

# **LOW PHASE NOISE 2 GHz FRACTIONAL-N CMOS SYNTHESIZER IC**

by

Gerhardus Ignatius Potgieter Veale

Submitted in partial fulfilment of the requirements for the degree

Master of Engineering (Microelectronic Engineering)

in the

Faculty of Engineering, Built Environment & Information Technology

University of Pretoria

July 2010

## SUMMARY

---

LOW PHASE NOISE 2 GHz FRACTIONAL- $N$  CMOS SYNTHESIZER IC

**BY** GERHARDUS IGNATIUS POTGIETER VEALE

Supervisor: Dr Saurabh Sinha

Department of Electrical, Electronic & Computer Engineering

Degree: M. Eng. (Microelectronic Engineering)

---

Low noise *low* division 2 GHz RF synthesizer integrated circuits (ICs) are conventionally implemented in some form of HBT process such as SiGe or GaAs. The research in this dissertation differs from convention, with the aim of implementing a synthesizer IC in a more convenient, low-cost Si-based CMOS process. A collection of techniques to push towards the noise and frequency limits of CMOS processes, and possibly other IC processes, is then one of the research outcomes.

In a synthesizer *low*  $N$ -divider ratios are important, as high division ratios would amplify in-band phase noise. The design methods deployed as part of this research achieve *low* division ratios ( $4 \leq N \leq 33$ ) and a high phase comparison frequency ( $>100$  MHz). The synthesizer IC employs a first-order fractional- $N$  topology to achieve increased frequency tuning resolution. The primary  $N$ -divider was implemented utilising current mode logic (CML) and the fractional accumulator utilising conventional CMOS. Both a conventional CMOS phase frequency detector (PFD) and a CML PFD were implemented for benchmarking purposes. A custom-built 4.4 GHz synthesizer circuit employing the IC was used to validate the research.

In the 4.4 GHz synthesizer circuit, the prototype IC achieved a measured in-band phase noise plateau of  $\mathcal{L}(f) = -113$  dBc/Hz at a 100 kHz frequency offset, which equates to a figure of merit (FOM) of -225 dBc/Hz. The FOM compares well with existing, but expensive, SiGe and GaAs HBT processes. Total IC power dissipation was 710 mW, which is considerably less than commercially available GaAs designs. The complete synthesizer IC was implemented in

Austriamicrosystems' (AMS) 0.35  $\mu\text{m}$  CMOS process and occupies an area of 3.15 x 2.18 mm<sup>2</sup>.

**Keywords:**

Fractional- $N$ , low division, SSB phase noise, CML, CML 2/3-Prescaler, pulse-swallow counter, CML 4-bit counter, CML PFD, CMOS PFD, CML-to-CMOS converter, in-band phase noise, CML flicker noise, high voltage charge-pump, programmable modulus accumulator

## SAMEVATTING

---

LAE FASE-RUIS 2 GHz FRAKSIONELE- $N$  CMOS-SINTETISEERDER

**DEUR GERHARDUS IGNATIUS POTGIETER VEALE**

Toesighouer: Dr Saurabh Sinha

Departement Elektriese, Elektroniese en Rekenaar-ingenieurswese

Graad: M. Ing. (Mikroëlektroniese Ingenieurswese)

---

Lae faseruis en *lae* deeltal 2 GHz RF-sintetiseerder geïntegreerde stroombane is tradisioneel in HBT-prosesse soos SiGe of GaAs geïmplementeer. Die navorsing in hierdie verhandeling wyk af van konvensie deur 'n CMOS-sintetiseerderimplementering. Si-gebaseerde CMOS-prosesse is sowel goedkoper as meer algemeen. Een van die verhandeling se uitsette is 'n versameling tegnieke wat die ruis- en frekwensielimiete van CMOS-prosesse aanspreek. Hierdie metodes kan waarskynlik ook vir ander geïntegreerde stroombaanprosesse gebruik word.

In 'n sintetiseerder is *lae*  $N$ -deelsyfers belangrik, aangesien hoë deelsyfers die binnebandfase-ruis sal versterk. Ontwerpmetodes wat deel vorm van die navorsing behaal *lae* deeltalle ( $4 \leq N \leq 33$ ) en 'n hoë fasevergelykingsfrekwensie ( $>100$  MHz). 'n Eerste-orde fraksionele- $N$  sintetiseerdertopologie is gerealiseer vir uitgebreide frekwensie verstelbaarheid. Die hoof  $N$ -deler is geïmplementeer in stroommoduslogika (SML) en die fraksionele akkumulator in konvensionele CMOS. Sowel 'n konvensionele CMOS-fasefrekwensie-vergelyker (FFV) as 'n SML FFV is geïmplementeer en met mekaar vergelyk. 'n 4.4 GHz sintetiseerdertoetsbaan is gebou om die geïntegreerde stroombaan prakties te meet.

In die 4.4 GHz toetsbaan is 'n binne-band faseruisvloer gemeet van  $\mathcal{L}(f) = -113$  dBc/Hz teen 'n frekwensie-afset van 100 kHz. Hierdie syfer transleer na 'n -225 dBc/Hz syfer van meriete wat goed vergelyk met bestaande en duurder SiGe- en GaAs-prosesse. Die totale drywingsverbruik is 710 mW, maar dit is heelwat minder as bestaande kommersiële GaAs-

ontwerpe. Die voltooide geïntegreerde stroombaan is vervaardig volgens Austriamicrosystems (AMS) se 0.35  $\mu\text{m}$  CMOS-proses en beslaan 'n area van  $3.15 \times 2.18 \text{ mm}^2$ .

**Sleutelwoorde:**

Fraksionele- $N$ , lae deeltal, ESB-faseruis, SML, SML 2/3-voordeler, puls-slukteller, SML 4-bis-teller, SML FFV, CMOS FFV, SML-na-CMOS-omsetter, binne-band faseruis, SML-flikkerruis, hoëspanning-stroompomp, programmeerbare modulusakkumulator

## ACKNOWLEDGEMENTS

---

I would like to thank several persons and organisations who helped and were involved during the research and writing of this dissertation.

- My supervisor, Dr Saurabh Sinha, for his support and availability during the entire process.
- Grintek Ewation (Pty) Ltd (GEW) for funding the layout and manufacturing of the evaluation printed circuit board (PCB).
- Jan Roux for laying out the evaluation PCB.
- Jannes Venter for his invaluable support on all the CAD tools provided by the Carl and Emily Fuchs Institute for Microelectronics (CEFIM).
- My wife Adri for her support during this dissertation.

This dissertation would also not have been possible without the grace of God and His faithfulness.

## TABLE OF CONTENTS

Chapter 1: Introduction.....	1
1.1 Motivation.....	1
1.2 Justification for the research .....	2
1.3 Organization of dissertation.....	4
1.4 Delimitations of scope and key assumptions .....	5
Chapter 2: Literature review.....	6
2.1 PLL basics.....	6
2.1.1 PLL linear model .....	7
2.1.2 PLL linear model with additive noise sources.....	12
2.1.3 <i>N</i> -divider architectures .....	15
2.1.4 Fractional- <i>N</i> division .....	20
2.1.5 Phase detector .....	23
2.1.6 Loop filter architectures .....	28
2.2 Phase noise.....	32
2.2.1 Phase noise basics.....	32
2.2.2 Reciprocal mixing .....	34
2.2.3 Jitter .....	35
2.2.4 Conclusion .....	37
2.3 Intrinsic noise.....	38
2.3.1 MOSFET small-signal noise model .....	39
2.3.2 Thermal noise .....	39
2.3.3 Flicker noise .....	41
2.3.4 Shot noise .....	42
2.3.5 Noise to phase jitter translation .....	43

2.4	PLL IC Figure of Merit (FOM) .....	45
2.4.1	Phase noise prediction from FOM.....	46
2.4.2	FOM underlying cause .....	47
2.5	Current mode logic .....	48
2.5.1	CML basics.....	49
2.5.2	CML design guidelines.....	50
2.5.3	CML standard building blocks .....	53
2.6	Conclusion .....	57
2.6.1	PLL system requirements .....	57
2.6.2	Circuit level requirements .....	57
Chapter 3: Research methodology.....		59
3.1	Research methodology outline.....	59
3.1.1	CML prescaler design and prototype.....	60
3.1.2	CML counter design .....	60
3.1.3	PFD and final design .....	60
3.2	CAD software used .....	61
3.3	IC prototyping.....	62
3.4	Experimental verification.....	64
3.4.1	Maximum operating frequency .....	64
3.4.2	FOM .....	65
3.4.3	RF test equipment used .....	66
Chapter 4: System Design .....		67
4.1	Background.....	67
4.2	CML subsystems.....	69
4.2.1	CML basics.....	69
4.2.2	CML CLK driver .....	76





4.2.3	CML 2/3-prescaler.....	77
4.2.4	CML 4-bit counter.....	84
4.2.5	CML reference clock amplifier.....	88
4.2.6	CML PFD.....	91
4.2.7	CML-to-CMOS converter.....	96
4.3	CMOS subsystems.....	98
4.3.1	Binary adders and subtractors.....	98
4.3.2	Pulse-swallow control logic.....	99
4.3.3	Programmable modulus accumulator.....	101
4.3.4	CMOS PFD.....	104
4.3.5	SPI interface.....	107
4.4	Floor plan.....	108
Chapter 5: Simulation and Measurement Results.....		109
5.1	Prototyped CML 2/3-prescaler.....	109
5.1.1	Test setup and general measurements.....	110
5.1.2	Input sensitivity.....	112
5.2	Prototyped fractional- <i>N</i> synthesizer IC.....	113
5.2.1	Evaluation PCB.....	114
5.2.2	Power consumption.....	117
5.2.3	Input sensitivity.....	118
5.2.4	Phase noise measurements.....	121
5.2.5	Fractional spur compensation.....	125
Chapter 6: Conclusion.....		128
6.1	Technical summary and contribution.....	128
6.1.1	FOM.....	128
6.1.2	CML low division high frequency divider.....	128



6.1.3	CML PFD .....	128
6.1.4	PFD reset delay effect.....	129
6.1.5	Programmable modulus accumulator .....	129
6.1.6	Power dissipation.....	129
6.1.7	High voltage CP .....	129
6.1.8	Fractional spurious compensation network .....	129
6.2	Recommendations for future work .....	130
6.2.1	MOSFET flicker noise .....	130
6.2.2	CML 4-bit counter architecture .....	130
6.2.3	SiGe HBT implementation .....	130
	References .....	131
	Appendix A: Evaluation PCB schematic .....	137
	Appendix B: Prototyped IC photographs .....	138
	Appendix C: Test graphical user interface (GUI) .....	143

## LIST OF ABBREVIATIONS

---

AC	Alternating current
ADC	Analogue to digital converter
AMP	Amplifier
AMS	Austriamicrosystems
BiCMOS	Bipolar and CMOS process
BJT	Bipolar junction transistor
BPF	Bandpass filter
CAD	Computer aided design
CLK	Clock
CML	Current mode logic
CMOS	Complementary metal oxide semiconductor
CP	Charge-pump
dB	Decibel
dBc	dB relative to carrier
dBm	dB relative to 1 mW power
DC	Direct current
DFF	D flip-flop
DRC	Design rule check
ECL	Emitter coupled logic
EIA	Electronic industries association
ESD	Electrostatic discharge
FA	Full adder
FRAC	Numerator of a fractional division
FM	Frequency modulation
FOM	Figure of merit
FSK	Frequency shift keying
GaAs	Gallium Arsenide
GDSII	Graphic data system II
GEW	Grintek Ewation (PTY) LTD
GHz	Gigahertz
GUI	Graphical user interface
HBT	Heterojunction bipolar transistor
IC	Integrated circuit
IF	Intermediate frequency
LC	Inductor capacitor
LD	Lock-detect
LNA	Low noise amplifier
LO	Local oscillator
LUT	Look up table
LVS	Layout vs schematic
MOD	Modulus
MOS	Metal oxide semiconductor
MOSFET	MOS field effect transistor



NDA	Non disclosure agreement
OD	Open drain
OPAMP	Operational amplifier
PCB	Printed circuit board
PD	Phase detector
PFD	Phase frequency detector
PLL	Phase locked loop
PM	Phase modulation
PSD	Power spectral density
PSS	Periodic steady state
QFN	Quad flat no leads
QPSK	Quadrature phase shift keying
R&S	Rohde & Schwarz
RCA	Ripple carry adder
RF	Radio frequency
RMS	Root mean square
SCL	Source coupled logic
Si	Silicon
SiGe	Silicon Germanium
SNR	Signal-to-noise ratio
SPI	Serial peripheral interface
SPICE	Simulation program with integrated circuit emphasis
SSB	Single side band
TFF	Toggle flip-flop
UP	University of Pretoria
VCO	Voltage controlled oscillator

## CHAPTER 1: INTRODUCTION

### 1.1 MOTIVATION

RF synthesizer integrated circuits (ICs) are essential building blocks in modern communication systems where they are used in phase-locked loops (PLLs) to implement digital clocks or local oscillators (LOs). A primary criterion for a clock or LO is its phase noise performance.

With any PLL implementation the phase noise outside of the loop bandwidth is mainly governed by the phase noise of the voltage controlled oscillator (VCO) and by that of the steering mechanism. Inside the loop bandwidth the phase noise of the VCO will be suppressed by the loop gain and an in-band phase noise floor will result. Figure 1 illustrates this concept with the PLL loop bandwidth  $\omega_p$  and output frequency  $f_{out}$  indicated.

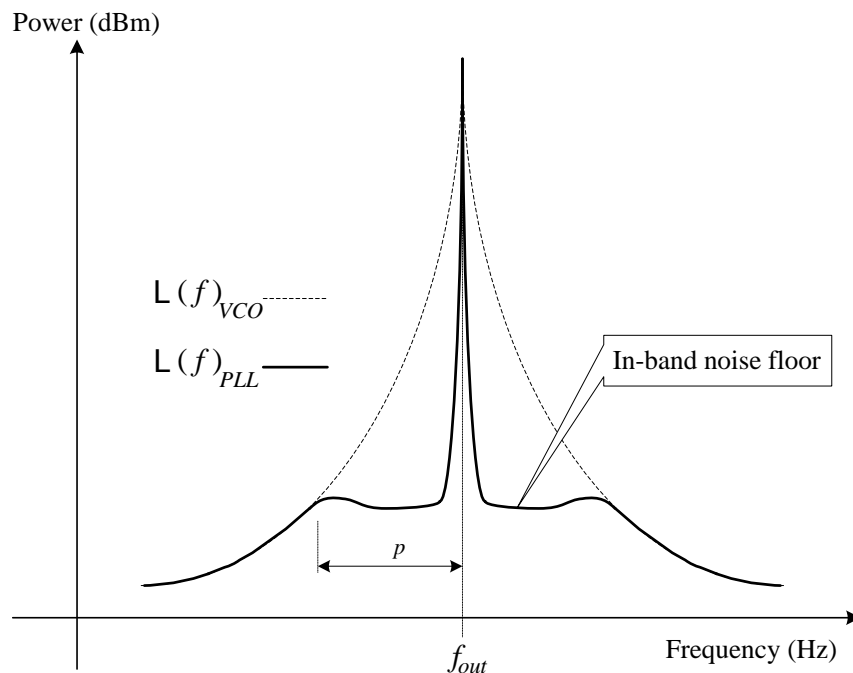


Figure 1. Phase noise of a phase locked VCO versus an unlocked VCO

With a synthesizer the in-band phase noise is mainly determined by the PLL division ratio  $N$  and the intrinsic noise floors of the digital divider and phase frequency detector (PFD) [1][2][3].

In a PLL system, this behaviour can be used to “clean up” a noisy VCO by using a large loop bandwidth and a low  $N$  division ratio. By using this approach, the dominant phase noise of a PLL becomes totally dependent on the performance and architecture of the synthesizer IC used, and not as much on the VCO used. Low noise and *low division* capable synthesizer ICs then become important for such PLL designs.

## 1.2 JUSTIFICATION FOR THE RESEARCH

High frequency *low division* ratio RF synthesizer IC designs are traditionally the domain of heterojunction bipolar transistor (HBT) processes. Although these processes are state of the art they suffer from price and power dissipation penalties. CMOS processes are cheaper but have traditionally not been used in high frequency *low division* architectures due to the slow speed of standard CMOS building blocks. High frequency architectures are possible in CMOS due to use of *high division* prescalers prior to the standard CMOS divider blocks, but have otherwise lacked low division ratios.

TABLE I lists a mixture of synthesizer scholarly work and commercially available devices, circa 2009, compared to the work done in this dissertation.

TABLE I  
WORK AND DEVICE COMPARISON

Work or Device	Technology	Max Freq	Prescaler	$N$ -divider	FOM (dBc/Hz)	Power consumption
[3]	0.35 $\mu$ m SiGe BiCMOS	2.43 GHz	*	152	-213	18 mW
[4]	0.5 $\mu$ m CMOS	900 MHz	8/9	112	-202	43 mW
[5]	0.5 $\mu$ m CMOS	2.4 GHz	*	50	-211	135 mW
[6]	BiCMOS	400 MHz 2.4 GHz	- 8/9	1-8191 56-65591	-222	17 mW
[7]	BiCMOS	4.8 GHz 8 GHz	16/17 32/33	240-131119 992-262175	-219	50 mW
[8]	SiGe BiCMOS	7 GHz	*	32-65567	-226	325 mW
[9]	GaAs HBT	7 GHz	4/5	12-259	-233	1.55 W
[10]	GaAs HBT	2.8 GHz	-	2-32	-233	1.25 W
[11]	0.18 $\mu$ m CMOS	6 GHz	4/5	158	-221	46 mW
[12]	90 nm CMOS	9 GHz	4/5	100-156	-222	60 mW
This work	0.35 $\mu$ m CMOS	2 GHz	2/3	4-33	-225	710 mW

\* = unknown

It can be seen from TABLE I that all the high frequency ( $f \geq 2$  GHz), *low division* ( $N \leq 30$ ) synthesizer ICs are predominantly GaAs HBT devices and exhibit very good figure of merits (FOMs),  $FOM \leq -226$  dBc/Hz. The high power dissipation levels are also very evident.

*A research question could then be asked if a low division low noise synthesizer IC can be implemented in a low cost CMOS process with similar high performance specifications and what would be the process limitations?*

This then became the aim of this dissertation, to research a collection of techniques to push towards the noise and frequency limits of CMOS processes. The research verification was done with the implementation of a fractional- $N$  synthesizer IC in 0.35  $\mu\text{m}$  CMOS process, being comparable in phase noise to existing GaAs HBT devices. Two types of phase frequency detectors (PFDs) were considered, one being a conventional CMOS and the other a current mode logic (CML) design. The research question was answered for the 0.35  $\mu\text{m}$  CMOS process but could apply to other processes where process limits or boundaries are pushed.

The outcome of this research was demonstrated using the prototyped CMOS synthesizer IC in a custom built 4.4 GHz test circuit. Low division ratios ( $4 \leq N \leq 33$ ) and a  $FOM = -225$  dBc/Hz at a 100 kHz offset frequency were demonstrated with a 110 MHz PFD operating frequency. The phase noise floor of the CML PFD proved superior to the CMOS PFD and was simulated having a maximum phase comparison frequency of 790 MHz. Power dissipation of the synthesizer IC was 710 mW which is far less than similar GaAs devices. The chip occupied an area of  $3150 \times 2180 \mu\text{m}^2$ .

### 1.3 ORGANIZATION OF DISSERTATION

The dissertation is organized as follows:

**Chapter 2** (*Literature review*) is a thorough theoretical and literature review of the fundamentals of CMOS synthesizers. The chapter starts with the basics of PLLs, the concept of phase noise, intrinsic noise sources in MOSFETs and concludes with CML basics. The design considerations for a low noise CMOS synthesizer IC are discussed throughout the chapter and then summarised.

**Chapter 3** (*Research methodology*) describes the research methodology used to develop a hypothesised low noise CMOS synthesizer IC design into a functional circuit. Steps involved to experimentally validate the research are also presented in this chapter.

**Chapter 4** (*System analysis and design*) details each subsystem and the overall synthesizer IC system in circuit, functional simulation and IC layout. The subsystems are divided between CML and CMOS blocks.

**Chapter 5** (*Simulation and measurements results*) documents the measured results of the prototyped ICs and compares it to relevant simulation data. Deviations from expected results are explained.

**Chapter 6** (*Conclusion*) summarises the research and draws concluding remarks about the work and provides suggestions for future work.

This dissertation also includes an appendix which presents the circuit diagram of the custom built 4.4 GHz synthesizer employing the prototype IC.





## **1.4 DELIMITATIONS OF SCOPE AND KEY ASSUMPTIONS**

The primary goal in this dissertation is synthesizer phase noise and speed. A low power design is of secondary importance as it is assumed that the primary goals outweigh this possible requirement. This assumption is also proven true in practise when comparing the power dissipations of commercial high performance synthesizer ICs (TABLE I). As a result the power dissipation of the prototyped IC is shown to be 710 mW, which is high but less than competing GaAs ICs.

The circuit design for this research is implemented in 0.35  $\mu\text{m}$  CMOS technology. One outcome of this research is a set of guidelines to push towards noise and frequency limits in CMOS processes. These guidelines could also be used for other IC processes to push towards noise and frequency limits as applicable to synthesizer ICs.

## CHAPTER 2: LITERATURE REVIEW

---

A discussion on fundamental concepts and building blocks regarding low noise PLLs is presented in this chapter. The discussion is in a form where each building block or concept is described and how it contributes to the in-band phase noise, first in architecture and then on circuit level details. The whole chapter will then form a collection of techniques to reduce in-band phase noise in CMOS digital synthesizer ICs, hereby pushing towards the noise and frequency limits of the CMOS process used.

The chapter starts with a section on basic PLL fundamentals, then with a section on phase noise and the negative implications of it. Sections on intrinsic noise and FOM follow. Lastly, a detailed section on CML is presented, as many building blocks have been implemented using CML. In the concluding section the collection of design techniques, for low in-band phase noise operation, is summarised.

### 2.1 PLL BASICS

A PLL is a negative feedback system that will phase-lock the output frequency  $f_{out}$  to the reference input frequency  $f_{ref}$ . A PLL basically consists of a phase-detector (PD), a low pass loop filter, a VCO and a frequency divider in the feedback path [13] as depicted in Figure 2.

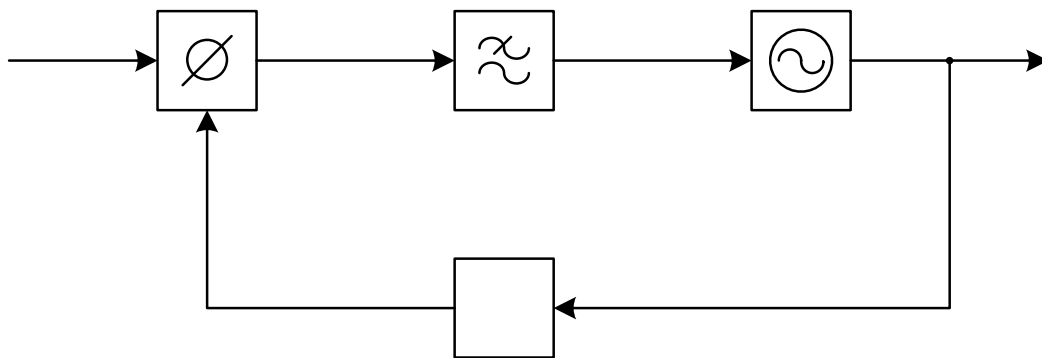


Figure 2. PLL block diagram

By choosing different  $N$ -divider values, the resultant output frequency  $f_{out}$  can be locked at multiples of the reference frequency  $f_{ref}$ :

$$f_{out} = f_{ref} \cdot N \quad [\text{Hz}] \quad (2.1)$$

And the PLL frequency resolution is simply:

$$Freq_{res} = f_{ref} \quad [\text{Hz}] \quad (2.2)$$

To aid in the analysis of a locked PLL and more specifically its phase noise response, a linear model is presented next in section 2.1.1

### 2.1.1 PLL linear model

Since the phase is the parameter of interest rather than the oscillation frequency, it is necessary to represent each building block in the PLL in the phase or Laplace domain. Figure 3 depicts the combined linear model for all the PLL components [13]. This model is only valid when the output  $\theta_{out}(s)$  is phase-locked to the input  $\theta_{ref}(s)$  or when the system is behaving in a linear way.

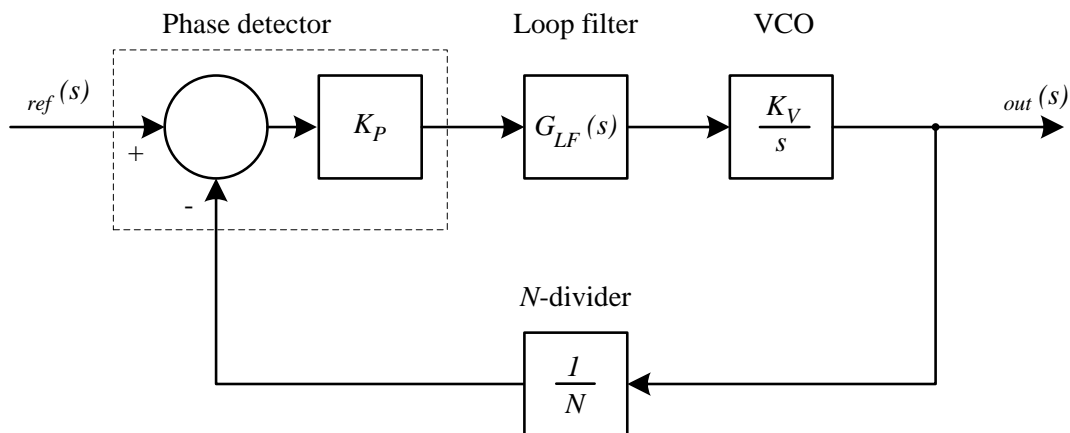


Figure 3. PLL linear model

Each building block will now be described and related to its Laplace transfer function.

### 2.1.1.1 VCO

The VCO is the oscillator used in a PLL system. The VCO output frequency can be expressed as a function of the tuning voltage  $v_T$  :

$$f_{VCO}(t) = f_o + \frac{K_V}{2\pi} v_T(t) \quad [\text{Hz}] \quad (2.3)$$

Where  $f_o$  is the VCO frequency when  $v_T$  equals zero and  $K_V$  is the VCO gain in [rad/(s.V)].

Since phase is the integral of frequency, the relative VCO phase is given by:

$$\theta_{VCO}(t) = 2\pi \int_{-\infty}^t (f_{VCO}(\tau) - f_o) d\tau = K_V \int_{-\infty}^t v_T(\tau) d\tau \quad [\text{rad}] \quad (2.4)$$

The VCO Laplace transfer function then becomes:

$$H_{VCO}(s) = \frac{\theta_{VCO}(s)}{v_T(s)} = \frac{K_V}{s} \quad (2.5)$$

### 2.1.1.2 N-divider

The frequency divider performs a frequency division with a ratio of  $N$  on the input signal  $f_{div-in}$ . The output frequency  $f_{div-out}$  can be related as:

$$f_{div-out} = \frac{f_{div-in}}{N} \quad [\text{Hz}] \quad (2.6)$$

The output phase then becomes:

$$\begin{aligned} \theta_{div-out}(t) &= 2\pi \int_{-\infty}^t f_{div-out}(\tau) d\tau = 2\pi \int_{-\infty}^t \frac{f_{div-in}(\tau)}{N} d\tau \\ &= \frac{\theta_{div-in}(t)}{N} \end{aligned} \quad [\text{rad}] \quad (2.7)$$

The Laplace transfer function becomes:

$$H_{divider}(s) = \frac{\theta_{div-out}(s)}{\theta_{div-in}(s)} = \frac{1}{N} \quad (2.8)$$

### 2.1.1.3 Phase detector

The phase detector compares the phases of two signals and produces a voltage or current output according to the phase difference:

$$V_{PD-out} = K_p(\theta_1 - \theta_2) = K_p\theta_{PD-in} \quad [\text{V}] \quad (2.9)$$

Where  $K_p$  is the gain of the phase detector with units of [V/rad] or [A/rad].

The Laplace transfer function becomes:

$$H_{PD}(s) = \frac{V_{PD-out}(s)}{\theta_{PD-in}(s)} = K_p \quad (2.10)$$

### 2.1.1.4 Loop filter

The loop-filter removes the correction pulses coming from the phase detector. This filtered signal then becomes the DC control signal for the VCO. The loop-filter also affects the loop dynamics such as stability, settling time and phase noise peaking. The transfer function of the loop filter,  $G_{LF}(s)$  will be defined by the filter circuitry employed. The filter implementation can be either passive or active. General loop-filter circuitry follows in section 2.1.6.

### 2.1.1.5 Transfer function of the combined linear model

From linear systems theory [13] and [14] it follows that the closed loop transfer function of a PLL is:

$$H_{PLL}(s) = \frac{\theta_{out}(s)}{\theta_{ref}(s)} = \frac{G1(s)}{1 + G1(s)G2(s)} = \frac{G1(s)}{1 + H_{OL}(s)} \quad (2.11)$$

Where  $G1(s)$  is the forward path,  $G2(s)$  the feedback path and  $H_{OL}(s)$  the combined open loop transfer function. From Figure 3 the forward and feedback paths can be determined:

$$G1(s) = \frac{K_p K_v G_{LF}(s)}{s} \quad (2.12)$$

$$G2(s) = \frac{1}{N} \quad (2.13)$$

The combined open loop transfer function then becomes:

$$H_{OL}(s) = G1(s)G2(s) = \frac{K_p K_v G_{LF}(s)}{N s} \quad (2.14)$$

The PLL closed loop transfer function Equation (2.11) then becomes:

$$H_{PLL}(s) = \frac{\theta_{out}(s)}{\theta_{ref}(s)} = N \left( \frac{H_{OL}(s)}{1 + H_{OL}(s)} \right) \quad (2.15)$$

### 2.1.1.6 PLL loop stability

With any linear feedback control system, stability issues will arise. With a PLL the order of the linear system is determined by the order of the loop filter; it is normally one higher than the order of the loop filter. The smallest PLL order is a 2<sup>nd</sup> order system [13] whose stability can be described in terms of its damping factor  $\zeta$  and its natural frequency  $\omega_n$ . Normally, for a selected natural frequency  $\omega_n$ , the damping factor is chosen as  $\zeta = \frac{1}{\sqrt{2}}$ , assuring loop stability [14].

In reality many PLL systems are higher order systems, making the use of damping factors etc. void. In these systems it is better to describe loop stability with parameters of phase margin  $\phi_m$  and loop bandwidth  $\omega_p$ . The stability of any feedback control system can be described with these two parameters, including 2<sup>nd</sup> order systems [14].

Phase margin and loop bandwidth can be described in terms of the open loop transfer function  $H_{OL}(s)$  of a feedback control system. Figure 4 graphically depicts the open loop transfer function of a typical PLL system, with  $\omega_p$  and  $\phi_m$  indicated. This is also known as a Bode plot. From [14] the following definitions:

The loop bandwidth  $\omega_p$  is defined as the cross-over frequency where the loop gain is equal to one:

$$|H_{OL}(j\omega_p)|=1 \quad (2.16)$$

The phase margin  $\phi_m$  is defined as the phase difference from  $-180^\circ$  at the cross-over frequency or loop bandwidth  $\omega_p$ :

$$\phi_m = \arg(H_{OL}(j\omega_p)) + 180^\circ \quad [^\circ] \quad (2.17)$$

For stability it is required that the phase margin be a maximum at the loop bandwidth  $\omega_p$  [23]:

$$\left. \frac{d\phi}{d\omega} \right|_{\omega=\omega_p} = 0 \quad (2.18)$$

This maximum value of  $\phi_m$  will however affect the noise peaking of the PLL [27]. More typical values are in the order of  $60^\circ$  plus.

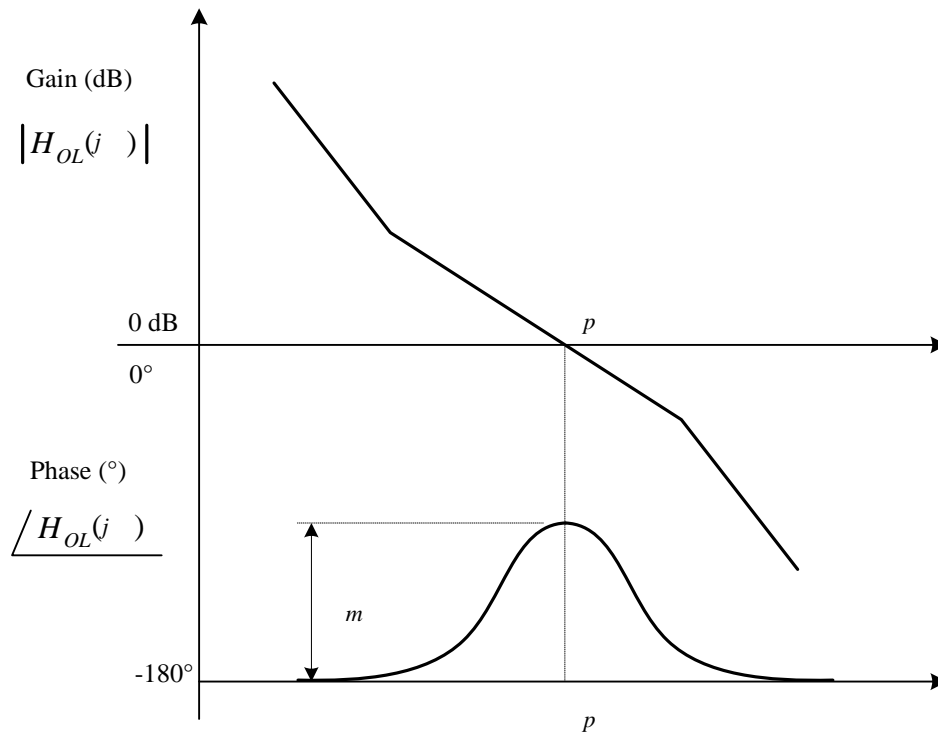


Figure 4. PLL typical open loop transfer function

### 2.1.1.7 In-band and out-band terminology

In PLL literature *in-band* and *out-band* responses are sometimes referred to. From Figure 4 the *in-band* response is defined where the loop gain  $|H_{OL}(j\omega)| \gg 1$  or to the left of  $\omega_p$ . The *out-band* response is defined where the loop gain is small  $|H_{OL}(j\omega)| \ll 1$  or to the right of  $\omega_p$ . These terminologies will become important when discussing phase noise in a PLL system in section 2.1.2 and further on.

### 2.1.2 PLL linear model with additive noise sources

The scope of any synthesizer design always includes noise or phase noise performance. For this reason it is necessary to investigate the effects of additive noise introduced at the different subsystems of a PLL. Figure 5 depicts the modified linear model with added noise sources [15].

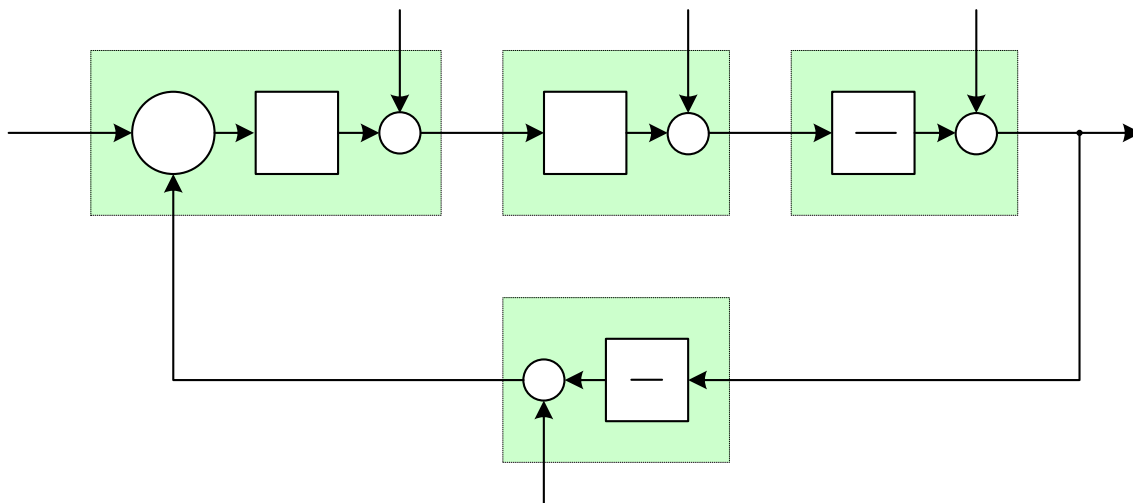


Figure 5. PLL linear model with additive noise sources

The noise sources are first treated as additional phase inputs so for each input a closed loop transfer function  $H_{PLL}(s)$  can be derived, similar to that of Equation (2.15). TABLE II then lists the transfer functions for the different sources [15]. TABLE II also indicates the in-band and out-band responses of these transfer functions.

$$\theta_{pd}(s)$$



TABLE II

GENERAL PLL CLOSED LOOP PHASE OR NOISE TRANSFER FUNCTIONS

Phase or Noise source	$H_{PLL}(s)$ Equation	Response	In-band Response $ H_{PLL}(j\omega) $	Out-band Response $ H_{PLL}(j\omega) $
1) Reference	$\frac{\theta_{out}(s)}{\theta_{ref}(s)} = N \left( \frac{H_{OL}(s)}{1 + H_{OL}(s)} \right)$	Lowpass	N	0
2) PD	$\frac{\theta_{out}(s)}{\theta_{pd}(s)} = \frac{N}{K_P} \left( \frac{H_{OL}(s)}{1 + H_{OL}(s)} \right)$	Lowpass	$\frac{N}{K_P}$	0
3) Loop filter	$\frac{\theta_{out}(s)}{\theta_{lf}(s)} = \frac{K_V}{s} \left( \frac{1}{1 + H_{OL}(s)} \right)$	Bandpass	<i>Simulate*</i>	<i>Simulate*</i>
4) VCO	$\frac{\theta_{out}(s)}{\theta_{vco}(s)} = \left( \frac{1}{1 + H_{OL}(s)} \right)$	Highpass	0	1
5) Divider	$\frac{\theta_{out}(s)}{\theta_{div}(s)} = -N \left( \frac{H_{OL}(s)}{1 + H_{OL}(s)} \right)$	Lowpass	N	0

\*The loop filter's closed loop phase transfer function is of a bandpass type. It will have a maximum value at the loop bandwidth,  $\omega_{LP}$ .

### 2.1.2.1 Phase noise implication

When the different inputs, as depicted in Figure 5, are considered as noise sources, the PLL double sided output phase noise spectral density,  $S_{out,\varphi}$  of each noise source  $\varphi$  simply becomes the mean-square of  $\theta_{out,\varphi}(s)$ :

$$\begin{aligned}
 S_{out,\varphi}(f) &= \left| \theta_{out,\varphi}(j2\pi f) \right|^2 \\
 &= \left| H_{PLL,\varphi}(j2\pi f) \cdot \theta_{\varphi}(j2\pi f) \right|^2
 \end{aligned}
 \quad [\text{rad}^2/\text{Hz}] \quad (2.19)$$

The individual noise sources are assumed to be uncorrelated so the total phase noise spectral density will be the summation of the individual phase noise densities as indicated in Equation (2.20). The effect of all noise sources must thus be considered.

$$S_{out,total}(f) = \sum_{n=1}^N S_{out,\varphi_n}(f) \quad [\text{rad}^2/\text{Hz}] \quad (2.20)$$

From Equation (2.19) and Equation (2.52) in section 2.2, the PLL SSB phase noise response  $\mathcal{L}_{PLL,\varphi}(\Delta f)$  of each noise source  $\varphi$  can be written in terms of its double sided phase noise spectral density  $S_{PLL,\varphi}$ :

$$\begin{aligned}\mathcal{L}_{PLL,\varphi}(\Delta f) &= 10\log\left(\frac{S_{PLL,\varphi}(\Delta f)}{2}\right) \\ &= 10\log\left(\frac{|H_{PLL,\varphi}(j2\pi\Delta f) \cdot \theta_{\varphi}(j2\pi\Delta f)|^2}{2}\right) \quad [\text{dBc/Hz}] \quad (2.21) \\ &= 20\log|H_{PLL,\varphi}(j2\pi\Delta f)| + \mathcal{L}_{\varphi}(\Delta f)\end{aligned}$$

Where  $\mathcal{L}_{\varphi}(\Delta f)$  is effectively the phase noise floor of each noise source  $\varphi$ .

For synthesizer ICs the in-band phase noise is important. From Equation (2.21) and TABLE II the in-band output phase noise relation of each additive noise source can now be written as:

$$\mathcal{L}_{PLL,ref}(\Delta f) = 20\log(N) + \mathcal{L}_{ref}(\Delta f) \quad [\text{dBc/Hz}] \quad (2.22)$$

$$\mathcal{L}_{PLL,pfd}(\Delta f) = 20\log\left(\frac{N}{K_P}\right) + \mathcal{L}_{pfd}(\Delta f) \quad [\text{dBc/Hz}] \quad (2.23)$$

$$\mathcal{L}_{PLL,div}(\Delta f) = 20\log(N) + \mathcal{L}_{div}(\Delta f) \quad [\text{dBc/Hz}] \quad (2.24)$$

From Equations (2.22)-(2.24) it becomes clear that to minimise the in-band phase noise of a PLL system, the phase noise floor  $\mathcal{L}_{\varphi}(\Delta f)$  of the individual noise sources must be minimised, the  $N$ -divider value must be small and the gain of the phase comparator  $K_P$  must be high. This conclusion then forms the focus of the research in this dissertation where an emphasis is placed on *low*  $N$ -divider values and low intrinsic noise levels.

The phase noise contribution of the loop filter is a special case as it has a bandpass response with a maximum value at the loop bandwidth  $\omega_p$ . It will thus affect the in-band phase noise in

the vicinity of the loop bandwidth and from there on the out-band phase noise. The effect is best simulated; however at around  $\omega_p$  the following relation will be true:

$$L_{PLL,lf}(\Delta f) \Big|_{\Delta f=2\pi\omega_p} \propto 20 \log(K_V) + L_{lf}(\Delta f) \quad [\text{dBc/Hz}] \quad (2.25)$$

Equation (2.25) dictates that the VCO gain constant  $K_V$  and the phase noise floor  $L_{lf}(\Delta f)$  of the loop filter be minimised to lessen the effect. Reducing  $K_V$  is not always practical for a given VCO but the noise floor  $L_{lf}(\Delta f)$  can be manipulated by choosing an active or passive loop filter as will be discussed in section 2.1.6. With wide tuning range or high gain VCOs the noise of the loop filter becomes important as it will adversely affect the out-band phase noise.

### 2.1.3 *N*-divider architectures

*N*-dividers in a PLL system divide the high frequency VCO output down to the required phase comparison frequency. *N*-dividers consist mainly of flip-flops with feedback paths employing combinational logic functions. These dividers can be grouped according to their mode of operation, being asynchronous or synchronous.

#### 2.1.3.1 *Asynchronous dividers*

In asynchronous dividers the output of the one block becomes the clock signal of the next block. The advantage of an asynchronous architecture is that subsequent blocks operate at lower frequencies than the first blocks. This then reduces power consumption. A very popular programmable asynchronous divider is from [16] and is depicted in Figure 6. This *N*-bit divider consists of cascaded 2/3-cells and the programmable inputs are  $P_0..P_{N-1}$ .

