40] and [41]. The objective function of the baseline method can be expressed as Equation (27). The optimization results are shown in Figure 7. Table 3 shows the comparison between the proposed method and the baseline method.

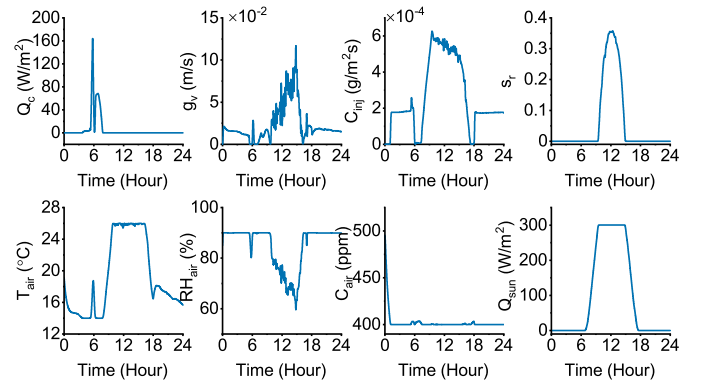


Figure 7: Optimization results of the baseline method

Table 2: Greenhouse model parameters

Parameter	Value	Unit	Parameter	Value	Unit
$\alpha_1$	0.7	—	$p_{gc}$	$1.8 \times 10^{-3}$	$\text{m}^\circ\text{C}^{-1/3}\text{s}^{-1}$
$\alpha_2$	10	$\text{Wm}^{-2}\text{C}^{-1}$	$p_o$	0.5157	R/kWh
$\gamma$	0.008	—	$p_s$	0.9446	R/kWh
$LAI$	2.6	—	$p_p$	3.1047	R/kWh
$C_{cap}$	30000	$\text{Jm}^{-2}\text{C}^{-1}$	$\lambda$	0.06	$\text{Wm}^{-3}$
$h$	7	m	$\eta$	0.75	—
$s$	40709	$\text{m}^2$	$g$	9.8	$\text{ms}^{-2}$
$L$	2450	$\text{Jg}^{-1}$	$h_w$	7	m
$r_b$	150	$\text{sm}^{-1}$	$\omega_3$	1000	R/ton
$\rho_{air}$	1.225	$\text{kgm}^{-3}$	$K_c$	0.7	—
$C_{p,air}$	1003	$\text{J}^\circ\text{C}^{-1}\text{kg}^{-1}$	$SCC$	50	\$/ton
$k_{eq}$	0.879	$\text{kg/kWh}$	$Q_p$	3	kW
$V_p$	10	$\text{m}^3$	$Q_f$	0.3	kW
$V_f$	5000	$\text{m}^3$			

Table 3: Comparison between the proposed method and the baseline method

Methods	Operating costs (Rand)	Carbon emissions (ton)	Total cost (Rand)
Baseline	12910	5.05	17288
Proposed	13096	3.89	16461

It can be observed that the operating costs, carbon emissions and total cost of the baseline method are R12910, 5.05 tons and R17288, respectively. The operating costs, carbon emissions and total cost of the proposed method are R13096, 3.89 tons and R16461, respectively. Compared with the baseline method, the proposed method increases the operating costs by R186 but reduces the total cost by R827 and the carbon emissions by 1.16 tons.

Figure 8 shows the total cost composition of the proposed method and the baseline. It can be observed that the cost of heating and cooling is the highest among all cost components, followed by the cost of carbon emissions, the cost of CO<sub>2</sub> supply, and the cost of irrigation. Moreover, there is little difference between the ventilation cost, irrigation cost and CO<sub>2</sub> supply cost of the two methods. However, the carbon emission cost and heating/cooling cost of the two methods are quite different. Compared with the baseline method, the proposed method increases the heating/cooling cost by R194 and reduces the CO<sub>2</sub> emission cost by R1011.

