Housing and the Great Depression*

Mehmet Balciar
Department of Economics
Eastern Mediterranean University
Famagusta, NORTHERN CYPRUS, via Mersin 10, TURKEY

Rangan Gupta
Department of Economics
University of Pretoria
Pretoria, 0002, SOUTH AFRICA

Stephen M. Miller**
Department of Economics,
University of Nevada, Las Vegas
Las Vegas, Nevada, 89154-6005 USA
E-mail: stephen.miller@unlv.edu

Abstract:
This paper considers the structural stability of the relationship between the real housing price and real GDP per capita for an annual sample that includes the Great Depression. We test for structural change in parameter values, using a sample of annual US data from 1890 to 1952. The paper examines the long-run and short-run dynamic relationships between the real housing price and real GDP per capita to determine if these relationships experienced structural change over the sample period. We find that temporal Granger causality exists between these two variables only for sub-samples that include the Great Depression. For the other sub-sample periods as well as for the entire sample period no relationship exists between these variables.

Keywords: Great Depression, Real House Price, Real GDP per Capita, Structural change

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** Corresponding author
1. Introduction

Recent events during the financial crisis and Great Recession confirm that movements in housing markets not only reflect developments in macroeconomic fundamentals, but also provide important impulses to business fluctuations (Iacoviello, 2010). In his introductory remarks at a conference on Housing and Mortgage Markets, Federal Reserve Chairman Bernanke (2008) noted that “… housing and housing finance played a central role in precipitating the current crisis.”, thus emphasizing the importance of spillover effects from the housing market onto the real economy. Reinhart and Rogoff (2009) conclude that the typical banking crisis, which characterizes the US experience in the late 2000s, involves excessive debt accumulation during the boom (e.g., private borrowing binges that inflate asset prices) and eventual insolvency of many banks due to large investment losses and/or a banking panic after the bust (e.g., falling asset prices leading to debt default).

Given the role played by housing in causing the Great Recession, a similar pertinent question applies to the Great Depression. Researchers offer a variety of explanations for the causes of the Great Depression. Early on, Fisher (1933) proposed the debt-deflation theory of the Great Depression, which directly relates to the contemporary work of Reinhart and Rogoff (2009). Friedman and Schwartz (1963) posited monetary policy errors or omissions as the proximate cause – the “money” view. Temin (1976), among others, argued for the collapse of aggregate demand, an autonomous fall in consumption demand, as the proximate cause – the “demand” view. Others adopted elements of the "money" and "demand" points of view to develop integrated arguments explaining the Great Depression. For example, Mishkin (1978) focused on the household balance sheet, combining elements of his liquidity hypothesis (Mishkin 1976) and the life-cycle hypothesis (Ando and Modigliani 1963), as critical factors in the explanation of the Great Depression. In his model, he highlighted the role of declining demand for housing and consumer durable goods. Bernanke (1983)
proposed that the financial crisis disrupted the credit allocation process, leading to higher credit allocation costs, reducing credit availability, and lowering aggregate demand. He highlighted two major factors as the root problem in the Great Depression -- the failure of financial institutions and the defaults and bankruptcies. Gordon and Wilcox (1981) stressed the roles of construction, consumption, the stock market, and the Hawley-Smoot tariff in explaining the severity of the Great Depression.

As our main objective, and to the best of our knowledge the first such attempt, we analyze if, and how, housing, specifically real house price movements, played a role in causing the Great Depression. To achieve our goal, we consider time-varying (using a rolling window of 15 years), bootstrapped causality between the real house price (proxy for housing wealth) and real GDP per capita over the annual period from 1890 to 1952. A full-sample causality test over this period may not help to decipher the leading role, if any, for the real house price in causing the Great Depression. That is, the relationship between real house price and real GDP per capita may prove unstable. We specifically test for such instability in both the short and long runs. We find that the full-sample causality tests do not prove reliable.

The possibility of spillover effects from the housing market to the real economy possesses well-grounded theoretical foundations. The permanent income hypothesis of Friedman (1957) and the life-cycle model of Ando and Modigliani (1963) imply that households allocate some of their permanent income or wealth to finance consumption. Thus, changes in housing wealth that affect permanent income or wealth alter consumption spending. Case, et al. (2005) provide a good recent review of wealth effects. While the original simple life-cycle model of consumption does not distinguish between different types of wealth, implicitly assuming that the marginal propensities to consume out of wealth remains the same across different wealth types, reasons exist to suggest that this implicit assumption is, in fact, invalid. Case, et al. (2005) offer five different possible rationalizations
for different marginal propensities to consume out of different types of wealth – differing perceptions about the effects of permanent and transitory components, differing bequest motives, differing motives for wealth accumulation, differing abilities to measure wealth accumulation, and differing psychological “framing” effects.

Another possible rationalization, not mentioned by Case, et al. (2005), involves whether the wealth holder receives consumption services from the holding of wealth. For example, owner occupied housing and consumer durable goods provide consumption services to holders of these components of wealth. Thus, households may adjust their consumption of nondurables and services, the usual measure of consumption for wealth-effect studies, differently to changes in the market values of owner occupied housing and consumer durables than to changes in other forms of wealth that do not deliver such services.

More recent theoretical work (e.g., Bajari, et al. 2005; Buiter 2010) suggests that house price changes that reflect changes in fundamental value do not produce aggregate consumption changes but merely redistributed wealth between households who are long and short in housing wealth. Nevertheless, changes in house prices that constitute changes in the speculative component of house prices do exhibit a wealth effect. Finally, other authors (e.g., Aoki, et al. 2004; Lustig and van Niewerburg 2010) argue that changes in house prices affect the collateral value and that this can affect actual consumption for those financially constrained households who want to consume more than their financial circumstances permit.

White (2009) argues that the "forgotten" real estate boom and collapse in the 1920s shares many "familiar characteristics" with the most recent US housing price run-up and collapse. He cites several factors ("weak supervision, securitization, and a fall in lending standards" p. 4) as well as two monetary factors ("a 'Greenspan put' by the Federal Reserve" and "low interest rates" p. 4) as common elements. The housing price index constructed by Grebler, et al. (1956) and used as one of the components by Shiller (2005) to construct his
housing price index series shows a clear peak in the nominal index in 1925, followed by a substantial decline in the index through 1934. Nicholas and Scherbina (2013) recently constructed real estate price indexes for Manhattan, New York, showing that prices peak in 1929 and then decline substantially during the 1930s. Nevertheless, the run-up and decline in housing price indexes in the 1920s and 1930s do not exhibit the magnitudes seen in the most recent housing price boom and collapse. White (2009) attributes the larger swing in housing prices in the most recent boom and collapse to “risk-taking induced by federal deposit insurance and aggressive homeownership policies absent in the 1920s.” (p. 4).

