Competition Reaction Based Prediction of Polyamines' Stepwise Protonation Constants: a Case Study Involving 1,4,7,10 tetrazadecane (2,2,2-tet)

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Supplementary Information

PART 1

Comments on conformational search procedure and competition reactions considered.

For both 3,2,3-tet and 2,2,2-tet, when the implicit solvation model was to be implemented, we varied each rotatable bond in steps of 60^0 each and retained thirty lowest energy LECs. These were fully optimized using the implicit solvation model to describe solvent environment in order to locate representative set of LECs. In implementing the discrete continuum solvation model for 2,2,2-tet, we used a similar conformational search protocol to that which was implemented in the case of implicit solvation but only retained twenty LECs based on their relative MMFF(aq) energies because our previous conformational analysis of 2,2,2-tet indicated that its representative LECs would most likely be found among the ten LECs obtained from an MMFF(aq) based search of its conformational space.¹ However, since 3,2,3-tet has a greater number of rotatable bonds than 2,2,2-tet due to its longer alkyl chain length and there has been no conformational analysis work reported for it, we carried out the conformational search for its LECs in the presence of explicit solvent molecules in two stages. This was to enable us investigate which torsional angle increment (60° or 120°) is best for locating its low energy conformers:

- In the first stage, each rotatable bond was allowed to change in 60° steps and thirty unique lowest energy conformers were retained based on their relative MMFF(aq) energies.

- For the second stage rotation of bonds was allowed in 120° steps and thirty unique lowest energy conformers were also retained based on their relative MMFF(aq) energies.

Conformers obtained from both stages were combined and for each tautomer examined, only the thirty unique LECs out of sixty generated, were selected for further optimizations. After full optimization, a thorough examination and analysis of the final structures and energies of LECs generated for 3,2,3-tet showed that in general most of its lowest in energy conformers were from the MM-based conformational search when each rotatable bond was allowed to vary in steps of 120°. Hence, as pointed out in our previous work on 2,2,2-tet, to identify representative LECs of any given aliphatic polyamine, it is sufficient to vary its rotatable bonds in increments of 120° each.

As depicted in Scheme 1 in the main body of the text, which involves all possible protonation sites of 2,2,2-tet (here $L^{(1)}$) and 3,2,3-tet (here $L^{(2)}$) when they are singly protonated, one must consider a number of possible reactions which indeed might take place in a real competition experiment in a solution. To reflect this fact, a general form of competition reaction 1 can be expressed in the following forms

$$
L^{(1)} + HL^{(2)}_p = HL^{(1)}_p + L^{(2)} \qquad \Delta G^{(1)}_{HL^{(1)}_p,HL^{(2)}_p} \qquad (S1)
$$

$$
L^{(1)} + HL^{(2)}_p = HL^{(1)}_s + L^{(2)} \qquad \Delta G^{(1)}_{HL^{(1)}_s,HL^{(2)}_p}
$$
 (S2)

$$
L^{(1)} + HL_s^{(2)} = HL_p^{(1)} + L^{(2)}
$$
\n
$$
\Delta G_{\text{HL}_p^{(1)}, \text{HL}_s^{(2)}}^{(1)} \tag{S3}
$$

$$
L^{(1)} + HL_s^{(2)} = HL_s^{(1)} + L^{(2)}
$$
\n
$$
\Delta G_{HL_s^{(1)},HL_s^{(2)}}^{(1)} \tag{S4}
$$

$$
L^{(1)} + HL_{p}^{(2)} + HL_{s}^{(2)} = HL_{p}^{(1)} + L^{(2)}
$$
\n
$$
\Delta G_{HL_{p}^{(1)},HL_{p+s}^{(2)}}^{(1)} \tag{S5}
$$

$$
L^{(1)} + HL^{(2)}_{p} + HL^{(2)}_{s} = HL^{(1)}_{s} + L^{(2)} \qquad \Delta G^{(1)}_{HL^{(1)}_{s},HL^{(2)}_{p+s}} \qquad (S6)
$$

$$
L^{(1)} + HL^{(2)}_p = HL^{(1)}_p + HL^{(1)}_s + L^{(2)} \qquad \Delta G^{(1)}_{\text{HL}^{(1)}_{p+s}, \text{HL}^{(2)}_{p}} \qquad (S7)
$$

$$
L^{(1)} + HL_s^{(2)} = HL_p^{(1)} + HL_s^{(1)} + L^{(2)}
$$
\n
$$
\Delta G_{HL_{p+s}^{(1)},HL_s^{(2)}}^{(1)} \tag{S8}
$$