### 5.2.3. Optimization based on different weather data

To make the conclusion more convincing, we studied the proposed optimization method based on different meteorological data. In this paper, the meteo-

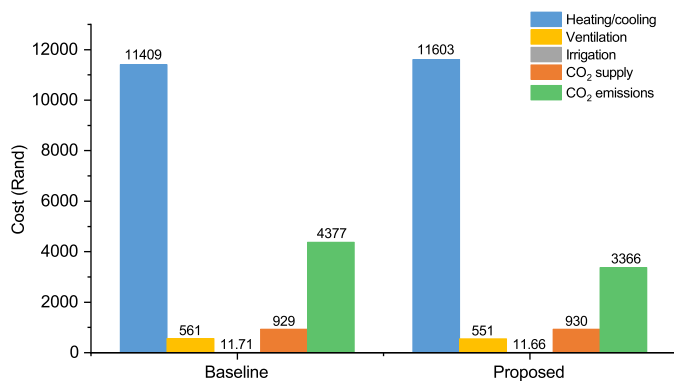


Figure 8: Total cost composition

rological data from July 2, 2020 to July 8, 2020 are used and shown in Figure 9. Figure 10 shows the optimization results.

We can find that the results obtained are similar to the optimization results shown in Figure 8. The cost of the greenhouse heating and cooling is the highest, followed by the cost of carbon emissions, the cost of CO<sub>2</sub> supply, the cost of ventilation and the cost of irrigation. It should be pointed out that the total cost of the greenhouse on July 3 and July 4 is lower than the cost on other dates. The reason is that the temperature in these two days is higher than that in other days. Less energy is consumed for heating, which reduces costs.

### 5.3. Sensitivity analysis

Sensitivity analysis can provide insight into the impact of model parameter uncertainty on the optimization results [42]. In this study, the impact of changes in electricity price, supplied CO<sub>2</sub> price and

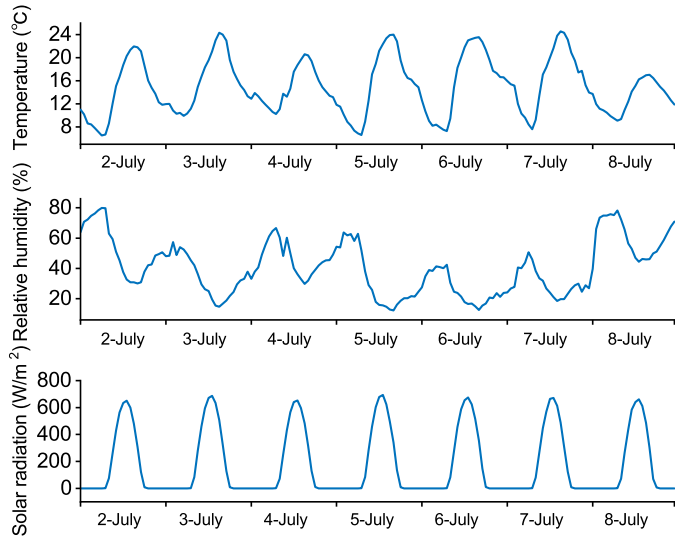


Figure 9: Meteorological data from July 2, 2020 to July 8, 2020

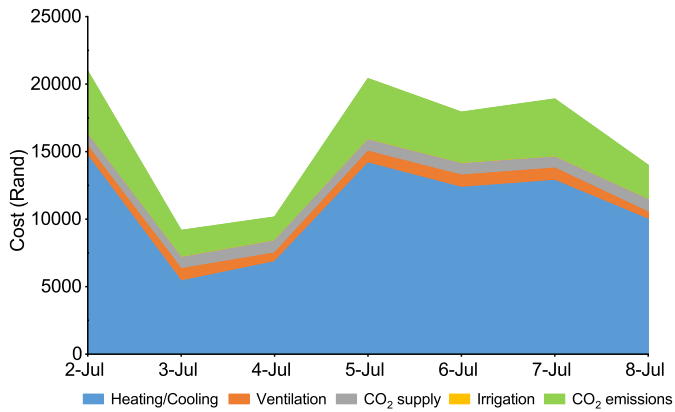


Figure 10: Optimization results of the proposed method with one week data

SCC on the total cost is analyzed. The changes of these parameters are -10%, -5%, 5% and 10% of the corresponding initial values, respectively. The results of the sensitivity analysis are shown in Figure 11.

We can find that the total cost increases with the increase of the electricity price, supplied CO<sub>2</sub> price and SCC. Among the three parameters analyzed, SCC has the greatest impact on the total cost, followed by electricity price, and the supply CO<sub>2</sub> price has the least impact on the total cost. The optimization results are more sensitive to changes in SCC than changes in electricity prices and supply CO<sub>2</sub> prices.