The rest of the paper is organized as follows: Section 2 outlines the econometric method. Section 3 discusses the data and presents the results on the relationship between the real housing price and real GDP per capita. Finally, Section 4 concludes.

2. **Method:**

We examine whether the real house price Granger causes real GDP per capita. Our null hypothesis is Granger non-causality, which we define as follows. Granger non-causality tests whether the lagged values of the real house price jointly prove insignificant, using Wald, likelihood ratio ($LR$), and Lagrange multiplier ($LM$) statistics. These standard Granger-non-causality test statistics assume stationary underlying time series. If the series exhibit nonstationarity, then standard asymptotic distribution theory does not hold. Park and Phillips (1989) and Toda and Phillips (1993, 1994), among others, illustrate the difficulties arising in the levels estimation of such nonstationary VAR models.

**Full-Sample Analysis**

Toda and Yamamoto (1995) and Dolado and Lütkepohl (1996) propose a modification to the standard Granger causality test, obtaining standard asymptotic distributions when the time series forming the $VAR(p)$, where $p$ is the lag order, are $I(1)$. Employing their method, one estimates a $VAR(p+1)$ in levels, where $(p+1)$ equals the lag order of the VAR system plus one
difference to achieve stationarity, and the resulting modified Granger causality tests remain valid irrespective of integration-cointegration properties of the variables. That is, the modification estimates a $VAR(p+1)$ and performs the Granger non-causality test on the first $p$ lags. Thus, one coefficient matrix, which relates to the $(p+1)^{\text{st}}$ lag, remains unrestricted under the null, giving the test a standard asymptotic distribution.  

To illustrate the bootstrap modified-$LR$ Granger causality test procedure, consider the following bivariate $VAR(p)$ process:

$$
egin{bmatrix}
  z_{ht} \\
  z_{yt}
\end{bmatrix}
= 

\begin{bmatrix}
  \phi_{h0} (L) & \phi_{hy} (L) \\
  \phi_{y0} (L) & \phi_{yy} (L)
\end{bmatrix}
\begin{bmatrix}
  z_{ht} \\
  z_{yt}
\end{bmatrix}
+
\begin{bmatrix}
  \varepsilon_{ht} \\
  \varepsilon_{yt}
\end{bmatrix},
\tag{1}
$$

where $z_h$ and $z_y$ are the real house price and real GDP per capita, respectively, $\varepsilon_t = (\varepsilon_{ht}, \varepsilon_{yt})'$ is a white noise process with zero mean and covariance matrix $\Sigma$, $p$ is the lag order of the process, $\phi_{ij}(L) = \sum_{k=0}^{p+1} \phi_{ijk} L^k$, $i, j = h, y$, and $L$ is the lag operator such that $L^k z_{it} = z_{it-k}$, $i = h, y$. In the empirical section, we use the Akaike Information Criterion ($AIC$) to select the lag order $p$.

For this bivariate system, we define two different hypotheses -- leading indicator (LI)
and housing fundamental (HF) hypotheses. The LI hypothesis states that lagged values of the real house price deliver explanatory power for real GDP per capita over and above that provided by lagged real GDP per capita. The HF hypothesis states that lagged values of real GDP per capita deliver explanatory power for the real house price over and above that provided by lagged real house prices. That is, the null hypothesis that the real house price does not Granger cause real GDP per capita implies:

$$ H_0^{LI} : \phi_{yh,1} = \phi_{yh,2} = \cdots = \phi_{yh,p} = 0. $$ (2)

Analogously, the null hypothesis that real GDP per capita output does not Granger cause the real house price implies:

$$ H_0^{HF} : \phi_{hy,1} = \phi_{hy,2} = \cdots = \phi_{hy,p} = 0. $$ (3)

Efron (1979) pioneered the bootstrap method, using critical or p values generated from the empirical distribution derived for the particular test using the sample data. In our case, we use the bootstrap approach to test for Granger non-causality. Several studies document the robustness of the bootstrap approach for testing Granger non-causality (e.g., Horowitz, 1994; Mantalos and Shukur, 1998; and Mantalos 2000). Using Monte Carlo simulations, Hacker and Hatemi-J (2006) show that the modified Wald test based on a bootstrap distribution exhibits much smaller size distortions compared to the use of asymptotic distributions. Moreover, these results hold irrespective of sample sizes, integration orders, and error-correction processes (homoskedastic or ARCH). In this paper, we adopt the bootstrap approach with the Toda and Yamamoto (1995) modified causality tests because of several advantages. In particular, this test applies to both cointegrated and non-cointegrated I(1) variables (Hacker and Hatemi-J, 2006).

Standard Granger non-causality tests assume that the VAR model’s parameters remain

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2 See footnote 1 for more details and references.
constant over time, an assumption which may not hold. Granger (1996) cited parameter non-
constancy as one of the most challenging issues confronting empirical studies today. 
Structural changes may shift the parameters and the pattern of the causal relationship may 
change over time. Although we can detect the presence of structural changes beforehand and 
we can modify our estimation to address this issue using several approaches, such as 
including dummy variables and sample splitting, such an approach introduces pre-test bias. In 
this paper, we adopt rolling bootstrap estimation to address parameter non-constancy and 
avoid pre-test bias. To examine the effect of structural changes, we use rolling window 
Granger causality tests, which also use the modified bootstrap test.

Recursive and Rolling Analysis

We now consider recursive and rolling estimates and implement the fluctuations \((FL)\) test of 
Ploberger \textit{et al.} (1989) and the moving-estimates \((ME)\) test of Chu \textit{et al.} (1995b). The \(FL\) and 
\(ME\) tests correspond to the recursive and rolling regressions. Recursive regressions start with 
an initial benchmark sample at the beginning of the full sample and then proceeds by 
expanding the sample by adding one observation at a time until reaching the end of the full 
sample. The rolling regression also begins with a benchmark sample at the beginning of the 
full sample and keeps the sample size constant as the subsample roll through the full sample 
adding one new observation and deleting the oldest observation each time until reaching the 
end of the full sample.

By structural change, we mean parameter instability in an econometric model, in 
which parameter estimates become worthless, statistical inference becomes invalid, and 
forecast accuracy becomes imprecise. We will check for stability of the both the short-run 
parameters in the \(VAR\) model and the parameters of the long-run equation between real GDP 
per capita and the real house price.
Since a model’s structure may deviate from assumed stability in numerous ways, tests that leave the form of instability unspecified possess desirable properties. As a practical matter, researchers require (1) a wide variety of tests to ensure that these tests exhibit power against some conceivable number of alternatives and (2) tools that permit an understanding of the nature of deviations from stability so that the researcher can date the structural change along with the causes. In view of (1), we include a battery of tests that possess power against both specific alternatives and unspecified alternatives, use robust estimation methods against the known issues, such as the nonstationarity, autocorrelation, and outliers. In view of (2), we use rolling and recursive estimations and tests that permit the determination of the form of deviations from the stability and also to date the structural changes. To wit, significance tests re-combined with graphical analysis based on rolling and recursive estimates gives insights on the nature and evolution of the structural change.