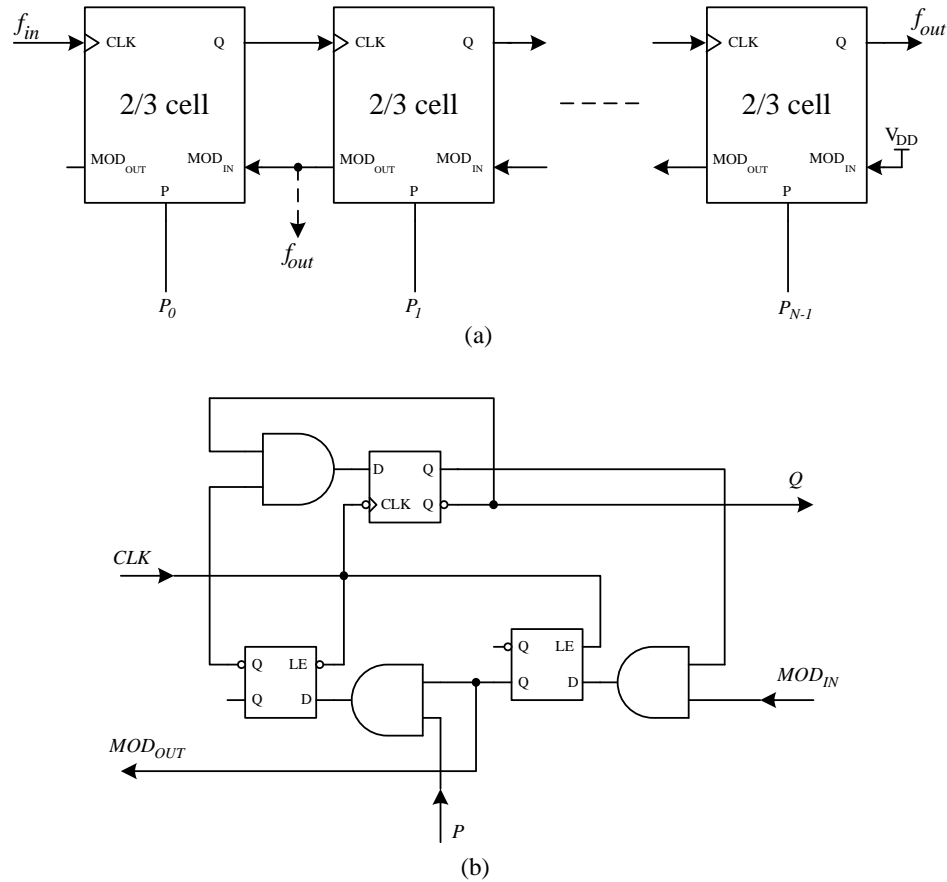


Figure 6. Multi-modulus asynchronous divider [16]: (a) Implementation, (b) 2/3 Cell

The asynchronous division ratio  $N_{DIV}$  is given by Equation (2.26):

$$N_{DIV} = \frac{f_{in}}{f_{out}} = 2^N + \sum_{n=0}^{N-1} P_n 2^n, \quad P_n = \{0|1\} \quad (2.26)$$

The limitation of this asynchronous divider is that the division ratio is bounded and more specifically the lower division ratio:

$$2^N \leq N_{DIV} \leq (2^{N+1} - 1) \quad (2.27)$$

For example a 4-bit divider will be bounded by  $16 \leq N_{DIV} \leq 31$ . This asynchronous architecture will then put a restriction on low division requirements. Synchronous dividers, as discussed next in section 2.1.3.2, overcome low division boundaries.

**2.1.3.2 Synchronous dividers**

In synchronous dividers, all the building blocks share the same clock signal. In general synchronous dividers are faster than asynchronous dividers due to the fact that there are no clock propagation delays between subsequent blocks. Synchronous dividers are generally implemented as counters. A conventional 4-bit down-counter is depicted in Figure 7:

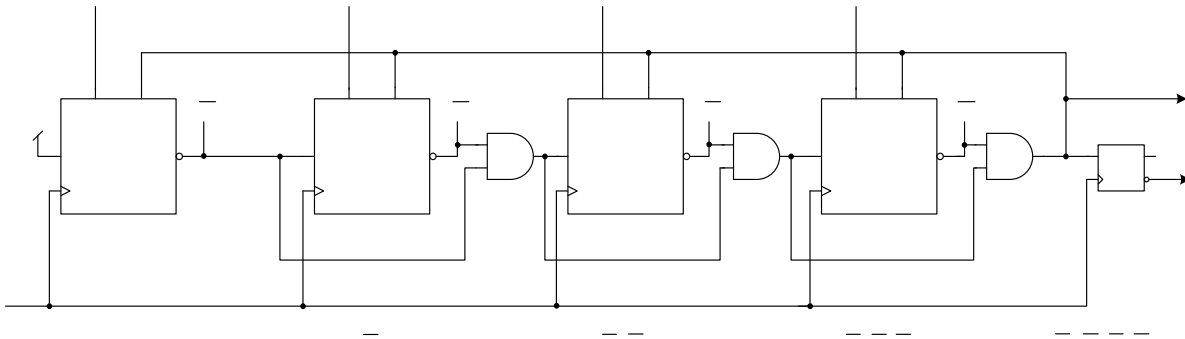


Figure 7. TFF synchronous counter implementation

The counter consists of cascaded  $B0$  toggle-flip-flops (TFFs) and programmable inputs  $B1..B3$ . Operation is such that when the count value reaches zero, the new  $B$  count value will be loaded synchronously by the  $LOAD$  signal. As seen in Figure 7, a synchronous counter uses TFFs. A TFF is a special kind of flip-flop where the output only changes state when the toggle input  $T$  is asserted. Typical loadable TFF implementations, using D-flip-flops (DFFs), are depicted in Figure 8.

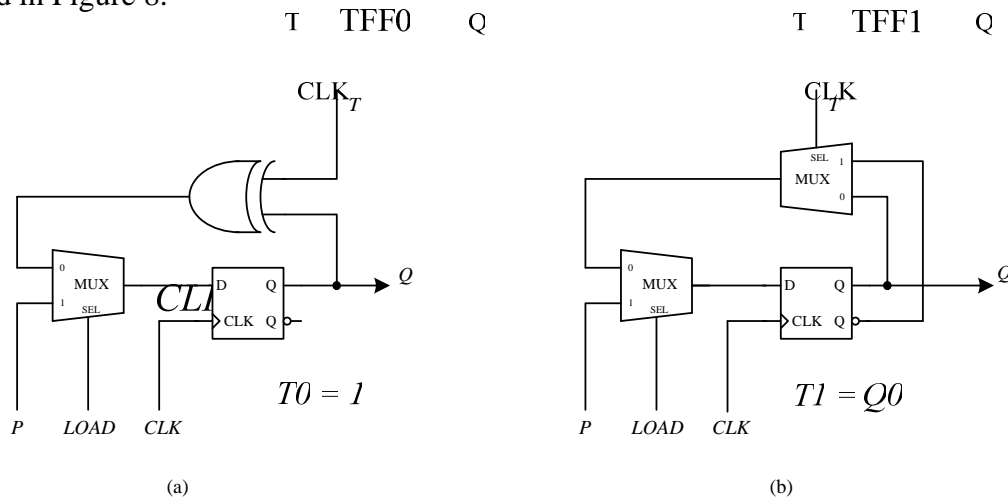


Figure 8. Loadable TFF implementations: (a) XOR feedback, (b) MUX feedback

In this dissertation however, a different approach was taken on the implementation of a synchronous counter, using look up tables (LUTs), as will become evident in chapter 4 section 4.2.4.

The count range of an  $N$ -bit synchronous counter is given by Equation (2.28) and the equivalent frequency divider  $N_{DIV}$  range by Equation (2.29):

$$0 \leq Count \leq (2^N - 1) \quad (2.28)$$

$$2 \leq N_{DIV} \leq 2^N \quad (2.29)$$

The lower divider limit of 2 is due to the fact that for a counter to produce an output clock or output pulse, the minimum count value must be one. A zero count or a hypothetically divide by one scenario will not produce a pulse but only a steady state output signal.

### ***2.1.3.3 Pulse-swallow dividers***

As seen from the previous sections, dividers consist mainly of flip-flops with combinational logic in the feedback paths. The maximum divider operating frequency is then a function of the individual propagation delays of the flip-flops and combinational logic. In a standard 0.35  $\mu\text{m}$  CMOS implementation, such as the AMS C35 process, the typical propagation delay for a DFF or a two-input NOR-gate is about 1 ns. This means for a cascaded NOR-DFF path the delay is 2 ns, implying a maximum clock frequency of 500 MHz. For dividers required to operate in the multi GHz range, these delays are too long. To overcome this problem either a faster or more expensive process could be selected or prescalers could be used. The pulse-swallow divider, employing a prescaler, is then an option [1]. Figure 9 depicts a typical pulse-swallow divider.

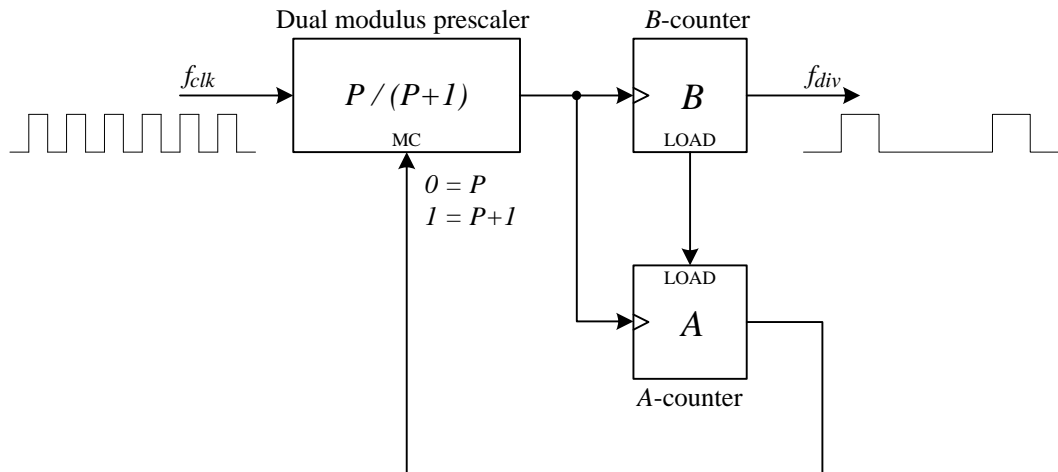


Figure 9. Pulse-swallow divider

The pulse-swallow divider consists of a dual modulus prescaler  $P$  and two conventional counters  $A$  and  $B$ . The  $A$  and  $B$  counters are sometimes referred to in literature as the swallow-counter and program-counter respectively [1]. For the pulse-swallow divider to work in a continuous mode the following condition must always be met:  $B \geq A$ .

The operation is as follows:

- 1) The  $B$ -counter has just timed out and both  $A$  and  $B$  counters are loaded with new values.
- 2) The prescaler now divides by  $P + 1$  until the  $A$ -counter times out.
- 3) For the remaining  $B - A$  cycles in the  $B$ -counter, the prescaler divides by  $P$ .
- 4) Eventually the  $B$ -counter times out and the divider cycle begins again.

The total number of  $f_{clk}$  counts in the divider's output  $f_{div}$  cycle is then:

$$N = A(P + 1) + (B - A)P = PB + A \quad (2.30)$$

The minimum and maximum divider values can also be presented in terms of the  $A$  and  $B$ -counter ranges. Normally the  $A$ -counter has a range of  $A \in [0, P - 1]$  and the  $B$ -counter must adhere to the  $B \geq A$  condition. So the minimum and maximum divider values become as indicated in Equations (2.31) and (2.32):

$$\begin{aligned}
 N_{min} &= PB_{min} + A_{min} \\
 &= PB_{min} + 0 \\
 &= PB_{min}
 \end{aligned} \tag{2.31}$$

$$\begin{aligned}
 N_{max} &= PB_{max} + A_{max} \\
 &= PB_{max} + (P-1) \\
 &= P(B_{max} + 1) - 1
 \end{aligned} \tag{2.32}$$

For a 2/3-prescaler and a 4-bit  $B$ -counter, as in the implementation of this dissertation, the minimum and maximum divider values are  $N_{min} = 4$  and  $N_{max} = 33$ , respectively. By choosing a low prescaler value, low divider values are still possible. Extension of the divider values can be obtained by increasing the number of bits in the  $B$ -counter.

#### 2.1.4 Fractional- $N$ division

"Fractional- $N$ " Synthesis technology was introduced by Hewlet Packard for the first time with the *HP3335A* Synthesizer in 1977 [17]. A fractional- $N$  synthesizer is essentially a single-loop digital synthesizer where the  $N$ -divider has been modified to divide by an integer plus a fraction. In this way extended frequency resolution is obtained without reducing the reference frequency. The main advantage of this approach is that by keeping the  $N$ -divider values low, the system's phase noise is not sacrificed, for the sake of frequency resolution. Loop settling times can also be reduced by using possible higher loop bandwidths, due to the higher reference or phase comparison frequency.

##### 2.1.4.1 Fractional- $N$ implementation

Division by a fraction is not possible with conventional dividers. Fractional division is however possible by averaging the value of a divider between  $N$  and  $N+1$  over a period of time. A digital accumulator performs the averaging and the total averaging time of both  $N$  and  $N+1$  divisions, in terms of accumulator clock cycles, is known as the modulus (*MOD*) of the system. The number of cycles where the divider divides by  $N+1$  is known as the numerator (*FRAC*) of the fractional division. The average divider value over time then becomes fractional as indicated in Equation (2.33).



$$\begin{aligned}
 N_{ave} &= \frac{NT_N + (N+1)T_{N+1}}{T_N + T_{N+1}} = N + \frac{T_{N+1}}{T_N + T_{N+1}} \\
 &= N + \frac{FRAC}{MOD} \\
 &= N + Fraction
 \end{aligned}
 \tag{2.33}$$

And the PLL frequency resolution becomes:

$$Freq_{res} = \frac{f_{ref}}{MOD} \quad [\text{Hz}] \tag{2.34}$$

Figure 10 depicts a fractional- $N$  implementation; it is a standard PLL block diagram with a digital accumulator added to manipulate the  $N$ -divider. The  $N$  and  $N+1$  altering is controlled by the accumulator's 'overflow' bit and the  $FRAC$  and  $MOD$  signals are the programmable inputs, defining the operation of the accumulator. The accumulator derives its clock input from the output of the  $N$ -divider.

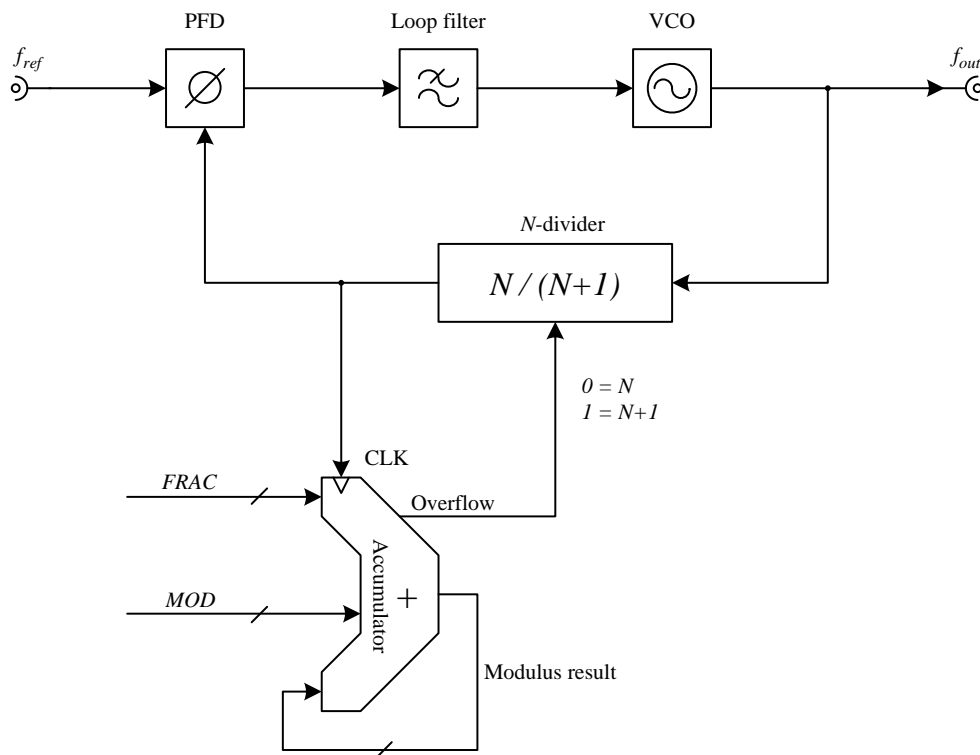


Figure 10. Fractional- $N$  PLL block diagram

In many fractional- $N$  implementations the modulus value is fixed in hardware, typically by a power-of-two  $2^n$  value, to ease the digital implementation. In this dissertation however the value is implemented to be programmable.

TABLE III shows an example of accumulator operation. The repetitive cycle equals the modulus value and the number of overflows generated in a cycle equals the FRAC part.

TABLE III

FRACTIONAL- $N$  ACCUMULATOR OPERATION

Cycle	CLK count	Accumulator result (MOD = 5, FRAC = 3)	Overflow
1 <sup>st</sup>	0	3 (3 MOD 5 = 3)	0
1 <sup>st</sup>	1	1 (6 MOD 5 = 1)	1
1 <sup>st</sup>	2	4 (4 MOD 5 = 4)	0
1 <sup>st</sup>	3	2 (7 MOD 5 = 2)	1
1 <sup>st</sup>	4	0 (5 MOD 5 = 0)	1
2 <sup>nd</sup>	5	3 (3 MOD 5 = 3)	0
2 <sup>nd</sup>	6	1 (6 MOD 5 = 1)	1

#### 2.1.4.2 Fractional spurs

A fractional- $N$  system is not without problems. For a 1<sup>st</sup> order fractional system, such as this one, fractional spurs will occur at multiples of the fractional frequency resolution, as stated in Equation (2.34). These spurs occur due to the huge spikes that the PFD causes at each  $N$  or  $N+1$  alteration. This is normal for the PFD. To counter these fractional spurs, several on-chip compensation techniques exist, but mostly at the cost of phase noise [1]. Three known techniques are [1]:

- a) Delay compensation
- b) DAC phase interpolation
- c)  $\Sigma\Delta$  modulation

Not to risk phase noise degradation, an off-chip fractional spur compensation method is used in the loop-filter for this dissertation. Details will follow in chapter 5.

### 2.1.5 Phase detector

In a PLL, the PD produces an output voltage or current according to phase difference between the reference signal and the output of the frequency divider. The most elementary form of a phase detector is a multiplying PD such as an analogue mixer or a digital XOR gate as depicted in Figure 11 [13].

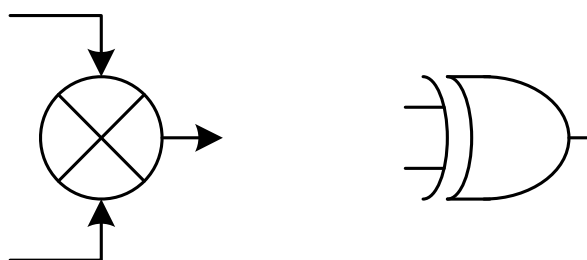


Figure 11. Multiplying PD: (a) Analogue mixer, (b) Digital XOR gate

As the name suggests, a multiplying PD works by multiplying two signals. The product will be a DC component and a high frequency component. The latter will be filtered out by the loop filter and only the DC component will remain. The two big disadvantages of multiplying PDs are that they are duty-cycle sensitive and cannot detect frequency differences between the input signals. In a PLL some form of frequency acquisition technique will always have to be used in conjunction with a multiplier PD and the input duty cycles must be kept at 50 %, for optimal operation [13].

#### 2.1.5.1 Digital tri-state PFD

With the invention of the digital tri-state PFD, many of the problems associated with multiplier PDs, were overcome. A tri-state PFD can detect both frequency and phase differences between two signals and is also duty-cycle insensitive. The first version of the digital PFD was published in 1976 by [18]. The version, as it is widely known today, is depicted in Figure 12.

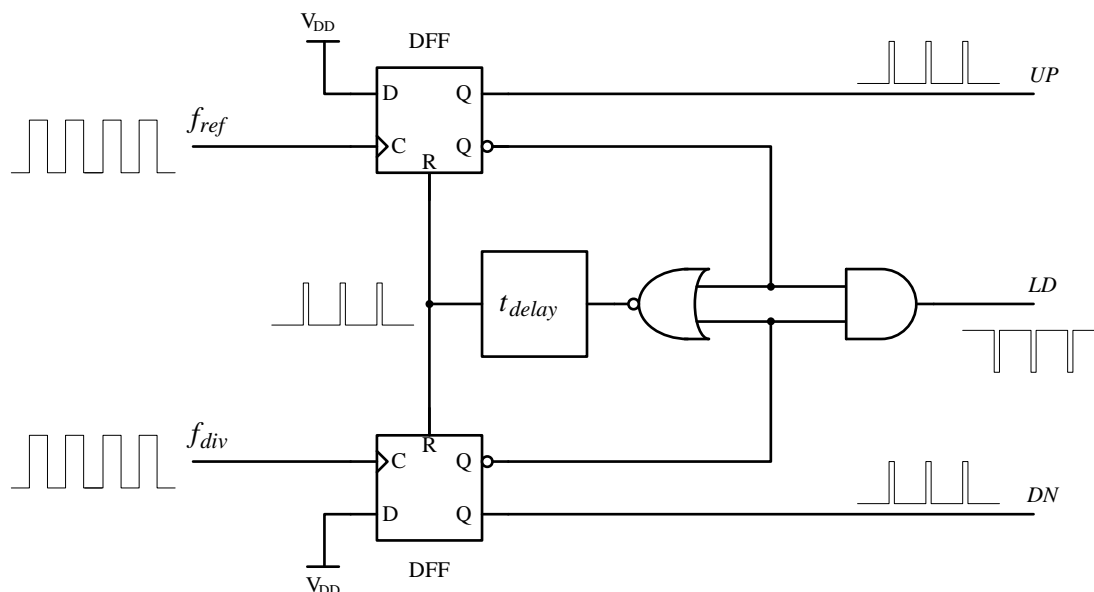


Figure 12. Tri-state PFD

The edge-triggered tri-state PFD consists of two resettable DFFs and logic to produce the reset signal. A weak point of a tri-state PFD is its dead zone (undetectable phase difference range). This occurs when the phases of the two signals are in close proximity of each other. To correct this, a delay is introduced in the reset path as depicted in Figure 12. The phase difference becomes the differential average of the two output signals  $UP$  and  $DN$ .

The functionality of the PFD is such that there are only three possible output states (tri-state). When the rising edge of the reference input  $f_{ref}$  leads that of the divided VCO output  $f_{div}$ , the PFD outputs are:  $UP=1$ ,  $DN=0$  and when the reference lags, the PFD outputs are:  $UP=0$ ,  $DN=1$ . When both input phases are the same, the PLL is in lock and the PFD outputs are:  $UP=0$ ,  $DN=0$ .

When in lock, the outputs will practically be low with narrow *high* going pulses due to the delay in the reset path. With a tri-state PFD it is also possible to extract a lock-detect (LD) indicator. When in lock, the LD output is essentially high with narrow *low* going pulses and when out of lock the output will be low. All the narrow pulses, high or low, will approximately have pulse-widths of  $t_{delay}$ .

The tri-state PFD has an idealistic linear phase detection range of  $\pm 2\pi$  radians as depicted in Figure 13. The transfer function in Figure 13 is the differential average  $\overline{K_\phi}$  of the two output signals and the slope  $\frac{K_P}{2\pi}$  is the gain of the PFD where  $K_P$  has units of [V/rad] or [A/rad].

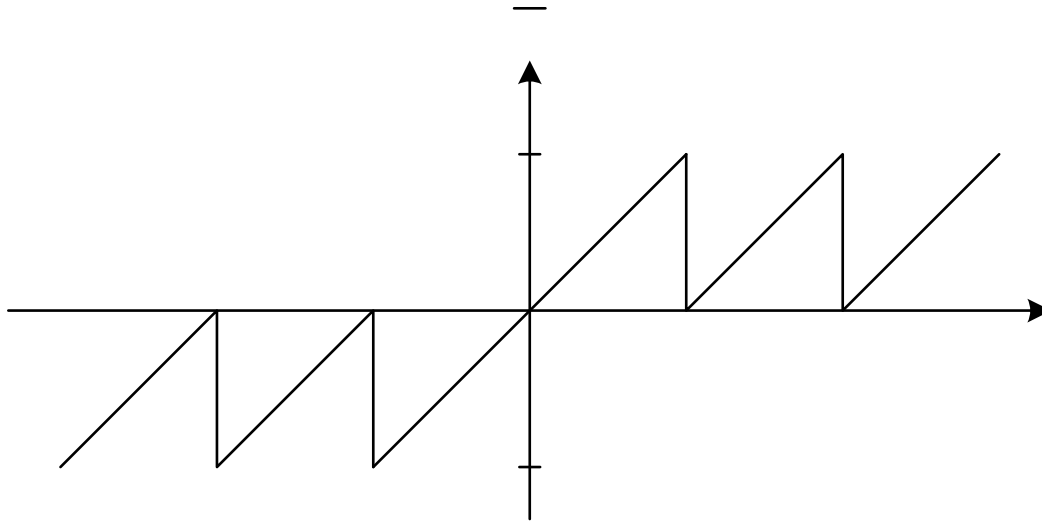


Figure 13. Ideal tri-state PFD transfer function

$K_\phi$

$K_P$

### 2.1.5.2 Non-ideal PFD

Due to the delay in the reset path of the PFD, which avoids the dead zone problem, the actual linear phase comparison range shrinks as shown in [20] to be:

$$\Delta\phi_{LIN} = \pm|2\pi - \Delta\theta|, \quad \Delta\theta = 2\pi \cdot t_{delay} \cdot f_{ref} \quad [\text{rad}] \quad (2.35)$$

Figure 14 depicts this scenario.

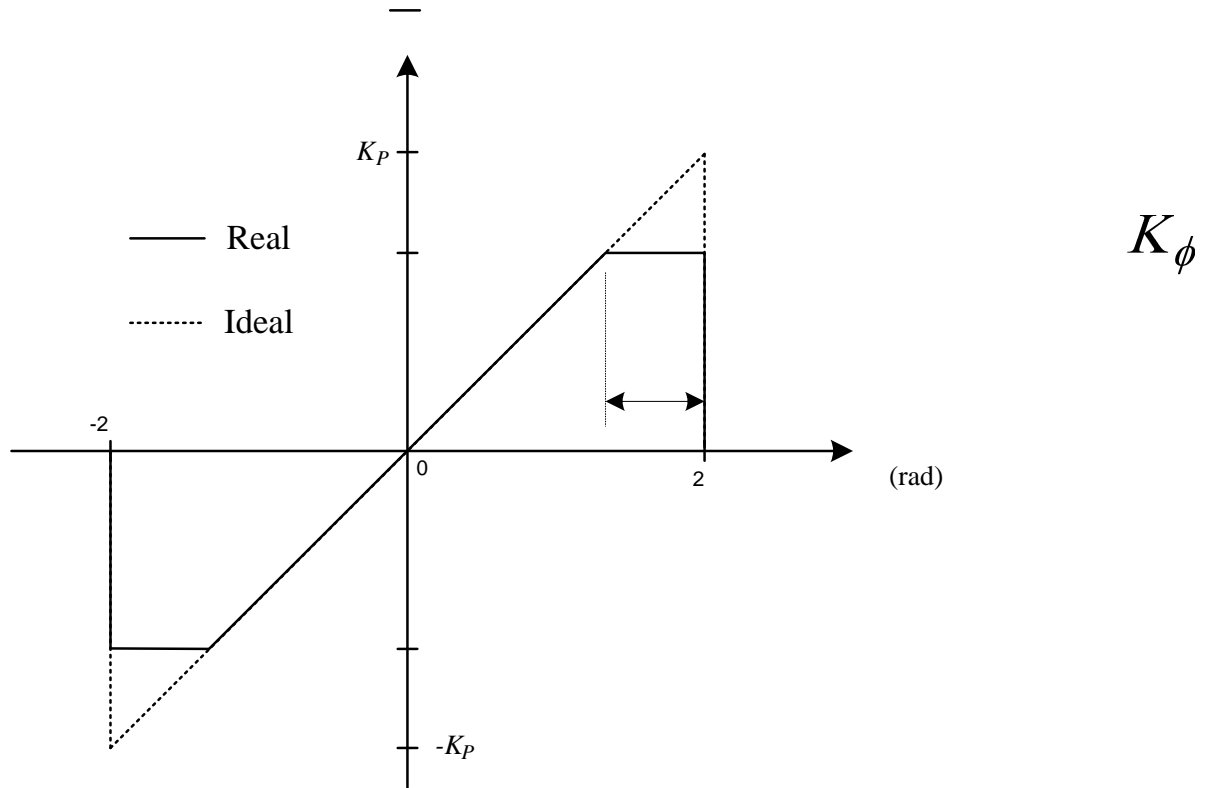


Figure 14. Real tri-state PFD transfer function

This reduced phase comparison range will not affect the gain of the PFD in the linear region. However the PLL lock-time will increase and the reset delay will also set an upper limit for the reference clock frequency when  $\Delta\theta = \pi$  [20]:

$$f_{ref}^{max} = \frac{1}{2 \cdot t_{delay}} \quad [\text{Hz}] \quad (2.36)$$

**2.1.5.3 Charge pump PFD**

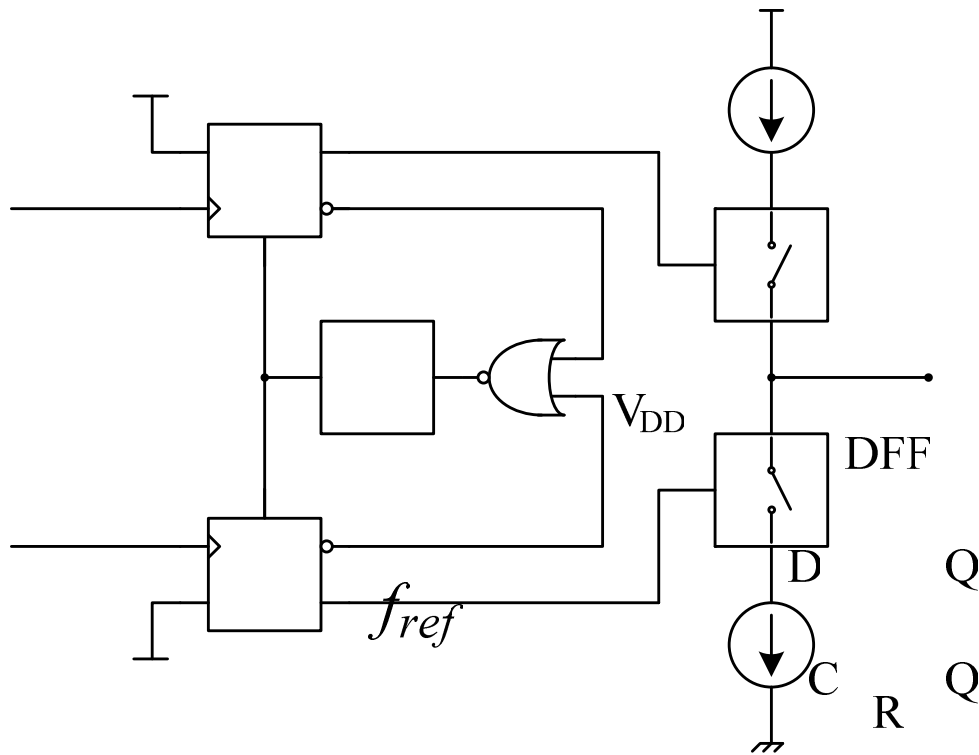


Figure 15. Charge-pump tri-state PFD

The most common PFD implementation is one with charge pumps [1] as depicted in Figure 15. The PFD *UP* and *DN* outputs are used to switch constant current sources to the output. In this dissertation CMOS technology is used and the current sources are implemented with MOSFET transistors. In section 2.3 the noise sources in MOSFET transistors, contributing to phase noise, are considered. When a CMOS charge-pump (CP) PFD is used, it is worth noting now that the thermal charge-pump noise current can be represented as [21]:

$$\overline{i_{CP}^2} = 2 \frac{t_{on}}{T_{ref}} f_{dim} \cdot \frac{2I_{CP}}{V_{GS} - V_{TH}} \Delta f \quad (2.37)$$

Where  $t_{on}$  is the turn-on time of the current source and is approximately equal to the reset delay

$$t_{delay} \text{ and } T_{ref} = \frac{1}{f_{ref}}.$$

$V_{DD}$

DFF

Equation (2.37) clearly shows the noise dependence on the reset delay. It follows from all the above that the reset delay should be kept to a minimum in order to maximise clock frequency and to minimise PLL lock-time and charge-pump phase noise. In reality the reset delay cannot be made zero, as it is required to eliminate the dead-zone. It should be made long enough to completely turn-on the switches in the CP PFD [22]. A minute pulse will not switch through the current sources and the dead-zone will appear.

### 2.1.6 Loop filter architectures

Passive and active loop filter architectures will be considered in this section with a general 2<sup>nd</sup> order transfer function as defined by Equation (2.38).

$$G_{LF}(s) = \frac{v_o(s)}{i_{CP}(s)} = \frac{sT1 + 1}{sT2(sT3 + 1)} \quad (2.38)$$

$T1$ ,  $T2$  and  $T3$  are the loop filter time constants defined by the applicable PLL system. The calculations of these time constants are discussed in section 2.1.6.3

#### 2.1.6.1 Passive loop filter

A standard passive loop filter is depicted in Figure 16 with an optional additional filter as from [24]. The additional filter helps with extra reference spur suppression. This architecture with an additional fractional spur modification is then also used in this dissertation.

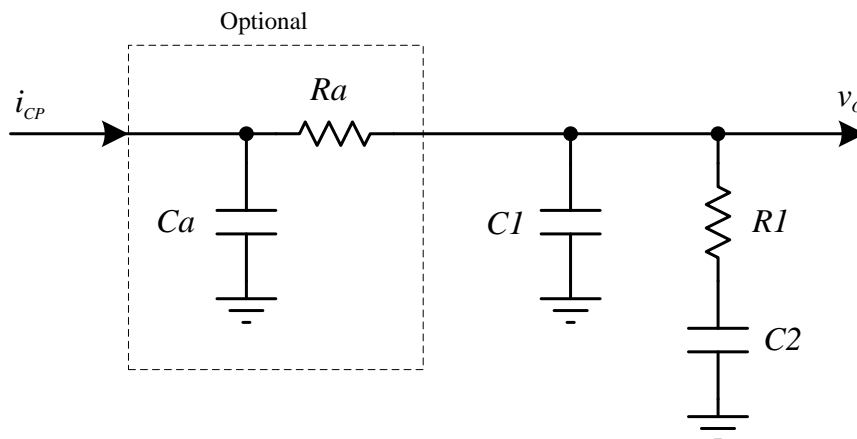


Figure 16. Passive loop filter



With a passive loop filter it is essential that the PFD CPs can do the voltage swing required to tune the VCO. If not, an active loop filter must be considered or an approach where the voltage swing of the CP can be extended, as is the case in the implementation of this dissertation.

Adapted from [23] the equivalent time constants for the passive loop filter are defined by Equations (2.39)-(2.41), as required by Equation (2.38):

$$T1 = R1 \cdot C2 \quad (2.39)$$

$$T2 = C1 + C2 \quad (2.40)$$

$$T3 = \frac{T1}{T2} \cdot C1 \quad (2.41)$$

The bandwidth of the optional reference spur filter is taken to be twenty times higher than the loop bandwidth to not affect the resulting phase margin [24]. Calculation of the capacitor or resistor values is then given by Equation (2.42):

$$Ca = \frac{1}{20 \cdot Ra \cdot \omega_p} \quad (2.42)$$

### 2.1.6.2 Active loop filter

Active loop filters are popular with wide tuning range VCOs as the upper limit of the output voltage is only restricted by the supply voltage of the operational amplifier (OPAMP). A typical active loop filter from [24] is depicted in Figure 17:

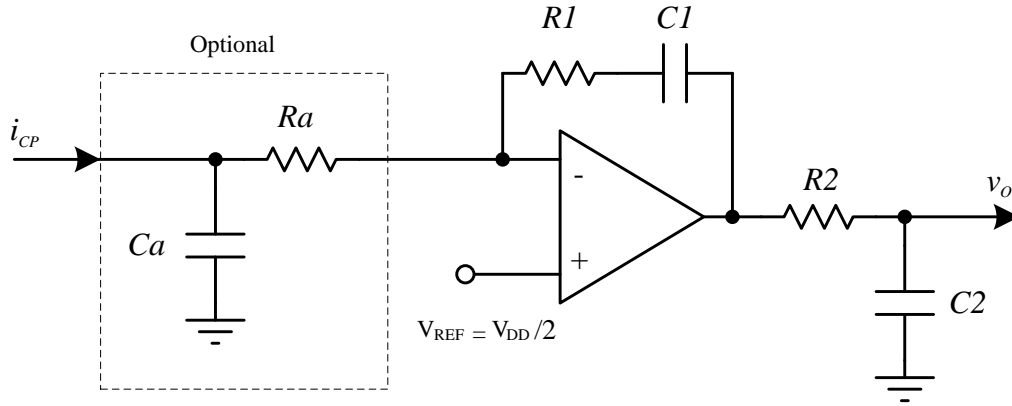


Figure 17. Active loop filter

By analysing the transfer function of the OPAMP filter it can be shown that the equivalent loop filter time constants are as indicated in Equations (2.43)-(2.45):

$$T1 = R1 \cdot C1 \quad (2.43)$$

$$T2 = C1 \quad (2.44)$$

$$T3 = R2 \cdot C2 \quad (2.45)$$

The additional reference spur filter can also be calculated by Equation (2.42).

A major shortfall of active loop filters is noise. Unlike passive loop filters, the OPAMP in an active loop filter is always “on” producing noise. The amount of noise will depend on the OPAMP used. From Table II.3 the contribution of the OPAMP noise will have a bandpass response, peaking at the loop bandwidth. Thus affecting the in-band phase noise in the vicinity of the loop bandwidth and onwards the out-band phase noise. For this reason a passive loop filter with a charge-pump voltage extension architecture was rather implemented in this dissertation.



### 2.1.6.3 Loop filter time constants calculation

The calculations of the loop filter time constants as required in Equation (2.38) are derived from the stability guidelines presented in section 2.1.1.6 and with adaptations from [23].

Equations (2.16) and (2.18) are specifically used in the process to derive the time constants.

Equations (2.46)-(2.48) then defines the time constants in terms of the required phase margin  $\phi_m$ , loop bandwidth  $\omega_p$ , VCO gain  $K_V$ , phase-detector gain  $K_P$  and the  $N$ -divider value:

$$T3 = \frac{-\tan\left(\phi_m \cdot \frac{\pi}{180}\right) + \sec\left(\phi_m \cdot \frac{\pi}{180}\right)}{\omega_p} \quad (2.46)$$

$$T2 = \frac{K_P \cdot K_V}{\omega_p^3 \cdot N \cdot T3} \quad (2.47)$$

$$T1 = \frac{1}{\omega_p^2 \cdot T3} \quad (2.48)$$

## 2.2 PHASE NOISE

This section describes and explains the concept of phase noise and the negative implications of phase noise in any communication or digital system. It will then become clear why it is important for PLL systems to have low phase noise and hence in synthesizer ICs.

### 2.2.1 Phase noise basics

Phase noise occurs in all practical clock signals and oscillators due to time-varying phase fluctuations which effectively spreads the carrier frequency. A sinusoidal clock or oscillator with an output frequency of  $f_c$  in Hz can be mathematically modelled as:

$$v(t) = A \cos[2\pi f_c t + \varphi(t)] \quad [\text{V}] \quad (2.49)$$

Where  $\varphi(t)$  then represents the random phase variation. When the phase variation  $\varphi(t)$  is small,  $|\varphi(t)| \ll 1$  rad, which will be the case for a stable carrier without FM modulation, Equation (2.49) can be simplified using trigonometric identities to:

$$v(t) \approx A \cos(2\pi f_c t) - A \varphi(t) \sin(2\pi f_c t) \quad [\text{V}] \quad (2.50)$$

This means that the spectrum of  $\varphi(t)$  is frequency-translated to  $\pm f_c$  or in other words the carrier is spread by the noise profile.

The measurement of phase noise is defined as such that it is measured as single sideband (SSB) phase noise  $\mathcal{L}(\Delta f)$  in dBc/Hz. This is defined as the ratio between the total carrier power  $P_{carrier}$  and the noise power  $P_{noise-1Hz}$ , in a 1 Hz bandwidth, at a frequency offset  $\Delta f$  from the carrier as depicted in Figure 18.

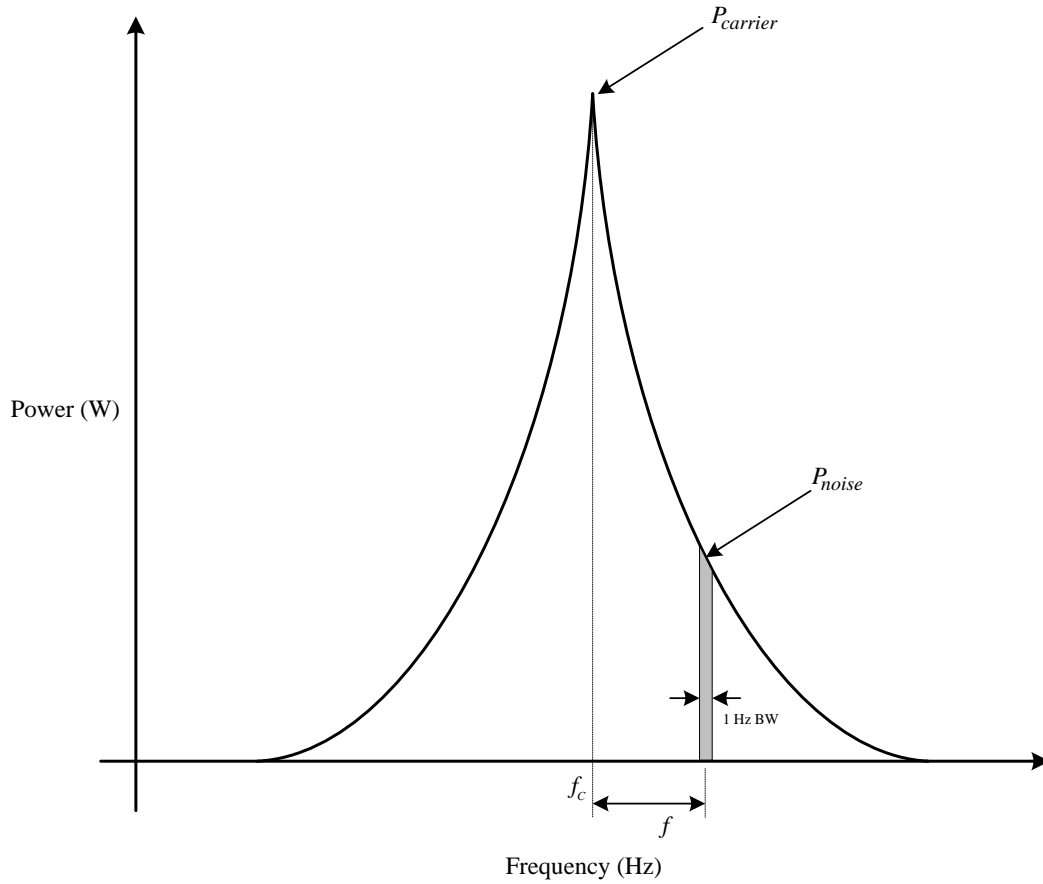


Figure 18. Oscillator phase noise

Mathematically, SSB phase noise can be defined as:

$$L(\Delta f) = 10 \log \left( \frac{P_{noise\ 1Hz\ at\ f_c + \Delta f}}{P_{carrier}} \right) \quad [\text{dBc/Hz}] \quad (2.51)$$

This is simply, but practically, one-half of the double sided phase noise spectral density  $S_\phi(\Delta f)$ , with units of  $\text{rad}^2/\text{Hz}$ , which contains both upper and lower sideband components:

$$L_\phi(\Delta f) = 10 \log \left( \frac{S_\phi(\Delta f)}{2} \right) \quad [\text{dBc/Hz}] \quad (2.52)$$

Phase noise measurements are normally displayed graphically on a logarithmic plot. The negative implications of phase noise will now be discussed in sections 2.2.2 and 2.2.3.