$$
L^{(1)} + HL^{(2)}_p + HL^{(2)}_s = HL^{(1)}_p + HL^{(1)}_s + L^{(2)} \qquad \Delta G^{(1)}_{\text{HL}_{p+s}^{\{1\}},\text{HL}_{p+s}^{(2)}} \tag{S9}
$$

where subscripts 's' and 'p' denote a primary and secondary N-atom of a ligand being protonated and the sequence of subscripts in the $\Delta G_{\text{CRn}}^{(1)}$ expressions shows tautomers of HL⁽¹⁾ and HL⁽²⁾ involved; their sequence follows the way $\Delta G_{\text{CRn}}^{(1)}$ is calculated ($G_{\text{products}} - G_{\text{reactants}}$) and, *e.g.*, for $\Delta G_{\text{CRn}}^{(1)} = \Delta G_{\text{ur}}^{(1)}$ $\Delta G_{\text{HL}_{p+s}^{(1)},\text{HL}_{p}^{(2)}}^{(1)}$ (expression S7) it means that two tautomers of a singly protonated polyamine under investigation, $HL_{p}^{(1)}$ and $HL_{s}^{(1)}$, and by default the free reference ligand $L^{(2)}$ were formed as a result of reaction between $L^{(1)}$ (by default) and the tautomer of the singly protonated reference polyamine with the primary N-atom being protonated, hence $\mathrm{HL}_\mathfrak{p}^{(2)}$.

1. Adeyinka, A.S.; Cukrowski, I.; *J. Mol Model.* **2015**, 21, 162.

Input structures used for the conformational search

Figure S1. Capped-stick representation of linear structures of $H_nLⁿ⁺$ forms of 2,2,2-tet with and without explicit water molecules used as inputs for conformational search by MM, also showing atoms' numbering: part (a) – L; part (b) – HL_{N1} (HL_p); part (c) – HL_{N2} (HL_s); part (d) – H_2L_{N1N3} (H_2L_{ps}) , part (e) – H_2L_{N1N4} (H_2L_{pp}); part (f) – H_3L_{N1N2N4} (H_3L_{psp}) and part (g) – H_4L .

6

Figure S2. Capped-stick representation of linear structures of $H_nLⁿ⁺$ forms of 3,2,3-tet with and without explicit water molecules respectively used as inputs for conformational search by MM, also showing atoms' numbering; -part (a) L, -part (b) $HL_{N1}(HL_p)$, -part (c) $HL_{N2}(HL_s)$, part (d) H_2L_{N1N3} (H_2L_{ps}) , -part (e) $H_2L_{N1N4}(H_2L_{pp})$, -part (f) H_3L_{N1N2N4} (H_3L_{psp}) and -part (g) H_4L .

PART 3

Comments on selection of a reference molecule used in the competition reaction

One must realize that it is also necessary to consider the selection of reference molecules in terms of resultant placement of charges among reactants and products. For instance, can one obtain better theoretical estimate of, *e.g.*, (i) the first protonation constant of $L^{(1)}$ using $HL^{(2)}$ or rather H₂L⁽²⁾ or (ii) the third protonation constants of H₂L⁽¹⁾ involving in the competition reaction $HL^{(2)}$, $H_2L^{(2)}$, $H_3L^{(2)}$, or rather $H_4L^{(2)}$? There is no easy way to predict this and, as an example, see Scheme S1 where (i) both products of the protonation competition reaction have exactly the same charge, (ii) the same number of tautomers for $L^{(1)}$ and $L^{(2)}$ is involved, but (iii) charges on reactants differ. This aspect has also been investigated in the present work in terms of accuracy in the computed protonation constants.

$$
H_{2}N-R-NH-R-NH-R-NH_{2}
$$
\n
$$
H_{2}N-R-NH-R-NH_{2}
$$
\n
$$
H_{2}N-R-NH-R-NH_{2}
$$
\n
$$
H_{2}N-R1-NH-R-NH-R1-NH_{2}
$$
\n
$$
H_{2}N-R1-NH-R1-NH-R1-NH_{2}
$$
\n
$$
H_{2}N-R1-NH-R1-NH-R1-NH_{2}
$$
\n
$$
H_{2}N-R1-NH-R1-NH-R1-NH_{2}
$$
\n
$$
H_{2}N-R-NH-R-NH_{2}
$$
\n
$$
H_{2}N-R1-NH-R1-NH-R1-NH_{2}
$$

