Interaction of Formal and Informal Financial Markets in Quasi-Emerging Market Economies

Harold P.E. Ngalawa*and Nicola Viegi[†]

January 10, 2013

Abstract

The primary objective of this paper is to investigate the interaction of formal and informal financial markets and their impact on economic activity in quasi-emerging market economies. Using a four-sector dynamic stochastic general equilibrium model with asymmetric information in the formal financial sector, we come up with three fundamental findings. First, we demonstrate that formal and informal financial sector loans are complementary in the aggregate, suggesting that an increase in the use of formal financial sector credit creates additional productive capacity that requires more informal financial sector credit to maintain equilibrium. Second, it is shown that interest rates in the formal and informal financial sectors do not always change together in the same direction. We demonstrate that in some instances, interest rates in the two sectors change in diametrically opposed directions with the implication that the informal financial sector may frustrate monetary policy, the extent of which depends on the size of the informal financial sector. Thus, the larger the size of the informal financial sector the lower the likely impact of monetary policy on economic activity. Third, the model shows that the risk factor (probability of success) for both high and low risk borrowers plays an important role in determining the magnitude by which macroeconomic indicators respond to shocks.

Key words: Informal financial sector, formal financial sector, monetary policy, general equilibrium

JEL Codes: E44, E47, E52, E58

1 Introduction

For many years, informal financial markets have been perceived as an economic ill that has only succeeded in exploiting impoverished peasants in quasi-emerging market economies

^{*}University of KwaZulu-Natal, Westville Campus, Durban 4000. Emails: ngalawa@ukzn.ac.za/ hn-galawa@yahoo.co.uk

[†]University of Pretoria, School of Economics, Lynnwood Road, Pretoria 0002. Emails: nicola.viegi@up.ac.za / viegin@gmail.com

(QEMEs) (Bolnick, 1992)¹. The policy prescription, as expected, has been to integrate the informal financial sector (IFS) in the formal financial sector (FFS) (see Aryeetey, 2008; Bolnick, 1992; Bell, 1990). Recent research, however, has shown an emerging change in opinion with the sector now being regarded more positively as an integral component of the whole financial sector. Chipeta and Mkandawire (1991), for instance, report that the IFS in Malawi plays an important role in alleviating economic hardships among low-income groups by enabling these groups to mobilise resources (savings effect), use the resources to earn income (investment effect) and obtain loans (credit effect). An account of similar findings is presented by Steel, Aryeetey, Hettige and Nissanke (1997) in a study of Ghana, Malawi, Nigeria and Tanzania. Steel et al. (1997) stress that informal financial institutions (IFIs) in the three countries are an important vehicle for mobilising household savings and financing small businesses, a function that is carried out using specialized techniques that address the problems of information, transaction costs and risks, which prevent banks from serving these market segments. In Kenya, Atieno (2001) observes that unlike commercial banks, informal credit sources provide easier access to credit facilities for small and micro-enterprises.

The co-existence of the FFS with a large IFS is one of the fundamental distinguishing features of QEMEs. Several studies have shown that the IFS in QEMEs is large (see for example African Development Bank, 1994; Chipeta and Mkandawire, 1991) and growing (see for example Chipeta, 1998; Sovibo, 1997; Bagachwa, 1995; Aryeetey, 1994; Chipeta and Mkandawire, 1991). According to the African Development Bank (1994), 70 percent of the total population in Cameroon and 80 percent in Zambia take part in informal financial activities. The African Development Bank (1994) also reveals that 85 percent of rural households in Niger and over 80 percent of smallholder farmers in Zimbabwe have access to informal credit, and 60 percent of the population in Ethiopia and 52 percent in Senegal participate in rotating savings and credit associations (ROSCAs). In Malawi, Chipeta and Mkandawire (1991) observed that in 1989, the IFS was larger than the FFS when measured in terms of credit extended to the private sector. They arrived at the same result by comparing savings mobilised by the formal and informal financial sectors. Field surveys carried out in Nigeria by Soyibo (1997), in Ghana by Aryeetey (1994), in Malawi by Chipeta and Mkandawire (1991) and in Tanzania by Bagachwa (1995) established that the IFS grew faster than the FFS in the reform years 1990-1992 (Chipeta, 1998).

Given its sheer size, the IFS's response to policy is expected to be non-trivial and the consequent effect on economic policy may not be obvious - it is likely to vary depending on whether informal financial markets are autonomous or reactive to formal financial markets (See Rahman, 1992; Acharya and Madhura, 1983; Sundaram and Pandit, 1984); whether the

¹We define QEMEs as low income countries characterised by weak monetary and fiscal institutions and a formal financial sector that co-exists with a large informal financial sector.

two markets are competitive or complementary; and whether the nature of their interaction frustrates or strengthens monetary policy. Unfortunately, nearly all QEMEs leave out informal financial transactions in official monetary data, effectively underestimating the volume of financial transactions and bringing into question the timing and effect of monetary policy on economic activity. This paper contributes to the literature by investigating these and other issues. Using a macromonetary model with microeconomic foundations, we study the interaction of formal and informal financial markets and analyse the resulting impact on economic activity in QEMEs.

The term informal finance is used in this study to refer to legal but unregulated financial activities that take place outside official financial institutions, and are not directly amenable to control by key monetary and financial policy instruments. Encompassed in this definition is the mobilisation and lending of financial resources by friends, relatives, neighbours, grocers, local merchants/traders, landlords, tenants, grain millers, moneylenders, non-rotating savings and credit associations (SCAs), rotating savings and credit associations (ROSCAs), cooperative and savings associations (CSAs), and microfinance institutions, among others.

The IFS is known for its fragmentation into sub-sectors. The village merchant, for instance, may agree to lend money only to those who buy regularly from his shop; a landlord may also give credit only to those who work for him; while friends, relatives and neighbours may only lend to each other. Effectively, the credit market is broken up into small 'credit islands'(Basu, 1997). There is no reason, however, to believe that these sub-markets are mutually exclusive. The market segments are likely to have interlocking spaces serving clients in more than one sub-market, making the concept of market fragmentation complex. For simplicity, the IFS is assumed to be one large market where interest rates may be different but generally change together in the same direction.

The choice of a DSGE framework for analysis is motivated by a number of factors. First, DSGE models are derived from microeconomic foundations of constrained decision-making. That is, they describe the general equilibrium allocations and prices in the economy where all agents dynamically maximise their objectives subject to budget or resource constraints (Tovar, 2008). Following the estimation of deep parameters, therefore, it is possible to avoid the Lucas Critique, where only models in which the parameters that do not vary with policy interventions are suited to evaluate the impact of policy change (Ibid, 2008). Indeed, according to Woodford (2003), DSGE models should not, at least in principle, be vulnerable to the Lucas Critique, unlike the more traditional macroeconomic forecasting models. Second, DSGE models are structural, implying that each equation has an economic interpretation which allows clear identification of policy interventions and their transmission mechanisms (Peiris and Saxegaard, 2007). Third, DSGE models are forward looking in the sense that

agents optimise model-consistent forecasts about the future evolution of the economy (Ibid, 2007). Fourth, DSGE models allow for a precise and an unambiguous examination of random disturbances. This is facilitated by the stochastic design of the models. To the best of our knowledge, there is no study that has examined the interaction of formal and informal financial sectors and their impact on economic activity in QEMEs using a macromonetary model developed within the context of a microfounded DSGE representation.