### 2.2.2 Reciprocal mixing

One of the unwanted side-effects of phase noise in a communication system, employing mixers, is reciprocal mixing [25]. Reciprocal mixing is the effect due to the phase noise of the local oscillator modulating the carrier of a strong signal. The carrier is then spread in frequency which results in a power spectral density that is proportional to the local oscillator's SSB phase noise. When a receiver is tuned to a weak signal  $f_{RX}$  near a strong carrier  $f_c$ , the resulting intermediate frequency (IF) spectrum may mask or block the weaker signal. Figure 19 depicts this scenario.

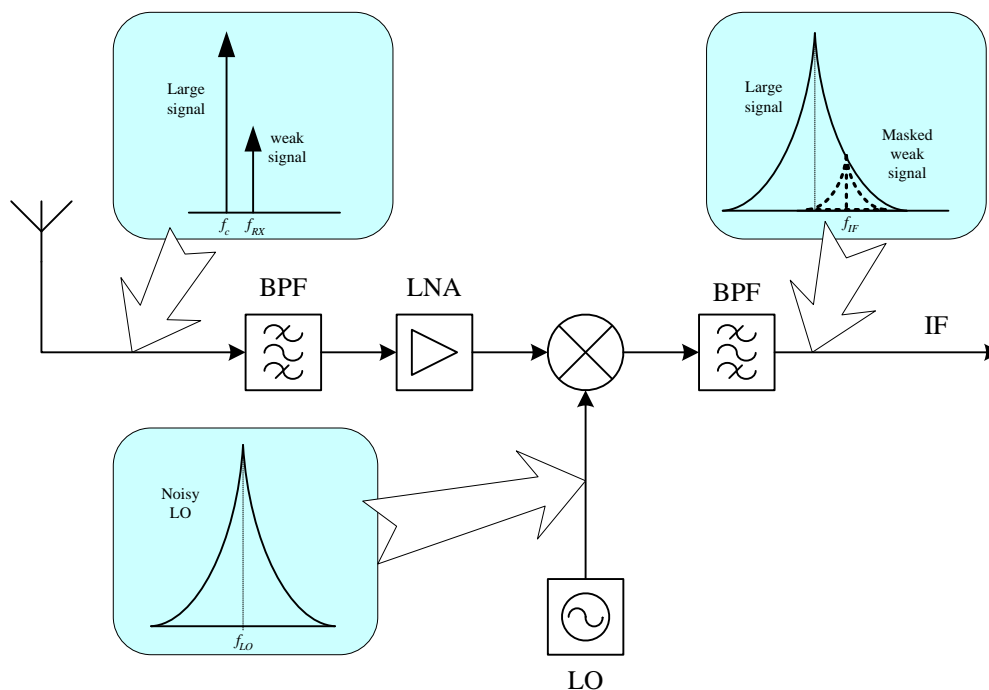


Figure 19. The effect of LO phase noise on receiver sensitivity.

Reciprocal mixing will then ultimately reduce the receiver's sensitivity in the presence of large co-channel signals. In literature this is also known as part of the blocking capability of a receiver [26].

### 2.2.3 Jitter

Another unwanted side-effect from phase noise is time jitter. This becomes important for clock signals in digital systems, especially for sampled systems such as wideband analogue to digital converters (ADCs). It can be shown that the full-scale dynamic range of an ADC is limited by the analogue input frequency and the jitter of the clock source [27]:

$$SNR_{FS} = -20 \log(2\pi f_{analogue} \Delta t_{RMS}) \quad [\text{dB}] \quad (2.53)$$

Where  $f_{analogue}$  is the analogue input signal and  $\Delta t_{RMS}$  is the RMS time jitter on the clock. It is thus important to minimise the time jitter as to maximise the possible full-scale signal-to-noise-ratio (SNR) or dynamic range.

The sum of all phase noise in a band limited signal translates to the time domain as a residual RMS phase jitter component and as an equivalent residual FM component. Time jitter can be calculated from the residual phase jitter component. Shown next, is how to calculate these residual components from an existing phase noise profile. The maximum value of these residual components sometimes forms part of some system specification and hence the additional need to calculate residual values. The equations used [1] originates from stochastic noise processes theory.

#### 2.2.3.1 Residual PM

Intuitively, residual phase jitter or residual phase modulation (PM) will also affect the possible SNR obtainable in any phase modulation scheme, as an example quadrature phase shift keying (QPSK), used in digital communications. It is not the scope of this dissertation to investigate to what degree phase noise affects digital communications but to merely point out that the effects exist.

The RMS residual phase jitter of a signal is related to the double sided phase noise spectral density  $S_{\phi}(f)$  of the signal.

The units of  $S_{\varphi}(f)$  is  $\text{rad}^2/\text{Hz}$ , so the RMS phase jitter becomes the square root of the integral of  $S_{\varphi}(f)$  over the band of interest  $f_1$ - $f_2$ , as indicated in Equation (2.54):

$$\Delta\theta_{RMS} = \sqrt{\int_{f_1}^{f_2} S_{\varphi}(f) df} \quad [\text{rad}] \quad (2.54)$$

From Equation (2.52) the relation to the logarithmic phase noise  $\mathcal{L}(\Delta f)$  follows:

$$\Delta\theta_{RMS} = \sqrt{2 \int_{f_1}^{f_2} 10^{\frac{\mathcal{L}(f)}{10}} df} \quad [\text{rad}] \quad (2.55)$$

With a given logarithmic phase noise plot of a signal and Equation (2.55) the residual RMS phase jitter can then be calculated.

Calculating the RMS time jitter in seconds then just becomes a translation from radians to seconds:

$$\Delta t_{RMS} = \frac{\Delta\theta_{RMS}}{2\pi f_o} \quad [\text{s}] \quad (2.56)$$

Where  $f_o$  is the frequency of the signal.

### 2.2.3.2 Residual FM

With analogue FM receivers or in the case of digital communications such as FSK systems, the carrier or LO phase noise also have an effect on the quality of the demodulated signal. With no modulation present in these systems, the demodulated output from the FM discriminator will show a residual noise component. The dynamic range or SNR of the demodulated signal is thus affected. This demodulated component is known as the residual FM component of the phase noise. Residual FM is also important in radar systems but this is beyond the scope of this dissertation.





The residual RMS FM component is calculated by the stochastic noise process formula for RMS, over the bandwidth of the demodulator  $f_1$ - $f_2$ :

$$\Delta f_{RMS} = \sqrt{\int_{f_1}^{f_2} f^2 S_{\varphi}(f) df} = \sqrt{2 \int_{f_1}^{f_2} 10^{\frac{L(f)}{10}} f^2 df} \quad [\text{Hz}] \quad (2.57)$$

#### 2.2.4 Conclusion

This then concludes the discussion on phase noise and why it is relevant in any communication system and hence in a digital synthesizer IC.

### 2.3 INTRINSIC NOISE

In electrical circuits, the three most common noise sources or types are [22]:

- a) Thermal or Johnson noise
- b) Flicker or  $1/f$  noise
- c) Shot noise

All of these noise sources can occur inside a synthesizer IC as they are generated internally by transistors or resistors and are therefore referred to as intrinsic noise sources. These noise sources will occur simultaneously in a circuit and can be distinguished by their spectral densities as shown in Figure 20:

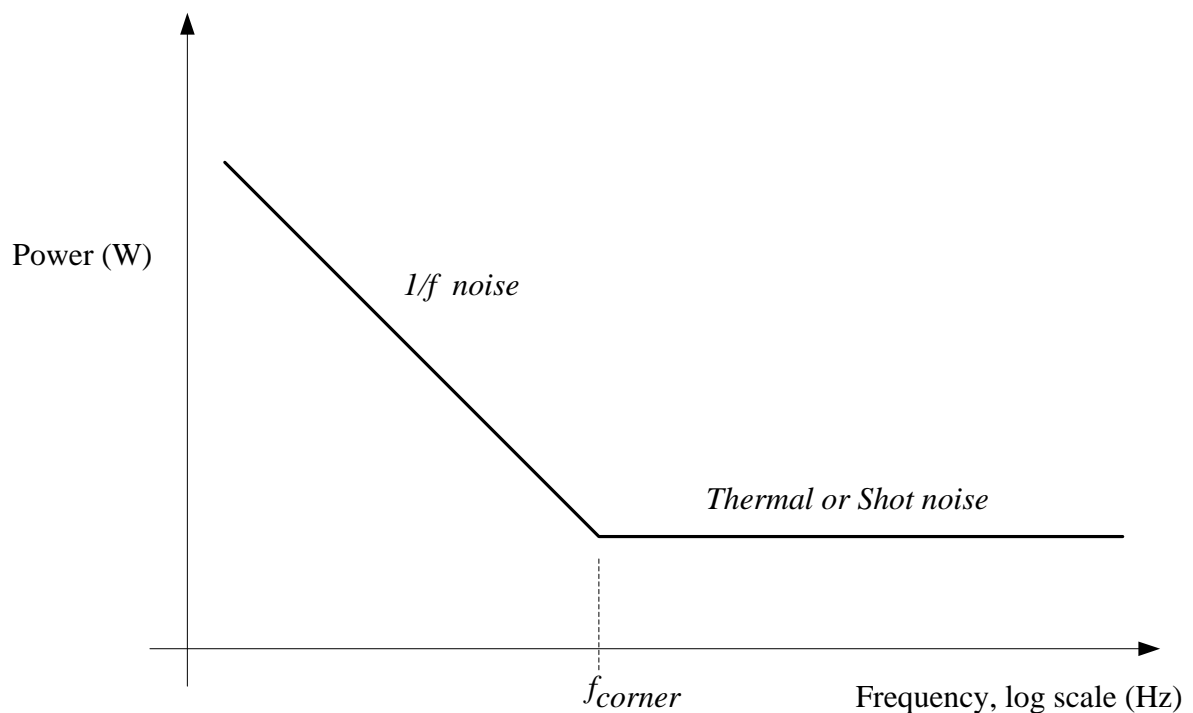


Figure 20. Spectral density of different noise types

The frequency at which the thermal noise starts to dominate above the flicker noise is known as the corner frequency  $f_c$  or flicker cut off frequency.

### 2.3.1 MOSFET small-signal noise model

This dissertation deals with a CMOS process so the three forms of intrinsic noise in MOSFETs are discussed next. Intrinsic noise sources are small and can be modelled by including their contribution in the MOSFET small-signal model as depicted in Figure 21:

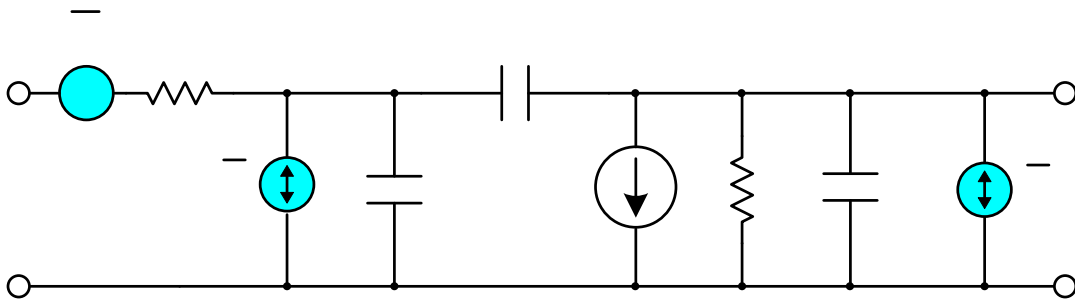


Figure 21. MOSFET small-signal model with noise sources [22][28]

The MOSFET gate noise is modelled as a thermal noise voltage  $\overline{v_g^2}$ , for the gate resistance  $r_g$  and as a shot noise current  $\overline{i_g^2}$ , for the gate leakage current. The MOSFET channel noise current  $\overline{i_d^2}$  is modelled as a composite thermal and flicker noise component.

### 2.3.2 Thermal noise

Thermal noise occurs in any resistive circuit and is due to the random motion of electrons in a conductor. The motion of these electrons is dependent on the absolute temperature and therefore the name “thermal” noise. This motion of electrons then introduces voltage fluctuations, or noise, across the conductor. Thermal noise has a white spectral density as already depicted in Figure 20 and has a Gaussian amplitude distribution. The mean-square (open-circuit) voltage and (short-circuit) current noise is modelled as [29]:

$$\overline{v_n^2} = 4kTR\Delta f \quad [\text{V}^2] \quad (2.58)$$

$$\overline{i_n^2} = \frac{4kT\Delta f}{R} \quad [\text{A}^2] \quad (2.59)$$

Where  $k = 1.38 \times 10^{-23}$  J/K is the Boltzmann constant,  $R$  is resistance of the conductor,  $\Delta f$  is

the unit bandwidth and  $T$  is the temperature in Kelvin.

Referring to Figure 21, thermal noise in a MOSFET occurs in two places, in the gate and in the drain-source channel. The gate noise voltage  $\overline{v_g^2}$  is due to the resistance of the gate  $r_g$  and is reduced by using multiple-finger designs as in section 4.2.1.6. The dominating thermal noise component in a MOSFET is the channel noise current  $\overline{i_d^2}$  [22]. Intuitively  $\overline{i_d^2}$  is expected to be dependent on the saturation mode output resistance  $r_o$ , as depicted in Figure 21 and defined in Equation (2.60) [30]:

$$r_o = \frac{1}{\lambda I_D} = \frac{V_A}{I_D} \quad [\Omega] \quad (2.60)$$

Where  $\lambda$  is the channel-length modulation parameter,  $V_A$  the Early-voltage of the process used and  $I_D$  the drain current.

However research [31][32] suggests that the thermal noise current  $\overline{i_d^2}$  is rather given by:

$$\overline{i_d^2} = 4kT\gamma g_m \Delta f \quad [A^2] \quad (2.61)$$

Where  $\gamma$  is a noise coefficient and  $g_m$  the transconductance of the MOSFET.

From enhancement MOSFET theory, the drain current of a MOSFET in saturation mode, is given by Equation (2.62) and can be approximated due to a normally small channel-length modulation parameter  $\lambda$ :

$$\begin{aligned}
 I_D &= \frac{1}{2} \mu C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS}) \\
 &\approx \frac{1}{2} \mu C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2
 \end{aligned}
 \tag{A} \tag{2.62}$$

Where  $\mu$  is the charge mobility,  $C_{ox}$  is the gate capacitance per unit area,  $W/L$  is the transistor aspect ratio,  $V_{GS}$  the gate-source voltage,  $V_{TH}$  the process threshold voltage and  $V_{DS}$  the drain-source voltage.

The transconductance  $g_m$  is defined as the partial derivative of  $I_D$ :

$$\begin{aligned}
 g_m &= \left. \frac{\partial I_D}{\partial V_{GS}} \right|_{V_{DS} = \text{const}} \\
 &= \mu C_{ox} \frac{W}{L} (V_{GS} - V_{TH})
 \end{aligned}
 \tag{S} \tag{2.63}$$

The saturation transconductance of a MOSFET can also be shown to be equal to [22]:

$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}
 \tag{S} \tag{2.64}$$

Hence the origins of Equation (2.37) in section 2.1.6.1 describing the thermal noise of a charge-pump PFD.

To reduce thermal noise in a MOSFET, it follows from Equation (2.61) that the transconductance  $g_m$  must be minimised. This is achieved by maximising the gate voltage swing  $V_{GS}$  or reducing the drain current  $I_D$  as suggested by Equation (2.64). This conclusion will become important when designing current mode logic circuits.

### 2.3.3 Flicker noise

Flicker noise dominates the noise spectrum at low frequencies. The noise spectral density is inversely proportional to frequency as depicted in Figure 20. For this reason flicker noise is also called  $1/f$  noise or “pink” noise. It is generally understood that flicker noise originates in

any device due to surface charge effects [22]. Flicker noise occurs in a MOSFET due to surface effects at the interface between the gate oxide and the silicon substrate [22]. Since the silicon crystals of the substrate reach an end at this interface, many “dangling” bonds appear, giving rise to extra energy states. As surface charge carriers move at the interface, some are randomly trapped and later released by these energy states, introducing “flicker” noise in the drain current. Unlike thermal noise, flicker noise power cannot be easily predicted and as such are different from one CMOS technology to another. The general drain noise current spectral density is given by Equation (2.65) [22]:

$$\overline{i_d^2} = \frac{K}{C_{ox} \cdot W \cdot L} \cdot \frac{I_D}{f} \cdot \Delta f \quad [A^2] \quad (2.65)$$

Where  $K$  is a process specific noise coefficient. The inverse dependence of (2.65) on area  $W$

$\times L$  suggests that to decrease  $1/f$  noise, the device area must be maximised or the drain current

$I_D$  must be reduced. This becomes important when designing low noise current mirrors, such as used in CML circuits.

As a final remark on  $1/f$  noise, it is known that bipolar junction transistors (BJTs) are less subjected to  $1/f$  noise than MOSFETs [33]. Intuitively this can be explained due to the fact that the majority of the collector-emitter current flows through the bulk of the device and not as with MOSFETs close to the surface. It is also believed that PMOS devices may exhibit less flicker noise than NMOS devices due to the fact that the holes are carried in a “buried” channel, not close to the oxide-silicon interface [22].

### 2.3.4 Shot noise

Shot noise is caused by the fact that a DC flowing across a potential barrier, such as a P-N junction, is not smooth, but is comprised of individual electrons arriving at random times. This

random flow gives rise to broadband white noise that gets worse with increasing current. The spectral density of shot noise is given by [29]:

$$\overline{i_d^2} = 2qI_{DC}\Delta f \quad [A^2] \quad (2.66)$$

Where  $q = 1.6 \times 10^{-19}$  C is the electron charge. MOSFETs operating in the saturation region

have very little shot noise due to the small gate leakage current and can be ignored for all practical reasons. In the sub-threshold region, shot noise dominates (instead of thermal noise) [34], but MOSFETs are rarely used in this region.

### 2.3.5 Noise to phase jitter translation

The effect of noise on a clock signal is discussed in this section as most subsystems inside a digital PLL are clocked digital blocks. Any noise voltage on the clock input of a digital block will introduce jitter and hence phase noise on its output. The noise-to-jitter translation will occur at the switching threshold voltage  $V_{TH}$  of the clock input. Figure 22 depicts a typical clock waveform with a period of  $T$  seconds and a slew rate of  $\lambda$  V/s at the switching voltage  $V_{TH}$ .

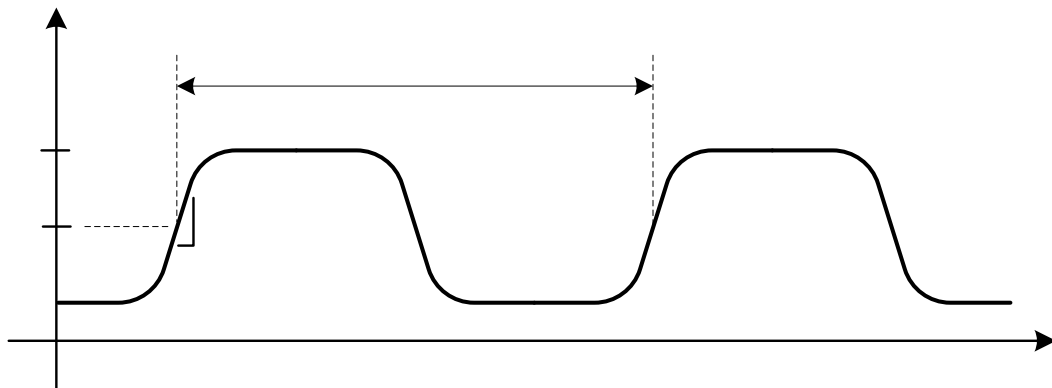


Figure 22. Digital clock waveform

When a RMS noise voltage  $v_n$  is present on the clock waveform, it follows from Figure 22 that the resulting RMS time jitter introduced at  $V_{TH}$  is:

$$\Delta t_n = \frac{v_n}{\lambda}, \quad \lambda = \left. \frac{dV}{dt} \right|_{v=V_{TH}} \quad [\text{s}] \quad (2.67)$$

The resulting RMS phase jitter  $\Delta\phi_n$  then becomes:

$$\Delta\phi_n = \frac{2\pi}{T} \Delta t_n = \frac{2\pi}{T} \cdot \frac{v_n}{\lambda} \quad [\text{rad}] \quad (2.68)$$

From Equation (2.68) it follows to minimise phase jitter; the slew rate of the clock waveform must be made as high as possible and the noise voltage should be made as small as possible. In practice these two requirements are conflicting. High slew rates generally implies high bandwidth designs which in turn implies high current designs. High current designs, as was seen earlier in this section, increase the levels of all noise types in transistors.



## 2.4 PLL IC FIGURE OF MERIT (FOM)

A figure of merit (FOM) was first proposed by [1] to compare the in-band phase noise plateaus of different digital synthesizer ICs employing digital tri-state PFDs. In literature it is also known as the normalized phase noise floor  $\mathcal{L}_{1\text{Hz}}$ . It differs from device to device and gives an idea of the amount of intrinsic noise jitter present in the dividers and PFD [35]. From a synthesizer IC design perspective it then becomes important to minimise the FOM.

For illustration a typical logarithmic PLL phase noise plot with an in-band plateau is depicted in Figure 23. With the FOM known it is then possible to predict the absolute value of this plateau. This plateau is the same plateau that was illustrated in Figure 1. The FOM is only applicable to the plateau and not to any sloped regions such as flicker noise.

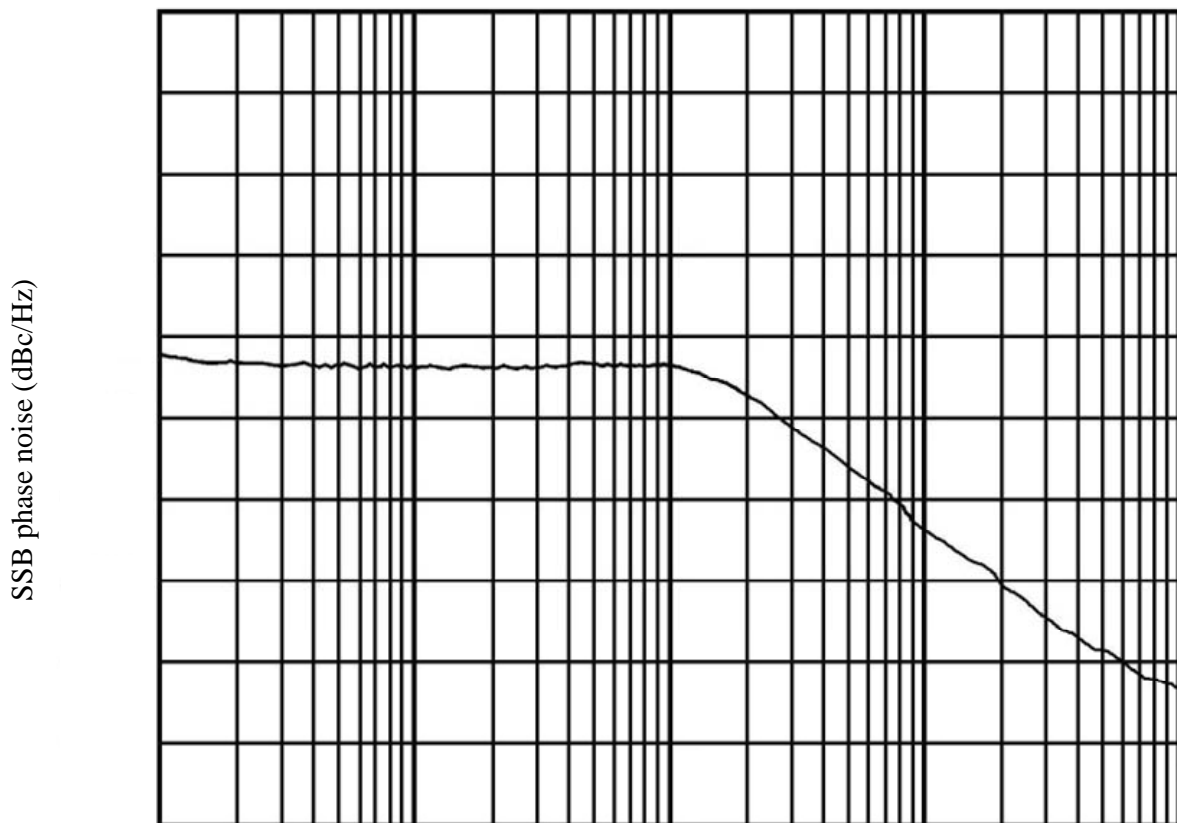


Figure 23. Typical PLL phase noise plot with in-band plateau

The FOM is a normalized 1-Hz phase noise floor with respect to the phase comparison frequency  $f_R$  at which the PFD operates and is defined as [1]:

$$FOM = L_{1\text{Hz}} = L(\Delta f) - 20\log N - 10\log f_R \quad [\text{dBc/Hz}] \quad (2.69)$$

TABLE IV compares the FOMs attained by other scholarly work and by this work:

TABLE IV

FOM COMPARISON

Reference	Technology	$\mathcal{L}_{1\text{Hz}}$ (dBc/Hz)
[3]	0.35 $\mu\text{m}$ SiGe BiCMOS	-213
[4]	0.5 $\mu\text{m}$ CMOS	-202
[5]	0.5 $\mu\text{m}$ CMOS	-211
[11]	0.18 $\mu\text{m}$ CMOS	-221
[12]	90 nm CMOS	-222
This work	0.35 $\mu\text{m}$ CMOS	-225

What is evident is the 12 dB improvement over a previous 0.35  $\mu\text{m}$  SiGe BiCMOS process.

#### 2.4.1 Phase noise prediction from FOM

As mentioned, when the normalized phase noise floor of an IC is known, it can be used to accurately predict the in-band phase noise performance for different divider ratios and phase comparison frequencies, provided the loop bandwidth is large enough to negate the effect of the VCO's phase noise contribution. This is shown in Equation (2.70) by rearranging Equation (2.69):

$$L(\Delta f) = L_{1\text{Hz}} + 20\log N + 10\log f_R \quad [\text{dBc/Hz}] \quad (2.70)$$

Equation (2.70) is very similar to Equation (2.22) as it once again shows the phase noise dependence on the  $N$ -divider value and in addition now to the phase comparison frequency  $f_R$ .

It basically states that the noise floor of a digital PFD will increase by a 10 log factor of the comparison frequency. This is a major drawback of a digital PFD, but the effect of reducing

the  $N$ -divider still outweighs the effect of an increased comparison frequency, as is shown next.

For a fixed PLL output frequency  $f_{out}$ , the  $N$ -divider value and the comparison frequency are related as by Equation (2.1), so Equation (2.70) can be rewritten in terms of just the  $N$ -divider or comparison frequency:

$$L(\Delta f) = L_{1\text{Hz}} + 10\log f_{out} + 10\log N \quad [\text{dBc/Hz}] \quad (2.71)$$

$$L(\Delta f) = L_{1\text{Hz}} + 20\log f_{out} - 10\log f_R \quad [\text{dBc/Hz}] \quad (2.72)$$

To minimise the phase noise of a digital PLL, Equation (2.71) still indicates that the  $N$ -divider must be as small as possible and in addition Equation (2.72) indicates that the phase comparison frequency must be as high as possible. Both equations indicate that the FOM or  $\mathcal{L}_{1\text{Hz}}$  must be minimised as well.

#### 2.4.2 FOM underlying cause

The concept of the 1 Hz FOM was first introduced by [1] but analytical models for the FOM limit have been investigated by several as in [2][3][35] and modelled as jitter being present at PFD input. From [2] Equation (2.73) indicates the relation of the FOM to the PFD input RMS timing jitter  $\Delta t_{in}$ :

$$L_{1\text{Hz}} = 20\log(2\pi\Delta t_{in}) \quad [\text{dBc/Hz}] \quad (2.73)$$

Equation (2.73) shows that the FOM or  $\mathcal{L}_{1\text{Hz}}$  has a 20 log relationship to the RMS timing jitter present at the input of the PFD. To minimise the FOM it is thus essential to minimise this timing jitter. This timing jitter is due to intrinsic noise processes inside the synthesizer IC as presented in section 2.3.

## 2.5 CURRENT MODE LOGIC

CMOS static logic is widely used in integrated circuits because of its scalability, high packing density and wide noise margins, etc. However CMOS static logic has speed and dynamic power dissipation limitations. The dynamic power dissipation of static CMOS is given by [36].

$$P_D = CV^2 f \quad [\text{W}] \quad (2.74)$$

Where  $C$  is the load capacitance,  $V$  the output voltage swing and  $f$  the switching frequency.

Another disadvantage of CMOS is the general absence of true complementary outputs, creating the undesired need for additional inverters to implement this and in return increasing propagation delays. Many of these limitations can be overcome by implementing CML circuits.

CML or as it is sometimes referred to in literature as source-coupled logic (SCL), when using MOSFETs, is generally recognized as one of the fastest switching logic topologies available. CML has its differential origins from emitter-coupled logic (ECL) dating from the mid 1960s. The power dissipation of a CML circuit is constant and independent of frequency, due to a constant current source being used, and it has a lower output voltage swing than that of a static CMOS circuit using the same supply voltage. The power dissipation will be higher than a conventional CMOS circuit at low clock frequencies, but it will be less or equal at higher frequencies. It is generally understood that the maximum clock frequency of a CML circuit will be substantially higher than a conventional CMOS circuit due to its lower voltage swing [37]. Another advantage of CML is its ability to suppress common mode noise such as substrate noise, due to its differential architecture. A summary of basic operation will be discussed next in section 2.5.1.

### 2.5.1 CML basics

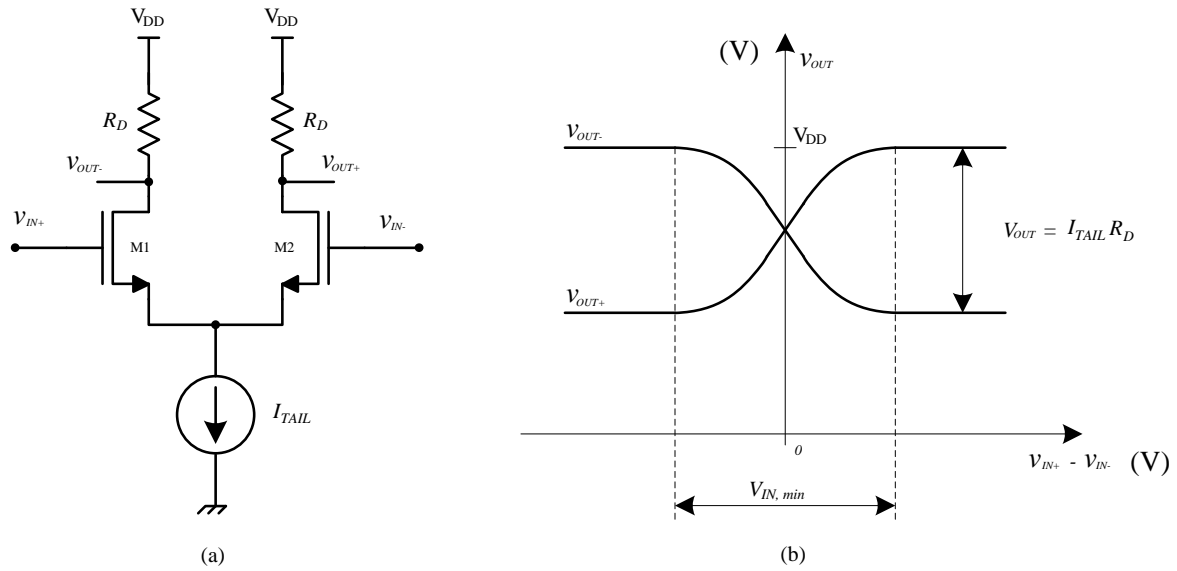


Figure 24. CML Buffer: (a) Circuit, (b) Transfer function

The CML buffer shown in Figure 24 is a basic differential amplifier operating in its non-linear (saturation) mode. For a certain minimum input differential voltage  $\Delta V_{IN,min}$ , one of the two NMOS transistors M1 or M2, depending on the polarity of  $\Delta V_{IN}$ , will be in total saturation and will act as a current steering switch for the current source  $I_{TAIL}$  hence the name “current” mode logic. As with all differential amplifiers the current source  $I_{TAIL}$  aids with the buffer’s input common mode extension [22] and ensures for input voltages greater than  $\Delta V_{IN,min}$ , the output voltage  $\Delta V_{OUT}$  remains constant as  $\Delta V_{OUT} = I_{TAIL}R_D$ . Since the circuit operates by completely switching the current from the one to the other side, the logic high and logic low values respectively are given by  $V_{DD}$  and  $V_{DD} - I_{TAIL}R_D$ . From Figure 24, the only design parameters of a CML buffer are the pull-up resistance  $R_D$ , the size of the NMOS transistors and the tail current  $I_{TAIL}$ . From the square law for drain current of a NMOS transistor in saturation, the relationship between the tail current and the minimum input voltage  $\Delta V_{IN,min}$  is given by Equation (2.75) as from [38] [40]:

$$I_{TAIL} = \frac{1}{2} \mu C_{ox} \frac{W}{L} \Delta V_{IN,min}^2 \quad [A] \quad (2.75)$$

## 2.5.2 CML design guidelines

The two main parameters to be designed or estimated are the output voltage swing and the minimum gate widths for the MOSFETs. The pull-up resistance  $R_D$  will be calculated from the required output voltage swing and the tail current  $I_{TAIL}$ . The tail current will be determined by bandwidth and output driving capabilities. The only design parameter left is the gate width  $W$ , as the gate length  $L$  is normally kept at the smallest possible process length. A first order design process for a CML buffer, as depicted in Figure 24, follows from [38] and is outlined next.

### 2.5.2.1 Output voltage swing

For the CML buffer depicted in Figure 24, the drain voltage, referenced to ground, is given by  $V_D = V_{DD} - \Delta V_{OUT}$  and hence the relative drain-source voltage  $V_{DS}$  by:

$$V_{DS} = (V_{DD} - \Delta V_{OUT}) - V_S \quad [\text{V}] \quad (2.76)$$

For the CML buffer to produce an output voltage  $\Delta V_{OUT}$ , it implies that the gate voltage must be high or equal to  $V_{DD}$ . The relative gate-source voltage  $V_{GS}$  is then given by:

$$V_{GS} = V_{DD} - V_S \quad [\text{V}] \quad (2.77)$$

For any MOSFET to operate in saturation mode it follows from MOSFET theory that the following conditions must be true [22]:

$$V_{GS} \geq V_{TH} \quad \text{and} \quad V_{DS} \geq V_{GS} - V_{TH} \quad [\text{V}] \quad (2.78)$$

Substituting Equations (2.76) and (2.77) in (2.78), the last part of (2.78) then simplifies to:

$$\Delta V_{OUT} \leq V_{TH} \quad [\text{V}] \quad (2.79)$$

Equation (2.79) places an upper limit for the output voltage if the buffer is to operate in pure saturation mode. It is desirable for the buffer to operate in saturation mode as this will ensure complete current switching from one side to the other.

### 2.5.2.2 Output voltage swing in multilevel topologies

A design process for a single level CML buffer was outlined. In reality the majority of CML circuits are multilevel; using stacked MOSFETs such as with multiplexers and D-latches etc. Some examples of standard stacked CML building blocks will be presented in section 2.5.3.

Referring to the CML multiplexer in Figure 25, the individual drain to source voltages  $V_{DS}$  of the stacked MOSFETs will intuitively be less than that of a buffer [39]. For these stacked MOSFETs to operate in saturation, it implies that  $\Delta V_{OUT}$  must be even smaller than the value obtained from Equation (2.79), to satisfy the saturation  $V_{DS}$  requirement in Equation (2.78). A smaller  $\Delta V_{OUT}$  implies a smaller  $\Delta V_{IN}$  for the next stage and in turn implies much larger MOSFETs. Larger MOSFETs will be needed for smaller gate voltages as will be seen from Equation (2.80). This will seriously start hampering the bandwidth of the logic block due to the increased gate capacitance.

From interpreting the work of others [39][40] it seems that bandwidth sacrifice can be lessened by rather operating these stacked topologies in the upper triode MOSFET region. This is done by increasing the CML output voltage swing  $\Delta V_{OUT}$  beyond the process threshold voltage  $V_{TH}$ . However a balance must be found as a too large voltage swing will increase the propagation delay and complete current switching will not occur [40]. A 90 % current switching scenario might still be adequate.

With stacked topologies it is then suggested that  $\Delta V_{OUT}$  initially be set to  $V_{TH}$  and then adjusted upwards if required. This will require parametric simulations for verification which is not always desirable.

### 2.5.2.3 Minimum MOSFET gate width

Generally with a CML design, the minimum input voltage swing  $\Delta V_{IN,min}$ , is taken to be the nominal output voltage swing  $\Delta V_{OUT}$  or a bit less to allow for design tolerances. From Equation (2.75) it then follows that the minimum gate width  $W_{min}$  for a buffer, to allow complete current switching, is calculated by:

$$W_{min} = \frac{2I_{TAIL}L}{\mu C_{ox}\Delta V_{IN,min}^2} \quad [\text{m}] \quad (2.80)$$

The inverse square relationship to the input voltage swing is clearly visible. A large  $W_{min}$  will however adversely affect the bandwidth of a MOSFET as the gate-capacitance is dependent on

the gate area  $W \times L$ :

$$C_g = W \times L \times C_{ox} \quad [\text{F}] \quad (2.81)$$

### 2.5.2.4 Minimum MOSFET gate width in multilevel topologies

In a stacked MOSFET topology as in Figure 25, each level of differential pairs should be sized separately, since the deeper a pair is located, the smaller its drain to source voltage and hence the wider it will have to be to switch the tail current [39]. Therefore, the differential pairs must be sized from the top down. Equation (2.80) is still a good estimate for the top differential pair closest to the  $V_{DD}$  rail. The differential pair closest to the tail current source can be much larger than the top pair, as will be evident with D-latches in section 4.2.

### 2.5.2.5 CML flicker 1/f noise

By the current switching nature of a CML circuit, any CML circuit effectively becomes a single-balanced current-commutating mixer. A current-commutating mixer implies any noise present in the tail current will be up-converted to noise sidebands at the output frequency of a CML circuit, visible then as phase noise. A detailed analysis on noise in CMOS current-



commutating mixers can be found in [41]. The up-converted noise is an important consideration for the flicker noise contribution of the current sources used. NMOS transistors are normally used as the current sources in CML circuits. These transistors should then be large, to reduce flicker noise, as from Equation (2.65) and [33].

### 2.5.3 CML standard building blocks

A good reference for standard CML building block topologies is [39]. For adders and XOR implementations [42] can be referenced. Some of the more widely used blocks such as a multiplexer, an AND/OR gate and a D-latch are shown briefly in Figures 25 to 27. Additional CML building blocks will be designed in section 4.2.

#### 2.5.3.1 CML multiplexer

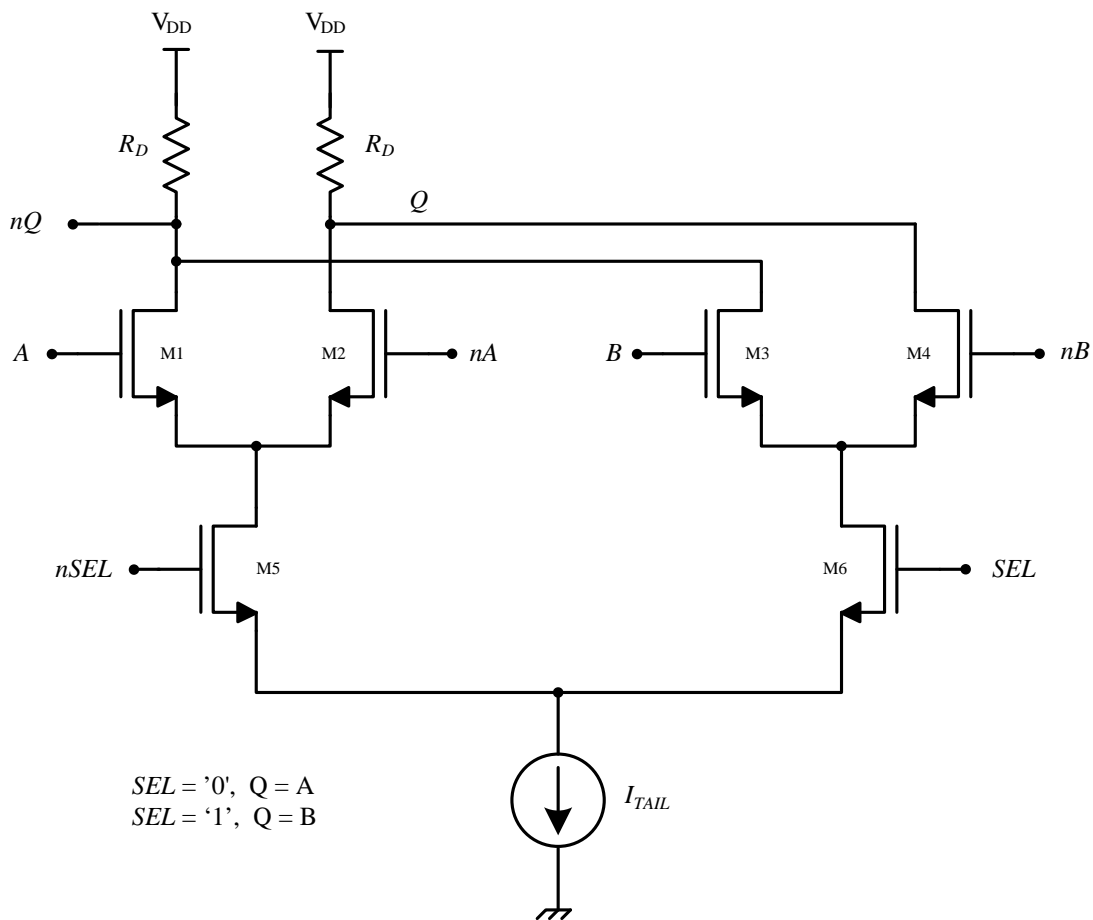


Figure 25. CML multiplexer

From Figure 25 the *SEL* signal selects the output *Q* to be *A* or *B* by enabling transistors M5 or M6.