 $\left\{\begin{array}{c} H_2N-R-NH-R-NH-R-NH_2 \ H^+ \ H_2N-R-NH-R-NH_2 \ H_3 \end{array}\right\} + \left\{\begin{array}{c} H_2N-R1-NH-R-NH-R1-NH_2 \ H^+ \ H_2 \end{array}\right\}$

Scheme S1 Possible tautomers of 2,2,2-tet and 3,2,3-tet $(R = -C_2H_4$ -; $R1 = -C_3H_6$) which were considered in the competition reaction based protocol when $L^{(1)}$ and $H_2L^{(2)}$ were employed to compute $\log K_{\rm H}^{\rm (1)}$ of ${\rm L}^{\rm (1)}.$

PART 4

Analysis of optimisation profiles

A thorough examination of the optimization profiles of hundreds of 2,2,2-tet conformers fully optimized in Gaussian revealed that there are common patterns when a relationship between electronic energy of a conformer after each optimization cycle and a step number was analysed: (i) a sharp decrease in *E* is observed in the first 3-5 steps in case of conformers which optimise within 10-15 steps; in such a case the relative energies of conformers generally do not change (Figure S3a), (ii) a major decrease in *E* is observed within first 10-15 optimization steps for each conformer and (iii) in many instances a large number of steps was required to reach convergence with insignificant energy change after 20-50*th* step (Figure S3b).

Figure S3. Examples of optimization profiles for selected conformers of 2,2,2-tet in CSM showing the change in the electronic energy E with the optimization step in cases of: part (a) - convergence reached within 15 optimization cycles, part (b) - convergence reached after large number of optimization cycles without (red triangles and black squares) and insignificant (blue circles) relative change of conformers' placement in their energy spectrum.

These observations provide a useful hint when one is interested only in the set of the lowest energy conformers needed to compute, *e.g.*, protonation constants; they are discussed in the main body of the text.

Lowest energy conformers discovered in the continuum solvation model, PCM.

Fig. S4. Structures of all lowest in energy conformers of the free ligand of 3,2,3-tet used to calculate protonation constants with continuum solvation model, PCM.

$$
C_{\rm s}01
$$

 $C_p 01$ $C_p 03$

Fig. S5. Structures of all lowest in energy conformers for HL form of 3,2,3-tet used to calculate protonation constants with continuum solvation model, PCM

$$
C_{\rm ps}03
$$

 C_{pp} 01

Fig. S6. Structures of all lowest in energy conformers for H₂L form of 3,2,3-tet used to calculate protonation constants with continuum solvation model, PCM.

$$
C_{\text{tn}}07
$$

 C_{tp} 09

Fig. S7. Structures of all lowest in energy conformers for H3L form 3,2,3-tet used to calculate protonation constants with continuum solvation model, PCM.

Fig. S8. Structures of all lowest in energy conformers for H4L form of 3,2,3-tet used to calculate protonation constants with continuum solvation model, PCM.

H12

Fig. S9. Structures of all lowest in energy conformers for the free ligand of 2,2,2-tet used to calculate protonation constants with continuum solvation model, PCM

 $C_s 01$ $C_s 03$

 C_s02 C_s04

 $C_p 02$ $C_p 01$

Fig. S10. Structures of all lowest in energy conformers for HL form of 2,2,2-tet used to calculate protonation constants with continuum solvation model, PCM.

Fig. S11. Structures of all lowest in energy conformers for H₂L form of 2,2,2-tet used to calculate protonation constants with continuum solvation model, PCM

$$
C_{\text{tn}}08
$$

Fig. S12. Structures of all lowest in energy conformers for H3L form of 2,2,2-tet used to calculate protonation constants with continuum solvation model, PCM.

 $C_{\text{fp}}02$ $C_{\text{fp}}05$

 C_{fp} 07

Fig. S13. Structures of all lowest in energy conformers for H4L form of 2,2,2-tet used to calculate protonation constants with continuum solvation model, PCM.

PART 6

Lowest energy conformers discovered in the discrete-continuum solvation model.

Fig. S14. Structures of all lowest in energy conformers of the free ligand of 3,2,3-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S15. Structures of all lowest in energy conformers for HL form of 3,2,3-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S16. Structures of all lowest in energy conformers of H₂L form of 3,2,3-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S17. Structures of all lowest in energy conformers for H3L form of 3,2,3-tet used to calculate protonation constants with discrete-continuum solvation model.

 $O48$

Н26

CAGS

Fig. S18. Structures of all lowest in energy conformers of H4L form of 3,2,3-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S19. Structures of all lowest in energy conformers of the free Ligand of 2,2,2-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S20. Structures of all lowest in energy conformers for HL form of 2,2,2-tet used to calculate protonation constants with discrete-continuum solvation model.