Following this introduction, the rest of the paper is structured as follows. A DSGE model for QEMEs is developed in Section 2. The model aims at building a quantitative macroeconomic representation from explicit optimising behaviour while allowing for a minimum amount possible of imperfections. Thus, the model is similar in many aspects to the Real Business Cycle (RBC) approach except on the monetary side (see Tovar, 2008; Mankiw, 2006). Calibrations of parameter and steady state values are presented in Section 3. Section 4 interprets simulation results of the model from three experiments, each illustrating impulse responses of selected macroeconomic indicators to a particular shock. The three shocks in the experiments include a positive production technology shock, a monetary policy shock and a risk factor shock. A summary and conclusions are presented in Section 5.

2 A DSGE Model for QEMEs

2.1 Basic Design

There are four sectors in the economy: households, firms, financial intermediaries and monetary authorities. The household maximises an intertemporal utility function separable in consumption, leisure, and real cash balances; and its financial resources are used for consumption or held as cash balances with the excess deposited in commercial banks or lent out to firms in the informal credit market. The financial system is segmented into formal and informal financial sectors. We generalise service providers in the FFS as commercial banks and in the IFS as moneylenders. While commercial banks are corporate institutions, moneylenders are usually individuals, each person operating as a business unit. In rare cases, moneylenders have been observed to hire agents (Bolnick, 1992).

Besides the fact that the business is run by individual persons, moneylending usually has no formal accounts and is often run without official registration. It is, therefore, difficult to isolate moneylending from the household as a completely separate institution. Accordingly, we consolidate the household and moneylending activities and assume that the behaviour of moneylenders is decribed within the household's utility maximisation problem. Nonetheless, we allow the moneylending function to operate distinctly within the household framework. We describe the household's credit function as 'moneylending' and we reserve the term 'moneylenders' for credit institutions in the IFS. Thus, the term 'moneylenders' is used as a blanket reference to all creditors in the IFS, including the moneylenders themselves, traders, landlords, estate owners and grainmillers, among others, rather than as a reference to the usury market only.

The firm produces its own capital by converting loans obtained from the formal or informal financial sectors, which are assumed to be perfect substitutes (see Dasgupta, 2004). Using capital and labour as the only factors of production, the firm produces final output using technology described by a Cobb Douglas production function. In the financial market, firms self-selectively seek loans either in the formal or informal credit markets. While lenders in the IFS deal with local communities for which they are able to identify risk levels of individual potential borrowers, the same does not apply to commercial banks in the FFS. Commercial banks are unable to distinguish between high and low risk borrowers ex-ante because high risk borrowers disguise themselves as low risk borrowers in order to enhance their chances of obtaining credit in the FFS. We assume the commercial banks have a preference for low risk borrowers emmanating from the view that low risk borrowers are associated with a relatively higher rate of loan repayment, which translates into higher expected profits for the banks than is the case with high risk borrowers. At this point, we invoke the Stiglitz and Weiss (1981) hypothesis that banks may ration credit in equilibrium.

The residual demand that is rationed out of the formal loan market spills over to the informal credit market. Accordingly, the IFS provides credit to this demand as well as the component of total credit demand which self selectively seeks loans in the IFS only. Finally, we assume that the population is constant so there is no aggregation bias with treating average quantities as aggregate quantities (see Dasgupta, 2004).

2.2 Household Sector

There is a continuum of identical households with identical endowments and preferences. The objective of a representative household of constant size with a constant amount of time per period and an infinite planning horizon is to maximise the expected sum of a discounted stream of instantaneous utilities U_t given by:

$$\max E_0 \sum_{t=0}^{\infty} \beta^t U_t \tag{1}$$

where $\beta \epsilon (0, 1)$ is the consumer subjective intertemporal discount factor. The utility function is assumed to be separable in consumption (C_t) , leisure $(1 - N_t)$ and real cash balances $\left(\frac{M_t}{P_t}\right)$:

$$U_t = \ln C_t + \Phi \ln \left(1 - N_t\right) + \Gamma \ln \left(\frac{M_t}{P_t}\right)$$
(2)

where N_t is time t labour (the amount of time worked) and $\Phi, \Gamma > 0$ represent the importance of leisure and real cash balances, respectively, in utility. The utility function $U_t(.,.,.)$ satisfies $U_{t,C_t} > 0, U_{t,(1-N_t)} > 0, U_{t,(\frac{M_t}{P_t})} > 0, U_{t,C_t,C_t} < 0, U_{t,(1-N_t),(1-N_t)} < 0$ and $U_{t,(\frac{M_t}{P_t}),(\frac{M_t}{P_t})} < 0$. The household's financial resources are used for consumption, deposited in commercial banks, held in cash or lent out to firms. We assume the household lends money to firms or deposits funds in commercial banks from its own earnings. Maximisation of the household's objective function, therefore, is subject to the following intertemporal budget constraint:

$$C_t + L_t^i + D_t + \frac{M_t}{P_t} = \left(1 + R_{t-1}^{li}\right) q L_{t-1}^i + \left(1 + R_{t-1}^{df}\right) D_{t-1} + \frac{M_{t-1}}{P_{t-1}} + W_t N_t$$
(3)

where L_t^i are loans to firms given by households (informal finance), which we generalise as moneylending, D_t are the household's deposits in commercial banks, R_t^{li} are interest rates on credit given by the households, q_t is the probability of repayment on loans given by the moneylenders, R_t^{df} are interest rates on deposits in commercial banks and W_t is the wage rate. Maximising the objective function given in equation (1) subject to the budget constraint in equation (3) with respect to consumption, labour, cash balances, and the household's loans to firms and deposits in commercial banks, yields the following first order conditions:

$$\frac{1}{C_t} = \beta \left(1 + R_t^{df} \right) E_t \left(\frac{1}{C_{t+1}} \right) \tag{4}$$

$$N_t = 1 - \frac{\Phi C_t}{W_t} \tag{5}$$

$$\frac{M_t}{P_t} = \Gamma \beta E_t \left(\frac{C_{t+1}}{R_t^{df}}\right) \tag{6}$$

$$1 + R_t^{df} = \left(1 + R_t^{li}\right)q\tag{7}$$

Equation (4) is the Euler equation (intertemporal consumption function). Equation (5) is a labour supply equation. It illustrates that consumption and labour supply are inversely related due to decreasing marginal utility of consumption. Equation (6) is a money demand equation. It states that the demand for real cash balances is negatively related to interest rates and positively related to future consumption. Equation (7) states that for the household in equilibrium, the effective return on deposits in commercial banks is equal to the return on loans given out on the informal financial market, taking into account the risk of default.

