EXPERIMENTAL AND NUMERICAL STUDIES ON VORTICAL STRUCTURE AND TEMPERATURE FIELD IN A BLUFF-BODY BURNER

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ABSTRACT
Vortical and thermal structures of non-premixed propane flame in a bluff-body burner are studied experimentally and numerically in the transition from laminar to turbulent flow. In particular, we focus attention on the effect of annular air flow on the flame. The annular air flow promotes development of a shear layer vortex street in the central fuel jet and lends to change in the direction of rotation of the vortex. These features are supported by the numerical simulation. The agreement of experimental and numerical vortex frequencies is satisfactory. The fluctuation in temperature corresponds well to the vortex dynamics, and there is a peak in rms temperature inside and outside the flame, respectively.

INTRODUCTION
Non-premixed flame stabilized by a bluff-body combustor, such as occurs when a central fuel jet issues into a surrounding annular air flow, is often used industrially. Such bluff-body combustors provide good flame stabilization as well as easy control of combustion.

There have been experimental studies on non-premixed flames for several fuels. Roquemore et al. [1] introduced a two-dimensional sheet-lighting technique coupled with a fast chemically reacting system to visualize the turbulent mixing and the vortex shedding processes of a bluff-body combustor for C₃H₈. Lin and Tankin [2] employed this technique and determined the effect of burner design and flow conditions on fuel jet penetration at low Reynolds numbers. Furthermore, Chin and Tankin [3] and Nishimura and Takemori [4] measured vortical shedding frequency using a flow visualization technique in a two-dimensional slot burner and cylindrical shaped burners, respectively. Huang and Lin [5] studied the flame behaviour and the time-averaged thermal structure for various C₃H₈ and air flows. Schefer et al. [6] and Namazian et al. [7] performed velocity and concentration measurements using laser Doppler velocimetry and a combined Raman scattering and laser-induced fluorescence imaging in turbulent flow for CH₄. Lee and Onuma [8] also measured velocity, temperature and chemical species in turbulent flow for H₂ in order to compare with numerical simulation.

Although they emphasized the importance of vortical structures in bluff-body burners, the relationship between the vortical and thermal structures under unsteady vortical motion has not been understood fully in the experimental studies. While, more recently, direct numerical simulation have been performed in the transitional flow regime for jet diffusion flames to capture the temporal and spatial development of vortical and thermal structures, i.e., Katta and Roquemore [9], Yamashita et al. [10]. Such a simulation will be extended to bluff-body burners in the near future. However, there have been few studies providing time-dependent experimental data to test and refine mathematical modelling. These aspects have motivated the present investigation. Vortical and thermal structures in a bluff-body burner are studied experimentally and numerically in the transition from laminar to turbulent flow as a necessary initial step in a more realistic situation involving fully turbulent flow. In the present study, we focus attention on the effect of annular air flow on the flame, and it is expected that the fuel jet in the transition regime is responsive to the annular air flow.

EXPERIMENTAL APPARATUS AND PROCEDURE
The bluff-body, vertical, unducted combustor used here consisted of a fuel nozzle located concentric to an annular region where air flowed, as shown in Figure 1. Commercial-grade propane was employed as the fuel gas. The diameters of the fuel nozzle D₂, the inner annulus D₁ and the outer annulus do were 10mm, 42mm and 56mm, respectively. One of the objectives of the present study is to examine the effect of the annular air velocity, listed in Table 1. It should be noted that the jet at this fuel velocity belongs to the transition regime, in the absence of the annular air flow.

The relationship between vortical structure and temperature field was examined by flow visualizations, velocity and
temperature measurements. A schematic diagram of the experimental set-up is shown in Figure 2. The vortical structure was visualized by combination of the shadowgraph method and high-speed camera. The motion pictures were analyzed with an image processor. The mean velocity is measured by a LDV system. A fine wire thermocouple compensated for the effect of thermal inertia was employed to examine the characteristics of temperature fluctuation, i.e., Pt-Pt/Rh 13%, 50 μm in diameter. No coatings were applied to the thermocouple to inhibit catalytic activity because of the increase in the time constant, 43ms. The thermocouple with the compensator is presumed to follow temperature fluctuations of 2kHz. The dominant temperature fluctuation is less than 0.5kHz in this experiment. The information on the flow visualization and temperature measurement was simultaneously monitored to make clear the interrelation of these data.