### 2.5.3.2 CML AND/OR gate

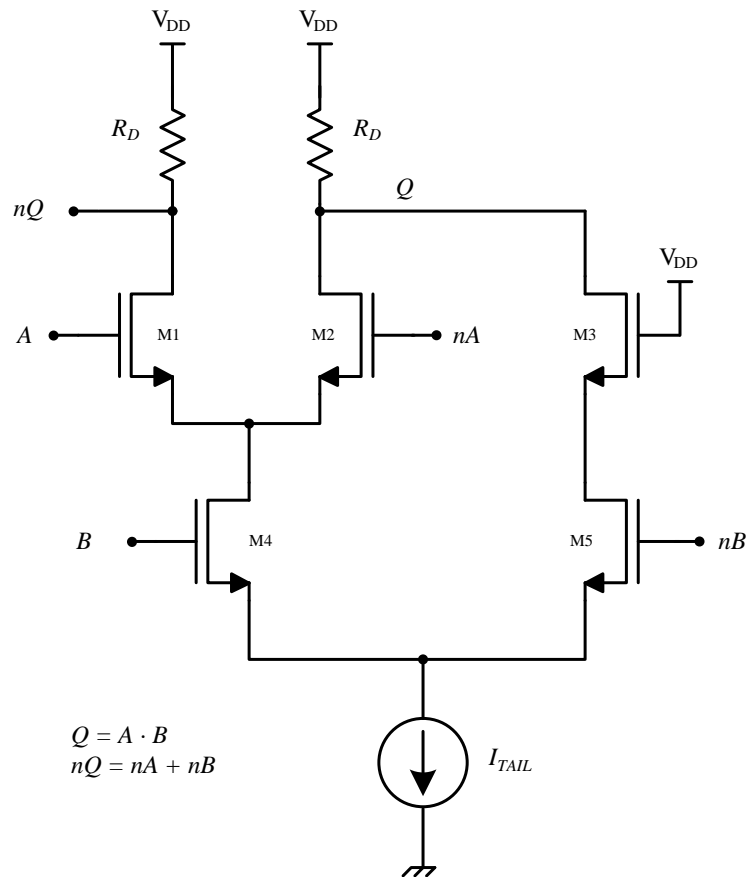


Figure 26. CML AND/OR gate

The basic form for an AND/NAND gate is depicted in Figure 26. By applying De Morgan's theorem to invert the inputs and output, the AND gate can be reused to construct an OR/NOR gate.



### 2.5.3.4 CML DFF

A CML DFF is constructed, like many other conventional DFFs, by combining D-latches in a master-slave configuration:

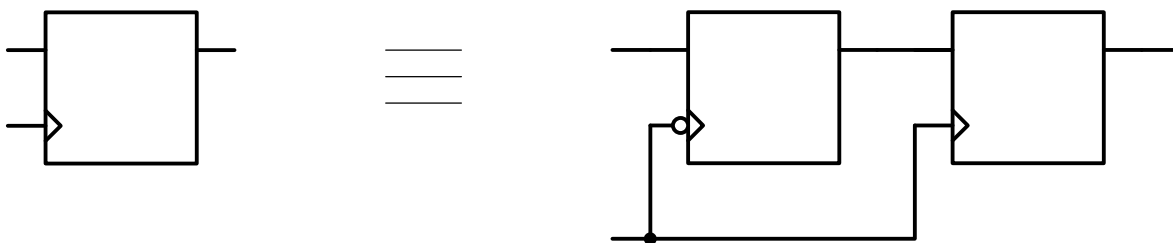


Figure 28. Master-slave D-Flip-flop implementation

When  $CLK=0$ , the input signal  $D$  is sampled by the first D-latch which is in transparent mode. The second D-latch at this stage is latching mode. When  $CLK=1$  the modes are reversed and the input signal, now at the output of the first D-latch, is transferred to the output  $Q$  on the rising edge of the clock. The main advantage of a DFF is then that it is edge sensitive and not level or duty cycle sensitive.

**D**      **Q**  
  
**CLK**

## 2.6 CONCLUSION

A review was done over all the topics and subsystems required for a low noise CMOS synthesizer IC implementation. This was done to aid research in pushing towards the limitations of conventional CMOS processes. The information gathered here will then be used in the design of the experimental CMOS synthesizer as outlined in chapter 4. The different design considerations for a low noise digital synthesizer IC, derived from this chapter, are now summarised in terms of PLL system requirements and on chip circuit requirements:

### 2.6.1 PLL system requirements

To minimise in-band phase noise coming from the PLL reference, divider and PFD circuits, the following should be done:

- a)  $N$ -divider values must be as small as possible
- b) PFD comparison frequency must be as high as possible
- c) PFD gain or the charge pump current  $I_{CP}$  should be maximised, without degrading the noise current

To meet requirement (a) an all CML fast *low division*  $N$ -divider topology is proposed in chapter 4 and both a CML and CMOS-PFD are evaluated for requirement (b). Requirements (a) and (b) will also inherently place restrictions on the tuning resolution of the proposed synthesizer IC, but this is then overcome by using a fractional- $N$  topology.

### 2.6.2 Circuit level requirements

The circuit level requirements have mostly to do with intrinsic noise levels and how to minimise it so as to minimise timing jitter and hence resulting in a better FOM.

#### 2.6.2.1 PFD reset pulse width

With a digital tri-state PFD it is essential to minimise the reset pulse width for the following reasons:

- a) The feed through of the charge pump noise to the loop-filter is minimised.
- b) A high PFD operating frequency is achieved.
- c) The phase comparison range of the PFD is maximised.

### **2.6.2.2 CML voltage swing**

The voltage swing of CML circuits must be optimised towards maximisation for two reasons:

- a) Lower MOSFET thermal noise due to a larger overdrive voltage at the gate.
- b) Higher bandwidth, less gate capacitance per MOSFET due to smaller MOSFETs that can be switched by the larger voltage swings.

The voltage swing can however not be maximised indefinitely, as this will restrict the switching MOSFETs to operate in saturation mode.

### **2.6.2.3 CML slew rate**

The CML output slew rate must be maximised to minimise the intrinsic noise to jitter translation in the output stage. This implies all output wave forms must be made as square or as fast as possible and sinusoidal signals must be avoided or amplified to square waves.

### **2.6.2.4 CML tail current sources**

In a CML circuit a 3-dimensional trade-off will exist between the tail-current  $I_{TAIL}$ , the induced noise current  $\overline{i_d^2}$  and the bandwidth of the circuit. It follows from a bandwidth perspective that the tail current must be maximised to reduce the RC effects from the output of one stage to the input of another. From a noise perspective however it becomes important to reduce the tail current. A balance must be struck between these two requirements, although bandwidth is given precedence in the circuit implementation later.

Some freedom does exist in terms of the flicker noise contribution of the current sources. From section 2.3.3 it follows that the area of a current source MOSFET can be increased to reduce its flicker noise in a circuit. It is then envisaged that all current sources and current mirrors used, should employ large devices.

This then concludes the literature review for this dissertation. Chapter 3 discusses next the research methodology followed to experimentally validate the research and hence the prototyped digital CMOS synthesizer IC.

## CHAPTER 3: RESEARCH METHODOLOGY

---

This chapter describes the methodology followed to research the CMOS process limitations inside the proposed high performance CMOS synthesizer IC.

### 3.1 RESEARCH METHODOLOGY OUTLINE

The research aim of this dissertation is to research CMOS process limitations as applicable to synthesizer ICs. Research verification was done with the implementation of a high performance CMOS synthesizer IC comparable with GaAs and HBT processes. The whole research process is illustrated in Figure 29.

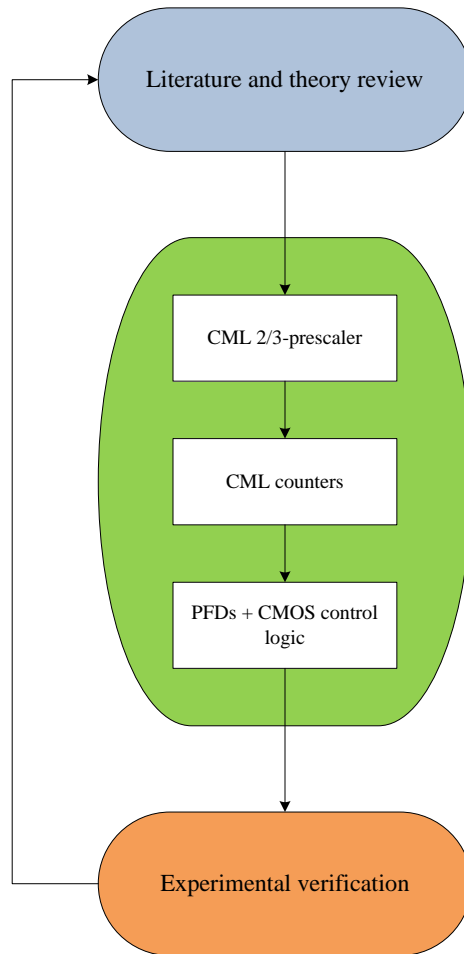


Figure 29: Research flow diagram

The research process is started with a thorough literature review and theoretical study regarding all aspects of low noise CMOS synthesizer IC design. These concepts or design guidelines are then applied to three design stages as depicted in Figure 29. Finally the IC is prototyped and experimentally verified in a laboratory. Experimental results are then compared with theory. The three major design stages are described next.

### **3.1.1 CML prescaler design and prototype**

In the construction of the high frequency programmable divider the first subsystem is a  $2/3$ -prescaler. In the synthesizer IC the prescaler operates at the highest frequency. The prescaler design is then fine tuned by simulations to yield the highest clock frequency possible. To verify the validity of the high frequency simulations, the prescaler was laid out, prototyped and tested. Measurement results provided valuable information for design modifications and were then applied to the prescaler and subsequent design phases.

### **3.1.2 CML counter design**

When the  $2/3$ -prescaler proved operational, the next step was to design the all CML pulse-swallow counter. The focus was first placed on the 4-bit program counter. Once again the design was fine tuned through simulations to yield the highest clock frequency possible. The CMOS pulse-swallow control logic was then designed and proven functional by simulation. The combined operation of the prescaler, program and swallow counters were also verified by simulation.

### **3.1.3 PFD and final design**

A synthesizer IC is incomplete without a PFD. For research benchmarking both a CML and a CMOS design were implemented, the phase noise effects were compared later. The CML design was optimised for the smallest reset pulse width. Operation of the CMOS PFD was verified through simulation. As part of this final design stage the programming interface was also designed and simulated. Finally the IC was laid out and prototyped. Experimentally measured results were then later compared with simulations.



## 3.2 CAD SOFTWARE USED

Integrated circuit (IC) design cannot be done without computer aided design (CAD) software. Any CAD software used or a combination of should ideally encompass four basic functions:

### a) Schematic capture

With schematic capture all electrical connections can be defined in a visual format. It is used to physically represent the circuit as it would look when drawn by hand. Hierarchical designs are possible due to the reuse of primitives and user defined building blocks.

### b) Simulation

The initial validity of the proposed design will be based on simulation results. The most basic simulator should be a Simulation Program with Integrated Circuit Emphasis (SPICE) simulator. Foundry supplied models for active and passive components are used in the simulations. These models normally consist of worst case process corner sets and a typical mean set. Worst case models include *worst case power* and *worst case speed* conditions. It is advisable that any IC design be simulated with these worst case scenarios and not just the typical mean model. Additional RF simulators such as phase noise simulators will be advantageous.

### c) Physical layout

The physical layout is done with this package. The output rendering should be a graphic data system II (GDSII) file which is accepted by most foundries as the definition or format for IC fabrication. Built into the package should be a Design Rule Check (DRC) engine that checks the layout against the foundry's design rules.

### d) Verification tools

A layout versus schematic (LVS) tool must be used. This verification tool extracts a net-list from the layout and compares it with the net-list from the schematics.

Throughout the time of the particular research the Tanner EDA® package from Tanner Tools® was available.

Tanner EDA® provides most of the basic functions as mentioned above at a reasonable price. The individual Tanner components used are as follows:

**Schematic capture:** S-Edit

**Simulation:** T-Spice, W-Edit

**Physical layout:** L-Edit

**Verification:** HiPer Verify, L-Edit Standard DRC, L-Edit LVS

A limitation with the Tanner suite is that it has inadequate capabilities for simulating noise and phase noise in general. A simulation package like SpectreRF® from the Virtuoso© Cadence Design Systems suite would have been helpful in this dissertation.

### 3.3 IC PROTOTYPING

The IC prototyping was done using the Austriamicrosystems (AMS)  $0.35 \mu\text{m}$  CMOS C35 process. The C35 process was chosen as it is representative of current state of the art CMOS processes at a reasonable cost. An extract of the process features [50] are given in TABLE V. Foundry data is protected by a non disclosure agreement (NDA) between the University of Pretoria, AMS and the author. As a result of the NDA, foundry data [50] is not repeated in this dissertation. It is also for this reason, TABLE V provides a range of values versus exact data.

It was decided to package the prototyped IC in a 56 pin surface mount Quad Flat No lead (QFN) package. Figure 30 depicts a typical QFN package with width and length dimensions added for a QFN-56 package.

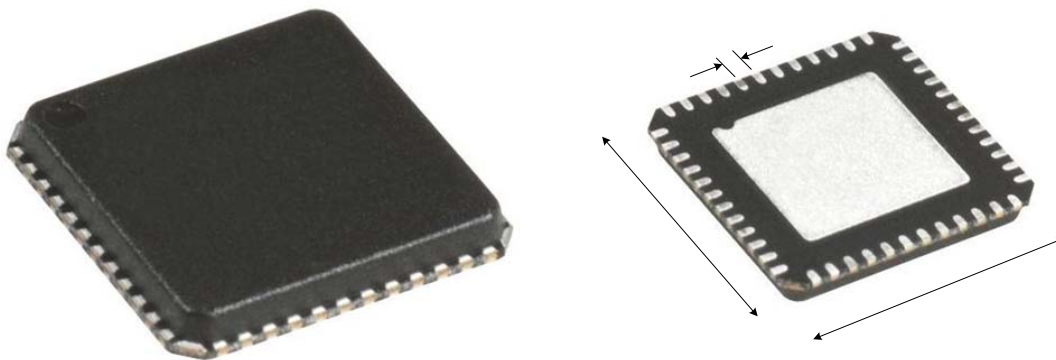


Figure 30: QFN Package – top and bottom view

A QFN package was chosen among other for the following benefits:

- Good thermal performance due to the exposed ground pad
- Good RF performance due to low lead inductance and also the exposed ground pad
- Thin low profile ( $h = 0.9 \text{ mm}$ ) for height sensitive applications

Figure 31 shows the mounting of an IC inside a QFN package with bonding wires visible.

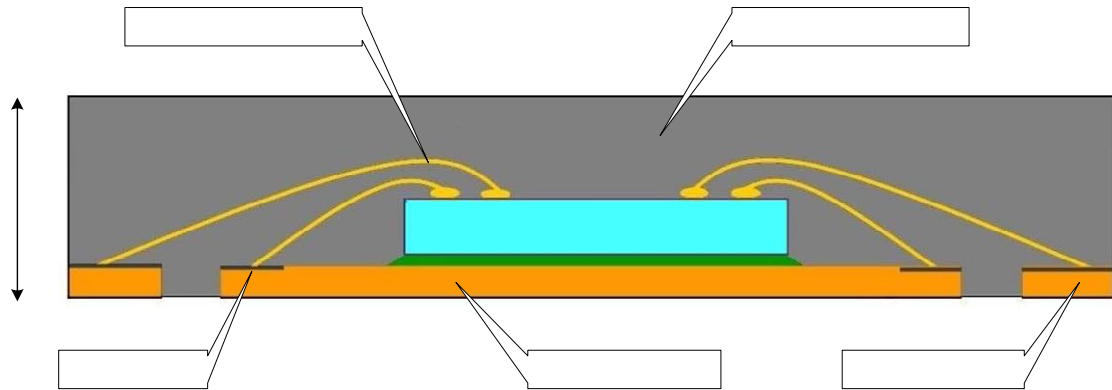


Figure 31: QFN Package - sectional view

TABLE V Au or Al bonding wire

TYPICAL 0.35  $\mu\text{m}$  CMOS PROCESS FEATURES

Parameter	Technology node: 0.35 $\mu\text{m}$
Drawn MOS channel length	0.35 $\mu\text{m}$
CMOS operating voltage range	2.5 - 3.6 V
Number of metal layers	4
NMOS short channel threshold voltage	0.4 - 0.6 V

0.9 mm

### 3.4 EXPERIMENTAL VERIFICATION

Two primary performance criteria must be verified with the prototyped CMOS synthesizer IC. The one being the maximum operating frequency and the other the phase noise FOM. All performance parameters will be tested by soldering the prototyped IC on an evaluation PCB, programming the IC by some control interface and measuring the RF parameters with laboratory test equipment. Details on the exact measurement procedures can be found in chapter 5. A list of the proposed test equipment used will be presented in section 3.4.3.

#### 3.4.1 Maximum operating frequency

The maximum operating frequency will be determined by sweeping the input frequency and amplitude with a signal generator and then observing the output of the main divider with a spectrum analyzer. This will be done for different programmed  $N$ -divider values; keeping the output frequency in the order of 100 MHz. Figure 32 depicts the proposed setup.

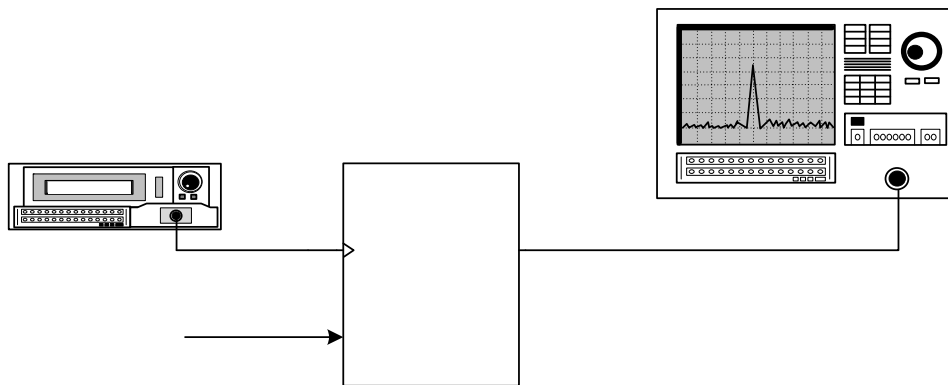


Figure 32: Maximum operating frequency test setup

Figure 32 depicts a general system setup to measure maximum operating frequency. Aspects like DC blocking capacitors and termination resistors have been omitted and will become evident in chapter 5.

### 3.4.2 FOM

The FOM is assumed to be low and hence the resulting in-band phase noise, when the IC is used stand alone in a PLL configuration. A standard high performance spectrum analyzer might not be able to measure this low in-band phase noise accurately. To aid in phase noise measurements, the IC will be tested in a 4 GHz PLL configuration with a wide loop filter. An external low noise  $\div 4$  prescaler will be added for an additional 12 dB of in-band phase noise amplification. The total division ratio would now be the product of the external prescaler and the programmed  $N$ -divider value of the prototyped IC. It should now be possible to measure the in-band phase noise with a standard high performance spectrum analyzer. Figure 33 indicates the proposed phase noise test setup:

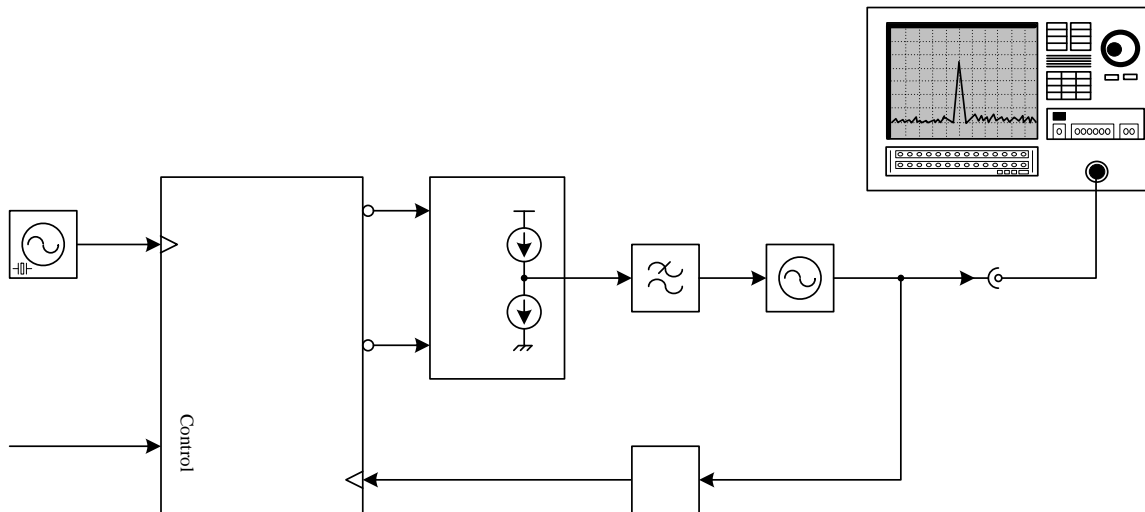


Figure 33: Phase noise test setup

In the PLL configuration it is proposed that a low noise 100 MHz reference crystal oscillator be used. It is also envisaged that the VCO used could have a wide tuning range, implying a high maximum tuning voltage. For this reason a high voltage CP circuit should be constructed as indicated in Figure 33. Details will follow in chapter 5.

### 3.4.3 RF test equipment used

TABLE VI lists the RF test equipment used and their relevant specifications to this dissertation. These are state of the art equipment and were available at Grintek Ewation (Pty) Ltd (GEW).

TABLE VI

RF TEST EQUIPMENT USED

Equipment	Make	Model	Specifications
Signal generator	Rohde & Schwarz (R&S)	SMB 100A	Freq: 9 kHz - 6 GHz
Spectrum analyzer	R&S	FSU8	Freq: 20 Hz - 8 GHz $L(f) \leq -120 \text{ dBc/Hz} @ \Delta f = 10 \text{ kHz}$

## CHAPTER 4: SYSTEM DESIGN

---

### 4.1 BACKGROUND

The goal of this dissertation is to research the possibility of implementing a low noise *low* division ( $N < 40$ ) synthesizer IC in a reasonably low cost 0.35  $\mu\text{m}$  CMOS process with an operating frequency in excess of 2 GHz. A fractional- $N$  topology is also required. By doing this the limitations of CMOS processes can be researched as applicable to high performance synthesizer ICs. The AMS 0.35  $\mu\text{m}$  CMOS C35 process was then selected for the implementation.

As mentioned in chapter 1, one of the biggest design challenges is the high speed low division programmable divider. An initial synchronous divider design was designed with standard 0.35  $\mu\text{m}$  CMOS building blocks and simulated. It proved that the highest clock frequency was about 500 MHz, far less than the 2 GHz required.

The CMOS divider topology was then ported to CML architecture and simulated. The 1.3 GHz result was better, as described in section 4.2.4.3, but still not what was required. It was clear that a dual modulus prescaler of some sort was needed. However a prescaler would impose a lower limit on the divide ratio, so the smallest dual modulus divide ratio,  $2/3$ , was chosen. Simulations with the CML  $2/3$ -prescaler alone showed an upper frequency limit of 2.5 GHz and in the combined pulse-swallow divider architecture an upper limit of 2.3 GHz. The lower boundary of the divide ratio was now limited to only four due to the minimum divide ratios of the prescaler and program counter. All of this promised to be adequate.

To verify the high frequency simulation, the  $2/3$ -prescaler was first prototyped and tested. The measurement results concurred mostly with the simulation results. From this background a synthesizer architecture was devised as shown in Figure 34.

From Figure 34 it is seen that the IC is divided in standard CMOS and then CML subsystems. The CMOS subsystems are used for low frequency functions such as the programming interface, the fractional accumulator, the pulse-swallow control and the CMOS PFD. CML subsystems are used for all the high frequency and critical path blocks. This includes the high frequency CML 6-bit pulse-swallow  $N$ -divider and CML PFD.

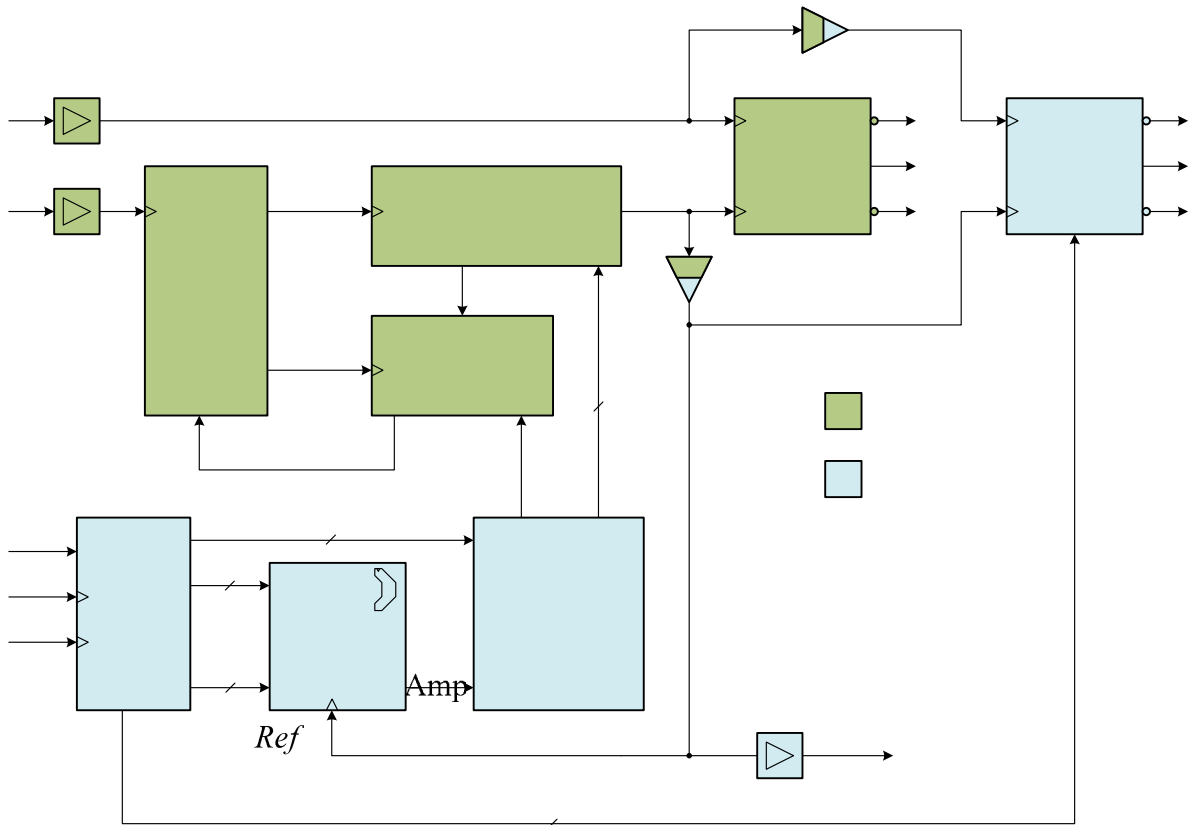


Figure 34. Synthesizer IC block diagram, with CMOS and CML subsystems

A CML-to-CMOS level converter circuit was designed to interface low voltage CML circuits to standard 3.3 V CMOS circuits. The range of the main  $N$ -divider is ( $4 \leq N \leq 33$ ) and the modulus of the fractional accumulator ( $1 \leq M \leq 16$ ). The output of the main  $N$ -divider was buffered and taken to a  $NDIV$  pin for off-chip monitoring. PFD lock detect signals were also routed to output pins. Each CML and CMOS subsystem will now be discussed separately.



## 4.2 CML SUBSYSTEMS

Basic analytical formulas and design guidelines exist for designing CML buffers as described in section 2.5. With stacked CML topologies, such as a D-latch, these formulas become less accurate [39]. These formulas still serve as an initial estimate for component sizes. Fine tuning of the component sizes is done by using transistor-level simulations. These simulations are first done with *typical mean* models for MOSFETs and polyresistors and then with models for worst case process scenarios such as *worst case power* and *worst case speed*. The *worst case speed* scenario is also an indication of what the IC will do in high temperature environments.

### 4.2.1 CML basics

The fundamental necessities in all the CML subsystems used are first discussed.

#### 4.2.1.1 Output voltage swing

From section 2.5.2 and Equation (2.79) it follows that a first estimate for the CML output voltage swing  $\Delta V_{OUT}$  is the nominal MOSFET process threshold voltage,  $V_{TH}$ . From [50] it follows that the average threshold voltage is  $V_{TH} = 0.5$  V with a tolerance of  $\pm 20$  %. Another thing to consider is the pull-up polysilicon resistors used in all the CML circuits, affecting the output voltage. These resistors also have a tolerance of  $\pm 20$  % [50]. The combined effect of these device tolerances makes it difficult to design a CML circuit for all process corners. To accommodate both device tolerances the CML output voltage swing  $\Delta V_{OUT}$  was scaled by +40 % of the nominal threshold voltage  $V_{TH}$  to become  $\Delta V_{OUT} = 0.7$  V.

But section 2.5.2.2 also indicates that  $\Delta V_{OUT}$  will have to be higher than  $V_{TH}$  to accommodate stacked CML topologies to not sacrifice bandwidth. Through fine tuning simulations it was found that  $\Delta V_{OUT} = 0.8$  V proved to be optimum for all process corners, especially for the D-latches and D-flip-flops.

#### 4.2.1.2 Tail current strength

It was decided to accommodate different capacitive loads by categorizing the different CML blocks in terms of their individual tail currents or then drive strengths. Standard tail currents of 500  $\mu$ A, 1 mA, 2 mA and 4 mA were selected for this purpose. This would then also imply a fixed set of polysilicon pull-up resistors to achieve the output voltage swing.

#### 4.2.1.3 Minimum MOSFET gate widths

The minimum CML input voltage swing  $\Delta V_{IN,min} = 0.65$  V was taken as the average between the process threshold voltage  $V_{TH} = 0.5$  V and the chosen output voltage swing  $\Delta V_{OUT} = 0.8$  V. From Equation (2.80) and  $\mu C_{ox} = 170 \mu\text{A}/\text{V}^2$  [50], it follows that for a 2 mA tail current the minimum gate width equals approximately  $W = 20 \mu\text{m}$  and for the other tail currents:  $W(500 \mu\text{A}) = 5 \mu\text{m}$ ,  $W(1 \text{ mA}) = 10 \mu\text{m}$  and  $W(4 \text{ mA}) = 40 \mu\text{m}$ . Many of the CML circuits will however use wider devices for more gain.

#### 4.2.1.4 NMOS current mirror

The current sources used in the CML blocks will be a NMOS transistor programmed by a common bias or reference voltage  $V_B$ . The bias voltage is the gate to source voltage of an existing reference NMOS connected in a diode configuration, so that the current source, in each CML block, mirrors the reference current. The reference current and bias voltage will be set by an off-chip resistor  $R_B$  as in Figure 35. It is assumed that the  $V_{DD}$  rail will be voltage regulated off-chip.

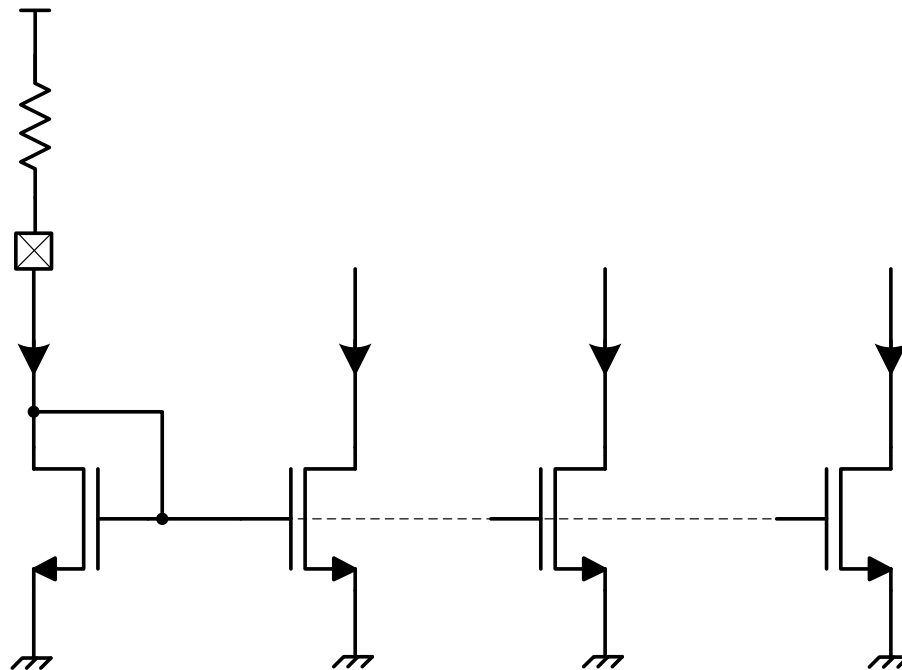


Figure 35. NMOS current mirrors

Reference voltage distribution is the easiest form of replicating currents around a chip but it is very sensitive to ground voltage variations, leading to current modulation in the current

sources [22][43]. A better way might be to distribute individual reference currents to each current source and then locally mirroring the current. This will however introduce much more complexity.

It was then decided to use the reference voltage option and by taking care that the ground connection of each current source is at the same potential. This is done by having large metal areas connecting the different ground sections and by having multiple ground pads on the perimeter of the chip. In the final layout or floor plan of the IC, as depicted in Figure 76, this is clearly visible. Off-chip these ground pads are then connected to the ground plane of the evaluation printed circuit board (PCB). From a RF point of view and of a thermal conductivity point of view this is also a good practise.

### **Current source transistor length $L$**

To reduce the flicker noise in a CML block, the current source must be large as from section 2.5.2. For a current mirror configuration it is also important that the output impedance of the current source be as high as possible. This will reduce current scaling errors when using different sized mirrors. From Equation (2.60) the output impedance  $r_o$  is proportionally dependent on the Early voltage  $V_A$  which in turn is dependent on the channel modulation parameter  $\lambda$ . Equation (4.1) shows the dependence [30]:

$$V_A = \frac{1}{\lambda} = \frac{L}{\lambda'} \quad [\text{V}] \quad (4.1)$$

Where  $\lambda'$  is the process specific channel modulation constant.

Equation (4.1) indicates to increase the Early voltage the MOSFET channel length  $L$  must be increased. It was decided to reduce the channel modulation effect by three fold and hereby arriving at  $L = 3 \times 0.35 \mu\text{m} \approx 1 \mu\text{m}$ . The desired effect was verified by simulating the current mirror.

### Current source transistor width $W$

The minimum gate width  $W$  was determined by the current source requirement for the CML level-shifted clock drivers, as will be seen in section 4.2.2. Here the current source had to have a high compliance by working with quite a low drain voltage.

From Figure 35, the current reference transistor M1 is in a MOS-diode connection, which implies that the drain-source voltage, or MOS diode voltage, is given by:

$$V_{MOSDIODE} = V_B = V_{DS} = V_{GS} \quad [\text{V}] \quad (4.2)$$

M1 also operates in saturation mode so the drain current  $I_D$  has the standard square voltage relationship as in Equation (2.62). By rearranging Equation (2.62) the MOS diode voltage can be calculated by Equation (4.3):

$$V_{MOSDIODE} = V_{TH} + \sqrt{\frac{I_D}{\frac{1}{2} \mu C_{ox} \frac{W}{L}}} \quad [\text{V}] \quad (4.3)$$

The MOS diode voltage is also the absolute minimum drain voltage at which the current mirror can operate, to keep the transistor operating point in saturation. It is thus essential to have a low minimum voltage here, to accommodate stacked CML topologies and CML level shifting clock drivers. With a hypothetically large  $W/L$  ratio the absolute lower limit will be the process threshold voltage  $V_{TH}$ . TABLE VIII list MOS diode voltages for a 1 mA drain current and some  $W/L$  ratios; all calculated by Equation (4.3) and  $\mu C_{ox} = 170 \mu\text{A}/\text{V}^2$  and  $V_{TH} = 0.5 \text{ V}$

TABLE VII  
MOS DIODE VOLTAGES

$W/L$	$I_D$ (mA)	MOS diode voltage (V)
10	1	1.58
20	1	1.27
40	1	1.04
80	1	0.88

From TABLE VIII a transistor width of  $W = 80 \mu\text{m}$  was selected for a 1 mA current source. This provided a reasonable low drain voltage operation (0.88 V) and a large transistor area for low flicker noise considerations. Hence the transistor widths for the other standard tail current sources were:  $W(500 \mu\text{A}) = 40 \mu\text{m}$ ,  $W(2 \text{ mA}) = 160 \mu\text{m}$  and  $W(4 \text{ mA}) = 320 \mu\text{m}$ .

### External bias resistor $R_B$

In the current mirror an accurate external bias resistor was chosen over an internal polysilicon resistor due to the high polysilicon resistive tolerances  $\pm 20\%$  [50]. These tolerances would adversely affect the accuracy of the reference current. From Figure 35 the off-chip bias resistor  $R_B$  can be calculated, for a required reference current  $I_{REF}$  and MOS diode voltage, by:

$$R_B = \frac{V_{DD} - V_{MOSDIODE}}{I_{REF}} \quad [\Omega] \quad (4.4)$$

For a 1 mA reference current and  $V_{MOSDIODE} = 0.88\text{ V}$  the external bias resistor  $R_B$  is calculated from Equation (4.4) as  $R_B = 2.4\text{ k}\Omega$  and rounded to the nearest Electronic Industries Association (EIA) E12 series value:  $R_B = 2.2\text{ k}\Omega$ . This ensured off the shelf availability.

#### 4.2.1.5 Polysilicon resistors

Polysilicon resistors are used for all the pull-up resistors in the CML blocks. The polysilicon has a maximum current density rating so the implemented resistor must be wide enough for the required tail current. As mentioned before the resistivity specification also has a  $\pm 20\%$  tolerance [50]. In all the designs a 50-80% margin has been left on the current density  $J$  specification, to allow for increased current scenarios and for rounded calculated resistor widths.

As an example, a  $400\ \Omega$  2 mA resistor is designed. From [50] it follows that  $J_{POLY2} = 0.3\text{ mA}/\mu\text{m}$  and  $R_{POLY2} = 50\ \Omega/\mu\text{m}^2$ . For a rounded width a 66% margin is chosen for  $J_{POLY2}$ . The resistor width is calculated as:

$$W = \frac{I}{J_{POLY2} \times \text{margin}} = \frac{2 \times 10^{-3}}{0.3 \times 10^{-3} \times 0.66} \approx 10\ \mu\text{m}$$

and the length :

$$L = \frac{W \times R}{R_{POLY2}} = \frac{10 \times 400}{50} = 80\ \mu\text{m}$$

To compact the layout, the resistor is laid out in a serpentine form as shown in Figure 36.

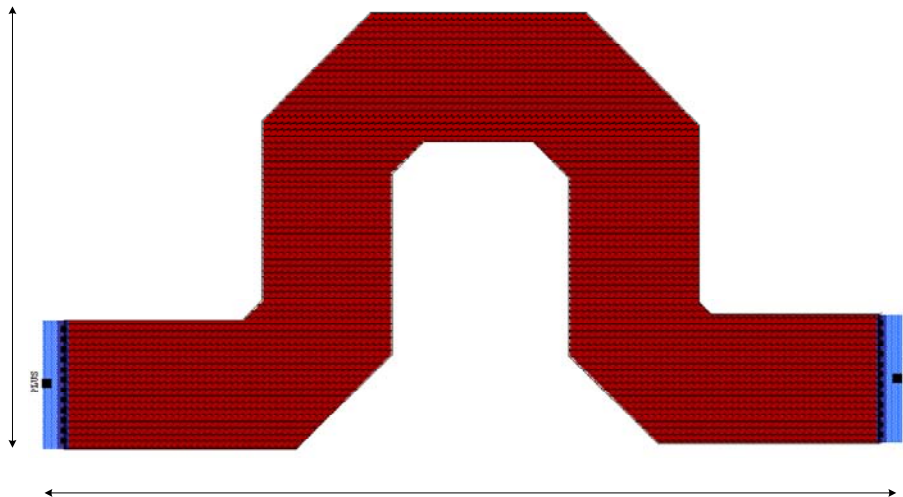


Figure 36. 400  $\Omega$  polyresistor layout  
35  $\mu\text{m}$

#### 4.2.1.6 Fingered MOSFET and guard rings

With large MOSFETs, a technique exists to reduce the resistance of poly gates and to reduce the individual capacitances of the drain and source terminals. This is done by breaking up the gate in smaller shorter sections and then connecting them as fingers. This will then improve the high frequency performance of the MOSFET. A similar layout as suggested by [44] is shown in Figure 37. Here a 40  $\mu\text{m}$  wide NMOS FET was broken up in 8 x 5  $\mu\text{m}$  fingers.

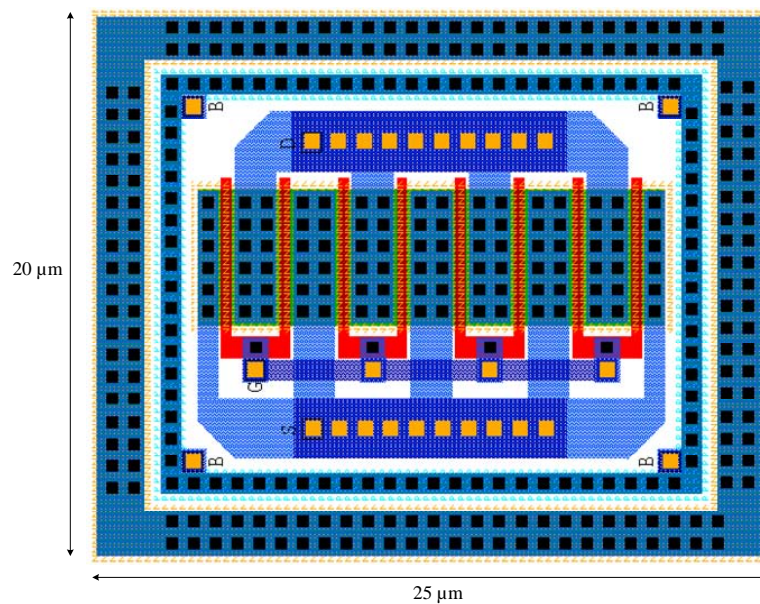


Figure 37. Fingered 40  $\mu\text{m}$  NMOS FET layout

Also visible from Figure 37 are guard rings. These are metal rings connected with vias to  $P+$  or  $N+$  diffusions. They are necessary to shield the MOSFET from substrate noise or minority carriers, all possibly injected by other devices into the substrate. Minority carriers can cause the transistor to enter a latch-up state. To be safe two guard rings are used. The outer ring is a  $N+$  diffusion connected to  $V_{DD}$  and the inner ring a  $P+$  diffusion connected to ground. The inner ring also serves as the bulk or substrate connection for the MOSFET.