2.3 The Firm

Agriculture in low income countries often accounts for at least half of GDP and 60 to 80 percent of total employment (International Finance Corporation, 2009). For generality, therefore, it is safe to assume that a representative firm in a QEME is small and engaged in agricultural activities. The firm owns land and requires working capital, which it borrows at the beginning of the period from either the formal or informal financial sector and repays at the end of the period after selling its harvest. For simplicity, we assume that a firm cannot borrow from both sectors at any given time. We further postulate that there are no adjustment costs and that the working capital is predetermined at time t (Ambler and Paquet, 1994). The equation of motion for the capital stock is given by:

$$K_{t+1} = (1 - \delta) K_t + I_t$$
(8)

where K_t is capital, I_t is investment and δ is depreciation. Since the working capital is used up in a single period, depreciation is equivalent to $\delta = 1$, which reduces equation (8) to $K_{t+1} = I_t$. We assume the loan is converted into current investment (change in capital) using a linear function described as:

$$I_t = \vartheta_{\tau,t} \left(L_t^f + L_t^i \right) \tag{9}$$

where ϑ_{τ} is a risk factor or probability of success ($\forall \tau = hr, lr$, where hr denotes high risk (low probability of success) and lr stands for low risk (high probability of success)); and L_t^f and L_t^i are formal and informal financial sector loans, respectively. We define high risk firms as those firms that have a lower probability of success in converting the loans into capital while low risk firms are defined analogously as those firms with a higher probability of success in converting their loans into capital (see Dasgupta, 2004). This is a case of a generic firm. In the aggregate, a proportion (ρ) of all firms are high risk borrowers and the remaining proportion $(1 - \rho)$ are low risk borrowers. Total lending, therefore, is described as:

$$I_{t} = \rho \vartheta_{hr,t} \left(L_{t}^{f} + L_{t}^{i} \right) + (1 - \rho) \vartheta_{lr,t} \left(L_{t}^{f} + L_{t}^{i} \right)$$
$$I_{t} = \left[\rho \vartheta_{hr,t} + (1 - \rho) \vartheta_{lr,t} \right] \left(L_{t}^{f} + L_{t}^{i} \right)$$
(10)

The firm's production technology is assumed to be given by a Cobb-Douglas formulation of the following form:

$$Y_t = e^{A_t} K_t^{\alpha} N_t^{1-\alpha} \tag{11}$$

where Y_t is output and $A_t > 0$ captures technology. The technology factor is assumed to evolve according to a first order autoregressive process given by:

$$A_t = \eta A_{t-1} + \varepsilon_t^A \tag{12}$$

where ε_t^A is independently and identically distributed (*iid*) with a standard deviation of σ_{ε^A} . The firm's cost minimisation problem subject to satisfying market demand, therefore, is given by:

$$\min_{K_t, N_t} W_t N_t + \left(1 + R_t^{lf}\right) L_t^f + \left(1 + R_t^{li}\right) q L_t^i + \phi_t \left(Y_t - e^{A_t} K_t^{\alpha} N_t^{1-\alpha}\right)$$
(13)

where ϕ_t is a Lagrangian multiplier. First order conditions with respect to labour, FFS loans and IFS loans yield demand functions for labour and formal and informal financial sector loans, in that order, given by:

$$W_t = \phi_t \left(1 - \alpha\right) \frac{Y_t}{N_t} \tag{14}$$

$$L_t^{df} = \frac{1}{\vartheta_{\tau t}} E_t \left[\frac{(1-\alpha)\left(1+R_t^{lf}\right)K_{t+1}^{\alpha}}{\alpha\vartheta_{\tau t}W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(15)

$$L_t^{di} = \frac{1}{\vartheta_{\tau t}} E_t \left[\frac{(1-\alpha) \left(1+R_t^{li}\right) q K_{t+1}^{\alpha}}{\alpha \vartheta_{\tau t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(16)

Equation (14) shows that wages increase with output but are inversely related to labour supply. Equations (15) and (16) show the self-selection of firms in seeking formal and informal financial sector loans, respectively. While some firms approach the FFS first, others selfselectively approach the IFS for credit. Given that $\alpha < 0$, both demand functions show that the demand for loans increases with higher expected wages and employment.

2.4 Financial Intermediaries

An important distinguishing feature of low income economies is the segmentation of the financial system into formal and informal financial sectors. Within the two broad segments, there are several different types of operators that usually have very little contact with one another and whose clients often do not overlap; and even when they overlap, they are able to sort out clearly which aspects of their financial business will be handled by which financial arrangement (Aryeetey, 2008). To model the two sectors, we build on the ideas of Dasgupta (2004).

2.4.1 Formal Financial Sector

Base lending rates are set as a mark-up (ζ) over the bank rate i.e. $R_t^{lf} = R_t^{nr} + \zeta$, where R_t^{nr} is the bank rate. The size of the mark-up depends on a commercial bank's market power, reflecting its estimate of the interest elasticity of the demand for credit (King, 2003). For simplicity, we assume the mark-up is fixed. Aggregate self-selection demand for loans in the FFS is given by:

$$L_{t}^{adf} = \frac{\rho}{\vartheta_{hr,t}} E_{t} \left[\frac{\left(1-\alpha\right) \left(1+R_{t}^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{hr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\left(1-\rho\right)}{\vartheta_{lr,t}} E_{t} \left[\frac{\left(1-\alpha\right) \left(1+R_{t}^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(17)

We assume commercial banks are not keen to give out loans to high risk borrowers as these are associated with a high rate of default in loan repayment, which reduces the banks' expected profits. The banks, however, are not able to distinguish between the two types of borrowers *a priori* because high risk borrowers have the incentive to mimic the behaviour of low risk borrowers in order to enhance their chances of accessing the FFS loans. Against this behaviour among potential borrowers, therefore, total revealed demand for loans in the FFS is given by:

$$L_{t}^{adf} = \frac{\rho}{\vartheta_{lr,t}} E_{t} \left[\frac{\left(1-\alpha\right)\left(1+R_{t}^{lf}\right)K_{t+1}^{\alpha}}{\alpha\vartheta_{lr,t}W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\left(1-\rho\right)}{\vartheta_{lr,t}} E_{t} \left[\frac{\left(1-\alpha\right)\left(1+R_{t}^{lf}\right)K_{t+1}^{\alpha}}{\alpha\vartheta_{lr,t}W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}} \\ L_{t}^{adf} = \frac{1}{\vartheta_{lr,t}} E_{t} \left[\frac{\left(1-\alpha\right)\left(1+R_{t}^{lf}\right)K_{t+1}^{\alpha}}{\alpha\vartheta_{lr,t}W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(18)