#### 5.4. Model predictive control

The parameters of the proposed MPC are as follows:  $N_c = N_p = 5$ ,  $Q = \text{diag}(100, 100, 100, 100)$ ,  $R = \text{diag}(1, 1, 1, 1)$ . The results of the proposed MPC

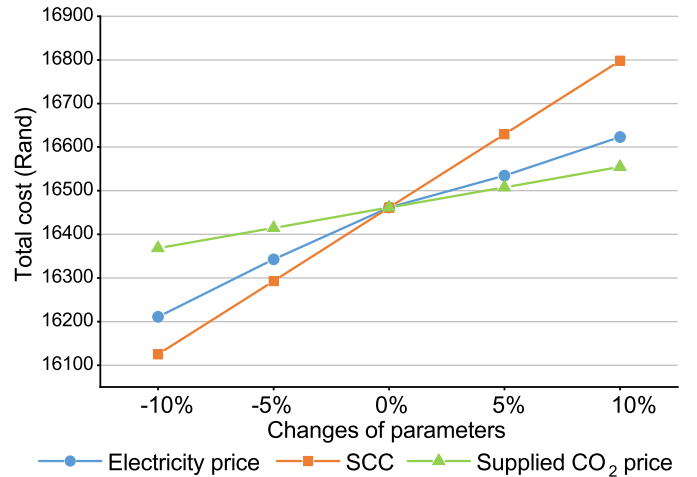


Figure 11: Results of the conducted sensitivity analysis

under three levels (1%, 5% and 10%) of system disturbances are shown in Figure 12.

In Figure 12, the red line, the yellow line, and the blue line represent the control results under 1%, 5% and 10% system disturbances, respectively. It can be seen that the designed MPC controller can well track the reference trajectories of temperature, relative humidity, CO<sub>2</sub> concentration and solar radiation power under different levels of system disturbances. The trajectories of the greenhouse environmental factors studied under MPC vary between small ranges around the corresponding reference trajectories.

The MPC tracking errors are listed in Table 4. We can find that the larger the system disturbance, the larger the average tracking error of the MPC controller designed. Moreover, the tracking errors under the three levels of system disturbances are small. For example, under 10% system disturbances, the average errors of tracking the reference trajectory of temperature, relative humidity, CO<sub>2</sub> concentration and incoming solar radiation power are 8.27%, 6.90%, 5.37% and 5.01%, respectively. The designed MPC controller is verified to have good control performance. Similar findings can be found in [43].

Table 4: The average tracking error of MPC under different levels of system disturbances

Environmental factors	Average tracking error		
	1%	5%	10%
Temperature (°C)	0.66%	3.40%	8.27%
Relative humidity (%)	0.70%	3.22%	6.90%
CO <sub>2</sub> concentration (ppm)	0.51%	2.63%	5.73%
Radiation power (W/m <sup>2</sup> )	0.52%	2.50%	5.01%