#### 4.2.1.7 NMOS decoupling capacitors

It is necessary to decouple the individual  $V_{DD}$  power supply lines of each block from one another, for reducing noise and interference. This is also important for the reference voltage of the current sources. The decoupling is then done by NMOS capacitors. The reason for using NMOS capacitors is that for any CMOS process used, the highest density capacitor can be constructed by connecting the drain and source terminals of a NMOSFET together as the negative electrode and then using the gate connection as the positive electrode. Figure 38 shows an example of a 1 pF NMOS capacitor:

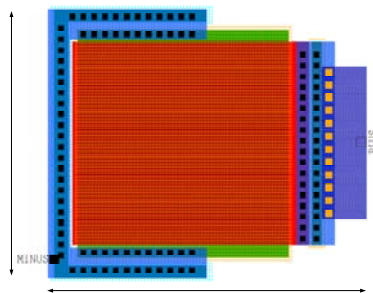


Figure 38. 1 pF NMOS capacitor

The gate oxide diffusion capacitance for the AMS C35 process is  $C_{ox} = 4.54 \text{ fF}/\mu\text{m}^2$  [50]. For a 1 pF capacitance it is then required that the gate area should approximately be  $220 \mu\text{m}^2 \approx 15 \mu\text{m} \times 15 \mu\text{m}$ . Figure 39 shows the symbol used in this dissertation for a NMOS capacitor.

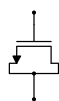


Figure 39. NMOS capacitor symbol

### 4.2.2 CML CLK driver

It was seen from the work of [45][46][47] that the bandwidth or speed of a CML DFF could be increased if the common mode voltage  $V_{CM}$  of the clock signal was optimised. This implied level shifting the clock signal downwards. Practically this resulted in smaller differential clock transistors inside a CML D-latch. The speed improvement was thus partly due to less gate capacitance. It was also seen that the output slew rate increased. The level shifting was done as in Figure 40 by adding a common mode load resistor to a CML buffer.

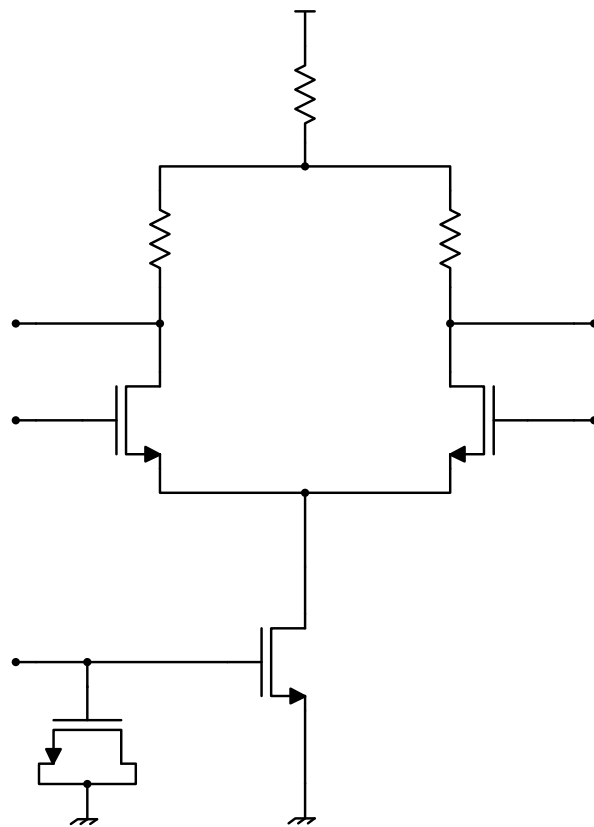


Figure 40. CML level shifting DFF CLK driver

From simulations it proved that an additional 360 – 400 mV clock offset does improve the speed of existing CML DFFs. A 180  $\Omega$  poly resistor was used for the common mode load. All CML DFF circuits were then equipped with this level shifting clock driver. As mentioned earlier, this approach does put more strain on the low drain voltage compliance of the tail current source.



### 4.2.3 CML 2/3-prescaler

As stated earlier a 2/3-prescaler was required for the front-end of the main divider. This prescaler should then be able to operate with an input frequency in the excess of 2 GHz.

#### 4.2.3.1 Logic design

Any prescaler can be designed by first creating a count state table and then converting it to a truth table by adding modulus control signal(s) and inserting dummy states to simplify the combinational logic. The idea is to use minimal combinational logic to reduce propagation delays. TABLE VIII then shows the count table for the 2/3-prescaler as required in this design. The greyed entries are when the counter resets.

TABLE VIII

2/3-PRESCALER COUNT TABLE

	÷3		÷2	
CLK Count	Q1	Q0	Q1	Q0
0	0	0	0	0
1	0	1	0	1
2	1	0	0	0
3	0	0	0	1

From the count table, the next state truth table can be constructed as in TABLE IX for the 2/3-prescaler. The greyed entries indicate the chosen dummy or don't care states, which will never occur. These dummy states were chosen to simplify the resulting combinational logic. The modulus control signal of  $MC=0$  were chosen for the ÷2 operation and  $MC=1$  for the ÷3 operation.

TABLE IX

2/3-PRESCALER TRUTH TABLE

÷3				÷2					
	Present		Next			Present		Next	
MC	Q1	Q0	Q1	Q0	MC	Q1	Q0	Q1	Q0
1	0	0	0	1	0	0	0	0	1
1	0	1	1	0	0	0	1	0	0
1	1	0	0	0	0	1	0	0	0
1	1	1	1	0	0	1	1	0	0

The state variable equations can now be derived from TABLE IX.

From TABLE IX the Boolean equations for the ÷3 section are:

$$Q0_{P=3} = MC \cdot \overline{Q1} \cdot \overline{Q0} \quad (4.5)$$

$$\begin{aligned} Q1_{P=3} &= MC \cdot \overline{Q1} \cdot Q0 + MC \cdot Q1 \cdot Q0 \\ &= MC \cdot Q0 \end{aligned} \quad (4.6)$$

Similarly, for the ÷2 section:

$$Q0_{P=2} = \overline{MC} \cdot \overline{Q1} \cdot \overline{Q0} \quad (4.7)$$

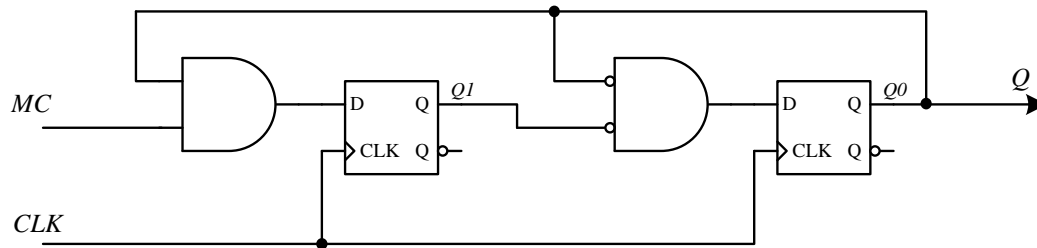
$$Q1_{P=2} = 0 \quad (4.8)$$

The final state variable equations are then the combination of the ÷2 and ÷3 equations:

$$\begin{aligned} Q0 &= Q0_{P=3} + Q0_{P=2} \\ &= MC \cdot \overline{Q1} \cdot \overline{Q0} + \overline{MC} \cdot \overline{Q1} \cdot \overline{Q0} \\ &= \overline{Q1} \cdot \overline{Q0} \end{aligned} \quad (4.9)$$

$$\begin{aligned} Q1 &= Q1_{P=3} + Q1_{P=2} \\ &= MC \cdot Q0 + 0 \\ &= MC \cdot Q0 \end{aligned} \quad (4.10)$$

The logic diagram for these state equations is shown in Figure 41.



$MC=0, P=2$

$MC=1, P=3$

Figure 41. General 2/3-prescaler logic diagram



Figure 43 shows the layout for the CML AND-D-latch and also visible are some dummy metal and poly structures to fill unused area. This is required to achieve minimum metal and poly density specifications as required by the specific process.

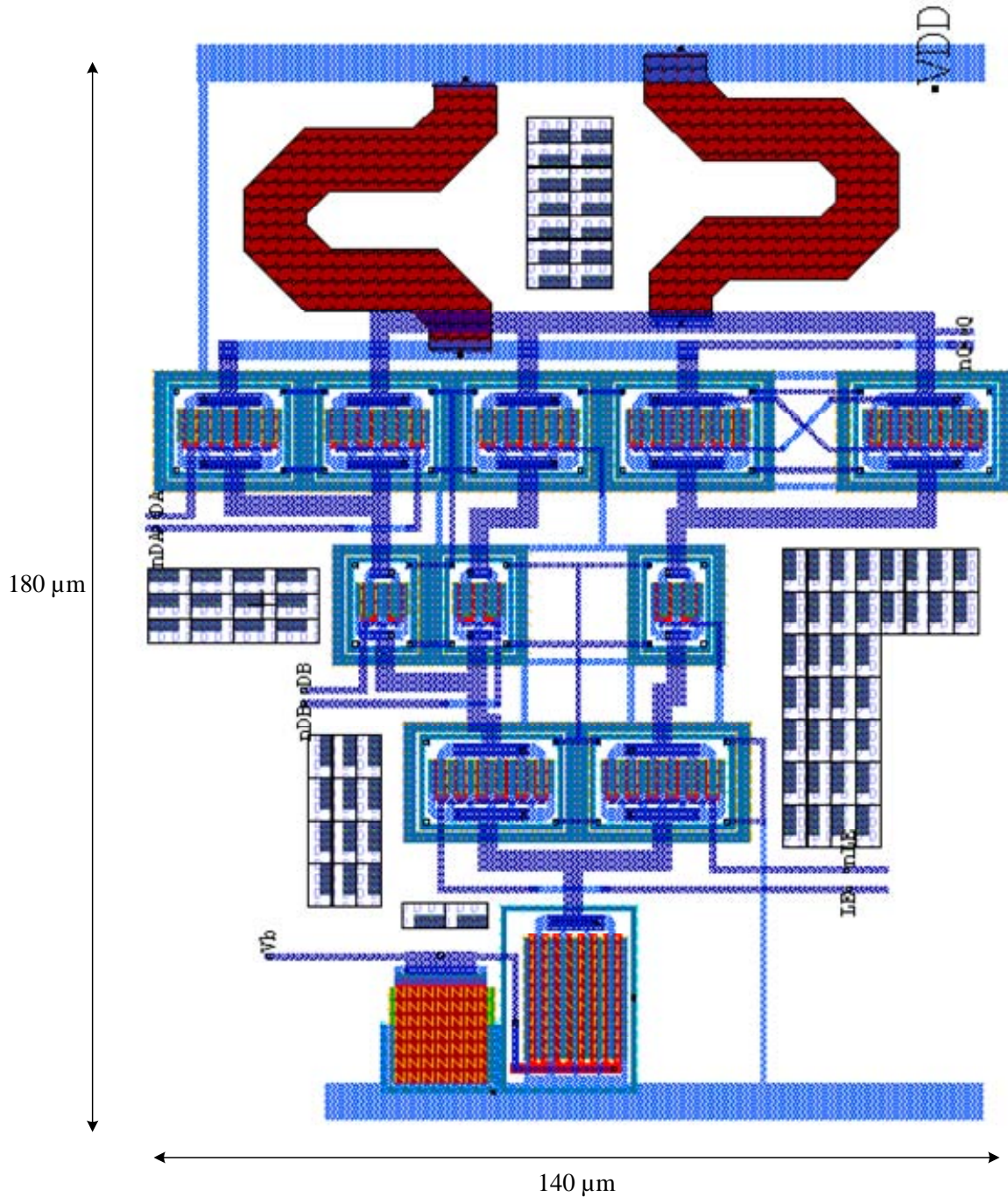


Figure 43. CML AND-D-latch layout

#### 4.2.3.3 Prescaler start-up meta-stability

In the  $2/3$ -prescaler, signals are fed from the two DFF outputs to the inputs, via the AND gates. During start-up the differential DFF outputs are at equilibrium, thus the differential output voltage is zero. This meta-stability state will not continue indefinitely but will correct itself after a while due to the gain present in the DFFs. This can be speeded up by purposely offsetting the pull-up resistor values from one another in the master D-Latch to create an initial voltage difference during start-up. In Figure 42 the nominal pull-up resistor value was  $450 \Omega$ , so a 1 % or  $5 \Omega$  offset was chosen and the resulting values were  $445 \Omega$  and  $455 \Omega$ . This resulted in the  $2/3$ -prescaler being operational within five clock cycles, which assisted for simulation process.

#### 4.2.3.4 Prescaler implementation

For the CML  $2/3$ -prescaler to be fully functional it was necessary to include the previously mentioned level shifters on the DFF clocks and an output buffer to provide enough drive strength for the next stage, as depicted in Figure 44. In chapter 5 simulations were done for the whole 6-bit pulse-swallow divider including the  $2/3$ -prescaler, over all process corners. It was then seen in one of the worst case process scenarios that the modulus control  $MC$  input signal was captured too late. This resulted in a lower maximum frequency. To remedy this, an additional D-latch synchronizing circuit was added to the  $MC$  signal as is visible in Figure 44.

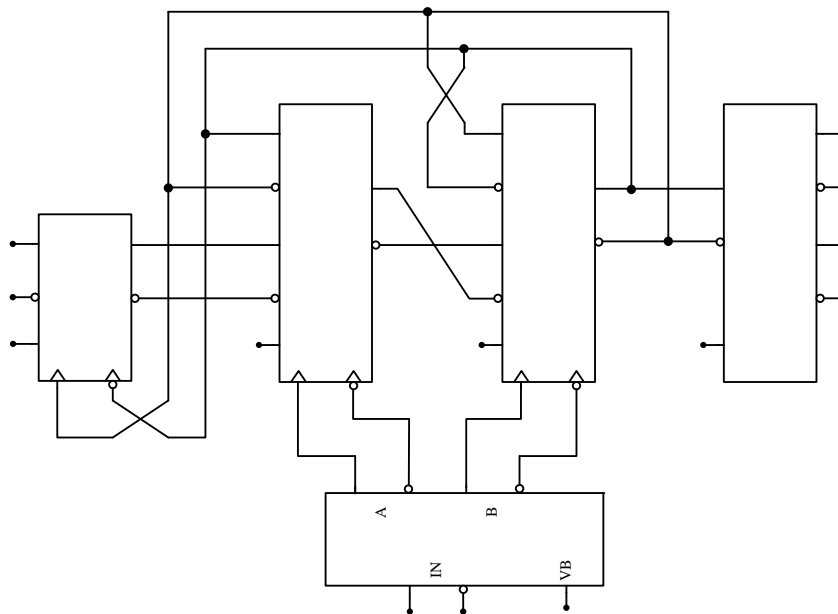


Figure 44. CML  $2/3$ -prescaler implementation

The final layout of the CML 2/3-prescaler is shown in Figure 45 with some sub circuits such as the VCO input amplifier and output buffer outlined.

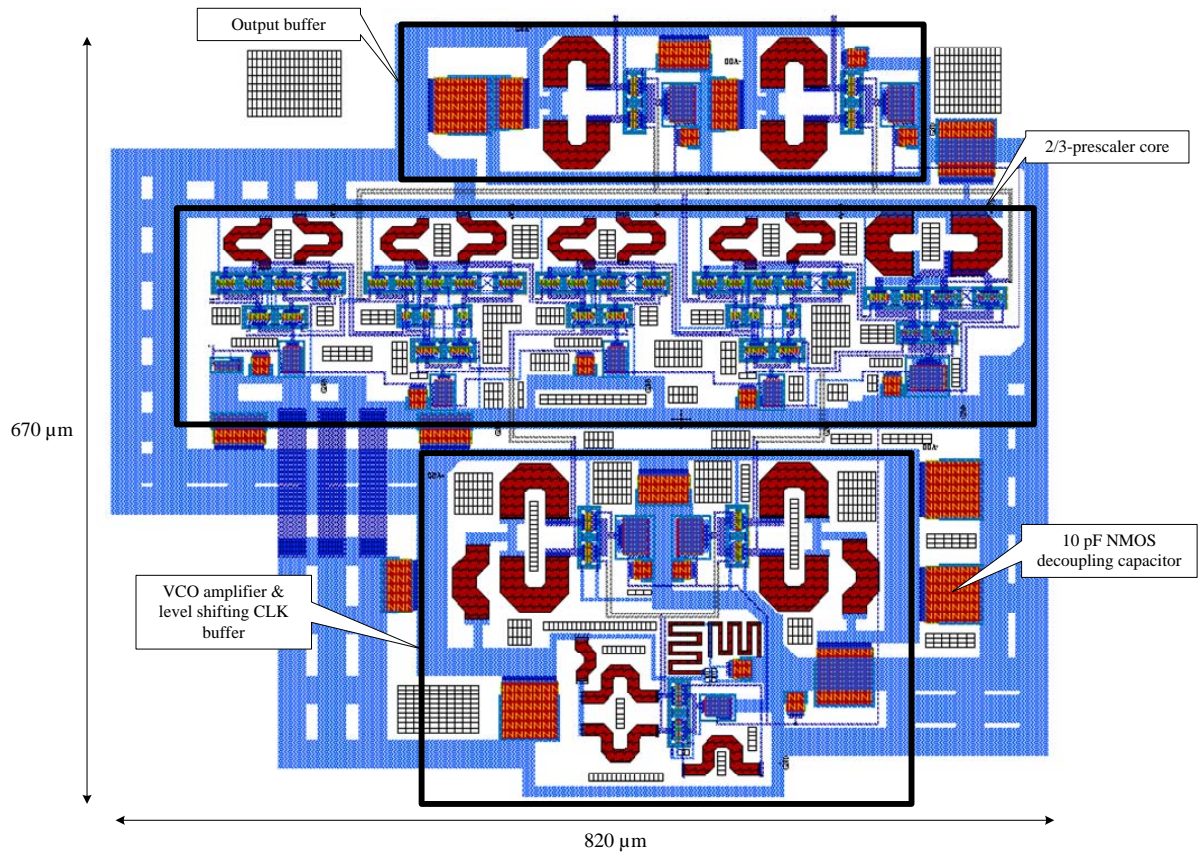


Figure 45. CML 2/3-prescaler layout

The VCO amplifier is similar to the reference clock amplifier as will be discussed in section 4.2.5. Visible also are 10 pF NMOS capacitors used for power supply decoupling between the +3.3 V rail and ground.

#### 4.2.3.5 Prescaler simulation

The CML 2/3-prescaler was proven operational by worst case process simulations with clock frequencies of 50 MHz - 2.5 GHz and  $MC = 1$  or a  $\div 3$  scenario. These included the effects of the level shifting clock drivers and general output buffers. Figure 46 shows the simulation setup and Figure 47 the resulting output waveform for a 2.5 GHz input frequency.

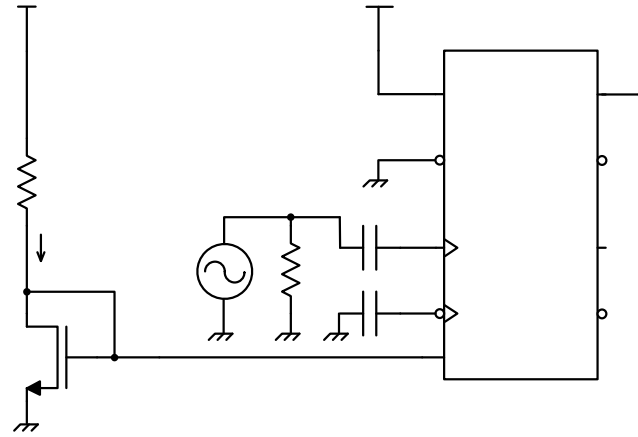


Figure 46. CML 2/3-prescaler simulation test protocol  $V_{DD}$

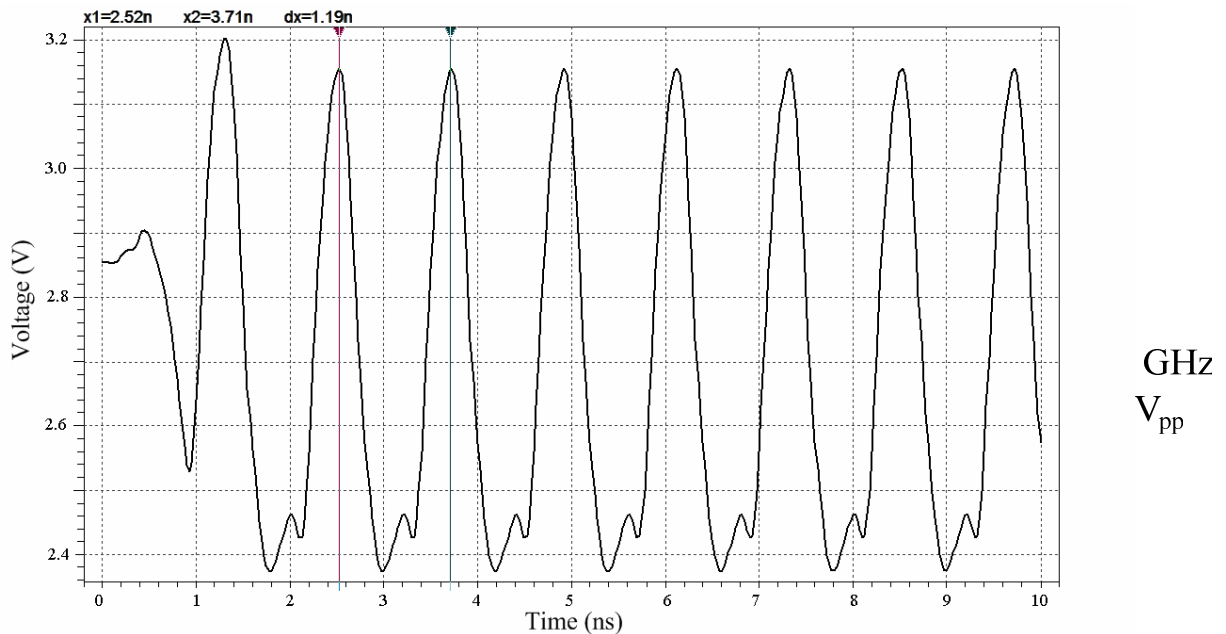


Figure 47. CML 2/3-prescaler simulation

The 1.2 ns period of the output waveform is clearly visible. The 2/3-prescaler was also prototyped on its own and results follow in chapter 5.

### 4.2.4 CML 4-bit counter

The 4-bit CML counter is the heart of the programmable low division frequency divider. The requirements are that the counter must be able to operate in excess of 1 GHz and be able to count down from a maximum of 15 to a minimum of 0. A very important requirement is that the counter should only load new counter values at the end of every count cycle. The counter should be prohibited to load new values during a count cycle. This is important for the fractional- $N$  implementation as the digital accumulator, controlling the effective  $N$ -divider value, may take a while to settle and initially corrupt the next required count value. For integer- $N$  architectures, this requirement is not necessary. The counter is then implemented as a synchronous down counter.

#### 4.2.4.1 LUT synchronous counter

It was decided, due to the many cascaded or chained AND and XOR gates in the conventional synchronous TFF counter implementation as in Figure 7, section 2.1.3.2, a faster topology could be designed by using look up tables (LUTs), for the state variables. Figure 48 depicts the logic diagram of the LUT based synchronous counter, implemented in this dissertation. The  $LOAD$  signal is also synchronized before using it as the divider output.

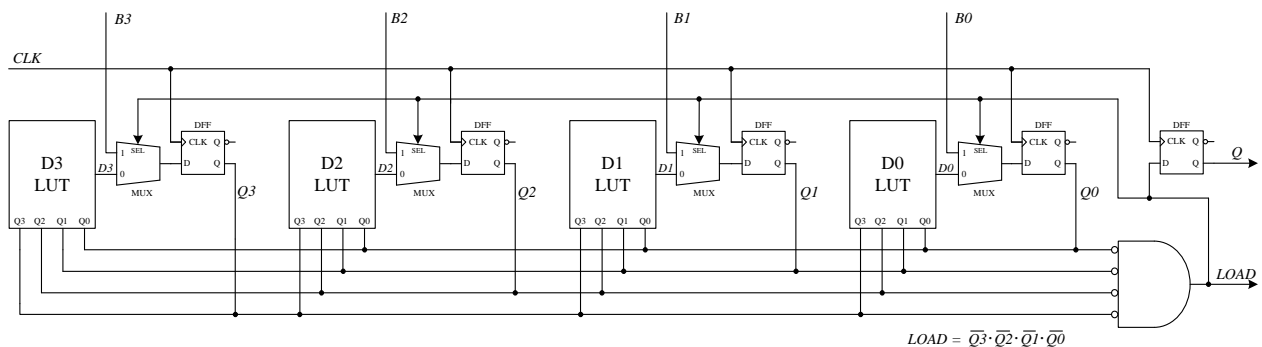


Figure 48. Synchronous LUT 4-bit counter

The LUT for each state variable  $Q3$ - $Q0$  was done by extracting the individual next state columns in the truth table shown in TABLE X. The LUTs were then implemented as four CML 16-1 multiplexers.



TABLE X

4-BIT COUNTER TRUTH TABLE

Count	Present state				Next state				LOAD
	Q3	Q2	Q1	Q0	Q3	Q2	Q1	Q0	
15	1	1	1	1	1	1	1	0	0
14	1	1	1	0	1	1	0	1	0
13	1	1	0	1	1	1	0	0	0
12	1	1	0	0	1	0	1	1	0
11	1	0	1	1	1	0	1	0	0
10	1	0	1	0	1	0	0	1	0
9	1	0	0	1	1	0	0	0	0
8	1	0	0	0	0	1	1	1	0
7	0	1	1	1	0	1	1	0	0
6	0	1	1	0	0	1	0	1	0
5	0	1	0	1	0	1	0	0	0
4	0	1	0	0	0	0	1	1	0
3	0	0	1	1	0	0	1	0	0
2	0	0	1	0	0	0	0	1	0
1	0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0	0	1

#### 4.2.4.2 CML 16-1 multiplexer

A 16-1 CML multiplexer was required for the LUT based synchronous counter. Figure 49 depicts the arrangement of four 4-1 multiplexers to create the 16-1 multiplexer and an instance of how a 4-1 multiplexer was created using three 2-1 multiplexers.

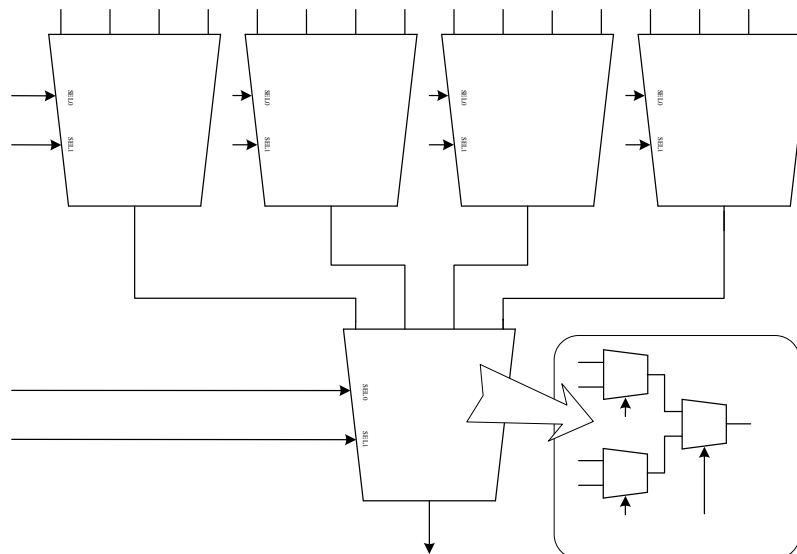


Figure 49. 16-1 multiplexer

Figure 50 shows the layout for a CML 4-1 multiplexer, using three CML 2-1 multiplexers with a circuit implementation as indicated previously in Figure 25.

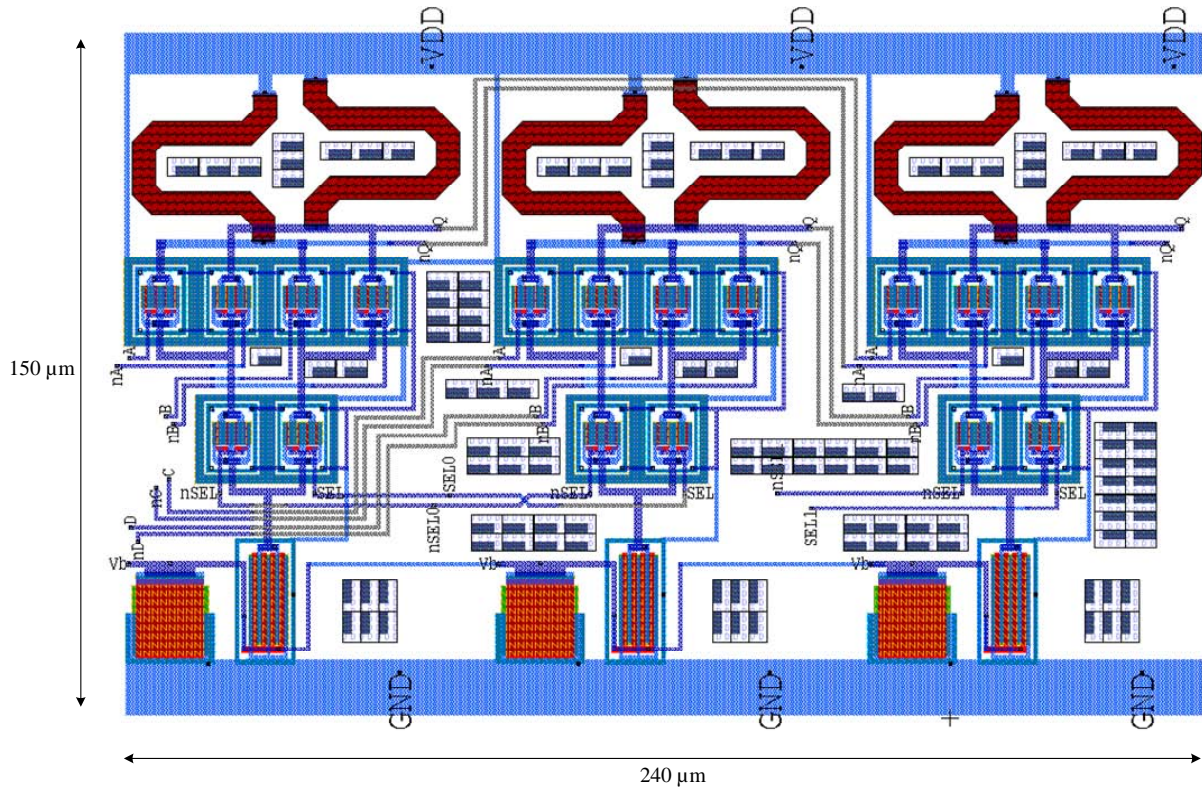


Figure 50. CML 4-1 multiplexer layout

All the switching transistors are  $20\ \mu\text{m}$  wide and each multiplexer has a tail current of 1 mA. The differential pull-up resistors are  $780\ \Omega$  and  $820\ \Omega$  respectively to resolve once again start-up meta-stability problems when the multiplexer is used in conjunction with a DFF, as is the case with the LUT counter implementation.

#### 4.2.4.3 CML 4-bit counter simulation

The complete CML LUT 4-bit counter, including level shifting clock buffers, was proven operational by worst case simulation with a maximum clock frequency of 1.2 GHz. Shown in Figure 51 the simulation setup and in Figure 52 the simulation results for a count scenario of  $B=4$  or in other words a frequency divide by 5 scenario. The 4.17 ns period of the output waveform is clearly visible.

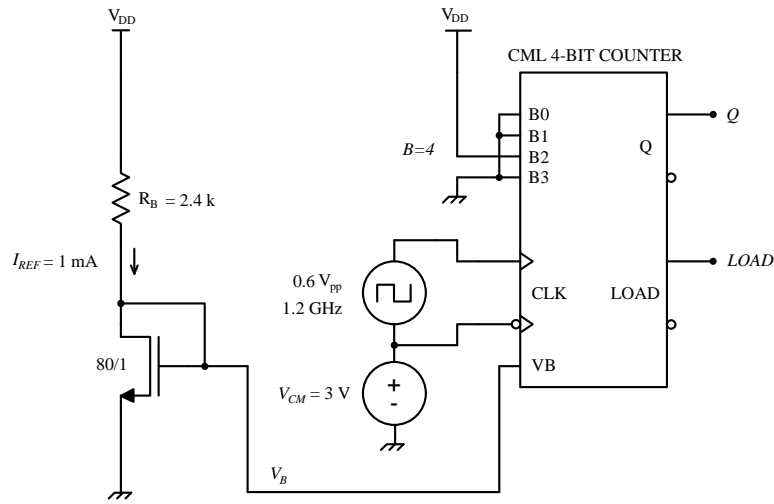


Figure 51. Synchronous CML LUT 4-bit-counter simulation test protocol

Ω

The CML clock input signal is modelled as 0.6 V<sub>pp</sub> square wave with a DC-offset of 3 V.

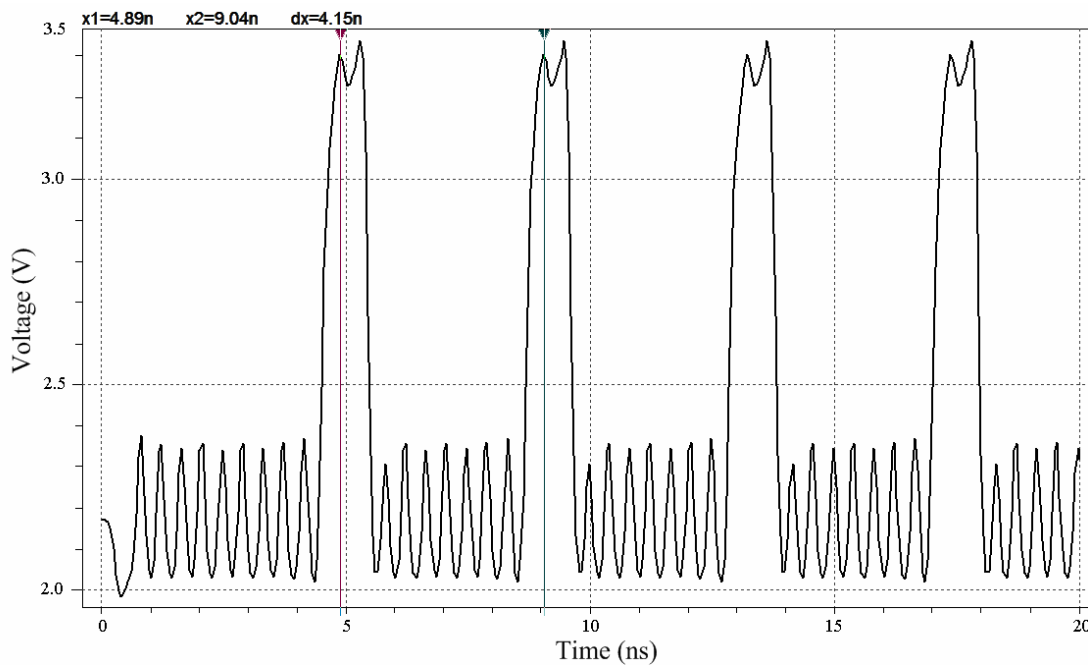


Figure 52. Synchronous CML LUT 4-bit-counter simulation

### 4.2.5 CML reference clock amplifier

For minimum noise to jitter translation, it is required that all signals be square waves. This is predominantly a problem with the low frequency reference clock. A dual high gain amplifier stage, as shown in Figure 53, was designed to convert the reference sinusoidal signal to square waves. It uses four wide 80  $\mu\text{m}$  MOSFETs. In the CML 2/3-prescaler a similar clock amplifier circuit was used as the VCO input amplifier. The major difference was the output buffer being replaced by two level shifting clock drivers.

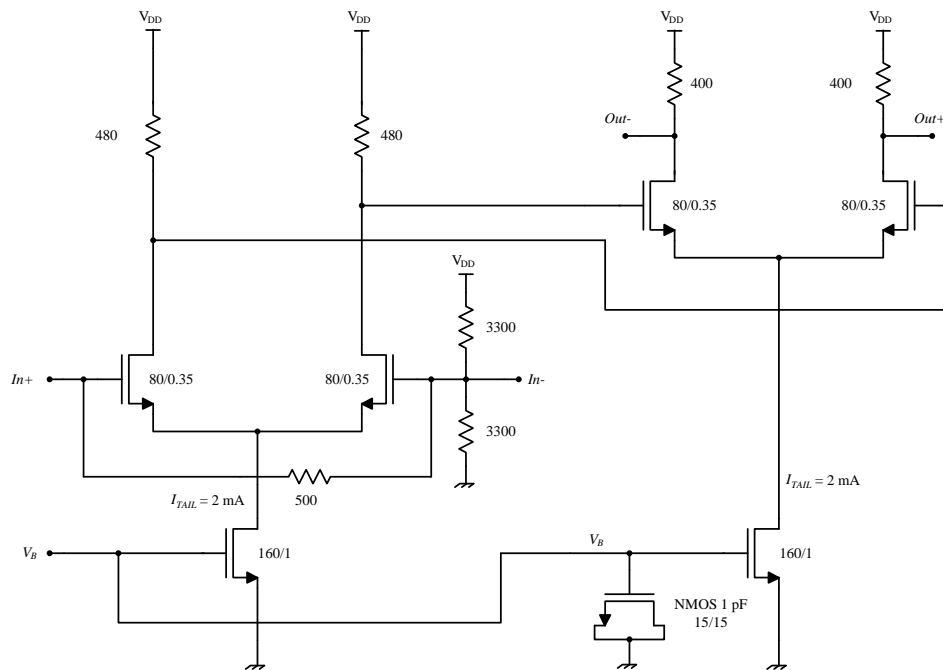


Figure 53. CML reference clock amplifier

From Figure 53, the input signals  $In+$  and  $In-$  are mid  $V_{DD}$  biased by two on-chip 3300  $\Omega$  polyresistors. This will ensure a wide input dynamic range operation. The  $In+$  signal is connected by a 500  $\Omega$  resistor to the  $In-$  signal. This provided both a common DC voltage between the  $In+$  and  $In-$  terminals and a way to fix the differential input impedance to 500  $\Omega$ . It also provided an easy way to verify the on-chip resistor tolerances of a prototyped IC by measuring the resistance of the  $In+$  and  $In-$  terminals. A 500  $\Omega$  input impedance was deemed

adequate as this was a moderate impedance which could easily be off-chip matched to either 200  $\Omega$  or 50  $\Omega$  systems.

To accommodate large input signals, up to +10 dBm in a 50  $\Omega$  system, the 500  $\Omega$  input polyresistor had to be large or wide. A resistor 2 mA RMS current rating was derived from the +10 dBm specification, implying a minimum polyresistor width  $W = 10 \mu\text{m}$ .

#### 4.2.5.1 CML reference clock amplifier simulation

The circuit was simulated with a 150 MHz signal and found to be operational. Figure 54 depicts the simulation setup and Figure 55 the sinusoidal to square wave waveform results.

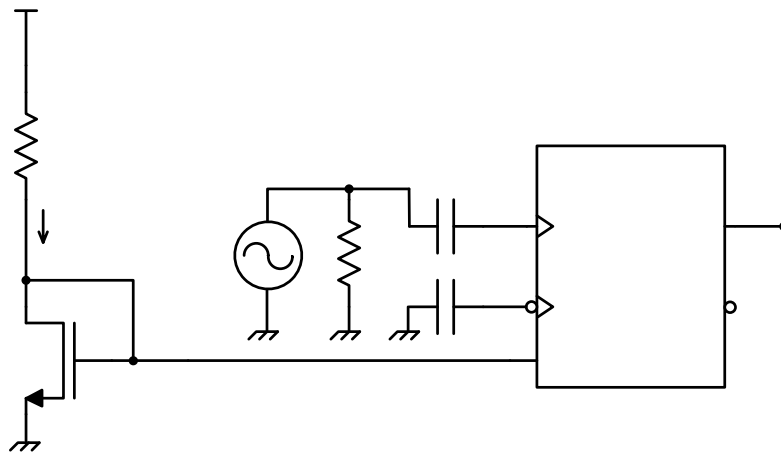


Figure 54. CML reference clock amplifier simulation test protocol

$$V_{DD}$$

$$R_B = 2.4 \text{ k}\Omega$$

$$I_{REF} = 1 \text{ mA}$$

$$150 \text{ MHz}$$

$$0.6 V_{pp}$$

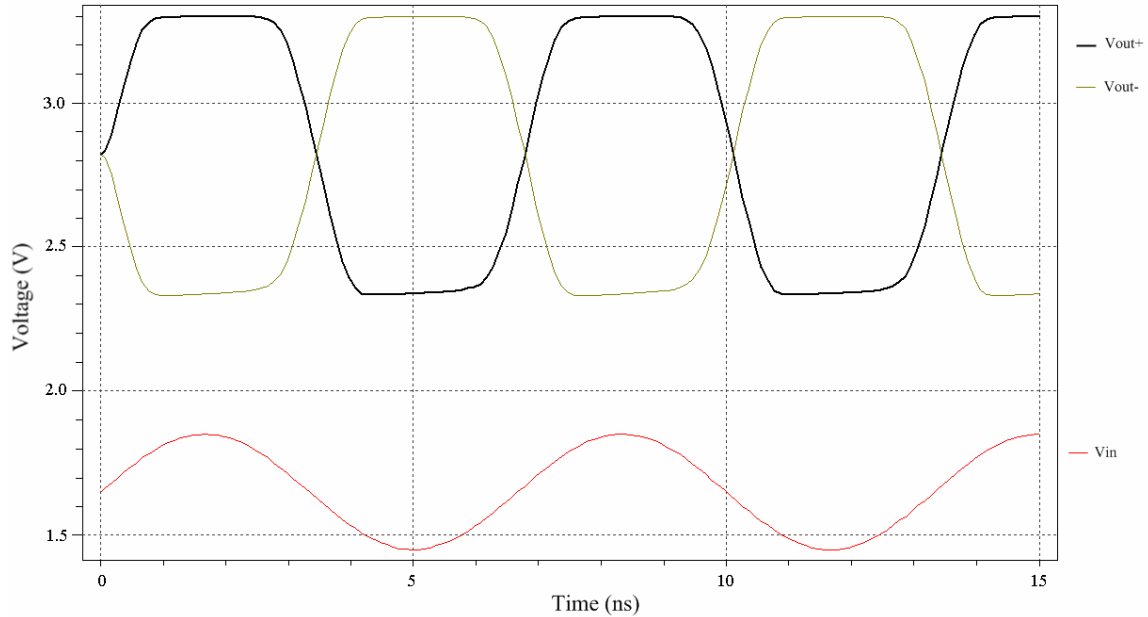


Figure 55. CML reference clock amplifier simulation

#### 4.2.5.2 CML reference clock amplifier layout

The layout used for the reference clock amplifier is shown in Figure 56. Also indicated are the electrostatic discharge (ESD) protection diodes used on the gates of the input MOSFETs. A small ESD diode, with a small capacitance, is used on the  $V+$  terminal as not to reduce the bandwidth of the amplifier. A larger ESD diode is used on the  $V-$  terminal, for it is assumed that off-chip this terminal will carry no RF signal and will be connected to ground by a capacitor, as indicated in Figure 54. Hence no bandwidth reduction should take place.