Fig. S21. Structures of all lowest in energy conformers for H₂L form of 2,2,2-tet used to calculate protonation constants with discrete-continuum solvation model.

 $A.780$

242

 C_{fp} 07

Fig. S23. Structures of all lowest in energy conformers for H4L form of 2,2,2-tet used to calculate protonation constants with discrete-continuum solvation model.

Table S1 Five lowest energy conformers of all H_nL in CSM, using either *E* or *G* values, for: part (a) 2,2,2-tet and part (b) 3,2,3-tet.^a (a)

(b)

^aConf stands for conformer; ΔE (ΔG) was calculated relative to the lowest $E(G)$ energy conformer; % is the %-fraction of the total population from Boltzmann distribution.

Reaction	$\log K_{\rm H}^{\rm (n)}$				
$HL^{(1)} + HL^{(2)} = H_2L^{(1)} + L^{(2)}$	15.56	6.56			
$H_2L^{(1)} + H L^{(2)} = H_3L^{(1)} + L^{(2)}$	15.47	8.89			
$H_3L^{(1)} + H L^{(2)} = H_4L^{(1)} + L^{(2)}$	14.33	11.06			
$L^{(1)} + H_2L^{(2)} = HL^{(1)} + HL^{(2)}$	3.01	-6.74			
$H_2L^{(1)} + H_2L^{(2)} = H_3L^{(1)} + H L^{(2)}$	8.72	2.14			
$H_3L^{(1)} + H_2L^{(2)} = H_4L^{(1)} + HL^{(2)}$	7.58	4.31			
Δ = computed – experimental log $K_{\mu}^{(n)}$					

Table S2. Examples of competition reactions in which reference molecule used had either smaller or larger, or similar number of protons relative to the molecule being investigated.

Table S3. Computed from E - and G -paths protonation constants, as $\log K_H^{(n)}$, for 2,2,2-tet using data from dispersion corrected DFT in a discrete-continuum solvation model using B3LYP-gD3 in part(a) and B97D in part (b) .^a (a)

	E -path				
	G of LEC		Weighted G		
Reaction	$\log K_{\rm H}^{(n)}$	Δ_1	$\log K_{\rm H}^{\rm (n)}$	Δ_2	$\Delta_1 - \Delta_2$
$L^{(1)} + HL^{(2)} = HL^{(1)} + L^{(2)}$	11.45	1.70	11.34	1.59	0.11
$HL^{(1)} + H_2L^{(2)} = H_2L^{(1)} + HL^{(2)}$	10.30	1.23	10.47	1.40	0.17
$H_2L^{(1)} + H_3L^{(2)} = H_3L^{(1)} + H_2L^{(2)}$	5.63	-0.95	5.37	-1.21	0.26
$H_3L^{(1)} + H_4L^{(2)} = H_4L^{(1)} + H_3L^{(2)}$	1.98	-1.29	2.14	-1.13	0.16
	G-path				
	G of LEC		Weighted G		
$L^{(1)}$ + HL ⁽²⁾ = HL ⁽¹⁾ + L ⁽²⁾	11.45	-1.70	11.62	-1.87	0.17
$HL^{(1)} + H_2L^{(2)} = H_2L^{(1)} + HL^{(2)}$	9.27	-0.20	9.21	-0.14	0.06
$H_2L^{(1)} + H_3L^{(2)} = H_3L^{(1)} + H_2L^{(2)}$	6.66	-0.08	6.68	-0.10	0.02
$H_3L^{(1)} + H_4L^{(2)} = H_4L^{(1)} + H_3L^{(2)}$	1.98	1.29	2.00	1.27	0.02

	E -path				
	G of LEC		Weighted G		
Reaction	$\log K_{\rm H}^{(n)}$	Δ_1	$\log K_{\rm H}^{\rm (n)}$	Δ_2	$\Delta_1 - \Delta_2$
$L^{(1)} + HL^{(2)} = HL^{(1)} + L^{(2)}$	10.56	-0.81	11.34	-1.59	0.78
$HL^{(1)} + H_2L^{(2)} = H_2L^{(1)} + HL^{(2)}$	9.78	-0.71	10.47	-1.40	0.69
$H_2L^{(1)} + H_3L^{(2)} = H_3L^{(1)} + H_2L^{(2)}$	6.30	0.28	5.37	1.21	0.93
$H_3L^{(1)} + H_4L^{(2)} = H_4L^{(1)} + H_3L^{(2)}$	2.12	1.15	2.14	1.13	0.02
	G-path				
	G of LEC		Weighted G		
$L^{(1)} + HL^{(2)} = HL^{(1)} + L^{(2)}$	10.56	-0.81	10.85	-1.10	0.29
$HL^{(1)} + H_2L^{(2)} = H_2L^{(1)} + HL^{(2)}$	8.89	0.18	8.97	0.10	0.08
$H_2L^{(1)} + H_3L^{(2)} = H_3L^{(1)} + H_2L^{(2)}$	7.18	-0.60	7.03	-0.45	0.15
$H_3L^{(1)} + H_4L^{(2)} = H_4L^{(1)} + H_3L^{(2)}$	2.12	1.15	1.92	-1.35	0.20