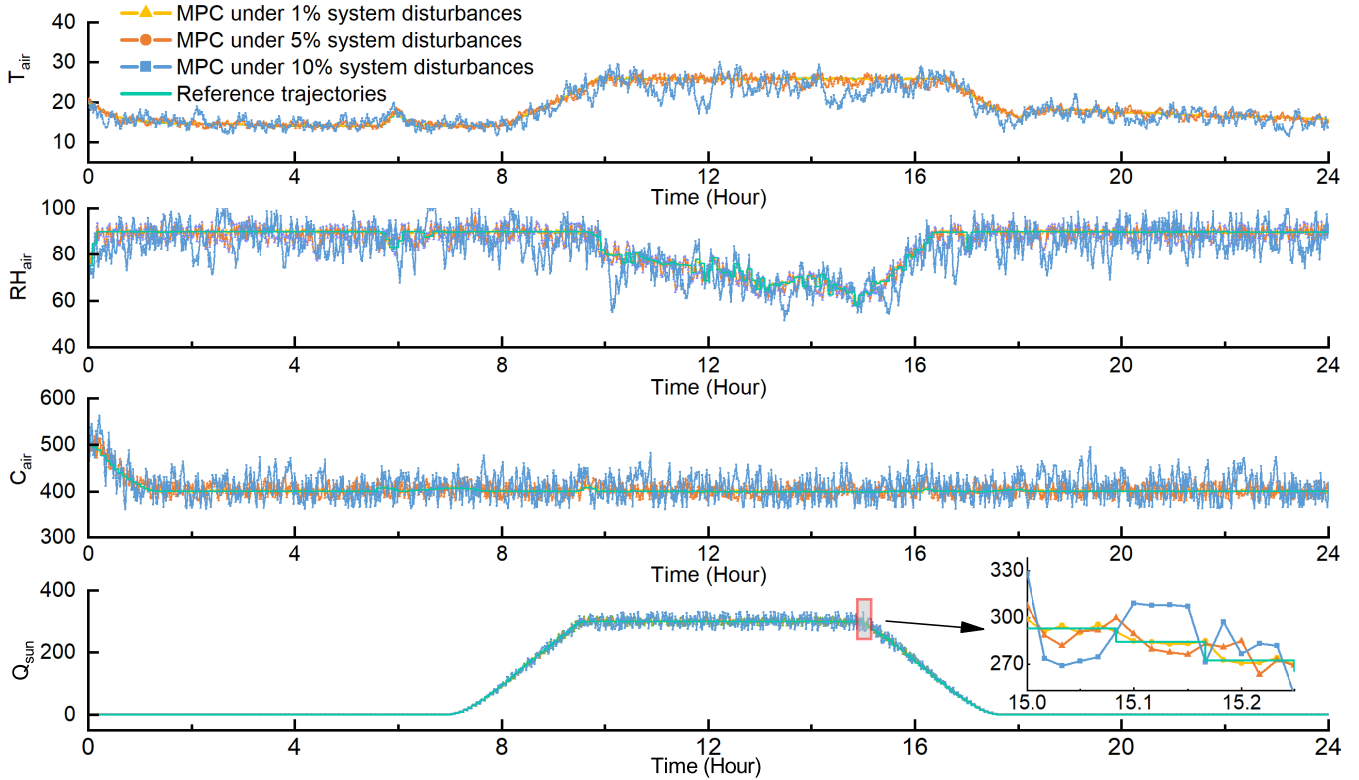


Figure 12: Results of MPC under different levels of system disturbances

## 6. Conclusions

In this paper, an economic model predictive control (EMPC) method is proposed for the operation optimization of a greenhouse system. The objective is to manage the greenhouse energy-water-carbon-food (EWCF) nexus for cleaner production and sustainable development. The proposed method consists of an optimization layer and a control layer. At the optimization layer, an optimization method to minimize the total cost of greenhouse heating/cooling, ventilation, carbon dioxide ( $\text{CO}_2$ ) supply and irrigation is studied. A sensitivity analysis is carried out to study the impact of the electricity price, supplied  $\text{CO}_2$  price and social cost of carbon (SCC) on the total cost. At the control layer, a model predictive control (MPC) method is used to address system disturbances. The proposed approach is studied based on meteorological data from Pretoria, South Africa.

Simulation results show that the proposed method can effectively reduce the total cost and carbon emissions of greenhouse operations while keeping greenhouse environmental factors (temperature, relative humidity,  $\text{CO}_2$  concentration and incoming solar radiation power) within the required ranges. Compared with a baseline method that minimizes the operating

costs, the proposed method increases the operating costs by R186 but reduces the total cost by R827 and the carbon emissions by 1.16 tons. In addition, the total cost increases with the increase of the electricity price, supplied  $\text{CO}_2$  price and SCC. The optimization is more sensitive to changes in SCC than changes in electricity price and supply  $\text{CO}_2$  price. Moreover, the designed MPC controller has good control performance and can deal with system disturbances well.

The proposed method can help achieve low-cost and cleaner greenhouse crop production, which provides a feasible solution to the challenges of poverty, food insecurity and climate change in South Africa. In addition, the proposed approach can be applied to different types of greenhouses in different countries. In future work, we will focus on the following aspects: 1) Energy-water-land-food nexus. Greenhouse operation planning needs to consider trade-offs between economic, resource and environmental concerns. Resources such as energy, water and land are critical to food production. How to use less energy and water resources to get more food in limited land is of great significance for alleviating the resource crisis and achieving sustainable development. 2) Using clean energy to power greenhouses. The use of

clean energy such as wind energy and solar energy can not only alleviate the energy crisis but also reduce the adverse impact of greenhouse operations on the environment. 3) Experimental validation of the proposed method. We will verify the effectiveness of the proposed method through experiments in future research.

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