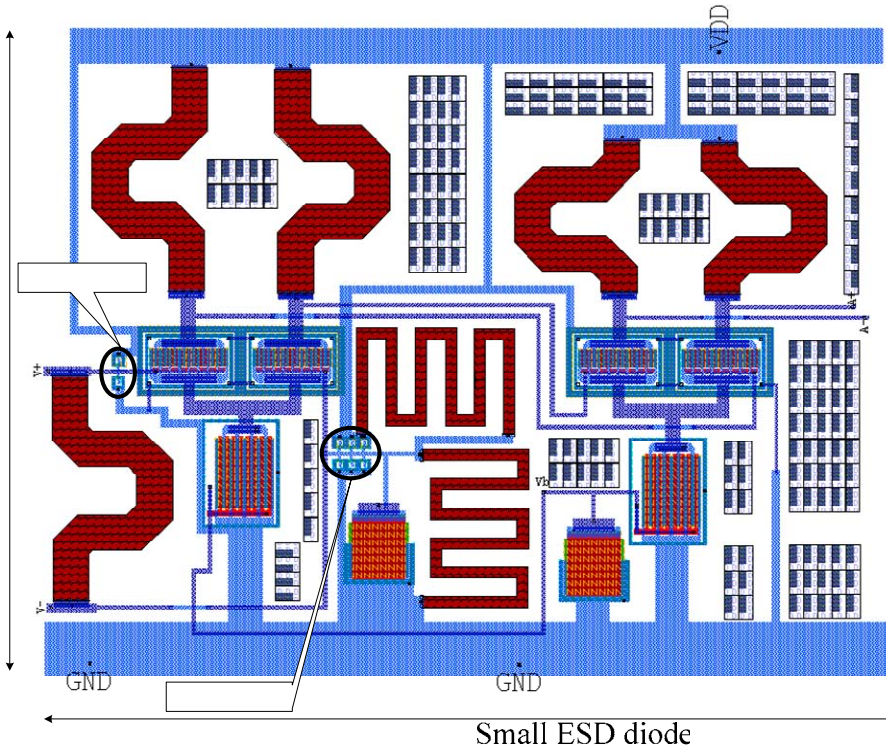


Figure 56. CML reference clock amplifier layout with ESD diodes

The conventional connection for an <sup>185 μm</sup> ESD diode pair is shown in Figure 57 with its associated layout. This ESD diode pair is used everywhere in this dissertation when signals are accepted from external off-chip sources.

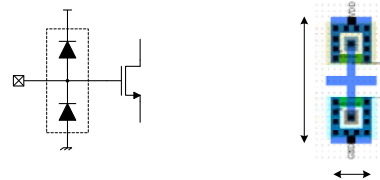


Figure 57. ESD diode protection: (a) Circuit, (b) Layout

#### 4.2.6 CML PFD

The CML PFD employed uses the same block diagram as described in section 2.1.5.1 depicted in Figure 12. The main differences relate to the delay required, particularly to avoid the dead-zone in the PFD. This is generated by inserting buffers at the DFF outputs, and after the AND gate, providing the reset signal for the DFFs. The charge pump is implemented as a 4 mA open drain (OD) buffer. The OD implementation is required for off-chip current mirroring

purposes, as will become clear in chapter 5. Figure 58 then shows the CML PFD implementation used.

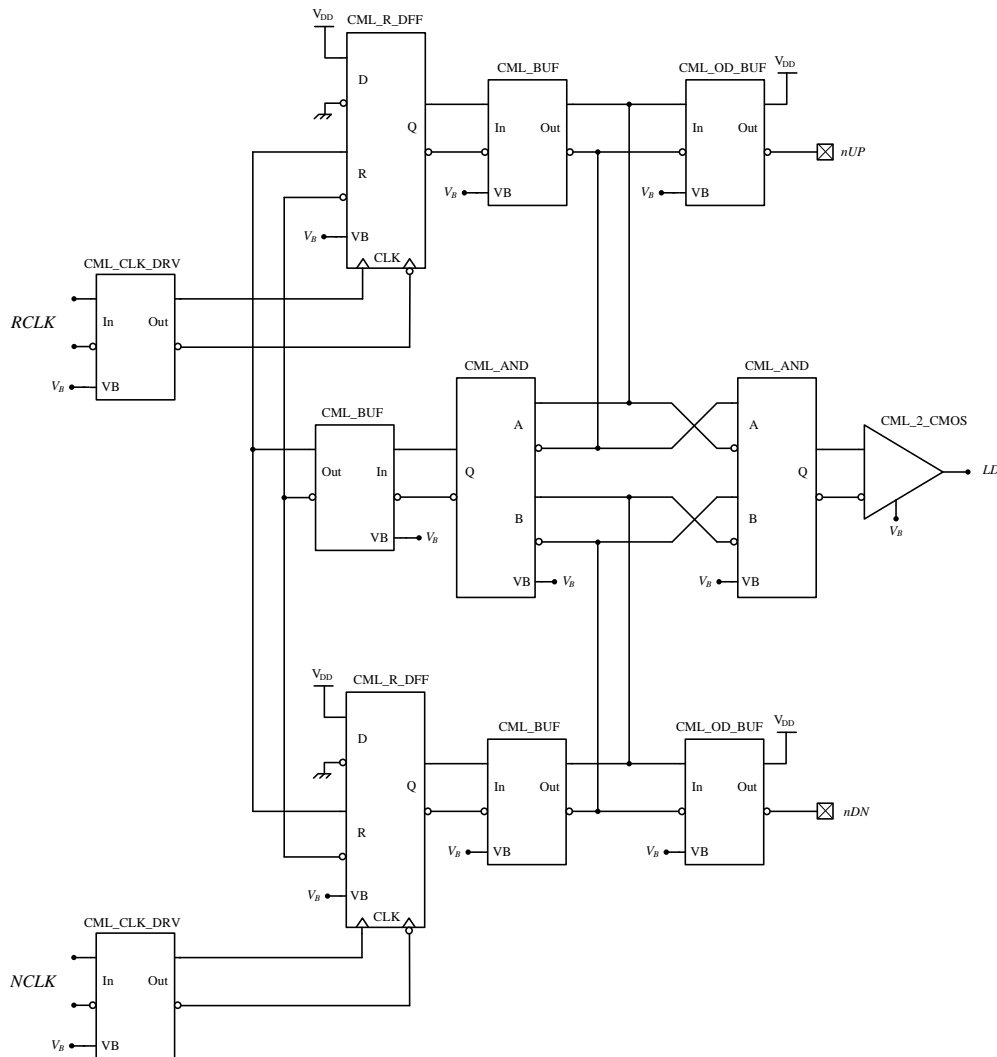


Figure 58. CML PFD implementation

Figure 58 also shows the level shifting clock drivers, on the *RCLK* and *NCLK* signals, required for the D-flip-flops and the generation of the CMOS *LD* signal via a CML-to-CMOS block.

#### 4.2.6.1 OD buffer

The OD buffer implemented in the CML PFD output is depicted in Figure 59. From Figure 58 it is seen that the + output terminals are strapped to  $V_{DD}$  and only the - terminals are used as the *nUP* and *nDN* current outputs. These current outputs will then be mirrored off-chip to complete the PLL charge-pump circuitry.



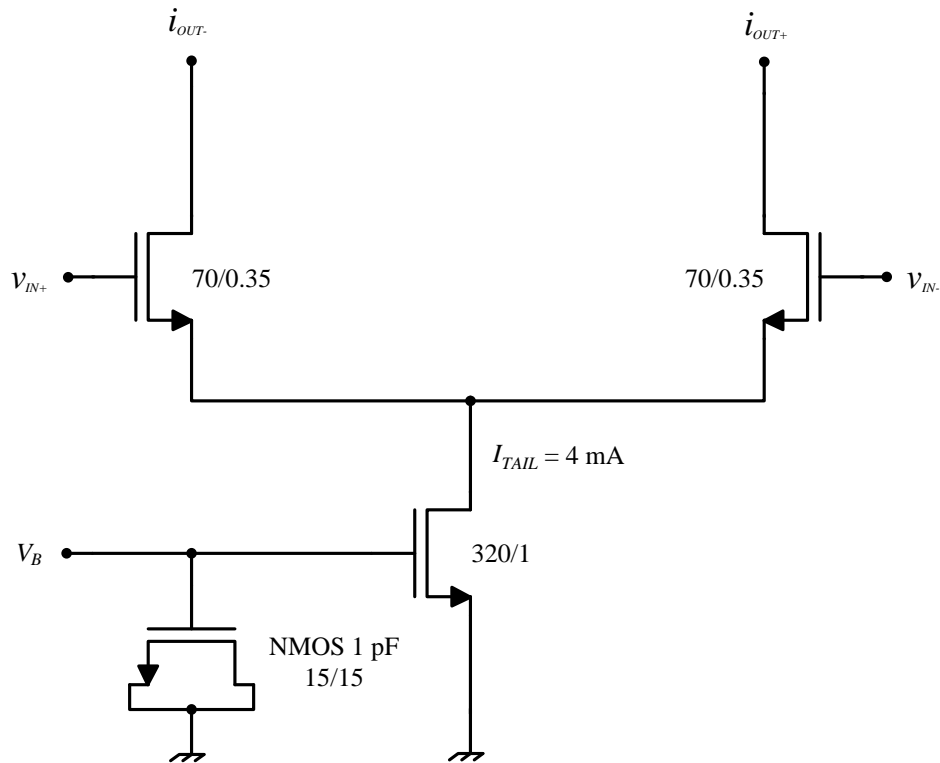


Figure 59. CML OD buffer

#### 4.2.6.2 Resettable CML D-latch

Primary to the CML PFD implementation is the resettable DFF. A resettable DFF is implemented by applying the reset signal to both master and slave D-latch circuits inside the DFF. A resettable D-latch is then constructed as depicted in Figure 60 by applying the reset signal  $R$  to both the tracking and regenerative sections.



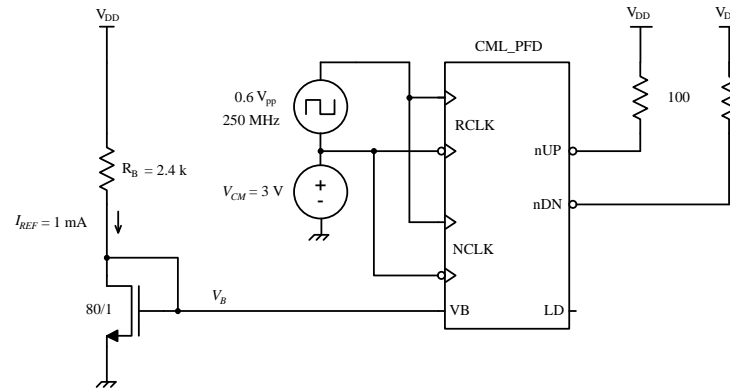


Figure 61. CML PFD simulation test protocol

With this configuration it was possible to observe the PFD's behaviour under a PLL *lock* condition or in other words to examine the minimum reset pulse width possible in the PFD's charge-pump output. The OD outputs were connected with 100  $\Omega$  pull-up resistors to  $V_{DD}$  and then the circuit was simulated. Figure 62 shows the simulation results for the PFD operating at 250 MHz. The reset pulse width was measured in the order of 630 ps and the depth approximately 400 mV, corresponding to 4 mA current pulses in the 100  $\Omega$  pull-up resistors.

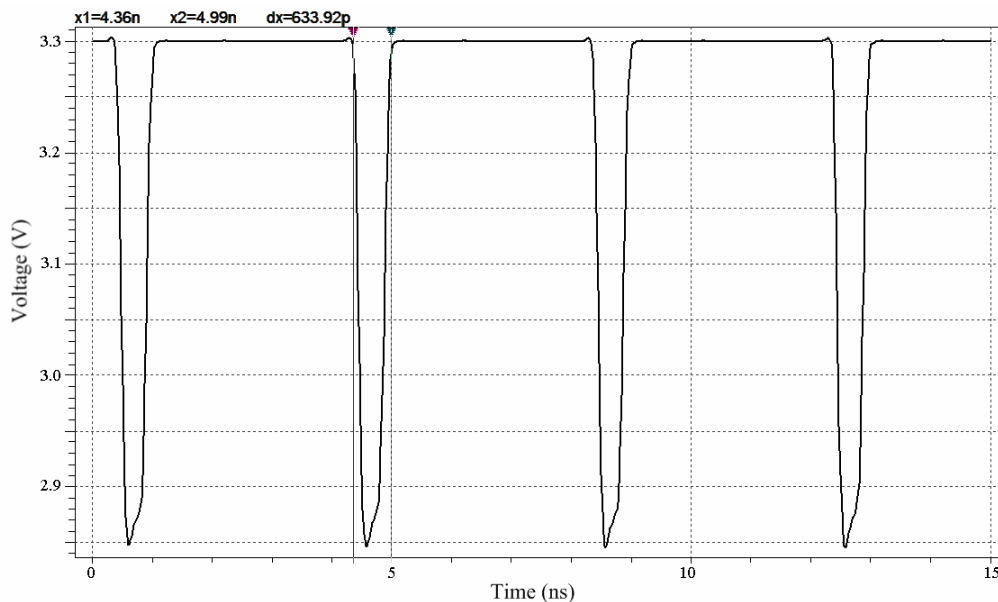


Figure 62. CML PFD simulation

From Equation (2.36) the maximum CML PFD operating frequency can be estimated from the simulation results as approximately 790 MHz.

#### 4.2.7 CML-to-CMOS converter

A CML-to-CMOS converter was needed to interface low voltage CML output signals to CMOS circuitry operating at 3.3 V. The *LD* output from the CML PFD and clock inputs for the CMOS PFD are examples. The approach taken was to use a high gain PMOS cross-coupled-load differential amplifier and then a classic differential to single ended amplifier followed by a high fan-out CMOS inverter as depicted in Figure 63.

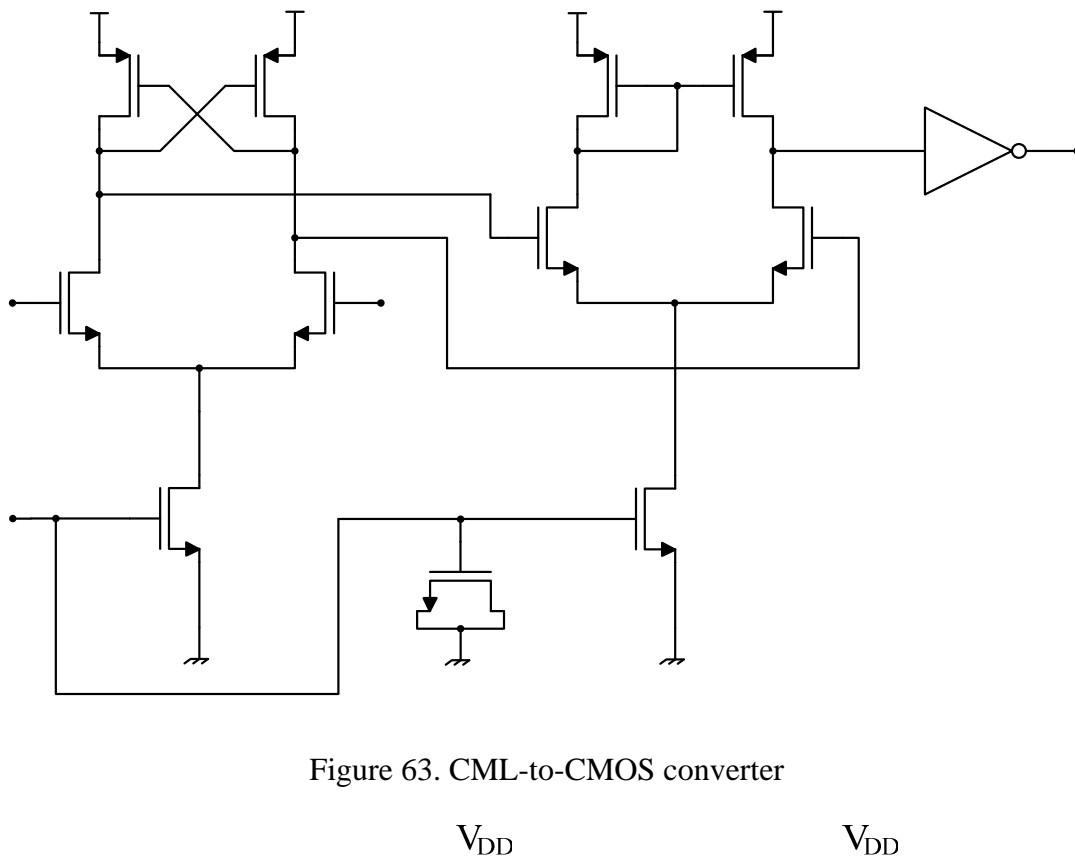


Figure 63. CML-to-CMOS converter

20/0.35

#### 4.2.7.1 CML-to-CMOS converter simulation

Circuit operation was verified by simulation up to 500 MHz with a 0.6 V<sub>pp</sub> CML clock input, as depicted in Figure 64. The high bandwidth was deemed necessary, to minimise jitter, especially for the clock signals feeding the CMOS PFD. The CMOS PFD is discussed in section 4.3.4.

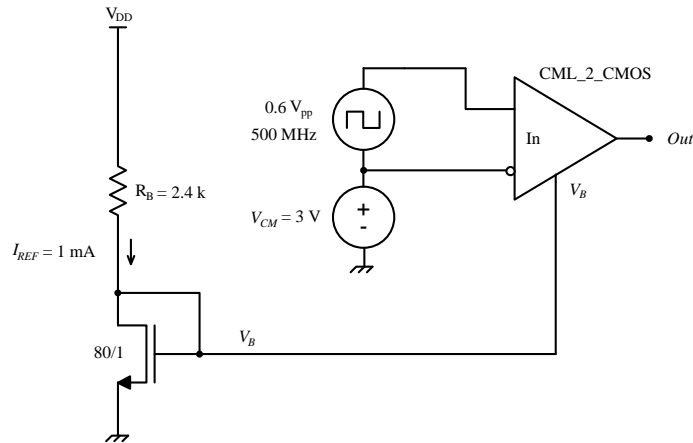


Figure 64. CML-to-CMOS simulation test protocol

Figure 65 shows the simulation results with a 360 ps propagation delay measured.

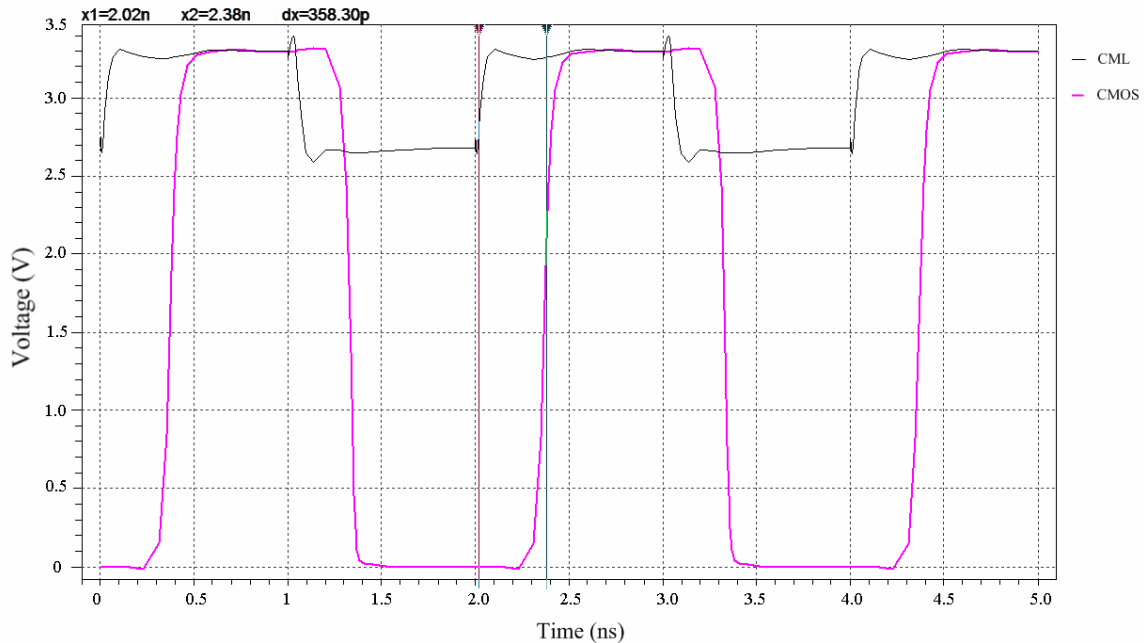


Figure 65. CML to CMOS simulation

### 4.3 CMOS SUBSYSTEMS

All CMOS subsystems were realized by using a combination of standard digital libraries from the AMS C35 process. Some building blocks required for the synthesizer IC were however not standard and had to be designed. These non-standard blocks are now discussed.

#### 4.3.1 Binary adders and subtractors

Binary adders and subtractors are required in the building blocks for the pulse-swallow control and programmable accumulator blocks. Binary adders perform the  $A+B$  math function. The easiest way to construct an adder is to use a standard full adder (FA) block in cascade. A full adder performs the binary addition of two bits and a carry in bit. The output is the sum bit and a carry out bit. The logic diagram for a full adder is depicted in Figure 66.

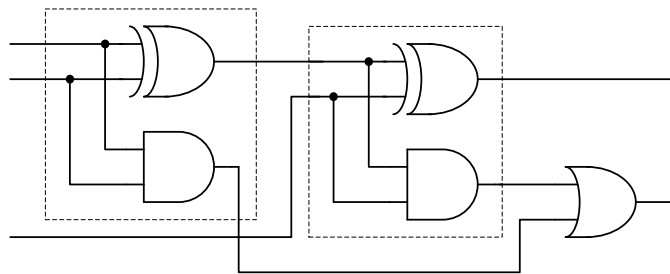


Figure 66. Full adder logic diagram

Full adders are however part of the AMS standard digital libraries and only the multi-bit binary adders need to be constructed. The required binary adder, utilizing cascaded full adders, is known as a ripple carry adder (RCA). Figure 67 depicts a 4-bit adder example with a general adder symbol.

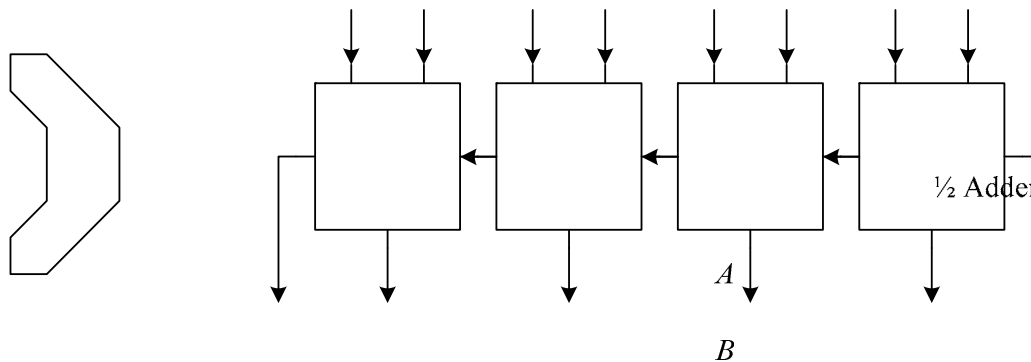


Figure 67. 4-bit binary adder: (a) Symbol, (b) FA implementation

Binary subtractors are also constructed from binary adders. The expression  $B-A$  can be written as  $B + (-A) = B + (2' \text{ complement of } A)$ . The  $2'$  complement of  $A$  is obtained by inverting  $A$  and adding a "1". The "1" is normally added to the adder's carry input port. Figure 68 depicts a typical 4-bit subtractor and a general subtractor symbol.

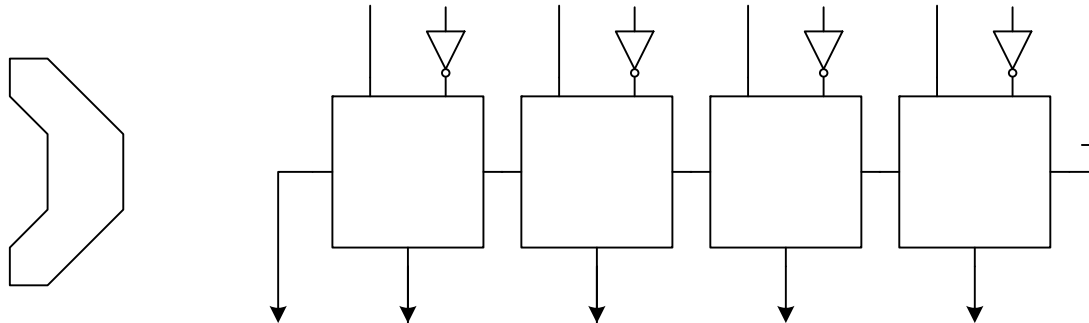


Figure 68. 4-bit binary subtractor: (a) Symbol, (b) FA implementation

$B3 \quad A3$

### 4.3.2 Pulse-swallow control logic

In this dissertation a pulse-swallow divider structure is used, therefore the  $A$  and  $B$ -counter values need to be calculated for every  $N$  value. The prescaler used in the synthesizer IC is a  $2/3$ -prescaler, which in turn defines the values of the  $A$  and  $B$ -counters. From section 2.1.3 and Equation (2.30) the  $A$  and  $B$ -counters are calculated as follows:

$$B-A \quad \text{CO} \quad \text{FA} \quad \text{CI} \quad \text{CO}$$

$$N = PB + A \quad (P = 2) \quad (4.11)$$

$$A \quad \therefore B = \left\lfloor \frac{N}{P} \right\rfloor = \left\lfloor \frac{N}{2} \right\rfloor \quad \text{Sum} \quad (4.12)$$

(where  $\lfloor x \rfloor$  denotes the integer part of  $x$ )

$$\therefore A = N - PB \quad \text{Carry} \quad S3 \quad (4.13)$$

(the remainder of the division)

(a)

In digital terms the implementation of Equations (4.12) and (4.13) are simple.

A divide by two operation is a binary right-shift operation and the remainder of this divide by two operation is the bit shifted away. With a 4-bit  $B$ -counter and a 6-bit  $N$  value, Equations (4.12) and (4.13) become:

$$\therefore B[3..0] = N[4..1] \quad (4.14)$$

$$\therefore A[0] = N[0] \quad (4.15)$$

The specific implementation of the 4-bit  $B$ -counter requires that the value calculated be decremented by one. Equation (4.14) then becomes Equation (4.16) :

$$B = \left\lfloor \frac{N}{2} \right\rfloor - 1 \quad (4.16)$$

$$\therefore B[3..0] = N[5..1] - 1$$

Figure 69 then shows the implementation for the calculation of the 4-bit  $B$ -counter and 1-bit  $A$ -counter values:

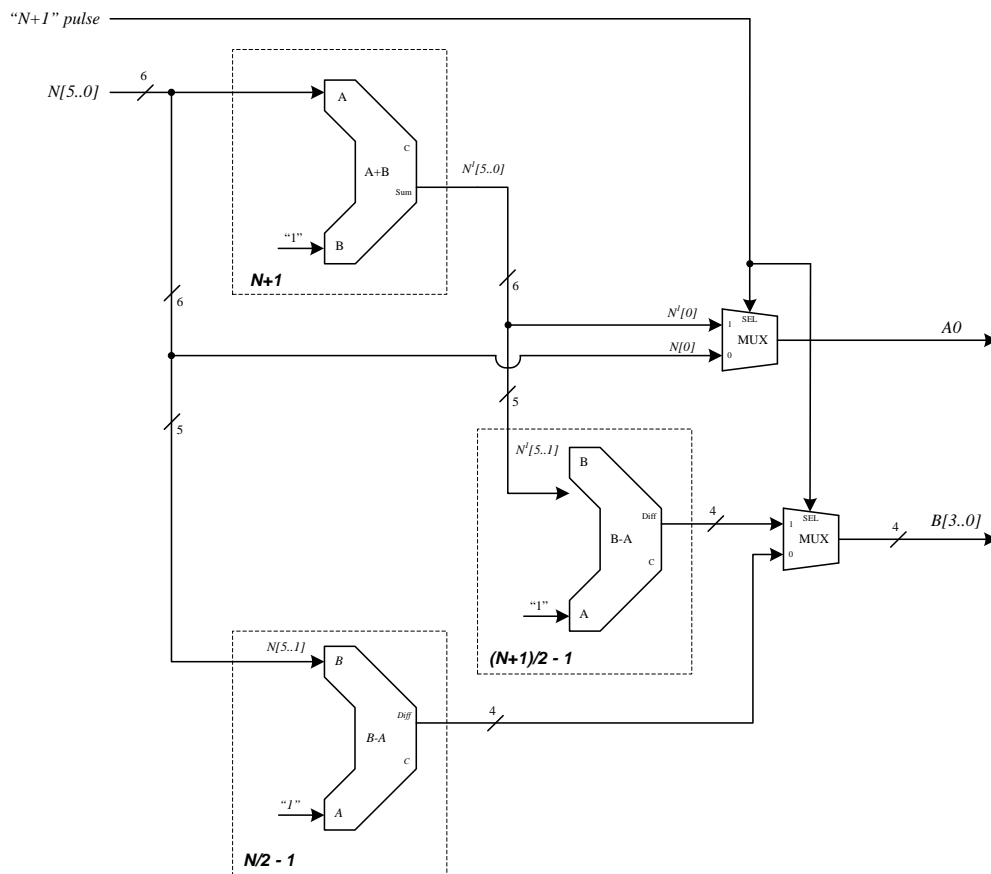




Figure 69. Pulse-swallow control

#### 4.3.2.1 Fractional- $N$ calculation delays

With a fractional- $N$  divider topology the fractional accumulator will provide an overflow or “ $N+1$ ” signal. This signal is then used to select a divider value one higher than the existing value. To minimise additional calculation delays, the calculations for the  $N$  and  $N+1$  scenarios are done simultaneously and the results are multiplexed by the “ $N+1$ ” or accumulator overflow signal. This concurrent calculation is also depicted in Figure 69. The  $N+1$  addition is done with a 6-bit binary adder.

### 4.3.3 Programmable modulus accumulator

In a fractional- $N$  PLL an accumulator is needed to alter the divide ratio between  $N$  and  $N+1$ . This is done by adding the required fractional part for every clock cycle to the existing sum or result. When the sum is equal or greater than the required modulus, the accumulator indicates an overflow condition and the result then becomes the difference between the sum and the modulus. Digitally speaking, the easiest way to construct an accumulator is to use a modulus-2 type, implying any power-of-two  $2^n$ , such as a MOD16 or MOD256, etc. This employs a standard binary adder where the output is clocked back to the adder input. The overflow indicator simply becomes the carry out bit of the adder.

A modulus-2 type or a fixed modulus accumulator however puts a limit on the value of the reference frequency used. The frequency resolution of a fractional- $N$  PLL, is defined in

Equation (2.34) as  $Freq_{res} = \frac{f_{ref}}{MOD}$ . For a certain frequency resolution required, the reference

frequency will then also be fixed. This characteristic is not attractive in a synthesizer architecture where industry standard reference frequencies are used, such as 10 MHz or 100 MHz. For this reason a programmable modulus accumulator is proposed as depicted in Figure 70.

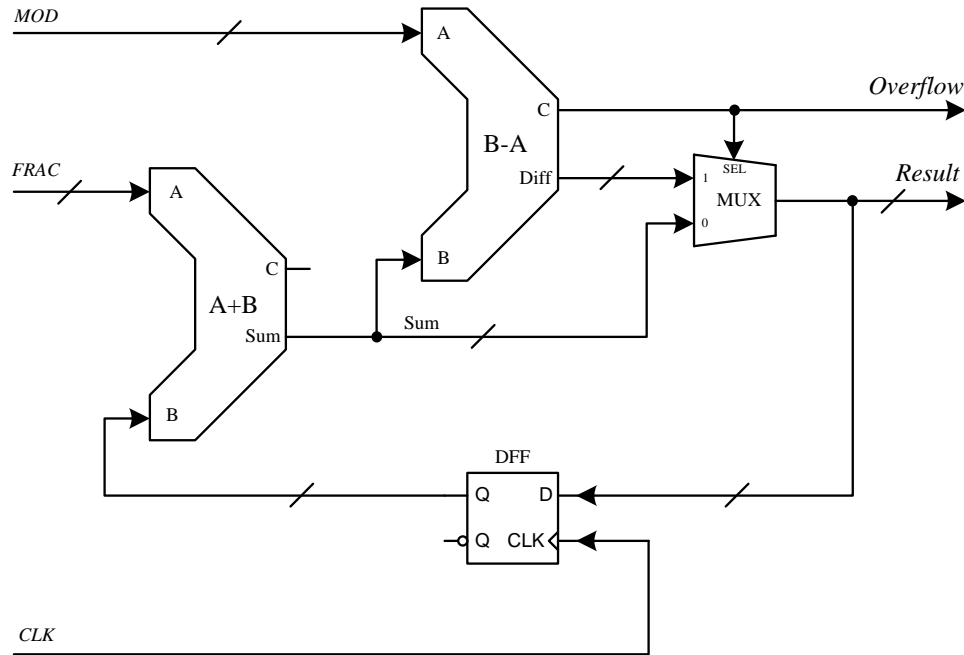


Figure 70. Programmable modulus accumulator

As described earlier the accumulator operates by adding the required numerator fractional part *FRAC* every clock cycle to the existing sum or result. When the sum is greater or equal than the required modulus *MOD*, the accumulator indicates an overflow condition and the result becomes the difference between the sum and the modulus. Otherwise the result is just the sum. The different results are multiplexed by the overflow condition as shown in Figure 70. The overflow condition then later controls the *N* or *N+1* divider selection. The accumulator implemented in this dissertation was a 6-bit version with a modulus range of ( $1 \leq MOD \leq 63$ ). Practically the accumulator was implemented with 7-bits to accommodate overflows in the adder and subtractor.

#### 4.3.3.1 Maximum accumulator clock frequency

The maximum accumulator clock frequency was estimated by accounting for all the propagation delays in the digital blocks making up the accumulator. Equation (4.17) calculates the total number of digital or gate delays  $N_{delays}$  as sixteen.

$$N_{delays} = 7_{adder\ bits} + 7_{subtractor\ bits} + 1_{MUX} + 1_{DFF} = 16 \quad (4.17)$$

The worst case propagation delay could now be estimated by multiplying  $N_{delays}$  with the worst case process propagation delay for an individual gate. Simulations showed a worst case gate delay of about 0.45 ns and hence a total delay of 7.2 ns was calculated. The maximum accumulator clock frequency was then estimated by Equation (4.18) as 138 MHz:

$$t_{delay\ total} = 16 \times 0.45\ ns = 7.2\ ns$$
$$\therefore f_{CLK(max)} = \frac{1}{t_{delay\ total}} \approx 138\ MHz \quad (4.18)$$

The upper limit of 138 MHz was adequate as the prototyped IC was evaluated with a 110 MHz reference or accumulator clock.

#### ***4.3.3.2 Magnitude comparator***

A novelty used in this programmable modulus accumulator is the dual function of the binary subtractor, used also as a magnitude comparator. With a subtractor, the carry out bit is normally not used, only the difference or result-bits are used. When a binary  $B - A$  operation is examined it can be seen that there will always be a carry bit when  $B \geq A$  and none when  $B < A$ . The accumulator overflow indication is then generated by the carry bit of the subtractor.



#### 4.3.4.1 CMOS PFD simulation

Verification of the CMOS PFD was done in a similar way as for the CML PFD. The CMOS PFD was verified correct by doing a simulation with a 110 MHz clock signal connected to both the *NCLK* and *RCLK* terminals as depicted in Figure 72. Both maximum and minimum delay settings were simulated.

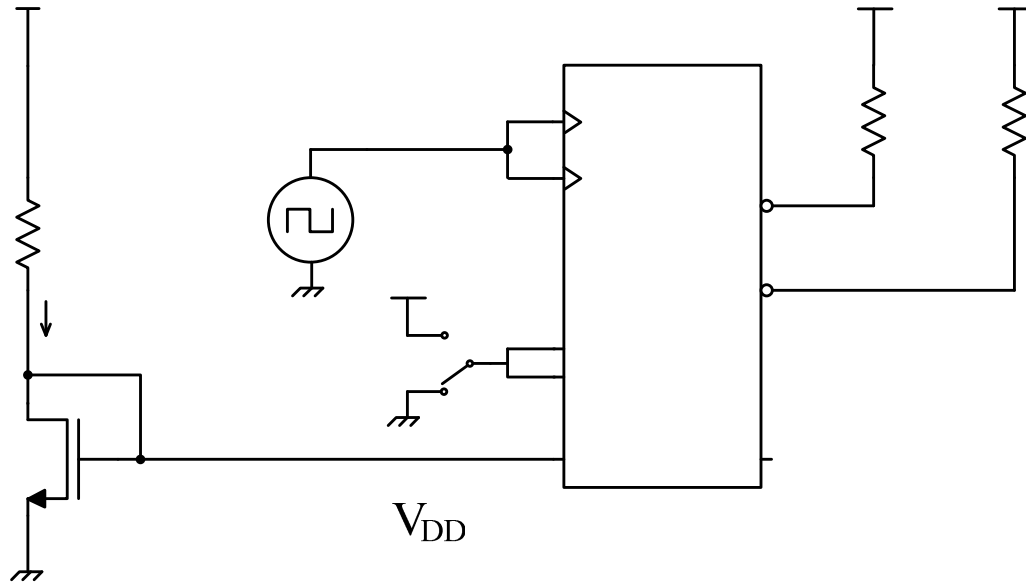


Figure 72. CMOS PFD simulation protocol

With this configuration it was once again possible to observe the PFD's behaviour under a PLL *lock* condition. The OD outputs were connected with 100  $\Omega$  pull-up resistors to  $V_{DD}$  and then the circuit was simulated. Figure 73 shows the simulation results for a minimum reset delay selected and Figure 74 for a maximum delay. Measured pulse widths are approximately 940 ps for the minimum delay selected and 2.5 ns for the maximum delay selected. From these pulse widths or reset delays the maximum CMOS PFD frequencies can be estimated by Equation (2.36) as approximately 530 MHz and 200 MHz respectively. The effect of the variable reset delay on phase noise is investigated in chapter 5. The 400 mV pulse depths are also visible, indicating the presence of 4 mA current pulses in the 100  $\Omega$  pull-up resistors.

3.3 V

110 MHz

$R_B = 2.4 \text{ k}\Omega$

$V_{DD}$

$I_{REF} = 1 \text{ mA}$

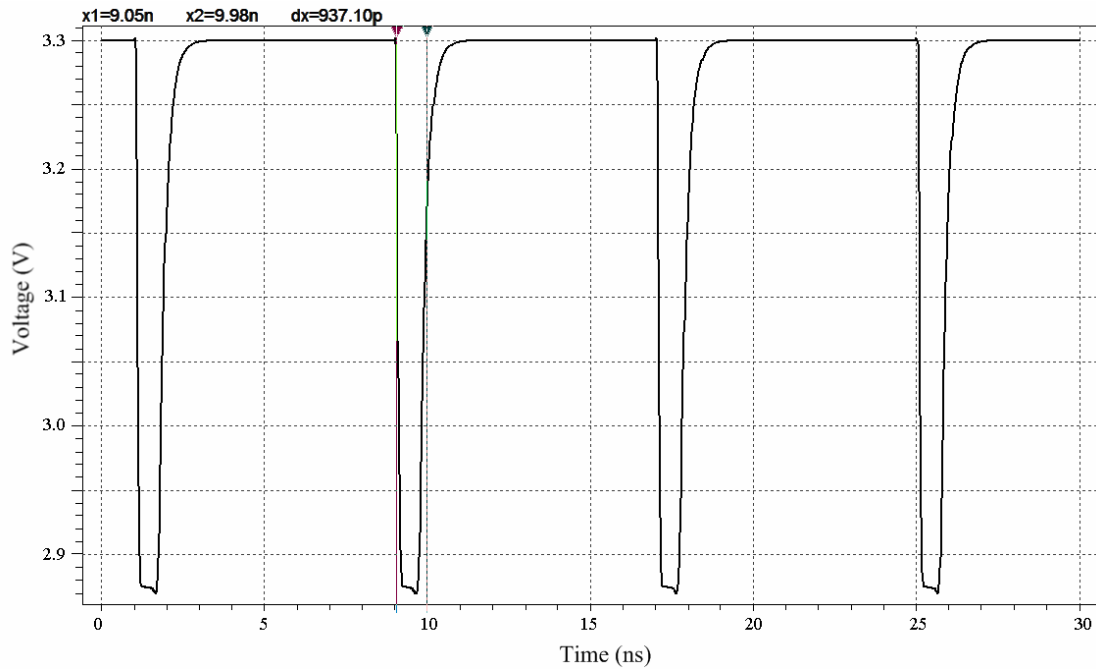


Figure 73. CMOS PFD simulation - minimum delay

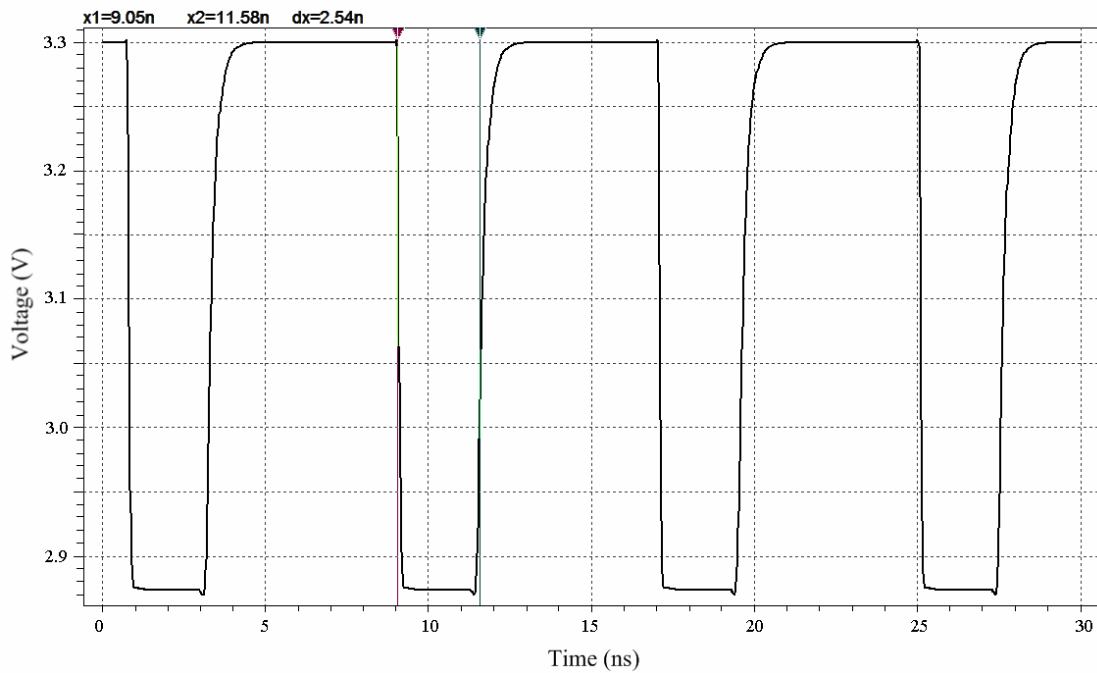


Figure 74. CMOS PFD simulation – maximum delay

### 4.3.5 SPI interface

To save in IC pin count, a serial data interface was chosen. A popular industry standard is the serial peripheral interface (SPI) bus. It was initially named by Motorola® and since adopted by many other IC vendors. A SPI bus is then also used in this dissertation to program the proposed synthesizer IC. It is a double buffered interface consisting of a serial clock line *SCLK*, a serial data line *SDAT* and a latch-enable *LE* line. All relevant settings are serialised into a single 20-bit word and activated or loaded by a rising edge on the *LE* signal. A shift register was implemented on-chip to decode the serial word.