In the absence of information that distinguishes the types, banks resort to credit rationing, turning down some loan applicants even if they are willing to pay a relatively high price (Stiglitz and Weiss, 1981). Indeed when formal credit markets are imperfect due to asymmetric information, credit rationing is the most common practice to minimise banks' exposure to risk (Dasgupta, 2004). We assume the commercial banks can only supply a fraction ϖ_t of the revealed demand for FFS loans. We further assume ϖ_t is endogenously determined within the banks' profit maximisation framework. Following the absence of information that identifies the types of potential borrowers, commercial banks decide to take a safe position by assuming the worst case scenario in which all potential borrowers are high risk. The supply function for FFS loans, therefore, is given by:

$$L_t^{sf} = \frac{\varpi_t}{\vartheta_{hr,t}} E_t \left[\frac{(1-\alpha)\left(1+R_t^{lf}\right)K_{t+1}^{\alpha}}{\alpha\vartheta_{hr,t}W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(19)

The loans given out by commercial banks to firms in the formal credit market (L_t^f) are converted from household deposits (D_t) and borrowing from the central bank (L_t^{cb}) . For simplicity, we assume there is no liquidity reserve requirement (LRR) i.e. all the deposits can be converted into loans. The intermediation technology, therefore, is assumed to be given by:

$$L_t^{sf} = D_t + L_t^{cb} \tag{20}$$

The commercial banks' profit maximisation problem is described by:

$$\max_{L_t^{adf}, \, \varpi_t} \varpi_t \left(1 + R_t^{lf} \right) L_t^{adf} + D_t + L_t^{cb} - \varpi_t L_t^{adf} - \left(1 + R_t^{df} \right) D_t - \left(1 + R_t^{nr} \right) L_t^{cb}$$

subject to $L_t^{adf} \leq (D_t + L_t^{cb})$, which reduces to:

$$\max_{L_t^{adf}, \ \varpi_t} \varpi_t R_t^{lf} L_t^{adf} - R_t^{df} D_t - R_t^{nr} L_t^{cb} \text{ subject to } L_t^{adf} \le \left(D_t + L_t^{cb} \right)$$
(21)

Taking FOCs with respect to L_t^{adf} , D_t and L_t^{cb} and solving for ϖ_t , we obtain:

$$\ell_t = \varpi_t R_t^{lf} = R_t^{nr} = R_t^{df} \tag{22}$$

$$\varpi_t = \frac{R_t^{df}}{R_t^{lf}} = \frac{R_t^{nr}}{R_t^{lf}}$$
(23)

where ℓ_t is a Lagrangian multiplier. Equation (22) states that in equilibrium, the cost of funds from the different sources (household deposits and borrowing from the central bank) will be equal (i.e. $R_t^{nr} = R_t^{df}$) and they will be proportional to the return on loans (ϖR_t^{lf}) . Alternatively, it can be inferred from equation (23) that the ratio of the cost of funds from the two identified sources defines the proportion of total demand for FFS loans that is satisfied by the commercial banks.

2.4.2 Informal Financial Sector

Loans in the IFS are provided by moneylenders. The self selection demand for IFS credit is given by:

$$L_{t}^{adi} = \frac{\rho}{\vartheta_{hr,t}} E_{t} \left[\frac{(1-\alpha) \left(1+R_{t}^{li}\right) q K_{t+1}^{\alpha}}{\alpha \vartheta_{hr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{(1-\rho)}{\vartheta_{lr,t}} E_{t} \left[\frac{(1-\alpha) \left(1+R_{t}^{li}\right) q K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$
(24)

Like commercial banks, moneylenders also face a pool of high and low risk borrowers. However, unlike the banks, the moneylenders are able to identify the risk levels of individual borrowers. Achievement of this feat owes to the localisation of moneylending to communities within the neighbourhood of the lenders, which makes risk-level information readily available.

The residual demand for credit in the FFS is defined by equation (25) as equal to the total self-selection demand for loans in the FFS (equation (17)) less the proportion of revealed demand for FFS loans that succeeds in getting loans from the commercial banks (equation (19)). This residual demand spills over to the IFS. Assuming moneylenders are able to correctly identify the risk level of each potential borrower, the FFS residual demand seeking loans in the IFS is given by:

$$\begin{split} L_t^{rf} &= \frac{\rho}{\vartheta_{hr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{hr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} - \frac{\overline{\omega}_t \left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{hr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} - \frac{\overline{\omega}_t \left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} - \frac{\overline{\omega}_t \left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} - \frac{\overline{\omega}_t \left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\vartheta_{lr,t} W_{t+1} N_{t+1}} \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\vartheta_{lr,t} W_{t+1} N_{t+1}} \left[\frac{\left(1-\alpha\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} W_{t+1} W_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} W_{t+1} W_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} W_{t+1} W_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1}^{\alpha}}{\varphi_{lr,t} W_{t+1} W_{t+1} W_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1} W_{t+1} W_{t+1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1} W_{t+1} W_{t+1} W_{t+1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1} W_{t+1} W_{t+1} W_{t+1}} + \frac{\overline{\omega}_t \left(1-\rho\right) \left(1+R_t^{lf}\right) K_{t+1} W_{t+1} W_{t+$$

$$L_{t}^{rf} = \left[\frac{\rho}{\vartheta_{hr,t}} \left(\frac{1}{\vartheta_{hr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)}{\vartheta_{lr,t}} \left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} - \frac{\varpi_{t}\rho}{\vartheta_{hr,t}} \left(\frac{1}{\vartheta_{hr,t}}\right)^{\frac{1}{\alpha-1}} - \frac{\varpi_{t}\left(1-\rho\right)}{\vartheta_{lr,t}} \left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}}\right]$$
$$E_{t} \left[\frac{\left(1-\alpha\right)\left(1+R_{t}^{lf}\right)K_{t+1}^{\alpha}}{\alpha W_{t+1}N_{t+1}}\right]^{\frac{1}{\alpha-1}}$$

$$L_{t}^{rf} = E_{t} \left[\left(\frac{1}{\vartheta_{hr,t}} \right)^{\frac{1}{\alpha-1}} \left(\frac{\rho \left(1-\varpi_{t}\right)}{\vartheta_{hr,t}} \right) + \left(\frac{1}{\vartheta_{lr,t}} \right)^{\frac{1}{\alpha-1}} \left(\frac{\left(1-\rho\right) \left(1-\varpi_{t}\right)}{\vartheta_{lr,t}} \right) \right] \\ \left[\frac{\left(1-\alpha\right) \left(1+R_{t}^{lf}\right) K_{t+1}^{\alpha}}{\alpha W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}}$$

$$(25)$$

Aggregate demand for loans in the IFS, therefore, is given by the sum of equations (24) and (25). Equation (25) is rewritten to take into account the lenders' risk hypothesis, which follows from equations (15) and (16) asserting that with the probability of default in the IFS taken into account, equilibrium formal and informal financial sector interest rates will be equal (see Basu, 1997).