To illustrate the structural change tests, let all coefficients of the $VAR(p)$ in equation (1) vary over time and stack the coefficient matrices in the matrix $\theta_t = [\Phi_0, \Phi_1, \ldots, \Phi_p]^\prime$. Then, we can write the $VAR(p)$ model in the following form:

$$z_t = x_t'\theta_t + \epsilon_t, \quad t = 1, 2, \ldots, T,$$

where $z_t = [z_{h_t}, z_{y_t}]'$, $x_t = I_2 \otimes [1, z_{t-1}, z_{t-2}, \ldots, z_{t-p}]$, the symbol $\otimes$ denotes the Kronecker product, and $\epsilon_t$ is multivariate, normally distributed with variance $\Sigma$, $\epsilon_t \sim N(0, \Sigma)$. In addition to the stability of the $VAR(p)$ model in equation (4), we also investigate the stability of the long-run relationship, if any, between real GDP per capita and the real house price. We can also redefine equation (4) for the long-run relationship as follows:

$$z_t = x_t'\theta_t + \epsilon_t, \quad t = 1, 2, \ldots, T,$$

where $z_t = z_{yt}$, $x_t = [1, z_{ht}]$, and $\theta_t = [\theta_0, \theta_1]'$. The parameter stability tests apply equally to the parameters of the $VAR$ model in equation (4) and the long-run relationship in equation (5).
In the following discussion, we will not make a distinction on how the tests apply to equations (4) and (5). We note differences, when they occur. Note that in equation (4), $z_t$ is a vector and $\theta_t$ is a matrix, while in equation (5), $z_t$ is a scalar and $\theta_t$ is a vector.

Parameter stability tests consider the null hypothesis of parameter stability,

$$H_0 : \theta_t = \theta_0, \quad \forall t = 1,2,\ldots, T,$$

against the alternative that at least one of the parameters in $\theta_t$ varies over time. Several patterns of deviation from the constant parameter specification under the null in equation (6) exist, including single or multiple breaks, swift or gradual changes, and random-walk parameters, and so on. Testing approaches assume that structural breaks occur in known or unknown periods. In our application, we will only consider tests that do not require prior knowledge of the dates of the structural breaks. We will also consider recursive and rolling analysis that leaves the time variation in parameters under the alternative unspecified. Hansen (2001) offers a survey of parameter stability tests and related issues. We implement $F$ tests, fluctuation tests, and maximum likelihood ($ML$) scores test, address the form of structural change in different ways, having power against different forms of deviations from the constant parameter case.

$F$ tests assume a single structural change under the alternative at an unknown time. Andrews (1993) and Andrews and Ploberger (1994) propose three type of $F$ tests: $Sup-F$, $Ave-F$, and $Exp-F$, either based on Wald, $LM$, or $LR$ statistics. $F$ tests rely on sequences of $F$ statistics for a structural change at time $i$. We compute the statistics from segmented regressions (i.e., one regression estimate for each subsample determined by the break point, where the break point sequentially increases by one).

The test computation involves estimating two regressions -- one with no structural change and parameters $\theta_t = \theta_0$ for $t = 1,2,\ldots, T$ and one with structural change and
parameters \( \theta_t = \theta_0 + \delta \) for \( t = i, i+1, \ldots, T \). We construct \( F \) tests for \( \delta = 0 \) at each \( i = T_h, T_h + 1, \ldots, T - T_h \). These \( F \) tests reject \( H_0 \), if their supremum, average, or mean functional is too large. We can apply the tests to general classes of models fitted by ordinary least squares (OLS), instrumental variables, or generalized method of moments (GMM).\(^3\) In our applications, we prefer LR based \( F \) tests since the LR tests possess advantages in our causality tests framework based on bootstrapping.\(^4\) \( F \) tests require trimming and we set \( T_h = [hT] \) with \( h=0.15 \) (i.e., we trim 15 percent of the observations from the both ends of the sample).

Unlike the \( F \) test, fluctuation tests do not assume \textit{a priori} any specific form of structural break or pattern of change in the parameters. Fluctuation tests first estimate the specified model in a recursive (expanding window) or rolling (fixed window) manner and then construct a process that captures the fluctuation either in residuals (Ploberger and Kramer 1992, Chu et al. 1995a) or estimates (Ploberger et al. 1989, Chu et al. 1995b). Under the null hypothesis that parameters are constant, these fluctuation processes are governed by functional central limit theorems, converging to a functional Weiner process or Brownian bridge. Therefore, we can determine the boundaries of the limit processes with fixed probability \( \alpha \) under the null hypothesis, allowing one to perform formal statistical tests. Under the alternative hypothesis, when true, the fluctuations in the processes generally increase. A visual inspection of the trajectory of these processes serves as an exploratory tool for determining the type of the deviation from the null hypothesis and the dating of structural

\(^3\) As the \( F \) tests are easy to interpret, can determine a single break date in a fixed interval, and possess some certain weak optimality against single-break alternatives, they gained popularity in the last two decades and have become the most preferred structural change tests in empirical studies.

\(^4\) In our empirical application, we have also calculated \( LM \) versions of the \( F \) tests and results were qualitatively the same. \( LM \) test results are available from the authors.
breaks. We can estimate the parameters of the model by ordinary least squares or ML with normal error assumption.