Figure 75 depicts the timing waveform and the sequence of the control bits.

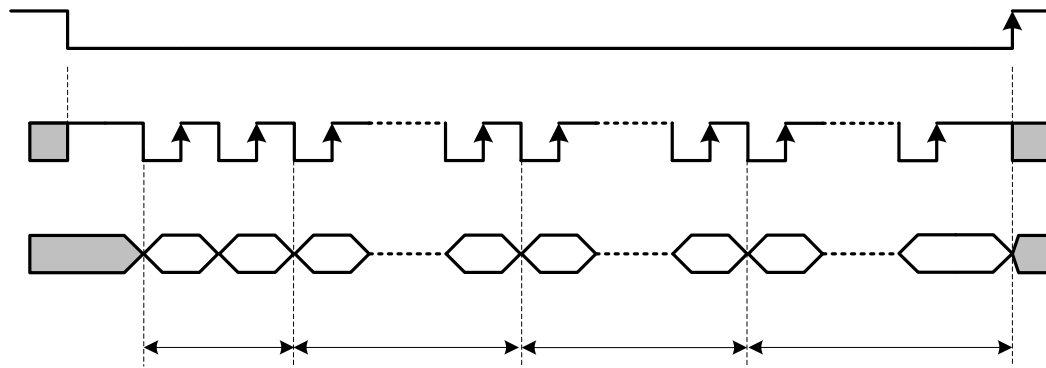


Figure 75. SPI timing waveform

The 20-bit serial word consists of two CMOS PFD delay bits  $DEL[1..0]$ , six modulus bits  $M[5..0]$ , six fractional bits  $F[5..0]$  and six *N*-divider bits  $N[5..0]$ . With this composition all aspects in the fractional-*N* synthesizer IC can be programmed in a single write transaction.

*LE*

*SCLK*

#### 4.4 FLOOR PLAN

Figure 76 depicts the final layout for the synthesizer IC as used in this dissertation and has dimensions of  $3150 \times 2180 \mu\text{m}^2$ .

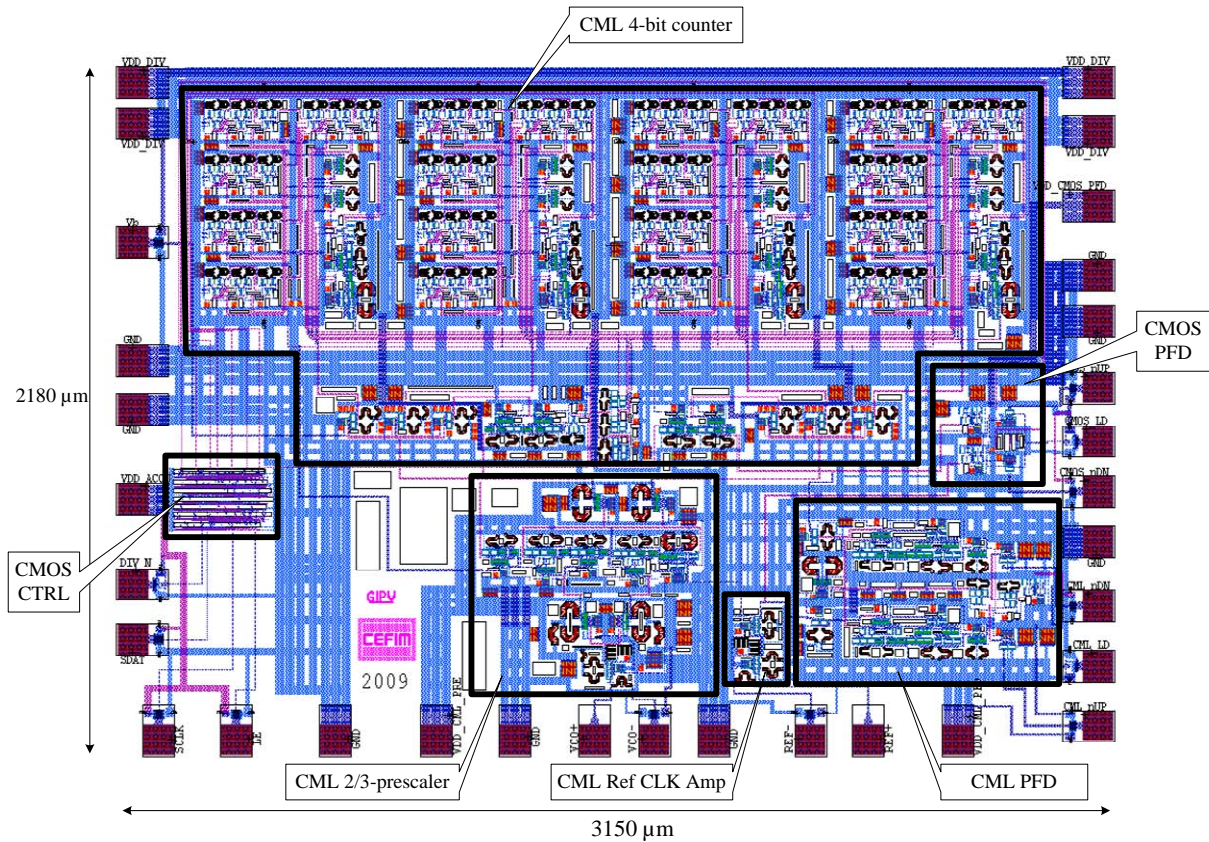


Figure 76. Prototyped IC floor plan

All major subsystems have been outlined and indicated. It is evident that the LUT based CML 4-bit counter takes up the majority of the area. As mentioned before, large ground metal areas have been incorporated into the design to assist in minimising ground differences with current mirrors and to aid with heat transfer to the perimeter of the chip. Each subsystem was allocated its own  $V_{DD}$  pad or set of  $V_{DD}$  pads. Where high power supply currents were expected, such as with the CML 4-bit counter, additional  $V_{DD}$  pads were added to assist in pad and bonding wire current sharing. In general for every  $V_{DD}$  pad an equivalent  $GND$  pad was added to cater for ground return paths in a specific subsystem.



## CHAPTER 5: SIMULATION AND MEASUREMENT RESULTS

---

This chapter documents the system simulation and measurements results. As was stated earlier two IC prototyping cycles were done. The first being the CML 2/3-prescaler and last the complete fractional- $N$  synthesizer IC. Many of the IC subsystems were simulated and proven correct by design in chapter 4. This chapter then only focuses on the overall performance of the ICs. The key performance parameters are the operating frequency, in-band phase noise and fractional spurious response. Each prototyped IC is evaluated separately.

### 5.1 PROTOTYPED CML 2/3-PRESCALER

The objective with the prototyped CML 2/3-prescaler was to determine whether the research methodology, assumptions and initial simulations done for the 0.35  $\mu\text{m}$  technology were correct, especially with regard to the maximum operating frequency. This would then serve as a basis for completing the final low noise fractional- $N$  synthesizer IC. Figure 77 shows the IC die photograph with thermo-sonic bonding wires visible and Figure 78 a zoomed version.

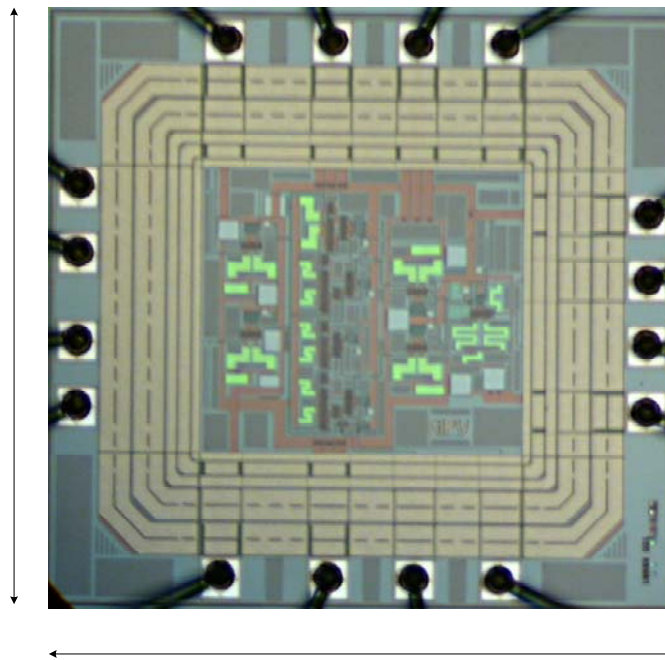


Figure 77. Prototyped CML 2/3-prescaler IC die photograph

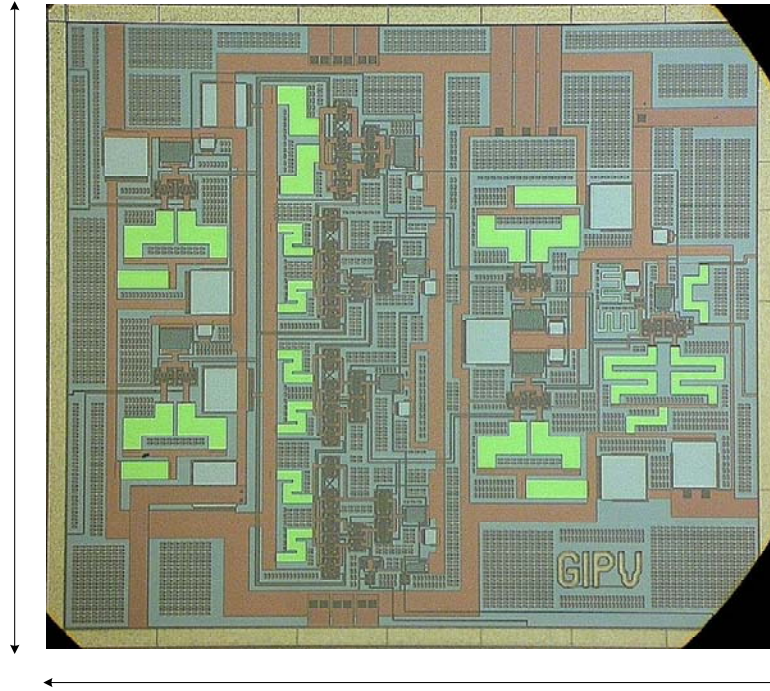


Figure 78. Zoomed prototyped CML 2/3-prescaler IC die photograph

### 5.1.1 Test setup and general measurements 670 $\mu\text{m}$

The primary objective with the CML 2/3-prescaler prototype IC is to determine the maximum operating frequency. This is done by sweeping the input frequency and amplitude with a signal generator and then observing the output with a spectrum analyzer. These results are discussed in section 5.1.2. The general setup for evaluating the CML 2/3-prescaler is depicted in Figure 79.

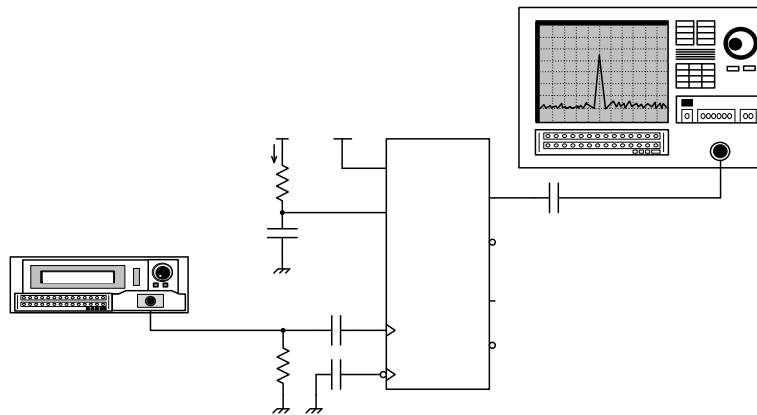


Figure 79. Prototyped CML 2/3-prescaler IC test setup



From section 4.2.1.4 the internal IC reference current source is set to 1 mA by  $R_B = 2.2 \text{ k}\Omega$  and a 1  $\mu\text{F}$  capacitor was added for decoupling to the  $V_B$  pin. The differential input section is DC blocked by 1 nF capacitors and shunted with a 56  $\Omega$  resistor to provide an approximate 50  $\Omega$  impedance for the signal generator. The divide ratio is fixed at  $\div 3$  by strapping the  $MC$  pin to  $V_{DD}$ . Current consumption and polyresistor measurements are discussed next.

### 5.1.1.1 Current consumption

The simulated current consumption of the prescaler formed part of the simulation results obtained in section 4.2.3.5 and is compared with the actual measured value in TABLE XI:

TABLE XI  
CML 2/3-PRESCALER CURRENT CONSUMPTION

Simulated	Measured	Deviation
29 mA	33 mA	13.8 %

The measured 33 mA compares well with the simulated 29 mA current consumption.

### 5.1.1.2 Polyresistor tolerances

As mentioned in section 4.2.5 the IC polyresistor tolerances can be verified by measuring the 500  $\Omega$  input polyresistor with an ohm meter as highlighted in TABLE XII:

TABLE XII  
POLYRESISTOR TOLERANCES

Designed	Measured	Deviation
500 $\Omega$	420 $\Omega$	-16 %

The -16 % deviation measured is however within the process tolerance  $\pm 20 \%$  [50]. This deviation for on-chip designed polyresistors could cause potential malfunctioning of CML circuits if they were not designed for such high tolerances. This was then one of the reasons why the CML output voltage swing was chosen higher than the process threshold voltage  $V_{TH}$  in chapter 4.

### 5.1.2 Input sensitivity

The measured input sensitivity graph, Figure 80, displays the behaviour of the CML 2/3-prescaler over frequency, indicating the maximum and minimum input levels and operating frequencies. From this graph the “window” of operation can be determined. From section 4.2.5 the maximum input level was limited to +10 dBm, as this was the power restriction on the internal 500 Ω input polyresistor.

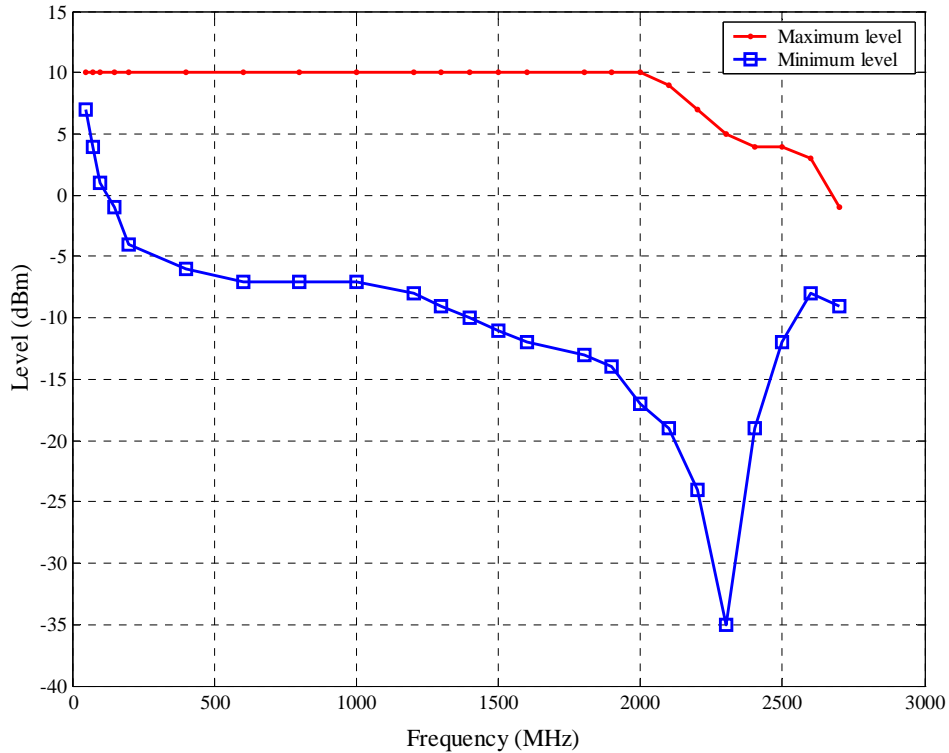


Figure 80. CML 2/3-prescaler input sensitivity graph

The maximum operating frequency was seen to be 2.7 GHz and proved to be better than the worst case simulated 2.5 GHz as obtained in section 4.2.3.5. Visible in Figure 80 is a “self resonant” frequency of 2.35 GHz which can in a way be explained by the low pass resonant peaking of the combination of the IC package lead inductance, bonding wire inductance, bonding pad capacitance and input MOSFET capacitance. This resonant effect is not necessarily undesirable but will cause the IC to oscillate at this frequency if no input signal is applied. Overall the performance of the CML 2/3-prescaler was satisfactory and it was concluded that proceeding to the final low noise synthesizer IC design would pose less risk.

## 5.2 PROTOTYPED FRACTIONAL- $N$ SYNTHESIZER IC

With the prototyped synthesizer IC it was possible to evaluate the limits of the 0.35  $\mu\text{m}$  CMOS technology used and the topology of the synthesizer IC itself. Figure 81 shows the die photograph with ultra-sonic bonding wires of the actual low noise fractional- $N$  synthesizer IC.

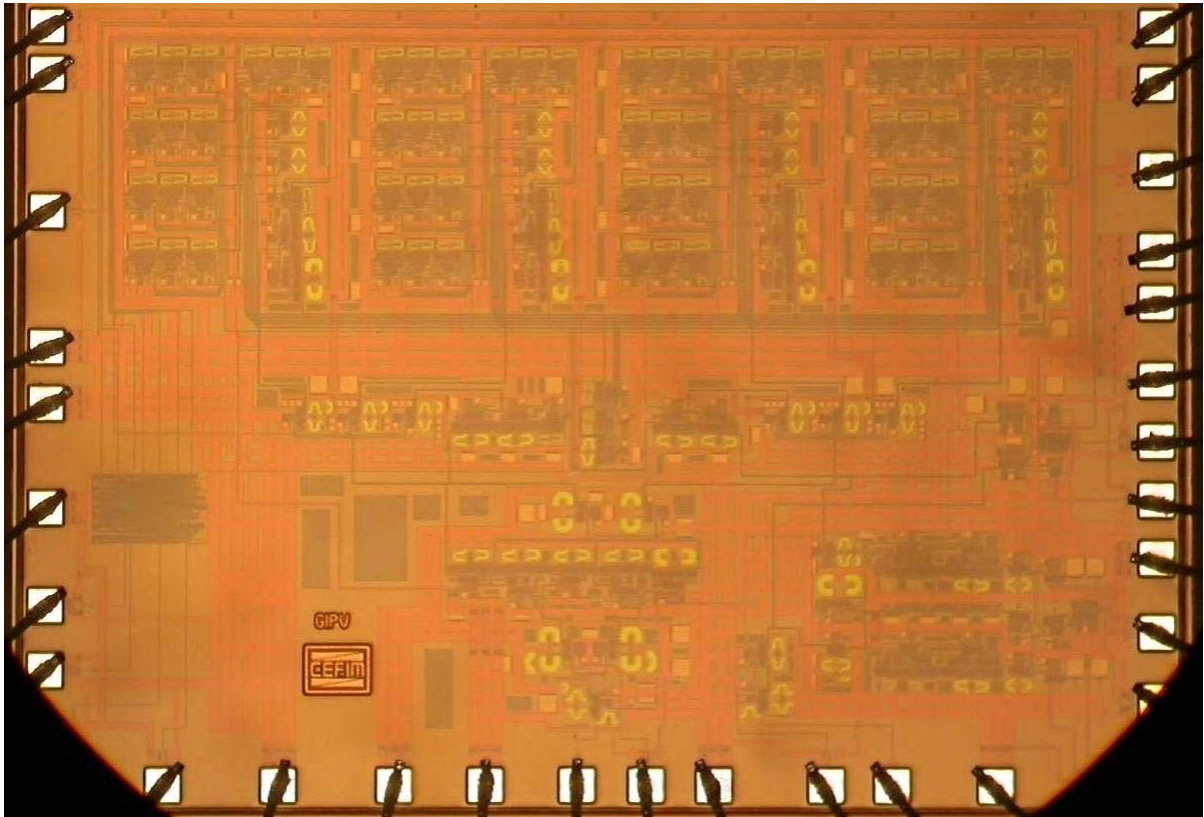


Figure 81. Zoomed prototyped IC die photograph

Location of the individual subsystems can be obtained by comparing Figure 81 with Figure 76. Some additional zoomed pictures of individual subsystems are presented in Appendix B.

### 5.2.1 Evaluation PCB

To evaluate the prototyped IC a complete frequency synthesizer system or infrastructure had to be designed around the IC. This included a high voltage BJT charge pump, loop filter, VCO, external  $\div 4$  prescaler and crystal reference oscillator as depicted in Figure 82. The prototyped IC was controlled or programmed via SPI by a graphical user interface (GUI) as presented in Appendix C.

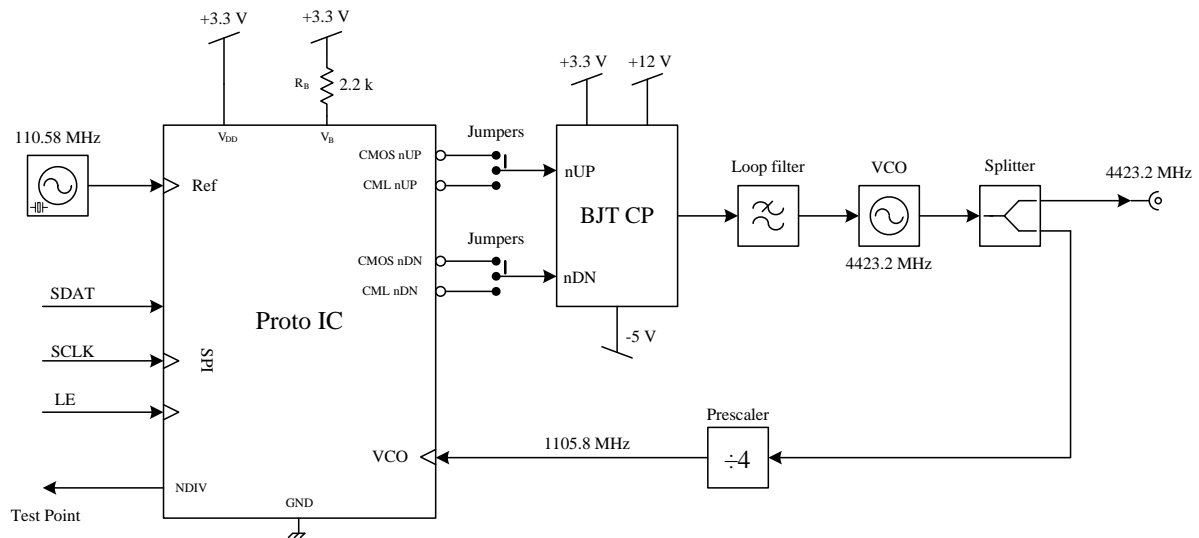


Figure 82. Evaluation PCB block diagram

Many of the components chosen were due to their availability at GEW. This is especially true for the 110.58 MHz low noise crystal reference oscillator and the 4.4 GHz VCO. The primary objective was to measure the in-band phase noise performance of the prototyped IC. As mentioned in chapter 3, the low division architecture incorporated into the IC design made it difficult to measure phase noise accurately with a standard high performance spectrum analyzer. For this reason an external off the shelf low noise  $\div 4$  prescaler was added in the PLL feedback path, to amplify the in-band output phase noise by another 12 dB. The total division ratio was the product of the external prescaler setting and the programmed  $N$ -divider value of the prototype IC. The other research objective was to benchmark the two types of PFDs. Wire jumpers were used to select between the CMOS or CML PFD as indicated in Figure 82.

The complete circuit diagram of the evaluation PCB can be found in Appendix A and a photograph of the evaluation PCB is shown next in Figure 83.

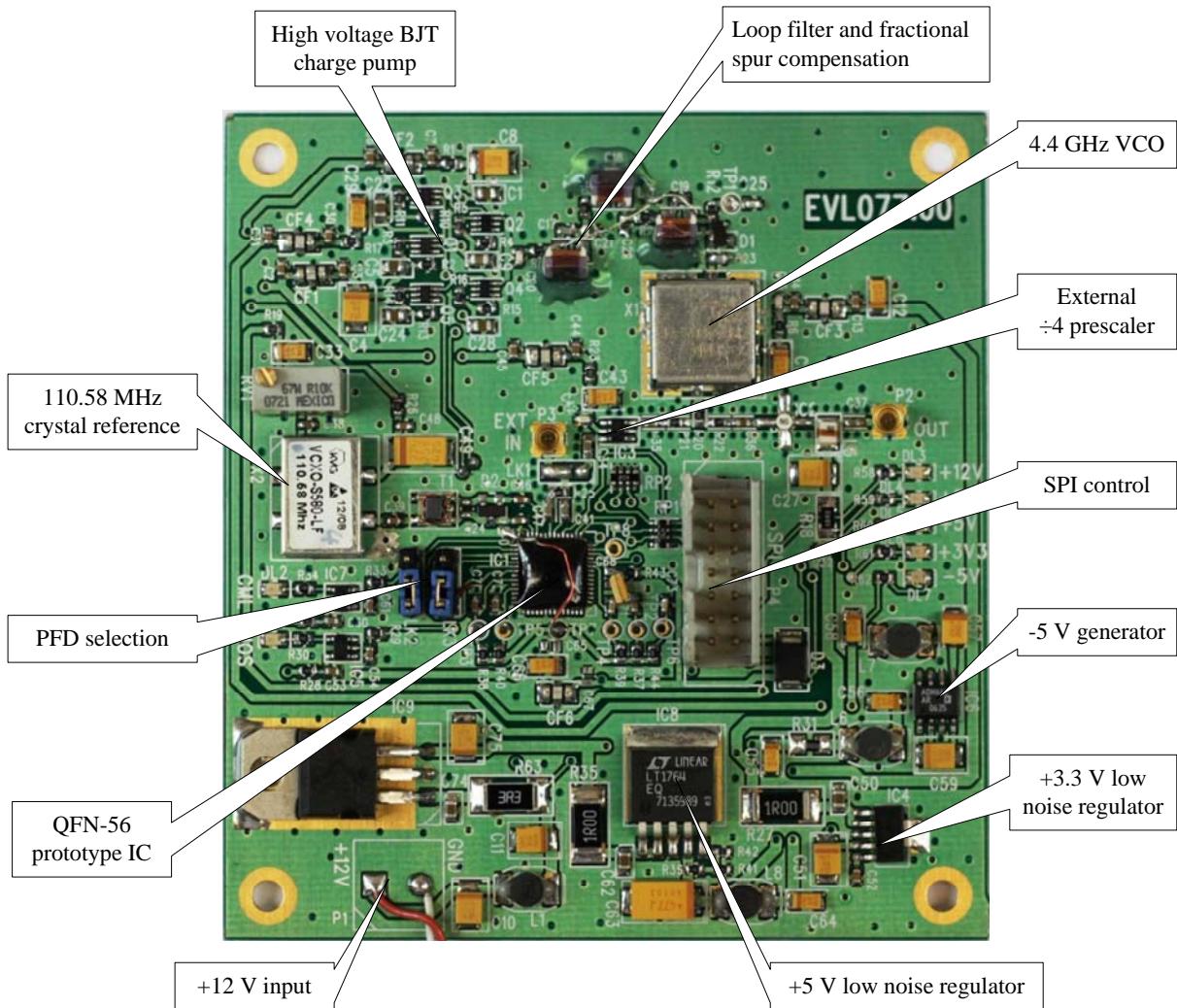


Figure 83. Evaluation PCB photograph

Indicated on the photograph are the different components making up the complete evaluation circuit. The PCB is 0.5 mm thick consisting of conventional FR4 dielectric material and two copper layers, one being a uniform solid ground plane at the bottom. A single +12 V supply was used as input and all the other required voltages were derived from this. Dedicated low noise regulators were used on the +3.3 V and +5 V voltages. Light emitting diodes (LEDs) were used to indicate CML PFD and CMOS PFD lock detect outputs.

### 5.2.1.1 High voltage BJT charge pump

As was stated earlier an active OPAMP based loop filter would introduce additional out-band phase noise. A passive loop filter was thus desirable. The problem was that the on-chip PFD charge pumps only had a maximum voltage swing of +3.3 V, which would be inadequate for a wide tuning range VCO. The solution was to mirror the on-chip PFD current pulses off-chip with high voltage BJT mirrors, creating a high voltage charge pump circuit as depicted in Figure 84.

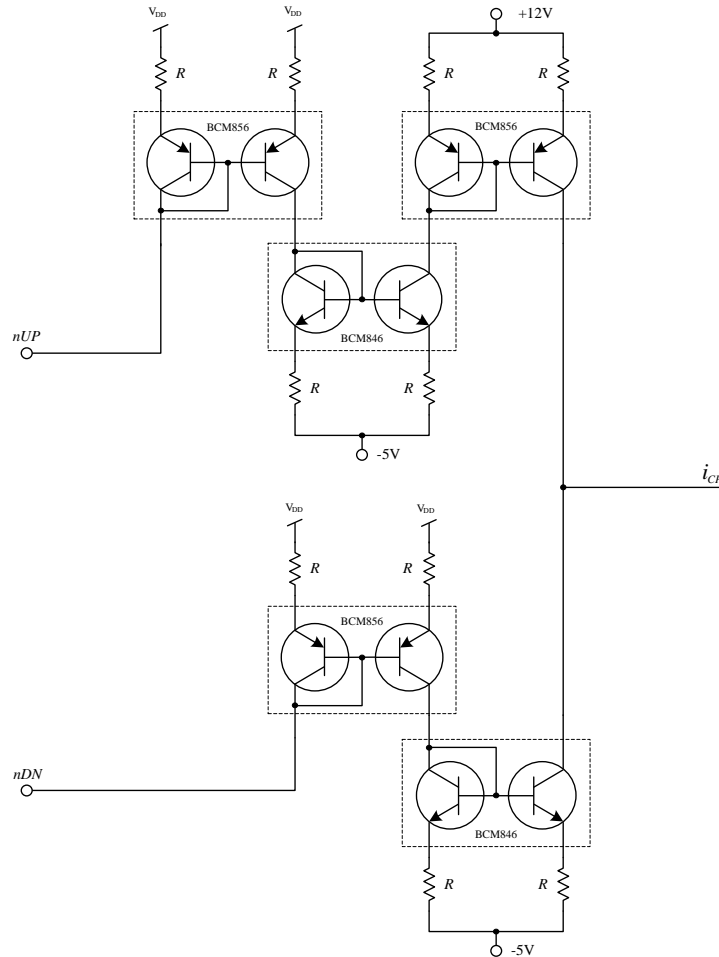


Figure 84. High voltage low noise BJT charge pump

The BJT current mirrors are modified Widlar current mirrors [53] where each transistor in a mirror has the same emitter resistor value. This ensures that the input and output currents, of a current mirror pair, are exactly the same. Commercially available high voltage ( $V_{CEO} = 65\text{ V}$ ) NPN and PNP matched transistor pairs (BCM846 and BCM856 from Infineon®) were used and the supply rail was set at +12 V. A higher rail voltage could be used if the VCO required



it. The emitter resistors were set at  $10\ \Omega$  for the +3.3 V rail mirrors and  $270\ \Omega$  for the +12 V and -5 V rail mirrors respectively. This prevented destructive high voltage failure of the transistors if a short circuit should present itself somewhere.

### 5.2.2 Power consumption

The simulated current consumption of the prototyped IC formed part of the simulation results obtained in section 5.2.3.1. Each subsystem in the IC was assigned its own  $V_{DD}$  rail and a subsequent power pin on the IC package. This simplified current measurements for each subsystem and provided access for circuit debugging. A  $1\ \Omega$  series resistor was included to all individual IC power pins on the evaluation PCB. Current consumption was obtained by directly measuring the voltage across each  $1\ \Omega$  resistor with a multi-meter. These  $1\ \Omega$  resistors are visible on the schematics of the evaluation PCB in Appendix A. TABLE XIII summarises the power consumption.

TABLE XIII  
POWER AND CURRENT CONSUMPTION

Block	Simulated (mA)	Measured (mA)	Power (mW)
CML Prescaler	32	30.8	102
CML A and B Counters	130	129.5	427
CML PFD	35	35.4	117
CMOS PFD	15	16.6	55
CMOS Control	3	2.9	10
<b>Total</b>	<b>215</b>	<b>215.2</b>	<b>≈ 710</b>

A total DC power consumption of 710 mW was noted. It is also clear from TABLE XIII that the current consumption simulations were good estimates to the actual measured values. As expected, the biggest power consumers were the CML A and B-counters.



### 5.2.3 Input sensitivity

One of the primary performance criteria of the prototyped synthesizer IC is the maximum operating frequency. This is done with the input sensitivity test. The maximum operating frequency was first estimated by simulation.

#### 5.2.3.1 Simulation

Continuing from chapter 4, the maximum worst case operating frequency was simulated to be in the order of 2.3 GHz. Figure 85 depicts the simulation setup for the combined internal CML 6-bit pulse-swallow divider, consisting of the CML 2/3-prescaler, A and B counters and the CMOS pulse-swallow control. A divide ratio of  $N=11$  was used.

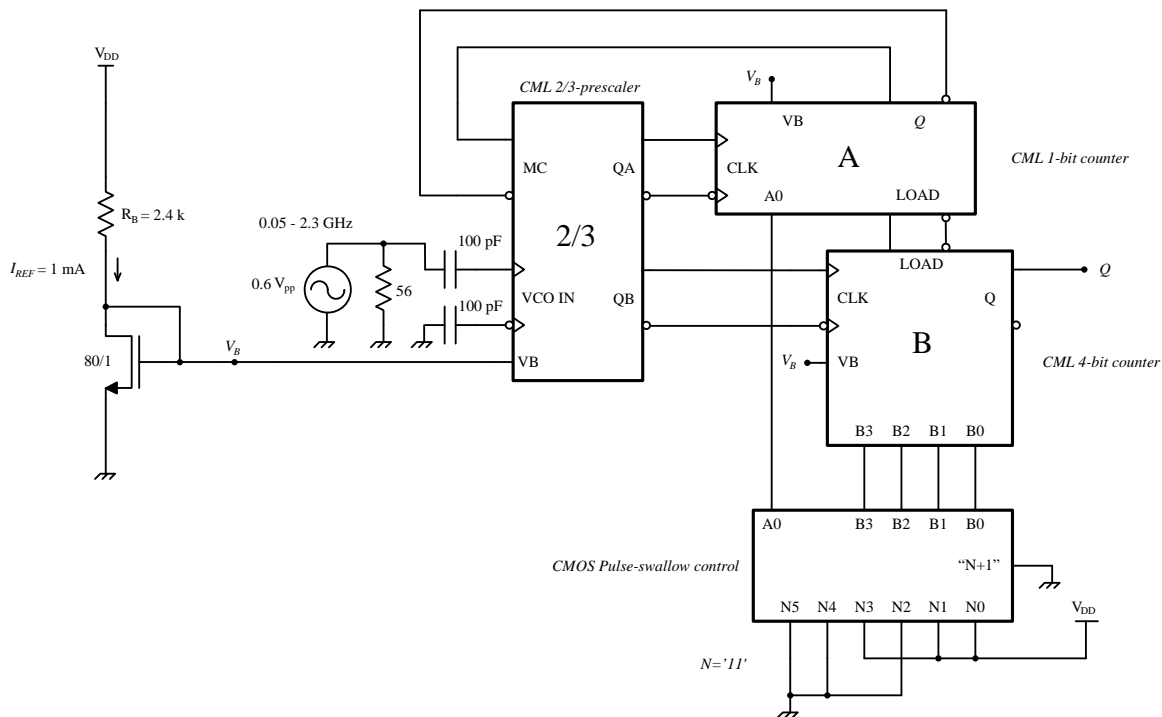


Figure 85. CML 6-bit pulse-swallow divider simulation setup

Visible in Figure 86 are the simulation results for a 2.3 GHz input signal. The 209.09 MHz main divider output and the CML 2/3-prescaler output are shown. Operation of the 2/3-prescaler is demonstrated by examining the lower graph in Figure 86 where the prescaler output alternates between 1.15 GHz ( $\div 2$ ) and 766.67 MHz ( $\div 3$ ), as set by the MC input.

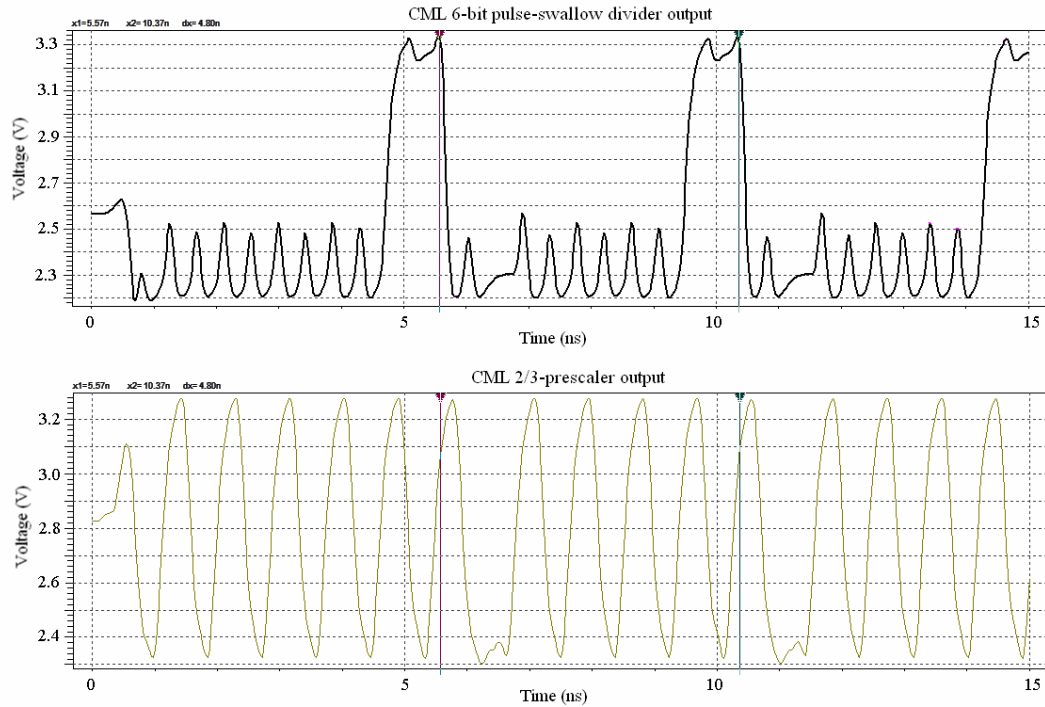


Figure 86. CML 6-bit pulse-swallow divider simulation results

### 5.2.3.2 Measurements

Input sensitivity measurements, for the prototyped IC, were done in a similar fashion as for the prototyped CML 2/3-prescaler, by sweeping the input frequency and amplitude with a signal generator and then observing the output on the *NDIV* test pin with a spectrum analyzer. The *NDIV* pin is a buffered output of the main pulse-swallow *N*-divider. On the evaluation PCB the input was for the moment disconnected from the external  $\div 4$  prescaler and connected to the output of the signal generator as depicted in Figure 87.

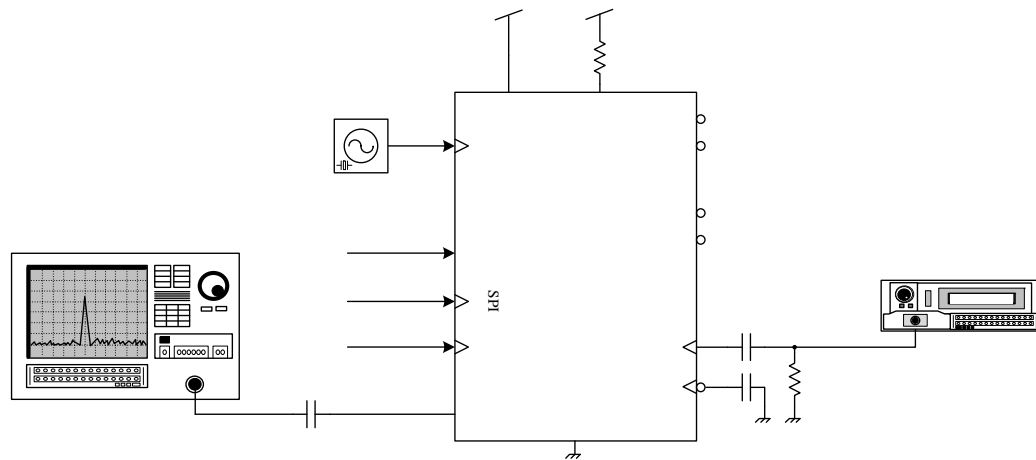


Figure 87. Prototyped IC input sensitivity test setup

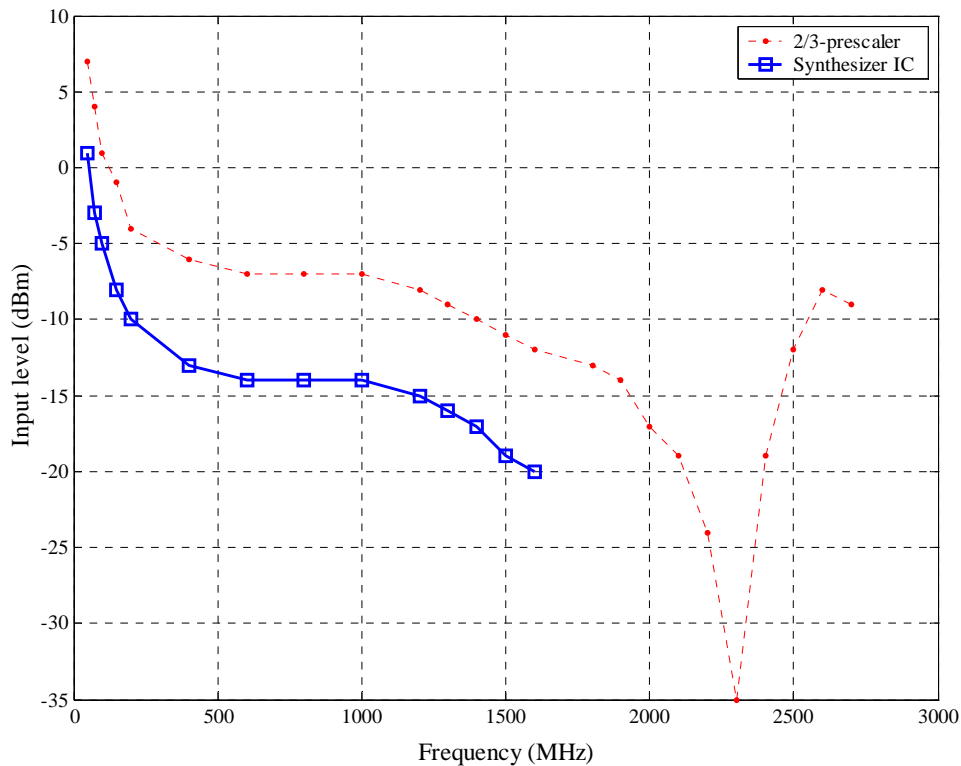


Figure 88. Prototyped IC input sensitivity graph

Figure 88 displays the results obtained. Different  $N$ -divider values were used during the test to obtain an average output frequency of around 100 MHz. The results were somewhat disappointing as it indicated a maximum  $N$ -divider operating frequency of 1.6 GHz and not around 2.3 GHz as estimated. By overlaying the sensitivity graph of the prototyped CML 2/3-prescaler on Figure 88, it can be seen that the two profiles are similar. The only difference being the amplitude offset which can be explained by the fact that the old prescaler design used 40  $\mu\text{m}$  MOSFETs, in the cascaded input amplifier, and the new design 80  $\mu\text{m}$  MOSFETs. This was done to improve the input sensitivity which is evident.