$$\begin{split} L_t^{adi} &= \frac{\rho}{\vartheta_{hr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{li}\right) q K_{t+1}^{\alpha}}{\alpha \vartheta_{hr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \frac{\left(1-\rho\right)}{\vartheta_{lr,t}} E_t \left[\frac{\left(1-\alpha\right) \left(1+R_t^{li}\right) q K_{t+1}^{\alpha}}{\alpha \vartheta_{lr,t} W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} + \\ E_t \left[\left(\frac{1}{\vartheta_{hr,t}}\right)^{\frac{1}{\alpha-1}} \left(\frac{\rho\left(1-\varpi_t\right)}{\vartheta_{hr,t}}\right) + \left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} \left(\frac{\left(1-\rho\right) \left(1-\varpi_t\right)}{\vartheta_{lr,t}}\right) \right] \right] \\ \left[\frac{\left(1-\alpha\right) \left(1+R_t^{li}\right) q K_{t+1}^{\alpha}}{\alpha W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha-1}} \end{split}$$

$$L_{t}^{adi} = \left[\frac{(1-\alpha)\left(1+R_{t}^{li}\right)qK_{t+1}^{\alpha}}{\alpha W_{t+1}N_{t+1}}\right]^{\frac{1}{\alpha-1}} \left[-\frac{\rho}{\vartheta_{hr,t}}\left(\frac{1}{\vartheta_{hr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)}{\vartheta_{lr,t}}\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1-\rho}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1-\rho}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1-\rho}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}} + \frac{(1-\rho)\left(1-\varphi\right)}{\vartheta_{lr,t}}\left(\frac{1-\rho}{\vartheta_{lr,t}$$

$$L_{t}^{adi} = E_{t} \left[\frac{(1-\alpha)\left(1+R_{t}^{li}\right)qK_{t+1}^{\alpha}}{\alpha W_{t+1}N_{t+1}} \right]^{\frac{1}{\alpha-1}} \left\{ \left(\frac{\rho}{\vartheta_{hr,t}}\right)\left(\frac{1}{\vartheta_{hr,t}}\right)^{\frac{1}{\alpha-1}}\left(2-\varpi\right) + \left(\frac{(1-\rho)}{\vartheta_{lr,t}}\right)\left(\frac{1}{\vartheta_{lr,t}}\right)^{\frac{1}{\alpha-1}}\left(2-\varpi\right) \right\}$$

$$L_{t}^{adi} = (2 - \varpi_{t}) E_{t} \left[\frac{(1 - \alpha) (1 + R_{t}^{li}) q K_{t+1}^{\alpha}}{\alpha W_{t+1} N_{t+1}} \right]^{\frac{1}{\alpha - 1}} \left\{ \left(\frac{\rho}{\vartheta_{hr,t}} \right) \left(\frac{1}{\vartheta_{hr,t}} \right)^{\frac{1}{\alpha - 1}} + \left(\frac{(1 - \rho)}{\vartheta_{lr,t}} \right) \left(\frac{1}{\vartheta_{lr,t}} \right)^{\frac{1}{\alpha - 1}} \right\}$$

$$(26)$$

2.5 Monetary Authorities

Monetary authorities in QEMEs generally have a choice among three different operating targets of monetary policy: money supply, interest rate and exchange rate targets. While inflation targeting is an alternative, it is an outside option for a majority of QEMEs. Most studies (see for example Masson, Savastano and Sharma (1998; 1997)) point out that preconditions for adopting an inflation targeting framework in QEMEs are not yet present. With the wave of liberalisation in the 1980s and the 1990s, exchange rate targeting has become less popular, leaving money supply and interest rates in the fold of common monetary policy operating targets for QEMEs. Countries may target one or both instruments. We experiment with a forward-looking monetary policy rule that treats the bank rate (R_t^{nr}) as an operating tool of monetary policy to characterise how monetary authorities conduct policy in QEMEs. The forward-looking specification allows the central bank to consider a broad array of information to form beliefs about the future condition of the economy (Clarida, Gali and Gertler, 2000). The rule calls for adjustment of the bank rate based on the return on

investment, the expected change in output and expected inflation:

$$R_t^{nr} = \chi_1 R_t^{rr} + \chi_2 \Delta Y^e + (1 - \chi_2) \pi^e + \mu_t$$
(27)

where R_t^{rr} is the real rate of interest or return on investment, ΔY^e is expected change in output i.e. $\Delta Y^e = E(Y_{t+1}) - Y_t$, π^e is expected rate of inflation defined as the expected difference between real and nominal interest rates in the next period and μ_t is a disturbance term assumed to be *iid*. Since our model is in discreet time, we postulate that the marginal productivity of capital in the next period is equal to the rate of interest (see Carlstrom and Fuerst, 2003; Benhabib, Carlstrom and Fuerst, 2005) as given by:

$$R_t^{rr} = \alpha e^{A_{t+1}} K_{t+1}^{\alpha - 1} N_{t+1}^{1 - \alpha} \tag{28}$$

2.6 Market Equilibrium

In equilibrium, clearing of the final goods market implies that aggregate production is equal to demand for household consumption and private investment:

$$Y_t = C_t + I_t \tag{29}$$

where $I_t = K_{t+1}$. We assume that money is required for all transactions in the goods market. In equilibrium, therefore, the following equality will hold:

$$P_t C_t = M_t \tag{30}$$

Equation (30) is an identity illustrating an ex-post equilibrium position connoting that prices operate only on the real side of the market. Since we have used N_t to represent labour supply by the household as well as labour demand by the firm, we have implicitly assumed clearing of the labour market. The equilibrium wage is determined by the market according to equations (5) and (14). The bank rate is determined by the monetary policy reaction function in equation (27). Commercial bank deposit and IFS interest rates are endogenously determined. Base lending rates are determined by loading a fixed mark-up over the bank rate. Self-selection demand for FFS and IFS loans is given by equations (15) and (16), in that order. Equations (19) and (26) represent loans supplied by the formal and informal financial sectors, respectively. Equilibrium in the two markets follow the simultaneous equation solution of the two equations, which takes into account the spill-over of demand from the FFS satisfied by the supply in the IFS. The sum of equations (19) and (26) determines the level of capital accumulation in the economy. We assume prices adjust to equate supply and demand in every market simultaneously (see Mankiw, 1989). We further assume that money supply is exogenous. Interest rates and the price level adjust to equate supply and demand in the money market.

3 Calibrations

Several parameter estimates are adopted from the literature where their values are fairly standard. Following Liu and Gupta (2007), Hartley, Salyer and Sheffrin (1997) and Hansen (1985), the autoregressive process for the technology factor, η , is approximated at 0.91; the consumer discount factor β is assumed to be 0.99; the share of labour in output is set at 0.63, implying a value of 0.37 for α ; and economic agents are assumed to spend an estimated 21 percent of their time on work activities, suggesting a value of Φ equal to 3. According to Hartley et al. (1997), evidence from many countries shows that the time spent working, which determines Φ , and capital's share in output (α), while different, do not vary dramatically (see Table 1).