Residual-based fluctuations tests are easy to compute and interpret. They do not give any intuition, however, about the likely cause of the rejection of parameter stability. In the estimates-based fluctuation tests, one process exists for each coefficient and we can examine each process separately. We can easily construct an overall process by aggregating over the individual components. Recursive and rolling fluctuation tests use the following recursive and rolling estimators, respectively,

$$\hat{\theta}_j = \left( \sum_{t=1}^{j} x_t x'_t \right)^{-1} \left( \sum_{t=1}^{j} x_t z_t \right), \quad j = k, 2, \ldots, T, \text{ and}$$

$$\hat{\theta}_{j,h} = \left( \sum_{t=j+1}^{j+hT} x_t x'_t \right)^{-1} \left( \sum_{t=j+1}^{j+hT} x_t z_t \right), \quad j = 0, 2, \ldots, T - \lfloor hT \rfloor + 1,$$

where $0 < h < 1$ determines the window size for the rolling estimates. Now, define

$$Q_{[mT]} = \frac{1}{mT} \sum_{t=1}^{[mT]} x_t x'_t, \quad \text{and} \quad Q_{[rT],h} = \frac{1}{[hT]} \sum_{t=\lfloor rT \rfloor}^{\lfloor hT \rfloor} x_t x'_t,$$

where $0 < m \leq 1$ and $0 \leq r < 1$. The full sample matrix $Q_T$ scales matrices in constructing recursive fluctuation ($FL$) test by Ploberger et al. (1989) and also by Chu et al. (1995b) in constructing the rolling fluctuation ($ME$) test. Kuan and Chen (1994) argue that the $FL$ and $ME$ tests experience serious size distortions in dynamic models (i.e., in the presence of autocorrelation). Therefore, these tests more likely reject null hypotheses of parameter constancy in dynamic models. Kuan and Chen (1994) further show that when the size of these tests improve significantly when using the subsample estimates $Q_{[mT]}$ and $Q_{[rT],h}$. In our case, the residuals may exhibit significant autocorrelation. Thus, to address this issue, we use the modified $FL$ and $ME$ tests proposed by Kuan and Chen (1994). The modified tests are defined as follows:
where $\hat{\sigma}_T^2$ is the estimator of the error variance and $\| \cdot \|$ is the $L_2$ norm. We prefer the $L_2$ norm because it aggregates over the components, which leads to better power and size properties when several, or all, parameters change simultaneously. In implementing the $ME$ test, we use a window parameter of $h=0.25$, implying that the ratio of the number of observations in each window to total number of observations is 0.25.\(^5\)

Nyblom (1989) proposed an $LM$ test based on the $ML$ scores, denoted $L_c$. Hansen (1992a, 1992b) generalizes the $L_c$ test to linear models and to models with integrated variables, respectively. We can transform the $ML$ scores test into the framework of the fluctuation tests, although it possesses a quite different motivation. The fluctuation processes in the $ML$ scores test comes from the first-order conditions. Indeed, the $L_c$ test uses the full sample parameter estimates. That is, given the parameter estimates, we evaluate the scores and form the fluctuation processes from the empirical scores. We can estimate the parameters with $OLS$, $ML$ with normal errors, or other methods such as the $GMM$ and fully-modified $OLS$ ($FM-OLS$) estimator (Phillips and Hansen 1990). In empirical applications, researchers usually prefer the $FM-OLS$, which we use due to its advantages. To examine the stability of the cointegration parameters, we emphasize the $L_c$ tests. The $L_c$ test is an $LM$ test for parameter constancy against the alternative hypothesis that the parameters follow a random-walk process and, therefore, time-varying, since the first two moments of a random walk

\[^5\] The results that use window parameters 0.20 and 0.30 are available from authors. They produce qualitatively similar findings to those reported in the empirical section.
depend on time. The random-walk alternative makes the $L_c$ test suitable as a test for cointegration, when the alternative is that the intercept follows a random walk.

In sum, parameter instability can occur in many ways. This fact precludes us from covering all conceivable forms of parameter instability. We can only avoid the problem if we know the exact form of the deviation from parameter constancy. Given the difficulty of test selection, we use several tests based on their optimality properties. The $Sup-F$ test exhibits good power against single breaks and can usefully date structural breaks. The $Sup-F$ test also performs better in detecting tail shifts in small samples. This test, however, displays low power when multiple breaks exist and in the presence of random-walk alternatives. With random-walk alternatives, the $ML$ scores based test $L_c$ possesses better power. The $L_c$ test performs well against mid-point structural breaks, but not well against tail breaks. Moreover, the $L_c$ test is preferred for examining the stability of long-run equilibrium regressions with $I(1)$ variables. In such cases, its use with the $FM-OLS$ estimator also serves as a test for cointegration. The recursive estimation-based fluctuation test $FL$ possesses similar properties to the $Sup-F$ test, particularly for visual inspection of the pattern of the structural change. The $Sup-F$ test assumes a single break and is best suited for detecting one-time structural changes. On the other, the rolling estimation based fluctuation test $ME$ displays better power against multiple-breaks and random-walk alternatives. The $ME$ test is particular appropriate where parameters temporarily deviate from a “normal” level. Like the $FL$ test, it serves a useful explorative tool for understanding the pattern and form of the structural change.

3. **Data and Results**

*Data Sources*

We test the relationships between the real house price and real GDP per capita, using annual US data from 1890 to 1952. While the real house price data come from Shiller (2005), the data for real GDP at constant 2005 dollars and population to compute the real GDP per capita
come from the Global Financial Database. Consistency with the theoretical models of wealth effects implies ideally that we should use data on housing wealth. The unavailability of housing wealth for the period under consideration requires us to use the housing price index as a proxy for housing wealth, which, of course, represents a limitation on our statistical analysis. First, we test for the order of integration of the two series. Second, we perform multivariate cointegration tests. Third, we determine the full-sample Granger causality tests. Fourth, we perform various tests on parameter stability from the coefficient estimates from our rolling VAR regressions. Finally, we estimate rolling VAR regressions and perform Granger causality tests with a fixed 15-year window.

**Full Sample Unit Roots, Cointegration, and Granger Temporal Causality**

We first test for the presence of unit roots in the real house price and real GDP per capita series using the Phillips (1987) and Phillips and Perron (1988) test. We perform tests with both a constant and a constant and a time trend. As test statistics exhibit nonstandard distributions and critical values, we use the critical values computed by MacKinnon (1996). Table 1 reports the results of unit-root tests. We fail to reject the null hypothesis of nonstationarity for the real house price and the real GDP per capita series at 5-percent level. Further, we do reject the null of nonstationarity for the first differences of these series, implying that both series are \( I(1) \) processes.\(^6\)

We next test for a common stochastic trend, which implies a cointegrating relationship between the two series. We use Johansen's (1991) maximum likelihood method, which requires that we first identify the lag structure of the bivariate VAR model. We search for the optimal lag order (\( p \)) using the sequential modified likelihood ratio (\( LR \)) test statistic, the final prediction error (\( FPE \)) criteria, the Akaike Information Criteria (\( AIC \)) the Schwarz

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\(^6\) We also perform the Elliott-Rothenberg-Stock (1996) DF-GLS test for unit roots. These tests confirm that PP test reported in Table 1. Results are available from the authors.
Information Criteria (SIC), and the Hannan-Quinn information criterion (HQIC), starting from $p=1$ to $p=5$. All lag-length selection criteria select one lag for our annual bivariate VAR model. Table 2 gives the results of the Johansen cointegration trace maximum eigenvalue test statistics. We cannot reject the null hypothesis of no cointegration for the real house price and real GDP per capita series at 5-percent significance level.\(^7\)

Even though no cointegration exists between the real house price and real GDP per capita, these two series may still exhibit Granger temporal causality. That is, the real house price may Granger cause real GDP per capita, real GDP per capita may Granger cause the real house price, or the two series may exhibit two-way Granger causality. Table 3 reports the results of full sample Granger-causality tests. The first test is the F-test performed on the standard VAR model, which fail to reject the null hypothesis that real house price does not Granger cause real GDP per capita and that real GDP per capita does not Granger cause the real house price at 5-percent significance level. In order to check the robustness of the F-test, we next perform bootstrap LR causality tests as reported in Table 3, which uses the p-values obtained with 2,000 bootstrap replicates and which fails to reject the null hypotheses that the real house price does not Granger cause real GDP per capita and that real GDP per capita does not Granger cause the real house price at 5-percent significance level.