**NUMERICAL MODEL**

The axial symmetry of the flow is satisfied from conventional experimental result in such flow field. Therefore, computation model was assumed the axially symmetry. The present computational domain is shown in Figure 3. The flow is time-dependent and two-dimensional. The axisymmetric coordinate system is taken such that \( x \) is the streamwise direction, \( r \) is the radial and the origin is the center of the fuel injection with a diameter of 1.0d, and the thickness of the bluff-body was made with 1.5d in order to be correspondent to burner nozzle used by the experiment. In addition, the annulus jet of air flow had a 0.7d. \( u \) and \( v \) represent the streamwise and transverse velocity, respectively, and \( z \) is the coupling function. The boundary conditions for \( u \), \( v \) and \( z \) for the combusting flow are described in the figure. The conservation equations for mass and momentum are given in the following forms.

\[
\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u)}{\partial x} + \frac{1}{r} \frac{\partial (r \rho v)}{\partial r} = 0
\]  

\[
\frac{\partial (\rho u)}{\partial t} + \frac{\partial (\rho uv)}{\partial x} + \frac{\partial (\rho uv)}{\partial r} = \frac{\partial}{\partial x} \left( \mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial u}{\partial r} \right) - \frac{\rho uv}{r} + \frac{\mu}{r} \frac{\partial r}{\partial r} - \frac{\partial \rho}{\partial r} + \frac{\partial}{\partial x} \left( \mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial r}{\partial r} \right) \]  

\[
\frac{\partial (\rho v)}{\partial t} + \frac{\partial (\rho uv)}{\partial x} + \frac{\partial (\rho uv)}{\partial r} = \frac{\partial}{\partial x} \left( \mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial v}{\partial r} \right) - \frac{\rho uv}{r} + \frac{\mu}{r} \frac{\partial r}{\partial r} + \frac{\partial}{\partial x} \left( \mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial v}{\partial r} \right) \]  

\[
\frac{\partial \rho}{\partial t} + \frac{1}{r} \frac{\partial (r \rho v)}{\partial r} = \frac{\partial}{\partial x} \left( \mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial v}{\partial r} \right) - \frac{\rho v}{r} + \frac{\mu}{r} \frac{\partial r}{\partial r} + \frac{\partial}{\partial x} \left( \mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial r} \left( \mu \frac{\partial v}{\partial r} \right) \]

where \( t \) and \( \rho \) are the time and density, suffix \( a \) denotes environment condition. Density is related to pressure \( p \), temperature \( T \) and mass fraction \( Y_i \) through the following state equation

\[
p = \rho \cdot R \cdot T \sum_{i=1}^{4} \left( \frac{Y_i}{m_i} \right)
\]

where \( m_i \) is the molecular weight of species \( i \) and \( R \) is the universal gas constant. The problem is further simplified by adopting the following coupling function \( z \), i.e., Shavb-Zeldvich formulation:

**Table 1 Test matrix**

<table>
<thead>
<tr>
<th>Case</th>
<th>Central fuel jet ( u_j ) (m/s)</th>
<th>Annular air flow ( u_a ) (m/s)</th>
<th>( \frac{u_j}{u_a} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.84</td>
<td>1957</td>
<td>0.84</td>
</tr>
<tr>
<td>B</td>
<td>0.84</td>
<td>1957</td>
<td>0.84</td>
</tr>
<tr>
<td>C</td>
<td>0.84</td>
<td>1957</td>
<td>1.24</td>
</tr>
</tbody>
</table>

**Figure 1** Bluff-body burner

**Figure 2** Experimental apparatus
Air flow \( T = T_\infty + (T_o - T_\infty)z + (q_o / m_F \nu_F c_p)z \)  

In the present study, we shall adopt the following assumptions.
* The mixture undergoes an overall one-step irreversible reaction.
* The reaction rate is infinitely fast and the reaction is concentrated within infinitesimally thin zone in the surface.
* The mixture behaves like an ideal gas.
* The Soret and Dufour effect, as well as the pressure diffusion, can be neglected.
* Specific heat at constant pressure of the mixture is constant.
* The Lewis number is equal to unity.
* Viscosity coefficient and diffusion coefficient depend on temperature.
* In the energy equation viscous dissipation can be neglected.

The numerical calculation was performed by the finite-difference method [10]. The scheme adopted here was the SIMPLE method. The time differential and convective terms in the governing equations are treated with the implicit Euler scheme and QUICK scheme, respectively. The computational domain is \( 0 \leq x \leq 15.0d \) and \( 0 \leq r \leq 8.0d \). The grid number are \( 121 \times 261 \) non-uniform grid systems.

**RESULTS AND DISCUSSION**

**Vortical Structures**

The flame formed by a bluff-body burner is formed by a fuel flow from the center of a concentric double pipe and an air flow emitted by an annulus.

Figure 4 shows a direct photograph of a flame under the conditions shown in Table 1. In case A, which involves the fuel jet alone, the flame attaches to the inside of the bluff body, while in case B, where an air flow is flowing, the flame attaches to the outside of the bluff body. In addition, comparison of the shape of the flame surface indicates that the flame surface in case A develops downstream with substantial bulges while in case B it is relatively smooth and appears as bands in the horizontal direction. In case C, in contrast, uneven folds are observed in the vertical direction.