Two parameter estimates and initial values are obtained directly from quarterly data for Malawi² covering the period 1988:1-2005:4. These include parameter estimate for the markup over the bank rate to obtain base lending rate (ζ) and initial value for commercial bank deposit rates (\mathbb{R}^{df}). Other parameter estimates are obtained from equilibrium relations within the framework of the model. These are consumption parameter characterising weight of real money balances in the utility function (Γ), the lagrangian multiplier in a firm's cost minimisation function (ϕ), the factor of inertia in the base lending rate (χ_1), and the weight of expected change in output in the monetary policy rule (χ_2). Initial values of some parameters are also obtained from the model's equilibrium relations. These include initial values of employment (N), capital stock (K), consumption (C), wage rate (W) and proportion of FFS loan demand that is satisfied (ϖ). From our knowledge of QEMEs, the probability of loan repayment in the IFS (q) is estimated at 0.85 and the proportion of high risk borrowers (ϑ_{hr}) and the risk factor (probability of success) for high risk borrowers (ϑ_{hr}) and the risk factor (probability of success) for low risk borrowers (ϑ_{lr}) are adjusted in the model with the experiments.

²We have used Malawi as a representative QEME. Malawi is a low income economy with a gross national income (GNI) per capita (calculated using the Atlas Method) of US\$290 (2009 estimate). According to World Bank's classification of countries based on the 2008 GNI per capita calculated using the Atlas method, countries with a GNI per capita of less than US\$975 are low income. In addition, Malawi has a very large informal financial sector, which according to Chipeta and Mkandawire (1991), was larger than the FFS when measured in terms of credit extended to the private sector as at 1989.

Parameter	Description	Value
α	Output elasticity of capital	0.37
β	Consumer subjective intertemporal discount factor	0.99
δ	Depreciation rate	1
η	Autoregressive process for the technology factor	0.91
Γ	Weight of real money balances in the utility function	3
q	Probability of loan repayment in the IFS	0.85
Φ	Leisure parameter	3
ϕ	Lagrangian multiplier in a firm's cost minimisation function	0.8
ρ	Proportion of high risk borrowers	0.15
ϑ_{hr}	Risk factor (rate of success) for high risk borrowers	0.275/0.8
ϑ_{lr}	Risk factor (rate of success) for low risk borrowers	0.3/0.95
ζ	Mark-up over the bank rate to obtain base lending rate	0.1
χ_1	Factor of inertia in the base lending rate	0.98
χ_2	Weight of expected change in output in the monetary policy rule	0.3
C	Initial value of consumption	0.8
K	Initial value of capital stock	0.2
N	Initial value of employment	0.3
ω	Initial value of proportion of FFS loan demand that is satisfied	0.7
W	Initial value of wage rate	0.3
R^{df}	Initial value of commercial bank deposit rates	0.075

Table 1: Calibrated Parameter and Steady State Values

4 Simulation Results and Inferences

The model is solved using DYNARE in MATLAB (see Juilliard, 1996). We focus our attention on three shocks namely, a positive production technology shock characterised by an unexpected improvement in production technology; a monetary policy shock identified by an unanticipated increase in the bank rate; and a risk factor shock represented by a sudden increase in the probability of success for high risk borrowers. Figure 1 shows the impact of a positive production technology shock on various macroeconomic indicators when the success rate for high risk borrowers is low ($\vartheta_{hr} = 0.275$) and when it is relatively high ($\vartheta_{hr} = 0.8$). Figure 2 repeats the experiment but for a monetary policy shock. Impulse responses of selected macroeconomic indicators following a shock on the probability of success for high risk borrowers with high and low probabilities of success for low risk borrowers ($\vartheta_{lr} = 0.95$ and $\vartheta_{lr} = 0.3$, respectively) are presented in Figure 3.

4.1 Production Technology Shock

Figure 1 shows the impact of a production technology shock when the rate of success for high risk borrowers is low (i.e. $\vartheta_{hr} = 0.275$) and when it is high (i.e. $\vartheta_{hr} = 0.8$). An unanticipated improvement in production technology when the rate of success for high risk borrowers is low (i.e. $\vartheta_{hr} = 0.275$), as illustrated in the figure, causes a decline in marginal costs across all firms leading to a jump in output and a decline in expected prices. Since the shock causes an improvement in the marginal productivity of capital, which is equal to the instantaneous interest rate (see Carlstrom and Fuerst, 2003; Benhabib et al., 2005), we observe a rise in real interest rates, the bank rate as well as commercial bank deposit and base lending rates. Holding the risk of default constant, interest rates in the IFS adjust upwards as well, in line with the lenders' risk hypothesis (see Basu, 1997). Thus, interest rates in both the formal and informal financial sectors change together in the same direction.

As a direct consequence of the improvement in technology, labour productivity increases, consequently pushing wage rates upwards. Coupled with the increase in employment, the higher wage rates lead to a rise in households' financial resources, resulting in an increase in loans supplied by moneylenders in the IFS. Commercial banks respond to the higher output by expanding their customer base, leading to a rise in FFS loans, albeit marginally. Formal and informal financial sector loans, therefore, respond as complements. Since capital stock depends on the sum of formal and informal financial sector loans, the increase in lending by commercial banks and moneylenders is followed by a rise in capital stock.

When the rate of success for high risk borrowers is increased to 0.8, a positive production technology shock causes a larger increase in loans extended by both formal and informal financial sectors as entrepreneurs are now encouraged to venture into new business establishments and expand existing ones to take advantage of the improvement in the success rate. Accordingly, capital stock and output increase by larger proportions and expected prices also decline by a larger margin. With larger amounts of capital and output, firms demand more labour and offer larger increases in wages than when the rate of success for high risk borrowers was low. The response of interest rates in both formal and informal financial sectors, however, does not change markedly.

4.2 Monetary Policy Shock

Figure 2 shows the impact of a monetary policy shock when the rate of success for high risk borrowers is low (i.e. $\vartheta_{hr} = 0.275$) and when it is high ($\vartheta_{hr} = 0.8$). When the rate of success for high risk borrowers is low (i.e. $\vartheta_{hr} = 0.275$), an unanticipated increase in interest



Figure 1: Impulse Responses of a Production Technology Shock with High and Low Probabilities of Success for High Risk Borrowers

rates (monetary policy shock) causes an increase in base lending rates and expected forward inflation. Facing higher expected prices, households smoothen their consumption by reducing their consumption expenditures. Firms respond to the expected lower sales by cutting down on production, employment and wage rates. Accordingly, capital formation and subsequently demand for both formal and informal financial sector loans decline. Thus, lending in the two sectors is complementary. The decline in IFS loans is reinforced by the lower wages and employment, which reduce households' financial resources, consequently lowering loanable funds for moneylenders.

Moneylenders initially reduce their lending rates, possibly because the reduction in their capacity to give out loans is proportionately lower than the decline in demand for IFS loans. Thus, at the pre-shock lending rates, moneylenders have excess supply of loans, *ceteris paribus*. Since IFS loans and commercial bank deposits are substitutes to households, the excess IFS loanable funds are deposited in commercial banks, leading to a decline in commercial bank deposit rates and a gradual increase in IFS interest rates until equilibrium is attained. In this instance, it is observed that formal and informal financial sector interest rates are changing in opposite directions unlike the case in Section 4.1.