At the moment, we conclude based on the full sample of annual data from 1890 to 1952 that no long- or short-run relationships exist between the real house price and real GDP per capita. We now turn to examining the stability of the estimates. Structural changes may shift parameter values and the pattern of the (no) cointegration and (no) causal relationship may change over time. The results of the cointegration and Granger causality tests will show sensitivity to sample period used and order of the VAR model, if the parameters are

\(^7\) We also conduct the Engle-Granger (1987) cointegration test and the findings support the Johansen results reported in the test. These results are available from the authors.
temporally unstable. Therefore, studies using different sample periods and different VAR specifications will find conflicting results for the causal links between the real house price and real GDP per capita. The results of cointegration and Granger causality tests based on the full sample also become invalid with structural breaks because they assume parameter stability.

Full-Sample Parameter Stability

Researchers use various tests in practice to examine the temporal stability of econometric, and in our case VAR, models (e.g., Hansen, 1992b; Andrews, 1993; Andrews and Ploberger, 1994). Although we can apply these tests in a straightforward way for stationary models, the variables in our model are nonstationary and potentially cointegrated.\(^8\) We consider the possibility of this integration (cointegration) property because in a cointegrated VAR, the variables form a vector error-correction (VEC) model. Thus, we investigate the stability of both the long-run cointegration and short-run dynamic adjustment parameters. If the long-run or cointegration parameters prove stable, then the model exhibits long-run stability. Additionally, if the short-run parameters are also stable, then the model exhibits full structural stability.

Since the estimators of cointegration parameters are superconsistent, we can perform the parameter stability testing procedure into two steps. First, we test the stability of the cointegration parameters. Second, if long-run parameters prove stable, then we can test the stability of the short-run parameters. To examine the stability of cointegration parameters, we use the \(L_c\) test of Nyblom (1989) and Hansen (1992a). Next, we use the Sup-F, Mean-F, and Exp-F tests developed by Andrews (1993) and Andrews and Ploberger (1994) to investigate

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\(^8\) Although the full-sample tests indicated no cointegration, we do not rule out the possibility of cointegration in our recursive and rolling analyses. That is, some sub-samples may suggest cointegration and other sub-samples may not.
the stability of the short-run parameters. These tests exhibit non-standard asymptotic distributions and Andrews (1993) and Andrews and Ploberger (1994) report the critical values. To avoid the use of asymptotic distributions, however, we calculate the critical values and p-values using the parametric bootstrap procedure.

We use these parameter constancy tests to investigate the temporal stability of the coefficients of the $VAR$ model formed by the real house price and real GDP per capita series. Table 4 reports the outcome of the tests, where these p-values come from a bootstrap approximation to the null distribution of the test statistics, constructed by means of Monte Carlo simulation using 2,000 samples generated from a $VAR$ model with constant parameters. We calculate the $L_c$ test for each equation separately using the $FM-OLS$ estimator of Phillips and Hansen (1990). The $Sup-F$, $Mean-F$, and $Exp-F$ tests require trimming at the ends of the sample. Following Andrews (1993), we trim 15 percent from both ends and calculate these tests for the fraction of the sample in $[0.15, 0.85]$.

The results for $L_c$ tests indicate that the real house price and real GDP per capita equations exhibit stable long-run parameters, or cointegration, at the 5-percent significance level. In Table 4, we also report the system $L_c$ statistics for the unrestricted $VAR(1)$ model, which indicates that the $VAR$ model as a whole proves unstable at the 1-percent level. This finding supports the view that the short-run parameters of the $VAR$ system are unstable.

The remaining three parameter constancy statistics also test for short-run parameter stability. The $Sup-F$ statistics tests parameter constancy against a one-time sharp shift in parameters. The $Mean-F$ and $Exp-F$ test for gradual shifting in the regime. The results for the sequential $Sup-F$, $Mean-F$, and $Exp-F$ tests reported in Table 4 suggest that significant evidence of parameter non-constancy exists in the real house price and real GDP per capita equations as well as the entire $VAR$ system at the 1-percent level, except for the $Mean-F$ test for the real house price equation at the 5-percent level.
In sum, the evidence obtained from the parameter stability tests indicate that the
cointegrated VAR model does exhibit constant long-run parameters whereas the short-run
dynamics of the model show parameter instability.

As a set of alternative tests, we also estimated the cointegration equation between the
real house price and real GDP per capita as follows:

\[ y_{zt} = \phi_0 + \phi_1 \cdot z_{ht} + \varepsilon_i, \]  \hspace{1cm} (12)

where \( y_{zt} \) denotes real GDP per capita and \( z_{ht} \) denotes the real house price. We estimate the
parameters in equation (12) using the FM-OLS estimator. Table 5 reports the results of the
various parameter stability tests. The Nyblom-Hansen \( L_c \) test cannot reject the null hypothesis
of cointegration at any reasonable level. Similarly, the Mean-\( F \) and Exp-\( F \) tests cannot reject
the null hypothesis of unchanging parameters in the cointegration equation. In other words,
we do not find evidence of gradual shifting of the parameters of the cointegration equation.
Finally, the Sup-\( F \) test, however, suggests a one-time shift in the cointegration relationship.