Figure 5 shows the streakline distribution determined by numerical calculations and shadowgraph photographs corresponding to Figure 4. According to shadowgraph photographs, shear vortices are formed in all of the fuel flows, and the position at which rotation of shear vortices from...
Shadowgraph images

Computational visualization

outward to inward due to the effects of the air flow shifts upstream. As became apparent in case C, shear vortices are disrupted downstream, and air flow through the flame largely affects fuel flow. The existence of a circulation flow and reversal of shear vortices corresponded well with calculated results, but the vortex breakdown in case C could not be reproduced. However, focusing on the area outside the flame indicated that vortices due to thermal buoyancy weakened due to the air flow.

Figure 6 shows the relationship between the frequencies of shear vortices in fuel and air flow. The calculated frequencies were determined from changes over time in the velocity components along the x axis at r/d = 0.5 and x/d = 5.0. In addition, in experiments these were measured based on shadowgraph images from a high-speed video camera. The St number, i.e. the dimensionless frequency, decreased due to an increase in air flow, and calculations and experiments roughly matched.
Next, Figure 7 shows the time-averaged velocity distribution at x/d = 7.0, which was used to examine the reversal of shear vortices. In experiments, this was measured by LDV. In case B, experiments and calculations agreed, but they did not do so in case C. This is because disruptions such as vortex breakdown could not be reproduced, as was mentioned previously. With regard to velocity in the fuel flow, however, velocity at the flame rather than in the center of the fuel increased, and the velocity gradient directly above the bluff body reversed. As became apparent, reversal of shear vortices depended on the velocity gradient, and its effects increased due to an increase in the air flow.

Although the above results revealed some inconsistencies between calculations and experiments, aspects such as the frequencies of shear vortices agreed, and the essential structure of vortices in the bluff-body burner can be ascertained.

![Figure 7](image7.png)

**Figure 7** Time-averaged axial velocity profiles at x/d = 7.0 for cases B and C

**Temperature field**

Figure 8 shows the temperature distribution in a horizontal cross-section at 3 points, which was used for quantitative comparison. Disparities in calculations and experiments were noted in the vicinity of the maximum temperature, indicating the reaction zone, but temperatures at other locations agreed in all of the cases. With regard to disparities in the vicinity of the maximum temperature, radiation corrections were made in experiments while the effects of radiation were ignored in calculations.

Last, RMS values of temperature fluctuations were divided by the time-averaged temperature and made dimensionless; the fluctuation intensity map obtained is shown in Figure 9. In the figure, the time-averaged position of the flame is also shown as a solid line. Qualitatively, calculations corresponded well with experiments, though absolute values for fluctuation intensity were larger in calculations than in experiments.

![Figure 8](image8.png)

**Figure 8** Radial profiles of time-averaged temperatures for cases A, B and C

The cause lies in the results of visualization: in calculated results, as mentioned previously, the macroscopic dynamic behaviour of vortices can be accurately ascertained, but the microscopic behaviour of vortices cannot be ascertained because of the level of precision of these calculations, and these fluctuations in behaviour of vortices appear more marked in experiments. Next, observation of the fluctuation intensity in each case indicated that in case A a strong peak of the same extent appeared outside and inside the flame in the vicinity of x/d = 7.0 in experiments and x/d = 8.5 in calculations. As indicated by frequency analysis [4], both were fluctuations produced by vortices due to thermal buoyancy; as became apparent, via the flame front these vortices caused strong fluctuations at the fuel jet as well. In contrast, in case B a peak in strong fluctuations outside the flame existed, but inside the flame fluctuations weakened. The peak in fluctuations outside the flame was similar to that in case A. Vortices due to thermal buoyancy had
an effect, but the peak inside the flame was due to the interaction of vortices due to thermal buoyancy and shear vortices. In case C, a peak of the same extent outside and inside the flame also appeared. This is due to the effects of the air flow flowing outside the flame. In addition, this fluctuating zone was more limited in calculated results than in experimental results; this is due to the effects of vortex breakdown observed in the downstream region in experiments. Based on the above results, the peak in temperature fluctuations corresponds to the behaviour of vortices due to thermal buoyancy and shear vortices.

**CONCLUSION**

This work conducted a numerical study of the relationship between the flame and vortical structures in an axisymmetric bluff-body burner, as is widely used in practical combustion fields. Given the validity of these calculations with respect to experimental results, the following findings were obtained:

1. As regards a combustion field with a circulation flow in the transition zone, the calculated results roughly matched the flow structure as indicated by experimental results.
2. In a combustion field with a circulation flow where an air flow is flowing, a stable recirculation zone is formed in the vicinity of the nozzle outlet, and this encourages the development of shear vortices in the fuel jet.
3. The position at which shear vortices in the fuel jet reverse shifts upstream with an increase in the Re number of the air.
4. Vortices due to thermal buoyancy and shear vortices each induce temperature fluctuations, and a peak in fluctuation intensity appears on both sides of the flame front. Within the range of conditions in this study, vortices due to thermal buoyancy had a more marked effect on temperature fluctuations than shear vortices.

**REFERENCES**