When the rate of success for high risk borrowers is increased to 0.8, an unexpected increase in the bank rate causes a larger decline in the demand for loans, both in the formal and informal financial sectors, leading to a larger drop in capital stock and a correspondingly larger decline in employment and output. Expected forward prices also go up by a larger margin causing a larger decline in consumption, output, employment, wages rates, lending (in both formal and informal financial sectors) and capital formation. There is, however, no marked change in the response of interest rates in both formal and informal financial sectors.

4.3 Risk Factor Shock

Figure 3 presents impulse response functions illustrating how various macroeconomic indicators respond to a shock on the probability of success (risk factor) for high risk borrowers. This experiment is evaluated against two scenarios: a high probability of success for low risk borrowers ($\vartheta_{lr} = 0.95$) in one instance and a low probability of success for the low risk borrowers ($\vartheta_{lr} = 0.3$) in another. Everything else remaining the same, an unexpected increase in the probability of success for high risk borrowers results in a rise in the proportion of borrowed funds that is turned into productive capital (see equations (9) and (10)). Consequently, capital, demand for labour, wage rates and output go up (see Figure 3). The expected higher wages translate into expected high costs of production, leading consumers to expect higher prices.



Figure 2: Impulse Responses of a Monetary Policy Shock with High and Low Probabilities of Success for High Risk Borrowers



Figure 3: Impulse Responses of a Shock on the Probability of Success for High Risk Borrowers with High and Low Probabilities of Success for Low Risk Borrowers

Banks perceive the unanticipated increase in the probability of success for high risk borrowers as a reduction in the risk of loans extended to this type of borrowers. Everything else being equal, overall risk on loans decreases and the banks respond by increasing their lending leading to further increases in capital, output, demand for labour, wage rates and expected prices. With the rise in employment and wage rates, households now have a larger capacity to lend. IFS lending, therefore, goes up as well. Thus, consistent with previous findings, formal and informal financial sector lending remain complementary.

Following the shock, high risk borrowers' capacity to repay their loans goes up, which motivates banks to reduce the risk premium on base lending rates as a way of attracting more borrowers. As a result, FFS interest rates decline. In the IFS, on the other hand, interest rates initially go up, reflecting the profit-sharing element that is typical in QEMEs. With higher anticipated output, the moneylender raises interest rates as a way of sharing the borrower's expected higher profits. The impact of the profit sharing element, however, is later offset by a reduction in the risk premium on lending rates necessitated by the increase in the probability of success for the high risk borrowers, causing IFS interest rates to decline. Thus, unlike the outcome in Section 4.1 and in agreement with findings in Section 4.2, we observe that interest rates in the formal and informal financial sectors are not changing together in the same direction.

Changing the risk factor (probability of success) for low risk borrowers (from 0.3 to 0.95 or vice versa), we observe that the impulse responses follow the same pattern with differences only in magnitudes. When the probability of success for low risk borrowers is increased from 0.3 to 0.95, the shock on the probability of success for high risk borrowers (characterised by an unexpected increase in the probability of success for the high risk borrowers) causes a larger increase in formal and informal financial sector loans and consequently a larger increase in capital and output. This result lends further support to previous findings that loans in the formal and informal financial sectors are complementary. A larger increase in FFS loans is followed by a larger increase in IFS loans. This occurence may be attributed to a decline in the average risk on loans following the increase in the probability of success for both types of borrowers, everything else remaining equal.

The higher rate of success for low risk borrowers ($\vartheta_{lr} = 0.95$) also leads to a larger reduction in FFS interest rates. This occurs for the same reason as outlined in the foregoing discussion. That is, a higher probability of success for low risk borrowers reduces the average risk on loans, which leads banks to respond by reducing interest rates with a relatively larger margin. The impulse responses of IFS interest rates, however, are observed to be nearly the same whenever the probability of success for low risk borrowers is high ($\vartheta_{lr} = 0.95$) and when it is low ($\vartheta_{lr} = 0.3$). Since we have assumed that there is no information asymmetry in the IFS, the reduction in the rate of success for low risk borrowers following an unexpected increase in the probability of success for high risk borrowers provides little additional information on the risk profile of potential borrowers. Accordingly, there is little justification to adjust IFS interest rates. Again, this finding is consistent with earlier results that changes in FFS interest rates are not necessarily followed by corresponding changes in IFS interest rates.

4.4 Inferences

We draw three important inferences from the experiments carried out in the model. First, the model reveals that although formal and informal financial sector loans may be substitutes in the borrowing firm's utility function, they are in effect complementary in the aggregate. A complementary credit link exists when growth in demand for credit from one sector is accompanied by an increase in demand for credit from the other sector (Chipeta and Mkandawire, 1991). This implies that an increase in capital formation financed by FFS credit creates additional productive capacity that can be utilised only with IFS credit in order to maintain the economy at an equilibrium level (see Aryeetey, 1992; Chipeta and Mkandawire, 1992). Since the IFS provides additional finance to firms in excess of what comes from the FFS, increasing the use of FFS credit increases the demand for credit in the IFS.

Second, the model shows that interest rates in the IFS are not necessarily driven by FFS interest rates. While interest rates in the two sectors are observed to change together in the same direction following a positive production technology shock, the same is not observed with either a monetary policy shock or a risk factor shock. In the case of a monetary policy shock, the response of IFS interest rates is diametrically opposed to the direction taken by FFS interest rates in response to the shock. The implication of this outcome is that the IFS may frustrate monetary policy. Illustrating this argument, Figure 2 shows that the impact of a monetary policy shock (a sudden increase in the bank rate) is partly offset by a decline in interest rates in the IFS. Following the sudden increase in the bank rate, credit extended by both the formal and informal financial sectors decline. That is, lending in the formal and informal financial sectors remains complementary. The decline in IFS loans, however, is lessened by the drop in IFS interest rates. Clearly, where the size of the IFS is large, its effect in partly offsetting the outcome of monetary policy is likely to be large as well. In the case of Malawi, for instance, where the IFS was found to be larger than the FFS in 1989 (see Chipeta 1991), the offsetting effect of the IFS on monetary policy may be so large that monetary authorities can almost be certain that the expected impact of their policy on the economy is incorrect unless the IFS is taken into account. To the extent that nearly all QEMEs leave out informal financial transactions in official monetary data, it can safely be concluded that monetary policy in these countries bring outcomes that are misaligned with expectations of the authorities. Besides simply underestimating the volume of financial transactions, the monetary authorities are also likely to err in the choice and timing of monetary policy.

Third, the model illustrates that the risk factor (probability of success) for both high and low risk borrowers plays an important role in determining the magnitude by which macroeconomic indicators respond to shocks. In the experiments with a positive production technology shock and a monetary policy shock, it is shown that the response of both formal and informal financial sector loans is sensitive to the rate of success for high risk borrowers. The responses of capital stock, output, employment, wage rates and expected prices to each of the two shocks also show sensitivity to the risk factor of high risk borrowers. Similarly, in the experiment with a shock on the risk factor for high risk borrowers, changes in the risk factor of low risk borrowers determine the magnitude by which macroeconomic indicators respond to the shock. Lending in both the formal and informal financial sectors, capital stock, output, wage rates and expected prices respond to the shock on the risk factor for high risk borrowers with different magnitudes depending on whether or not the risk factor for low risk borrowers is low or high.