Recursive and Rolling-Window Parameter Stability

Since the parameter constancy tests point to structural change, we estimate the VAR model
using recursive and rolling window regression techniques. The recursive estimator starts with
a benchmark sample period and then adds one observation at a time keeping all observations
in prior samples so that the sample size grows by one with each iteration. The rolling-window
estimator, also known as fixed-window estimator, alters the fixed length benchmark sample
by moving sequentially from the beginning to the end of sample by adding one observation
from the forward direction and dropping one from the end. Assume that each rolling
subsample includes 15 annual observations (i.e., the window size is equal to 15). In each step
for the recursive and moving window models, we determine a VAR model using the LR, FPE,
AIC, SIC, and HQIC to choose the lag length and perform the Granger causality tests using
Bootstrap method on each subsample. This provides us with a sequence of 48 causality tests instead of just one. The recursive and rolling estimations that we adopt are justified for a number of reasons. First, recursive and rolling estimations allow the relationship between the variables to evolve through time. Second, the presence of structural changes introduces instability across different subsamples and recursive and rolling estimations conveniently capture this, in our case, by considering a sequence of 48 different subsamples (starting with the benchmark sample from 1890 to 1905). The rolling window uses a 15-year fixed window plus one lag for the VAR.

For the rolling estimations, the window size is an important choice parameter. Indeed, the window size controls the number of observations covered in each subsample and determines the number of rolling estimates, since a larger window size reduces the number of observations available for estimation. More importantly, the window size controls the precision and representativeness of the subsample estimates. Koutris et al. (2008) show that a large window size increases the precision of estimates, but may reduce the representativeness, particularly in the presence of heterogeneity. On the contrary, a small window size will reduce heterogeneity and increase representativeness of parameters, but it may increase the standard error of estimates, which reduces accuracy. Therefore, the choice of the window size should balance the trade-off between accuracy and representativeness. Pesaran and Timmerman (2005) examine the window size under structural change, where the optimal window size depends on persistence and size of the break. Their Monte Carlo simulations shows that we can minimize the bias in autoregressive (AR) parameters with window sizes as low as 20 when frequent breaks exist. In order to reduce the risk of including multiple shifts in the subsamples, the window size should be small. We follow Koutris et al. (2008) and Pesaran and Timmerman (2005) and use a rolling window of small size (i.e., 15 annual observations) to guard against heterogeneity and structural breaks. Our choice of small
window size may lead to imprecise estimates. Therefore, we apply the bootstrap technique to each subsample estimation to obtain more precise parameter estimates and tests.9

Consider first the VAR(1) system. Table 4 reports the findings for the rolling window estimates in the next to last row. The ME-$L_2$ test implies that both the real house price and real GDP per capita equations exhibit parameter instability at the 5-percent level, while the ME-$L_2$ test for the VAR system also implies parameter instability at the 5-percent level. Figure 1a provides a sample-by-sample picture of the ME-$L_2$ test statistic for the individual equation as well as the VAR system.10 Based on the ME-$L_2$ test statistic, we cannot reject the null hypothesis of stable parameters at the 5-percent level.11 The Figure does indicate several periods of time when we can reject the null of parameter stability at the 5-percent level – 1899-1901, 1907-1908, 1925-1928, 1930, and 1934. The instability in the first two periods reflect proximately instability in the GDP equation during the recessions of 1899-1900 and 1907-08,12 while during the remaining periods, the instability reflects proximately instability of the real house price equation, which occurs in 1925, 1927-1928, 1930, and 1932-1934.13 For these latter periods, the first two periods of instability largely occur during expansions while the second two periods largely occur during recessions.

Table 4 also reports the findings for the recursive estimates in the last row. Now, only the real GDP per capita equation shows evidence of parameter instability at the 1-percent

9 We also ran an analysis with a window size of 25. The qualitative results did not change, although some changes did occur in the quantitative findings. These findings are available from the authors.

10 Figure 1 only reports the significance level and mean $L_2$ norm test for the VAR system and not for the individual equations.

11 We reject parameter stability for both individual equations and VAR system, when we use sup norm. This implies that we cannot reject a temporary, but somewhat persistent, deviation from the normal parameter levels, but we can reject it against a single-break alternative.

12 All references to recessions and expansions come from the National Bureau of Economics (NBER) Business Cycle Dating Committee.

13 The 5-percent critical values for the individual equations in the rolling and recursive specifications equal 2.2448 and 1.5444, respectively, which are not shown in the Figure.
level, whereas the real house price equation does not show evidence of parameter instability. Moreover, the VAR system also shows evidence of parameter instability at the 5-percent level. Figure 1b plots the FL-L2 test statistic for the individual equation as well as the VAR system. Based on the FL-L2 test statistic, we can reject the null hypothesis of stable parameters at the 5-percent level. Moreover, we also see on long-period of time when we reject the null hypothesis of parameter stability for the recursive subsamples – 1901-1944. The instability over this period always reflects instability in the GDP equation, which occurs from 1901-1944, while instability in the real house price equation only occurs from 1930-1938.

Finally, Table 5 reports the long-run trend regression. The findings for the rolling and recursive window specifications paint different pictures. The ME-L2 test implies that long-run trend equation exhibits parameter stability for the rolling regression at the 5-percent level, but parameter instability for the recursive specification at the 1-percent level. For the rolling window regressions, Figure 1c plots the ME-L2 test statistic. The ME-L2 test statistic indicates that the parameters remain stable over the entire period. The statistics reported for each subsample over the entire period, however, suggest parameter instability at the beginning and end of the full sample – 1896-1900 and 1938-1944. For the recursive regressions, Figure 1d plots the FL-L2 test statistic. The FL-L2 test statistic indicates that the parameters do not remain stable over the entire period. In addition, the statistics reported suggest that parameter instability begins shortly after the beginning of the full sample and ends just before it ends, That is, the test suggests instability from 1895-1949.

While we find mixed evidence of parameter stability and instability across our full sample, certain patterns of stability and instability still exist. Generally, our findings support stability of the long-run parameters, but instability of the short-run parameters. When we examine, however, the stability tests for the individual rolling or recursive estimates across
the full sample, we find evidence of instability in all cases for certain portions of the full sample. Any instability of parameters uncovered argues that the full-sample Granger causality tests prove unreliable. Thus, we turn now to an analysis of our rolling 15-year window estimates of Granger causality over the full-sample period from 1890 to 1952. These tests will give a better picture of the changing nature of Granger temporal causality over our sample period.

Rolling-Window Estimates

Since we want to consider how Granger temporal causality may alter as we move through the sample period 1890 to 1952, we propose to estimate the $VAR(1)$ system on a rolling basis with a 15-year window.\textsuperscript{14} In addition, we estimate the bootstrap p-value of observed $LR$-statistic rolling over the whole sample period 1898 to 1945 to further examine the likely temporal changes in the causality relationship.\textsuperscript{15} As stated above, we adopt the bootstrap approach with the Toda and Yamamoto (1995) modified causality tests because of several advantages. In particular, this test applies to both cointegrated and non-cointegrated $I(1)$ variables (Hacker and Hatemi-J, 2006). We calculate the bootstrap p-values of the null hypotheses that the real house price does not Granger cause real GDP per capita and that real GDP per capita does not Granger cause the real house price using the $RB$ method. More precisely, we compute the $RB$ p-values of the modified $LR$-statistics that tests the absence of Granger causality from the real house price to real GDP per capita or vice-versa. We compute these from the $VAR(1)$ defined in equation (2) fitted to rolling windows of 15 observations. For this reason, we only report the results with window size of 15.