^aWeighted *G* values were obtained using each conformers fraction of the total population (from Boltzmann distribution) as a weight for their *G* contribution ($w \times G$); Δ_n = computed – experimental $\log K_{\rm H}^{\rm (n)}$.

Figure S24. Graphical presentation of differences between successive stepwise protonation constants, Δ log $K^{(n,n+1)}$ = log $K_H^{(n)}$ – log $K_H^{(n+1)}$, for computed data at the B3LYP-gD3 level of theory with DCSM (values obtained for experimental data is also included for comparison).

		$2,2,2$ -tet	$3,2,3$ -tet		F-set	R-set	F-set	R -set
Prot. form	The LEC	LECs	The LEC	LECs	$log K_H^{(2)}$	$\log K_{\rm H}^{(2)}$	$\log K_{\rm H}^{(3)}$	$log K_H^{(3)}$
L	yes	yes	yes	yes				
HL_p	yes	yes	yes	yes				
HL_s	yes	yes	yes	yes				
H_2L_{ps}	yes	$no(1)*$	yes	yes	8.68	8.75	6.25	6.19
H_2L_{pp}	yes	yes	yes	yes				
H_3L	yes	yes	yes	yes				
H_4L	yes	yes	yes	yes				

Table S4. Summary of identified (yes) and missed (no) lowest energy conformers of 2,2,2-tet and 3,2,3 tet in DCSM from proposed the pre-optimization protocol involving selection of conformers after 20 optimization steps with 4 kcal/mol *E*-window showing also an impact on computed protonation constants.^a

^aProt. form stands for protonated form of a polyamine, The LEC stands for the lowest in electronic energy conformer, F-set = full set of LECs found after full optimization, R-set = reduced set of LECs as found from pre-optimization protocol. *(1) indicates that one new conformer was added to the set of LECs after full optimization.

Table S5. Step-wise selection of conformers needed and sufficient for protonation constants calculations using the 3-step (*EGB*), 4-step (*EEGB*) and most timeeffective 5-step (*EEBGB*) protocol.* Data obtained for each tautomers are shown in PART (a) for 2,2,2-tet and PART (b) for 3,2,3-tet.

*MM confs = MM-generated conformers; **Step-1** is common to all protocol and it involves selection of lowest energy conformers (LECs) falling within 4 kcal/mol *E*-window from pre-optimization in Gaussian after 20 cycles; **Step-2** in *EGB***-protocol** involves selection of LECs falling within 2 kcal/mol *G*-window after frequency calculation; **Step-3** in *EGB***-protocol** involves selection of conformers with %-fraction > 5 after Boltzmann distribution on selected LECs in Step-2; **Step-2** in *EEGB***-protocol** involves selection of LECs falling within 2 kcal/mol *E*-window after full optimization of conformers selected in Step-1; **Step-3** in *EEGB***protocol** involves selection of LECs falling within 2 kcal/mol *G*-window after frequency calculation; **Step-4** in *EEGB***-protocol** involves selection of conformers with %-fraction > 5 after Boltzmann distribution on selected LECs in Step-3; Step-2 in *EEBGB*-protocol is as Step-2 in *EEGB*-protocol; Step-3 in *EEEGB***protocol** involves selection of conformers with %-fraction > 5 after Boltzmann distribution on selected LECs in Step-2; **Step-4** in *EEEGB***-protocol** involves selection of LECs falling within 2 kcal/mol *G*-window after frequency calculation; **Step-5** in *EEEGB***-protocol** involves selection of conformers with %-fraction > 5 after Boltzmann distribution on selected LECs in Step-4.

Scheme S2. Time most demanding and least accurate 3-step selection *EGB*-protocol tested for protonation constants calculations of polyamines.

Scheme S3. Time efficient and well-performing 4-step selection *EEGB*-protocol tested for protonation constants calculations of polyamines.

Scheme S4. 2-step selection *EE*-protocol tested for selection of conformers for protonation constants calculations.