5 Summary and Conclusions

This paper set out to investigate the interaction of formal and informal financial sectors and to examine how economic activity is consequently affected. Commencing with the observation that the IFS in QEMEs is large and plays a non-trivial role in determining the direction of economic activity, we developed a four-sector macro-monetary DSGE model for analysis. The model demonstrates that while formal and informal sector loans may be substitutes in a borrower's utility function, they are in the aggregate complementary. Thus, increasing the use of FFS credit increases the demand for credit in the IFS. The observed behaviour of formal and informal financial sector interest rates presents another important finding. The model demonstartes that interest rates in the IFS are not necessarily driven by FFS interest rates. When experimenting with a positive production technology shock, interest rates in the two sectors were observed to move together in the same direction while in the experiments involving a monetary policy shock and a risk factor shock, they were not. In the monetary policy shock experiment, the two interest rates were in fact moving in opposite directions. The implication of this finding is that the IFS has the potential to frustrate monetary policy and its impact is likely to be more pronounced in countries where the sector is very large. Finally, the study shows that the risk factor of borrowers is an important determinant of the extent to which macroeconomic indicators respond to various shocks. In all the three experiments demonstrating how selected macroeconomic indicators respond to a positive production technology shock, a monetary policy shock and a shock on the probability of success for high risk borrowers, the model shows that changing the risk factors of either low or high risk borrowers results in most macroeconomic indicators responding with different magnitudes.

References

- Acharya, S. and Madhura, S. (1983). Informal credit markets and black money: Do they frustrate monetary policy?, *Economic and Political Weekly* 8: 1751–1756.
- African Development Bank, A. (1994). African development report, African Development.
- Ambler, S. and Paquet, A. (1994). Stochastic depreciation and the business cycle, International Economic Review. 44: 101–116.
- Arycetey, E. (1992). The relationship between formal and informal sectors in the financial market in ghana, *AERC Research Paper Series* **10**.
- Aryeetey, E. (1994). Financial integration and development in sub-saharan: A study of informal finance in ghana, Overseas Development Institute Working Paper Series WP/78.
- Aryeetey, E. (2008). From informal finance to formal finance in sub-saharan africa: Lessons from linkage efforts, Paper presented at the African Finance Seminar organised by IMF and the Joint Africa Institute from 4-5 March 2008 in Tunis, Tunisia. Unpublished Manuscript.
- Atieno, R. (2001). Formal and informal institutions' lending policies and access to credit by small-scale enterprises in kenya: An empirical assessment, AERC Research Paper Series RP111: 1–46.
- Bagachwa, M. (1995). Financial integration and development in sub-saharan africa: A study of informal finance in tanzania, *ODI Working Paper Series*.
- Basu, K. (1997). Analytical Development Economics: The Less Developed Economy Revisited, revised edition edn, Massachussetts: The MIT Press.
- Bell, C. (1990). Interactions between institutional and informal credit agencies in rural india, The World Bank Economic Review 4(3): 297–327.
- Benhabib, J., Carlstrom, C. and Fuerst, T. (2005). Introduction to monetary policy and capital accumulation, *Journal of Economic Theory* **123**: 1–3.

- Bolnick, B. (1992). Moneylenders and informal financial markets in malawi, World Development **20**(1): 57–68.
- Carlstrom, C. and Fuerst, T. (2003). Investment and interest rate policy: A discrete time analysis, *Federal Reserve Bank of Cleveland Working Paper Series* **WP/03/20**: 1–24.
- Chipeta, C. (1998). Improving the intermediation role of the informal financial sector in africa, Paper Presented at the United Nations Asia-Africa High-Level Workshop on Advancing Financial Intermediation in Africa, Port Louis, Mauritius, 20-22 April 1998
- Chipeta, C. and Mkandawire, M. (1991). The informal financial sector and macroeconomic adjustment in malawi, *AERC Research Paper Series* **RP4**: 1–58.
- Chipeta, C. and Mkandawire, M. (1992). Links between the informal and formal /semi-formal financial sectors in malawi, AERC Research Paper Series 14: 1–39.
- Clarida, R., Gali, J. and Gertler, M. (2000). Monetary policy rules and macroeconomic stability: Evidence and some theory, *The Qauarterly Journal of Economics* February: 147–180.
- Dasgupta, B. (2004). Capital accumulation in the presence of informal credit constraints: Does the incentive mechanism work better than credit rationing under asymmetric information?, University of Connecticut, Department of Economics Working Paper Series 2004-32.
- Hansen, G. (1985). Indivisible labour and the business cycle, Journal of Monetary Economics 16: 309–327.
- Hartley, J., Salyer, K. and Sheffrin, S. (1997). Calibration and business cycle models: An unorthodox experiment, *Journal of Macroeconomics* 19(2): 1–17.
- International Finance Corporation, . (2009). Ifc and agribusiness, *IFS Issue Brief* August: 1–2.
- Juilliard, M. (1996). Dynare: A program for the resolution and simulation of dynamic models with forward variables through the use of a relaxation algorithm, CEPREMAP Working Paper Series WP 9602: 1–13.
- Liu, G. and Gupta, R. (2007). A small-scale dsge model for forecasting the south african economy, *South African Journal of Economics* **75**(2): 179–93.
- Mankiw, G. (1989). Real business cycles: A new keynesian perspective, *Journal of Economic Perspectives* **3**(3): 79–90.

- Mankiw, G. (2006). The macroeconomist as scientist and engineer, *Journal of Economic* Perspectives **20**(4): 29–46.
- Masson, P., Savastano, M. and Sharma, S. (1997). The scope for inflation targeting in developing countries, *IMF Working Paper Series* WP/97/130: 1–53.
- Masson, P., Savastano, M. and Sharma, S. (1998). Can inflation targeting be a framework for monetary policy in developing countries?, *Finance and Development* March: 34–37.
- Peiris, S. and Saxegaard, M. (2007). An estimated dsge model for monetary policy analysis in low income countries, *IMF Working Paper Series* WP/07/282.
- Rahman, A. (1992). The informal financial sector in bangladesh: An appraisal of its role in development, *Development and Change* 23: 147–168.
- Soyibo, A. (1997). The informal financial sector in nigeria: Characteristics and relationship with the formal sector, *Development Policy Review* 15: 5–22.
- Steel, W., Aryeetey, E., Hettige, H. and Nissanke, M. (1997). Informal financial markets under liberalisation in four african countries, World Development 25(5): 817–830.
- Stiglitz, J. and Weiss, A. (1981). Credit rationing in markets with imperfect information, The American Economic Review 71(3): 393–410.
- Sundaram, K. and Pandit, V. (1984). Informal credit markets, black money and monetary policy: Some analytical and empirical issues, *Economic and Political Weekly* 19: 695– 677 & 679–682.
- Tovar, C. (2008). Dsge models and central banks, BIS Working Paper Series WP No. 258.

Woodford, M. (2003). Interest and prices: Foundations of a theory of monetary policy.