\textsuperscript{14} To do this, we estimate the $VAR$ model in equation (1) for a time span of 15 years rolling through $t = \tau - 14, \tau - 12, ..., \tau = 1905, ..., 1952$. Since we estimate a $VAR(1)$ system, we lose one observation at the beginning of the sample, which explains why the first 15-year sample runs from 1891 to 1905.

\textsuperscript{15} Recall that our first 15-year sample period runs from 1891 to 1905. We report the findings for that sample at the mid-point of the 15 years from 1891 to 1905, or 1898. In other words, the point for 1898 reports the value for the 1891 to 1905 15-year window.
We also compute the magnitude of the effect of the real house price on real GDP per capita and the effect of real GDP per capita on the real house price. We calculate the effect of the real house price on real GDP per capita as the mean of the all bootstrap estimates, that is, 

$$N_b^{-1} \sum_{k=1}^{P} \hat{\phi}_{hy,k}^{*},$$

where $N_b$ equals the number of bootstrap repetitions. Analogously, we calculate the effect of real GDP per capita on the real house price as the mean of the all bootstrap estimates, that is 

$$N_b^{-1} \sum_{k=1}^{P} \hat{\phi}_{yh,k}^{*}.$$ 

We calculate these results rolling through the whole sample with a fixed window size of 15 years. The estimates $\hat{\phi}_{hy,k}^{*}$ and $\hat{\phi}_{yh,k}^{*}$ are the bootstrap least squares estimates from the VAR in equation (2) estimated with the lag order of $p$ determined by the BIC for each subsample. In our case, the number of bootstraps equals 2,000 and the number of lags equals one. We also calculate the 95-percent confidence intervals, where the lower and upper limits equal the 2.5th and 97.5th quantiles of each of $\hat{\phi}_{hy,k}^{*}$ and $\hat{\phi}_{yh,k}^{*}$, respectively.

Figure 2 plots the bootstrap p-values of the rolling test statistics, while Figure 3 plots the magnitude of the effects of each series on the other with the horizontal axes showing the mid-point observation in each of the 15-year rolling windows. For example, the value posted at year 1936 in the Figures represents the rolling window of 1929 to 1943. Figure 2 shows the bootstrap p-values of the rolling test statistics, testing the null hypotheses that the real house price does not Granger-cause real GDP per capita and vice versa. We will evaluate the non-causality tests at 5-percent significance level. Figure 3a shows the bootstrap estimates of sum of the rolling coefficients for the effect of the real house price on real GDP per capita, while Figure 3b shows the bootstrap estimates of sum of the rolling coefficients for the effect of real GDP per capita on the real house price.
Figure 2 shows that the p-values change substantially over the sample. In addition, we do not reject the null hypotheses that the real house price does not Granger-cause real GDP per capita and vice versa at the 5-percent significance level during most of the sample. We can reject the null hypothesis that the real house price does not Granger-cause real GDP per capita at the 5-percent significance level during 1925 and 1927-1934. We can also reject the null hypothesis that the real GDP per capita does not Granger-cause the real house price at the 5-percent significance level only during 1928-1929. Figure 3a shows that the effect of the real house price on real GDP per capita proves significantly negative at the 5-percent level (two-tailed test) during 1911-1912 and significantly positive during 1925 and 1927-1934, while Figure 3b shows that the effect of the real GDP per capita on the real house price proves significantly negative at the 5-percent level (two-tailed test) during 1916-1917, 1919, 1922-1923, 1926-1930, 1932, and 1934-1936 and significantly positive during 1940-1945.

Shiller (2005) notes a sharp fall in real home prices following WWI, which he links to the 1918-1919 flu pandemic. That is, potential home buyers did not look to purchase new homes, implying a significant drop in demand. Further, real home prices did not boom along with stock prices during the “roaring twenties,” nor did real home prices move much during the Great Depression as nominal housing prices and the consumer price index (CPI) fell in unison. The next major change in real housing prices occurred during WWII, when real housing prices jumped to much higher levels. Shiller (2005) argues that real housing prices began increasing in 1942 as home buyers anticipated a housing shortage as veterans returned from war to start a family. From 1940 to 1945, real GDP per capita caused a significant positive effect on real housing prices.

In sum, we find evidence of the real house price Granger causes real GDP per capita during the Great Depression, but not during other periods of our 1890 to 1952 sample of annual data. Moreover, when the real housing price Granger causes real GDP per capita, we
also generally find some evidence that real GDP per capita Granger causes the real housing price. Finally, when bidirectional causality existed, the effects tended to stabilize rather than destabilize their movements. That is, when real GDP per capita significantly increased real housing prices, real housing prices significantly decreased real GDP per capita during 1937-1930, 1932, and 1934.

4. Conclusion

This paper considers the role of the real housing price in the Great Depression, examining structural stability between the real housing price and real GDP per capita. Using annual US data from 1890 to 1952, the paper examines the long-run and short-run dynamic relationships between the real housing price and real GDP per capita to see if these relationships change over time. More specifically, we adopt the bootstrap approach with the Toda and Yamamoto (1995) modified causality tests because of several advantages.16

Overall, our tests suggest that the relationship between real GDP per capita and the real house price experienced structural shifts over the 62-observation sample from 1890 to 1952. Clear evidence suggests that the real house price Granger caused real GDP per capita only in rolling sub-samples that include a sufficient number of Great Depression years, but not other rolling sub-samples that exclude most of the Great Depression. That is, we find such evidence for 15-year subsamples that cover data from 1918 to 1941. At the same time, somewhat less evidence also exists that real GDP per capita Granger caused the real house price only during the Great Depression. Moreover, when bidirectional causality existed, the two effects did not lead to reinforcing movements, but rather the effects tended to offset each other. Here, we find such evidence for 15-year subsample that cover data from 1921 to 1936.

16 One might consider using fractional integration and cointegration, since fractional integration intimately relates to parameter stability (Granger and Hyung, 2004). The Toda-Yamamoto (1995) approach, however, does not require cointegration, but just I(1) variables. Lack of cointegration also highlights long-run instability. So, with the existence of short-run instability as well, our analysis of doing rolling causality is well-motivated.
Furthermore, no evidence of Granger causality between real GDP per capita and the real house price exists for any other periods in our full sample from 1890 to 1952.

Fisher’s (1933) debt deflation theory of the Great Depression may play a role in our findings, although our empirical analysis does not explicitly consider mortgage debt, but rather the effect of real housing prices. As noted above, real housing prices did not fall during the Great Depression, but nominal housing prices did. Thus, as Shiller (2005, p. 15-16) notes falling nominal housing prices pushed some home owners with (short-term) mortgages into negative equity positions, precipitating mortgage defaults. The defaulting on mortgage debt due to deflation may explain to some extent our findings that real housing prices did play a role in the movement of real GDP per capita. Furthermore, the role of CPI deflation, in general, and housing price deflation, in particular, gives credence to the “money” view of the Great Depression.

Finally, as noted in the introduction, Bernanke (2008) identified the importance of the housing market and housing finance in the Great Recession. Further, Reinhart and Rogoff (2009) note that financial crises, which can involve housing market and housing finance distress, generate much longer and deeper recessions, on average. Thus, our findings for the Great Depression can provide some guidance for understanding the most recent financial crisis and Great Recession.

References:


### Table 1: Unit-Root Test Results

<table>
<thead>
<tr>
<th>Series</th>
<th>Level</th>
<th>First differences</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Constant(^a)</td>
<td>Constant and Trend(^b)</td>
</tr>
<tr>
<td>Real House Price</td>
<td>-1.94</td>
<td>-1.73</td>
</tr>
<tr>
<td>Real GDP per Capita</td>
<td>-0.28</td>
<td>-2.05</td>
</tr>
</tbody>
</table>

Notes: Phillips-Perron test statistics based on the Newey-West Bartlett kernel with bandwidth 3.

\(^a\) A constant is included in the test equation; one-sided test of the null hypothesis that a unit root exists; 1-, 5-, and 10-percent significance critical values equal -3.54, -2.91, and -2.59, respectively.

\(^b\) A constant and a linear trend are included in the test equation; one-sided test of the null hypothesis that a unit root exists; 1-, 5-, and 10-percent critical values equal -4.11, -3.48, and -3.17, respectively.

* indicates significance at the 1-percent level.

### Table 2: Multivariate Cointegration Test Results: Real House Price and Real GDP per Capita

<table>
<thead>
<tr>
<th>Series</th>
<th>Null Hypothesis</th>
<th>Alternative Hypothesis</th>
<th>Trace Test</th>
<th>Maximum Eigenvalue Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>Real House Price and GDP</td>
<td>( r = 0 )</td>
<td>( r &gt; 0 )</td>
<td>3.49</td>
<td>3.20</td>
</tr>
<tr>
<td>Real GDP per Capita</td>
<td>( r \leq 1 )</td>
<td>( r &gt; 1 )</td>
<td>0.29</td>
<td>0.29</td>
</tr>
</tbody>
</table>

Notes: One-sided test of the null hypothesis that the variables are not cointegrated. The critical values for the trace and maximum eigenvalue tests come from Osterwald-Lenum (1992) and equal 5-percent critical values equal to 15.49 and 14.26, respectively, for testing \( r = 0 \) and 3.84 and 3.84, respectively, for testing \( r \leq 1 \).

** indicates significance at the 5-percent level.

### Table 3: Full-Sample Granger Causality Tests

<table>
<thead>
<tr>
<th></th>
<th>( H_0: ) Real House Price does not Granger cause Real GDP per Capita</th>
<th>( H_0: ) Real GDP per Capita does not Granger cause Real House Price</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Statistics</td>
<td>( p)-value</td>
</tr>
<tr>
<td>Standard VAR(1) LR-Test</td>
<td>0.028</td>
<td>0.866</td>
</tr>
<tr>
<td>Bootstrap LR Test</td>
<td>0.027</td>
<td>0.887</td>
</tr>
</tbody>
</table>

Notes: * and *** indicate significance at the 10 and 1 percent levels, respectively.
### Table 4: Parameter Stability Tests in VAR(1) Model

<table>
<thead>
<tr>
<th></th>
<th>Real House Price Equation</th>
<th>Real GDP per Capita Equation</th>
<th>VAR(1) System</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Statistics</td>
<td>Bootstrap p-value</td>
<td>Statistics</td>
</tr>
<tr>
<td>Mean-F</td>
<td>7.01</td>
<td>0.03</td>
<td>20.93</td>
</tr>
<tr>
<td>Exp-F</td>
<td>12.06</td>
<td>&lt;0.01</td>
<td>24.36</td>
</tr>
<tr>
<td>Sup-F</td>
<td>31.51</td>
<td>&lt;0.01</td>
<td>55.58</td>
</tr>
<tr>
<td>$L_c$</td>
<td>0.12</td>
<td>0.86</td>
<td>0.70</td>
</tr>
<tr>
<td>Rolling Fluctuation (ME)</td>
<td>1.23</td>
<td>0.32</td>
<td>1.16</td>
</tr>
<tr>
<td>$L_2$ norm</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Recursive Fluctuation (FL)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$L_2$ norm</td>
<td>0.68</td>
<td>0.20</td>
<td>3.20</td>
</tr>
</tbody>
</table>

Notes: We calculate $p$-values using 2,000 bootstrap repetitions.

### Table 5: Parameter Stability Tests in Long-Run Relationship FM-OLS

<table>
<thead>
<tr>
<th></th>
<th>Mean-F</th>
<th>Exp-F</th>
<th>Sup-F</th>
<th>$L_c$</th>
<th>Rolling $L_2$ norm</th>
<th>Recursive $L_2$ norm</th>
</tr>
</thead>
<tbody>
<tr>
<td>$z_{yt} = \phi_0 + \phi_1 \cdot z_{ht}$</td>
<td>129.76</td>
<td>133.64</td>
<td>274.02</td>
<td>0.17</td>
<td>1.34</td>
<td>5.14</td>
</tr>
<tr>
<td>Bootstrap $p$ value</td>
<td>1.00</td>
<td>1.00</td>
<td>&lt;0.01</td>
<td>0.70</td>
<td>0.24</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Notes: We calculate $p$-value using 2,000 bootstrap repetitions.
Figure 1a: Rolling VAR Stability: ME-$L_2$ Test

Figure 1b: Recursive VAR Stability: FL-$L_2$ Test
Figure 1c: Rolling Long-Run *FM-OLS* Stability: ME-$L_2$ Test

Figure 1d: Recursive Long-Run *FM-OLS* Stability: FL-$L_2$ Test
Figure 2: Granger Causality Test p-Values: Rolling Window Estimates
Figure 3a: Granger Causality: Sum Coefficients, Real House Price Causes Real GDP per Capita

Figure 3a: Granger Causality: Sum Coefficients, Real GDP per Capita Causes Real House Price