The only conclusion that can be drawn from Figure 88 is that the internal CML 4-bit counter is not fast enough. When examining the floor plan of the IC, as in Figure 76, it is clear that the CML 4-bit counter takes up most of the space. It is possible that the simulations did not accurately model the large interconnect distances and associated capacitances and inductances. This could all be attributed to the unaccounted bandwidth restriction.

### 5.2.4 Phase noise measurements

Phase noise measurements were done at a carrier frequency of 4.4232 GHz where the VCO was locked to a 110.58 MHz reference giving a total  $N$ -division ratio of 40. Initially the measurements were done with a 100 kHz loop bandwidth, but this proved to be too narrow as the thermal noise floor of synthesizer IC was still not exposed. A second set of measurements were then done with a 500 kHz loop bandwidth which did expose the thermal noise floor. With both sets of measurements, the CML PFD and CMOS PFD were benchmarked against each other. The CMOS PFD was benchmarked with a minimum reset delay setting and a maximum delay setting.

To put this 0.35  $\mu\text{m}$  CMOS research in context, the prototyped synthesizer IC was also benchmarked against a high performance, commercially available, GaAs HBT device. The HMC440 device [10] from Hittite Microwave Corporation® served as a reference as it was used in a circuit with exact the same divide ratio, reference frequency source, loop bandwidth, loop filter architecture and VCO.

#### 5.2.4.1 100 kHz loop bandwidth

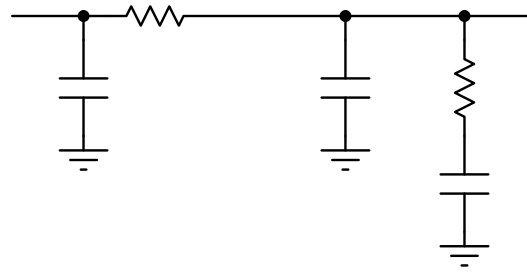
The loop bandwidth can be manipulated by the components making up the passive loop filter. By using the formulas presented in sections 2.1.6.1 and 2.1.6.3, the passive loop filter components for a 100 kHz loop bandwidth were calculated by using the following input parameters as indicated in TABLE XIV.

TABLE XIV

LOOP FILTER CALCULATION INPUT PARAMETERS

Parameter	Value	Motivation
Phase detector gain:	$K_p = \frac{I_{CP}}{2\pi} = \frac{4 \text{ mA}}{2\pi}$	By design $I_{CP} = 4 \text{ mA}$
VCO gain:	$K_v = 2\pi \times K_{VCO} = 2\pi \times 16 \text{ MHz/V}$	$K_{VCO} = 16 \text{ MHz/V}$ from VCO CRO4400 datasheet
Phase margin:	$\phi_m = 68^\circ$	$68^\circ$ will give less noise peaking
Loop bandwidth:	$\omega_p = 2\pi \times 100 \text{ kHz}$	100 kHz required for test
$N$ -divider value	$N = 40$	Required for output frequency

The rounded calculated values, as used on the evaluation PCB, are displayed in Figure 89.



100 Ω

Figure 89. Loop filter - 100 kHz loop bandwidth

Figure 90 summarises the 100 kHz loop bandwidth phase noise measurements.

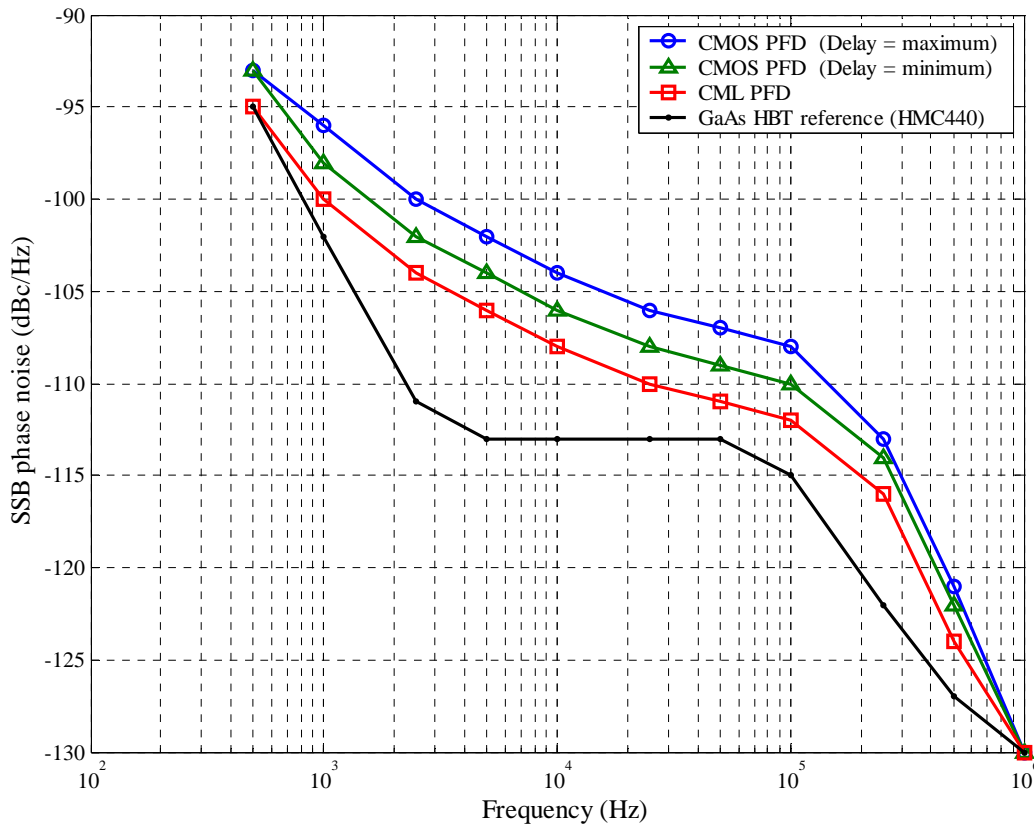


Figure 90. SSB phase noise results - 100 kHz loop bandwidth

From Figure 90 a limitation of the spectrum analyzer used is observed. All measurements below a 1 kHz offset tend to bundle together indicating a phase noise limitation of the

spectrum analyzer at these low offsets. At higher offset frequencies the performance of the spectrum analyzer is adequate to accurately measure the phase noise of the prototyped synthesizer IC. What is clear from Figure 90 is the fact that the flicker noise of the CMOS synthesizer IC dominates the spectrum. The thermal noise plateau has not been reached in any of the measurements except for the HMC440 GaAs HBT reference device. In the case of the GaAs HBT device the noise plateau was reached at an offset of 5 kHz with a value of  $\mathcal{L}(f) = -113$  dBc/Hz. One of the goals of this research is to determine the FOM which is only applicable to the in-band noise plateau. For this reason it was decided to widen the loop bandwidth so to expose the thermal noise floor. A loop bandwidth of 500 kHz was chosen.

#### 5.2.4.2 500 kHz loop bandwidth

In a similar way, as for the 100 kHz loop bandwidth, the loop filter components for the 500 kHz loop bandwidth are displayed in Figure 91.

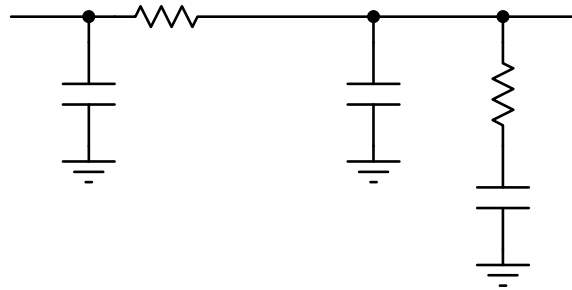


Figure 91. Loop filter - 500 kHz loop bandwidth

The culmination of phase noise results for this research is depicted in Figure 92. From this graph it is seen that the in-band phase noise plateau is reached at an offset of 100 kHz, with a value of  $\mathcal{L}(f) = -113$  dBc/Hz for the CML PFD.

The FOM can be calculated for the CML PFD by using Equation (2.69):

$$\begin{aligned}
 FOM &= L(\Delta f) - 20\log N - 10\log f_R \\
 &= -113 \text{ dBc/Hz} - 20\log(40) - 10\log(110.58 \text{ MHz}) \\
 &= -225.5 \text{ dBc/Hz}
 \end{aligned}$$

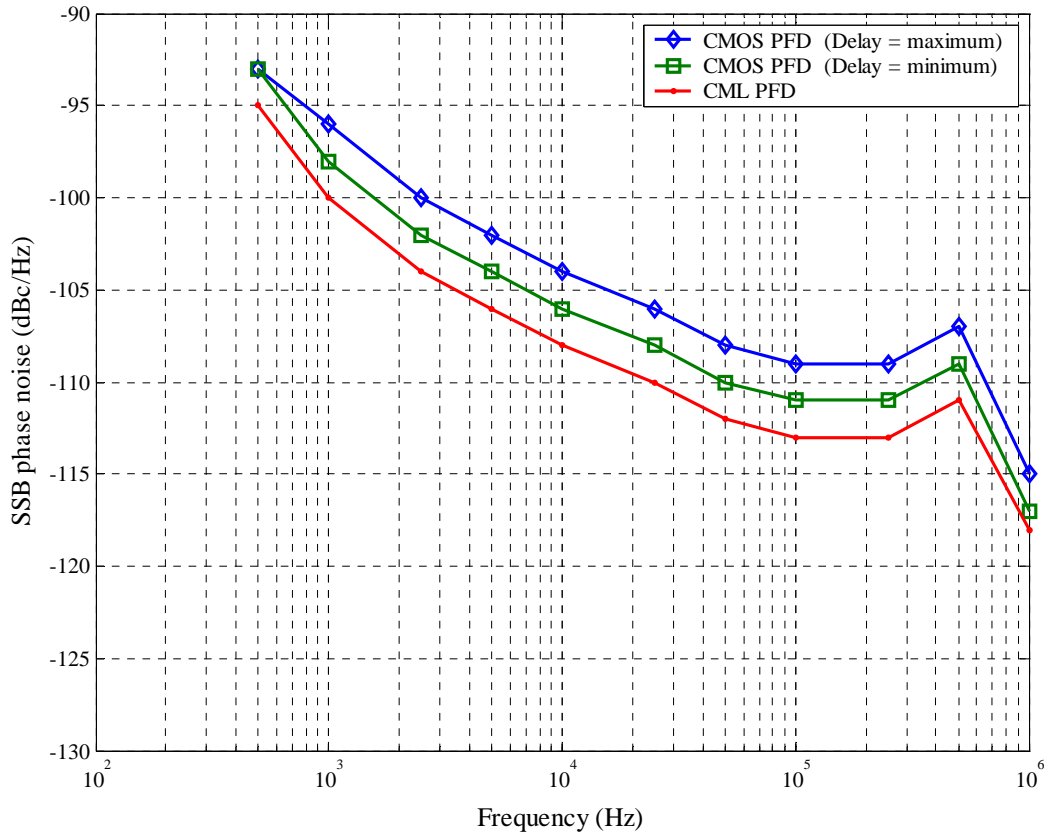


Figure 92. SSB phase noise results - 500 kHz loop bandwidth

At a 500 kHz offset some phase noise peaking is observed which can be due to the finite bandwidth of the high voltage charge pump or the input capacitance of the VCO, thus affecting the phase margin. What is clear from Figure 90 and Figure 92 is the differences in technologies (HBT vs CMOS) and PFD implementations. The prototyped CMOS IC only reaches the same noise floor (-113 dBc/Hz) as the GaAs HBT device at an offset of 100 kHz. This is twenty times higher in offset frequency than the GaAs HBT device. Fortunately the CML PFD has the same wideband noise floor as the GaAs HBT device. The CML PFD is definitely superior to the CMOS PFD, even for the minimum delay case. The PFD phase noise differences can possibly be explained by the reset pulse delay in all cases.



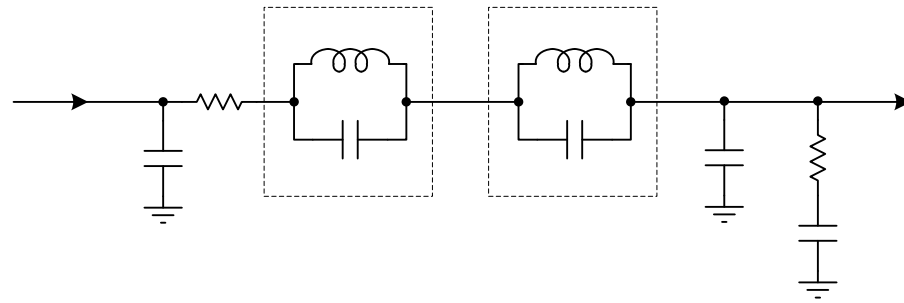
From simulations in chapter 4 and Equation (2.37), the CMOS PFD had longer reset delays and thereby allowing more charge-pump noise to accumulate, hence degrading the phase noise performance. It is also possible that the CML-to-CMOS translator block is noisy.

### 5.2.5 Fractional spur compensation

Mentioned in chapter 2 was the fact that any fractional- $N$  synthesizer IC would introduce fractional and in addition reference boundary spurious signals to the output spectrum. In conventional fractional- $N$  topologies the fractional spurs are dithered away with higher order  $\Sigma\Delta$  modulators. This comes at the cost of increased in-band phase noise [1]. Up to date not much can however be done on-chip for reference boundary spurs, to the author's knowledge. These spurs occur in a fractional- $N$  topology where the loop bandwidth is normally much larger than the frequency resolution of the synthesizer. A reference boundary spur will occur when the output frequency is within a small offset from a multiple of the reference frequency. If the offset frequency falls inside the PLL loop bandwidth the spurs will manifest themselves at exactly the offset frequency on both sides of the carrier. Both fractional and reference boundary spurs occur due to the non-linear behaviour of the PFD.

As the PFD causes these spurs, a way around this problem is to limit the tuning resolution to a frequency step size way bigger than the loop bandwidth. An additional off-chip analogue filter can then easily filter out the PFD's fractional and reference boundary contributions. The analogue filter may however adversely affect the PLL phase margin. It is best to choose the frequency step size high enough to not disturb the phase margin for a given loop bandwidth. Such an analogue filter can then be incorporated into an existing loop filter.

In the custom built 4.4 GHz synthesizer circuit, evaluating the prototyped IC, a fractional modulus of 40 was used. A tuning resolution of 2.7645 MHz for a 110.58 MHz PLL reference resulted. This implied that fractional spurs would occur on multiples of 2.7645 MHz. To counter these spurs, an analogue fractional spur compensation network was implemented by a set of cascaded LC notch filters. The notch filters took the form of parallel resonant traps resonating at multiples or harmonics of 2.7645 MHz. The existing loop filter was then modified as indicated in Figure 93.



*LC trap*

*L*

Figure 93. Modified passive loop filter - fractional spurious compensation

Moderate Q-factors were used for the traps as too high Qs would require the inductor and capacitor values to be manually trimmed, to cater for component tolerances. The Q-factor for an inductor is defined as the ratio of the reactance  $X_L$  over the internal series resistance  $R$ :

$$Q = \frac{X_L}{R} = \frac{2\pi f L}{R}$$

*1<sup>st</sup> harmonic*

In any resonating LC circuit the total Q-factor will be limited by the element with the lowest Q-factor. In this case it is the inductor. For the 2.76 MHz trap, a 22  $\mu$ H inductor from Coilcraft® (1812CS-223) was selected. This inductor had a rated Q-factor of 32 at 10 MHz. A 150 pF capacitor was calculated to resonate with the inductor at 2.76 MHz. The 2<sup>nd</sup> harmonic 5.52 MHz trap was designed with a 10  $\mu$ H inductor and an associated 82 pF capacitor to resonate. Exact implementation of the compensation network can be found in Appendix A.

Shown on the next page are the measured effects of this compensation network.

Figure 94 shows the spectrum scenario where the prototyped fractional- $N$  synthesizer IC is programmed for a VCO output frequency of 4.434258 GHz. With the 110.58 MHz PLL reference and the external  $\div 2$  prescaler, this frequency corresponds to following accumulator settings:  $MOD = 40$  and  $FRAC = 2$ .

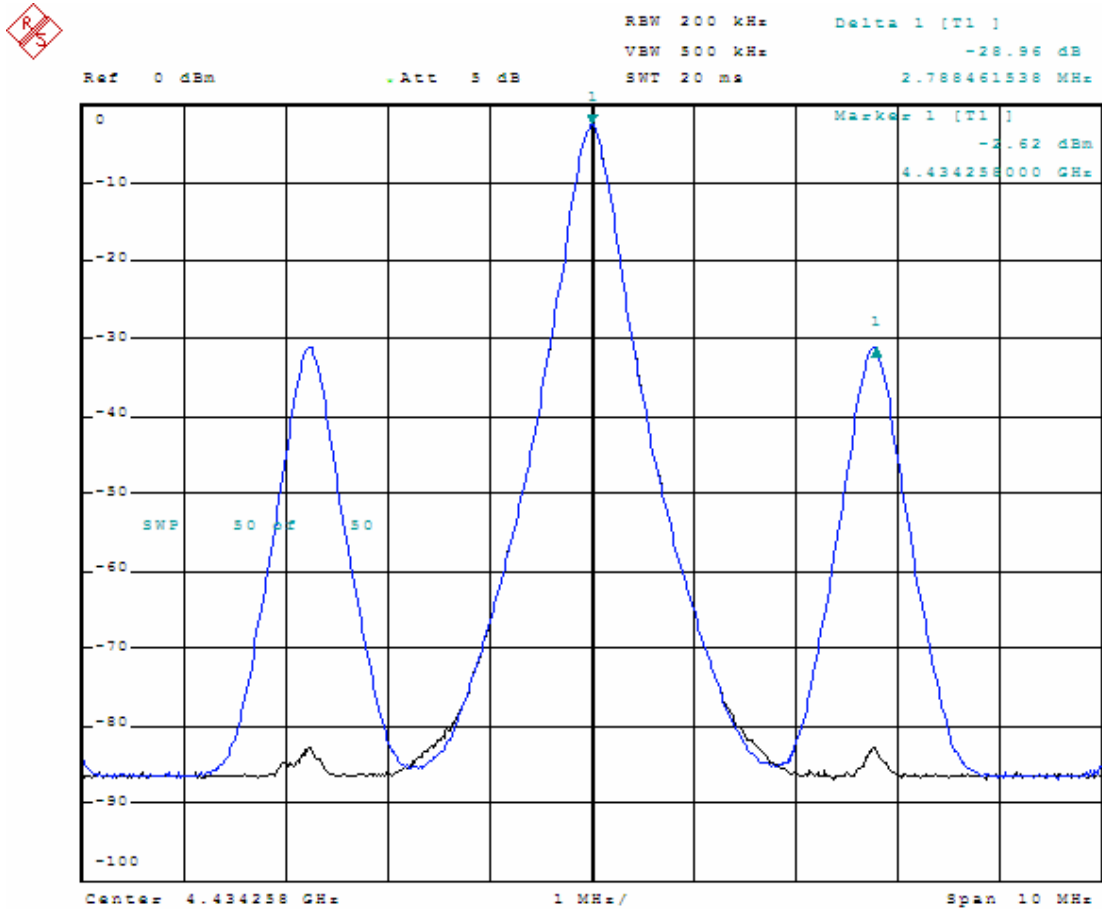


Figure 94. Fractional spurious comparison

Visible in Figure 94 is the effect on the first 2.76 MHz fractional spur when using the modified loop filter or not. Without the LC trap modification the normal spurious suppression is about 29 dB and with it 80 dB. An improvement of approximately 50 dB is achieved.

## CHAPTER 6: CONCLUSION

---

This chapter concludes the research and summarises the results. The objective of this dissertation was to research a collection of techniques, as applicable to high performance synthesizer ICs, to push towards the noise and frequency limits of CMOS processes in general. By doing this the performance of existing HBT synthesizer ICs could maybe be rivalled by a low cost CMOS IC. The research was verified by implementing a low noise *low* division ( $4 \leq N \leq 33$ ) synthesizer IC in a reasonably low cost 0.35  $\mu\text{m}$  CMOS process with a designed operating frequency in the excess of 2 GHz. A fractional- $N$  topology was also incorporated.

### 6.1 TECHNICAL SUMMARY AND CONTRIBUTION

A summary of all technical achievements and contributions are discussed next.

#### 6.1.1 FOM

The low noise requirement was demonstrated with a  $\text{FOM} = -225 \text{ dBc/Hz}$  at an offset frequency of 100 kHz for a 0.35  $\mu\text{m}$  CMOS process. This FOM is comparable to the best high performance expensive SiGe and GaAs HBT devices out there.

#### 6.1.2 CML low division high frequency divider

Due to the slow speed of 0.35  $\mu\text{m}$  CMOS dividers ( $f < 500 \text{ MHz}$ ), consisting of standard CMOS logic blocks, an all CML low division ( $4 \leq N \leq 33$ ) high frequency divider was designed and demonstrated. The divider was a 6-bit pulse-swallow divider consisting of a 2/3-precaler, 4-bit counter and a 1-bit counter. Although only practically operational at 1.6 GHz it was still a major improvement over standard CMOS dividers.

#### 6.1.3 CML PFD

An all CML PFD was demonstrated with a maximum simulated comparison frequency of 790 MHz. It was also the CML PFD that achieved the low  $\text{FOM} = -225 \text{ dBc/Hz}$  value. Part of the CML design also required a resettable CML D-latch.

#### **6.1.4 PFD reset delay effect**

Demonstrated was the effect of a variable reset delay in a PFD circuit. Measured results concurred with theory that the delay must be minimised to achieve a good FOM.

#### **6.1.5 Programmable modulus accumulator**

Many commercially available fractional- $N$  synthesizer ICs fix the modulus value of the fractional accumulator in hardware with some power-of-two  $2^n$  value. This eases digital implementation. In this dissertation the modulus was implemented programmable ( $1 \leq MOD \leq 63$ ). A requirement in the programmable accumulator was a binary magnitude comparator. This was implemented in a novel way by using the carry out bit of a standard binary subtractor.

#### **6.1.6 Power dissipation**

A nominal IC power dissipation of 710 mW was observed. This is high in terms of conventional CMOS terms but in comparison to many high performance GaAs HBT synthesizer ICs (see TABLE I) it is a major improvement.

#### **6.1.7 High voltage CP**

A high voltage off-chip BJT charge-pump circuit was demonstrated for low out-band phase noise operation with high gain wide tuning range VCOs.

#### **6.1.8 Fractional spurious compensation network**

An off-chip LC network was added to an existing passive loop filter to aid in the suppression of fractional spurs. A 50 dB improvement was seen over the conventional loop filter implementation.

## **6.2 RECOMMENDATIONS FOR FUTURE WORK**

The results from this research are very promising and indeed it seems possible that well designed low noise CMOS synthesizer ICs can rival GaAs HBT synthesizer ICs in many areas. There are however a few suggestions and considerations for future work on this topic.

### **6.2.1 MOSFET flicker noise**

The biggest obstacle for future work will be the inherently high flicker noise of any MOSFET design. This is quite apparent in CML architectures. Figure 90 clearly illustrates the flicker noise difference between the referenced GaAs HBT device and the prototyped IC. As a way forward a RF phase noise simulator must definitely be used to optimise CML circuits for phase noise. One such a simulator is SpectreRF® from the Virtuoso© Cadence Design Systems suite. Additional methods could be further investigated to reduce flicker noise in MOSFETs.

### **6.2.2 CML 4-bit counter architecture**

The CML main divider proved operational to 1.6 GHz but not to 2.3 GHz as was simulated. The CML 2/3-prescaler however was proven operational to 2.7 GHz. It was then concluded from input sensitivity results that the LUT based CML 4-bit counter was at fault. The speed deficiency of the counter is speculated to the large interconnect distances associated with the design. It is then recommended that a standard more conventional synchronous counter architecture be implemented as depicted in Figure 7. This implementation should have reduced long distance interconnects.

### **6.2.3 SiGe HBT implementation**

If a higher performance synthesizer IC is required and a moderate escalation in IC manufacturing costs is acceptable, then a SiGe HBT design may be the solution. This research contains a collection of low noise design techniques which can be made applicable to other IC processes. A SiGe design will address many of the limitations associated with CMOS processes, such as flicker noise and speed. CML circuits are particularly well suited for SiGe HBT implementation.

## REFERENCES

- [1] D. Banerjee, “*PLL Performance, Simulation, and Design*”, National Semiconductor, 1998.
- [2] I. Thompson and P.V. Brennan, “Phase noise contribution of the phase/frequency detector in a digital PLL frequency synthesiser”, *Proc.: IEE Circuits, Devices and Systems*, vol. 150, no. 1, pp.1-5, Feb. 2003.
- [3] T.A.D. Riley, N.M. Filiol and J.Q. Du Kostamovaara, “Techniques for in-band phase noise reduction in  $\Delta\Sigma$  synthesizers”, *IEEE Trans. on Circuits and Systems II: Analog and Digital Signal Processing*, vol. 50, no. 11, pp. 794-803, Nov. 2003.
- [4] W. Rhee, B. Sup-Song and A.A. Ali, “A 1.1 GHz CMOS fractional- $N$  frequency synthesizer with a 2-b third-order  $\Delta\Sigma$  modulator,” *IEEE Jour. Solid-State Circuits*, vol. 35, no. 10, pp. 1453-1460, Oct. 2000.
- [5] S. Willingham, M. Perrott, B. Setterberg, A. Grzegorek, B. McFarland, “An integrated 2.5 GHz  $\Delta\Sigma$  frequency synthesizer with 5  $\mu$ s settling and 2 Mb/s closed loop modulation,” *Proc. of the International Solid-State Circuits Conf.*, San Francisco, pp. 200-201, Feb. 2000.
- [6] ADF4002 datasheet, “400 MHz frequency synthesizer”, Analog Devices. Available: <http://www.analog.com>.
- [7] ADF4108 datasheet, “8.0 GHz PLL frequency synthesizer”, Analog Devices. Available: <http://www.analog.com>.
- [8] HMC700 datasheet, “8 GHz 16-Bit Fractional- $N$  Synthesizer”, Hittite Microwave Corporation. Available: <http://www.hittite.com>.

- [9] HMC698 datasheet, “7 GHz integer- $N$  synthesizer ( $N = 12 - 259$ )”, Hittite Microwave Corporation. Available: <http://www.hittite.com>.
- [10] HMC440 datasheet, “2.8 GHz Integer- $N$  synthesizer ( $N = 2 - 32$ )”, Hittite Microwave Corporation. Available: <http://www.hittite.com>.
- [11] H. Hedayati, W. Khalil, B.M. Bakkaloglu, “A 1 MHz Bandwidth, 6 GHz 0.18  $\mu\text{m}$  CMOS Type-I Fractional- $N$  Synthesizer for WiMAX Applications”, *IEEE Jour. of Solid-State Circuits*, vol. 44, no. 12, pp. 3244-3252, Dec. 2009.
- [12] M. Guermandi, E. Franchi, A.H. Gnudi, “A CMOS 90 nm 55 mW 3.4-to-9.2 GHz 12 Band Frequency Synthesizer for MB-OFDM UWB”, *IEEE Microwave and Wireless Components Letters*, vol. 19, no. 11, pp. 752-754, Nov. 2009.
- [13] F.M. Gardner, *Phase lock techniques*, Wiley, 1979.
- [14] J. van de Vegte, *Feedback Control Systems*, 2<sup>nd</sup> ed., Prentice-Hall, 1990
- [15] K. Shu and E. Sánchez-Siencio, *CMOS PLL Synthesizers Analysis and Design*, New York, Springer, 2005.
- [16] C.S. Vaucher, I. Ferencic, M. Locher, S. Sedvallson, U. Voegeli, Z. Wang, “A Family of Low-Power Truly Modular Programmable Dividers in Standard 0.35  $\mu\text{m}$  CMOS Technology”, *IEEE Jour. Solid-State Circuits*, vol. 35, no. 7, pp. 1039-1045, Jul. 2000.
- [17] HP Bench Briefs, May-Aug. 1977.
- [18] C.A. Sharpe, “A 3-state phase detector can improve your next PLL design”, *EDN*, pp. 55-59, Sept. 1976.



- [19] F.M. Gardner, "Charge-Pump Phase-Lock Loops," *IEEE Trans. on Communications*, vol. 28, pp. 1849-1858, Nov. 1980.
- [20] M. Mansuri, D. Liu, C.K.K. Yang, "Fast Frequency Acquisition Phase-Frequency Detectors for GSamples/s Phase-Locked Loops", *IEEE Jour. Solid-State Circuits*, vol. 37, no. 10, pp. 1331-1334, Oct. 2002.
- [21] J. Craninckx and M. Steyaert, *Wireless CMOS Frequency Synthesizer Design*, 1<sup>st</sup> ed., Kluwer, 1998.
- [22] B. Razavi, *Design of Analog CMOS Integrated Circuits*, 1<sup>st</sup> ed., McGraw-Hill, 2001.
- [23] W.O. Keese, "An analysis and performance evaluation of a passive filter design technique for charge pump phase-locked loops", *National Semiconductor, Application note AN-1001*, May 1996.
- [24] ADIsimPLL®, "PLL Design & Simulation for Analog Devices's PLLs", Analog Devices. Available: <http://www.analog.com>.
- [25] C.J. Grebenkemper, "Local Oscillator Phase Noise and its effect on Receiver Performance," *Watkins-Johnson Company: Tech Note*, vol. 8, no. 6, Nov./Dec. 1981.
- [26] "Specifications and Measurement of Local Oscillator Noise in Integrated Circuit Base Station Mixers", *Maxim Integrated Products, Application Note AN-2021*, May 2003.
- [27] Brannon B., "Sampled Systems and the Effects of Clock Phase Noise and Jitter", *Analog Devices Application Note-AN756*.
- [28] P.R. Gray, P.J. Hurst, S.H. Lewis and R.G. Meyer, *Analysis and design of analog integrated circuits*, 4<sup>th</sup> ed., Wiley, 2001.

- [29] S. Haykin, *Communication Systems*, 2<sup>nd</sup> ed., Wiley, 1983.
- [30] A.S. Sedra and K.C. Smith, *Microelectronic Circuits*, 5<sup>th</sup> ed., Oxford University Press, 2004.
- [31] A. van der Ziel, *Noise in Solid State Devices and Circuits*, 1<sup>st</sup> ed., Wiley, 1986.
- [32] S. Tedja, J. Van der Spiegel and H.H. Williams. “Analytical and Experimental Studies of Thermal Noise in MOSFETs”, *IEEE Trans. on Electron Devices*, vol. 41, no. 11, pp. 2069-2075, Nov. 1994.
- [33] F. Dulger, E. Sanchez-Sinencio and A. Bellaouar, “Design considerations in a BiCMOS dual-modulus prescaler”, *Proc.: IEEE Radio Frequency Integrated Circuits (RFIC) Symposium*, pp. 177-180, Philadelphia, 8-10 Jun. 2002.
- [34] K.H. Lundberg, “Noise Sources in Bulk CMOS”, MIT papers.  
<http://web.mit.edu/klund/www/papers>
- [35] P. White, “Understanding Phase Noise From Digital Components in PLL Frequency Synthesizers,” *Applied Radio Labs: Design file DN006*, December 2000.
- [36] J. Rabye, *Digital Integrated Circuits*, Prentice Hall, 1996.
- [37] M. Alioto and G. Palumbo, *Model and Design of Bipolar and MOS Current-Mode Logic (CML, ECL and SCL Digital Circuits)*, Springer, 2005.
- [38] T. Kuboki, A. Tsuchiya and H. Onodera, “Low-Power Design of CML Drivers for On-Chip Transmission-Lines”, *IEICE Trans. on Electronics 2007 (E90-C)*, vol. 6, no. 1, pp. 274-1281, 2007.

- [39] S. Badel, I. Hatirnaz and Y. Leblebici, "Semi-automated design of a MOS current-mode logic standard cell library from generic components", *Research in Microelectronics and Electronics*, 2005 PhD, vol. 2, pp. 155-158, July 2005.
- [40] M.M. Green and U. Singh, "Design of CMOS CML circuits for high-speed broadband communications", *Proc. of the 2003 IEEE International Symposium on Circuits and Systems*, vol. 2, pp. 204-207, Bangkok, 25-28 May 2003.
- [41] M.T. Terrovitis and R.G. Meyer, "Noise in current-commutating CMOS mixers", *IEEE Jour. Solid-State Circuits*, vol. 34, no. 6, pp. 772-783, June 1999.
- [42] E.J. Brauer and Y. Leblebici, "Sub-70 ps Full Adder in MOS Current-Mode Logic Using 0.18 $\mu$ m CMOS Technology", *IASTED International Conf. Circuits, Signals, and Systems*, Clearwater Beach, 28 Nov.- 11 Dec. 2004.
- [43] J. Twomey, "Designing analog and mixed-signal circuits on digital-CMOS processes", *EDN*, pp. 109-116, Aug. 2000.
- [44] T.E. Kolding, "Compact Model Specification of RF MOSFET with DC and AC Evaluations", *Technical Report R99-1005, RF Integrated Systems & Circuits (RISC) group*, Sept. 1999.
- [45] H.D. Wohlmuth and D. Kehrer, "A high sensitivity static 2:1 frequency divider up to 27GHz in 120nm CMOS", *Proc. of the 28th European Solid-State Circuits Conf. ESSCIRC 2002*, pp. 823- 826, Florence, 24-26 Sept. 2002.
- [46] H.D. Wohlmuth and D. Kehrer, "A 15 GHz 256/257 dual-modulus prescaler in 120 nm CMOS", *Proc. of the 29th European Solid-State Circuits Conf. ESSCIRC 2003*, pp. 77-80, Estoril, 16-18 Sept. 2003.

- [47] K.L.J. Wong, A. Rylyakov and C.K.K. Yang, "A broadband 44-GHz frequency divider in 90-nm CMOS", *Proc. of the IEEE Compound Semiconductor Integrated Circuit (CSIC) Symposium*, pp. 196-199, Palm Springs, 30 Oct. - 2 Nov. 2005.
- [48] C.H. Long and C.T.G. Leung, *Low-Voltage CMOS RF Frequency Synthesizers*, Cambridge, Cambridge University Press, 2004.
- [49] R.B. Staszewski and P.T. Balsara, *All-Digital Frequency Synthesizer in Deep-Submicron CMOS*, Wiley, 2006.
- [50] Austriamicrosystems, "0.35  $\mu\text{m}$  CMOS C35 Process Parameters", ENG-182. Available: <http://www.austriamicrosystems.com>.
- [51] Tanner EDA Home Page. Tanner EDA. Available: <http://www.tanner.com/EDA/>
- [52] Austriamicrosystems, "0.35  $\mu\text{m}$  CMOS C35 Design Rules", ENG-183. Available: <http://www.austriamicrosystems.com>.
- [53] R.S. Widlar, "Some circuit design techniques for linear integrated circuits", *IEEE Trans. on Circuit Theory*, CT-12, 1968.

## APPENDIX A: EVALUATION PCB SCHEMATIC

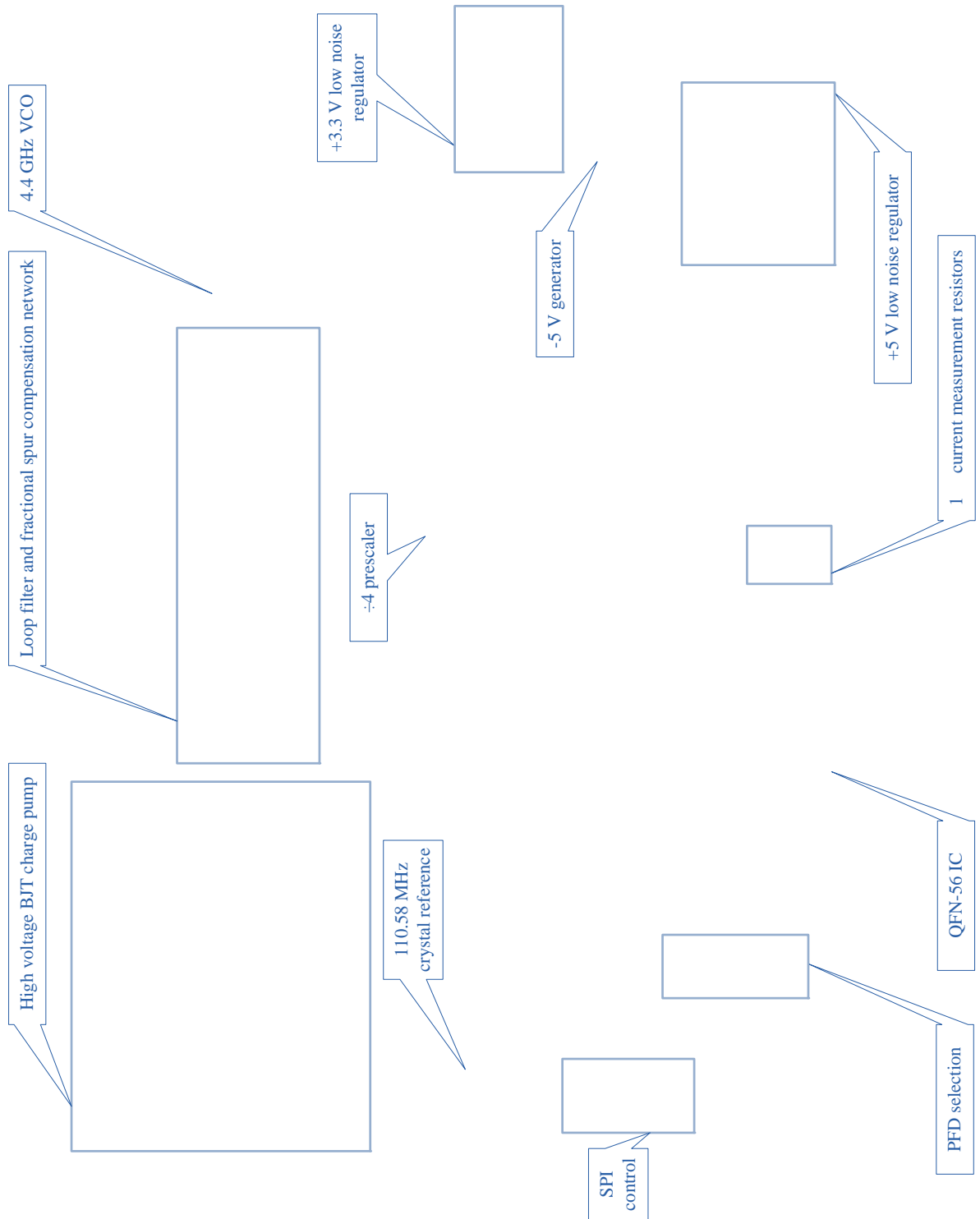


Figure A.1 Evaluation PCB schematic

## APPENDIX B: PROTOTYPED IC PHOTOGRAPHS

---

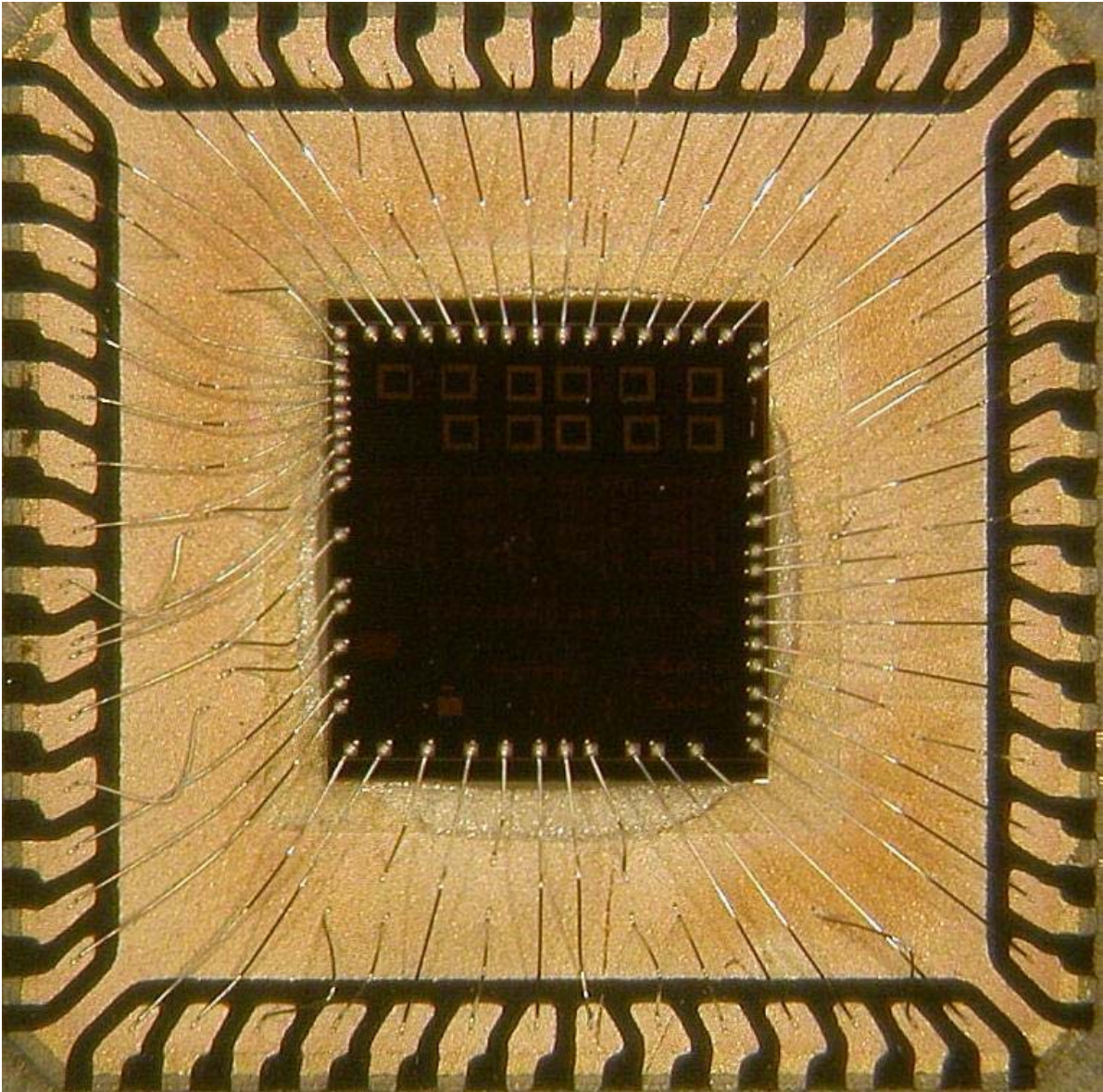


Figure B.1 QFN Frame bonding wires with dedicated ground bonding visible

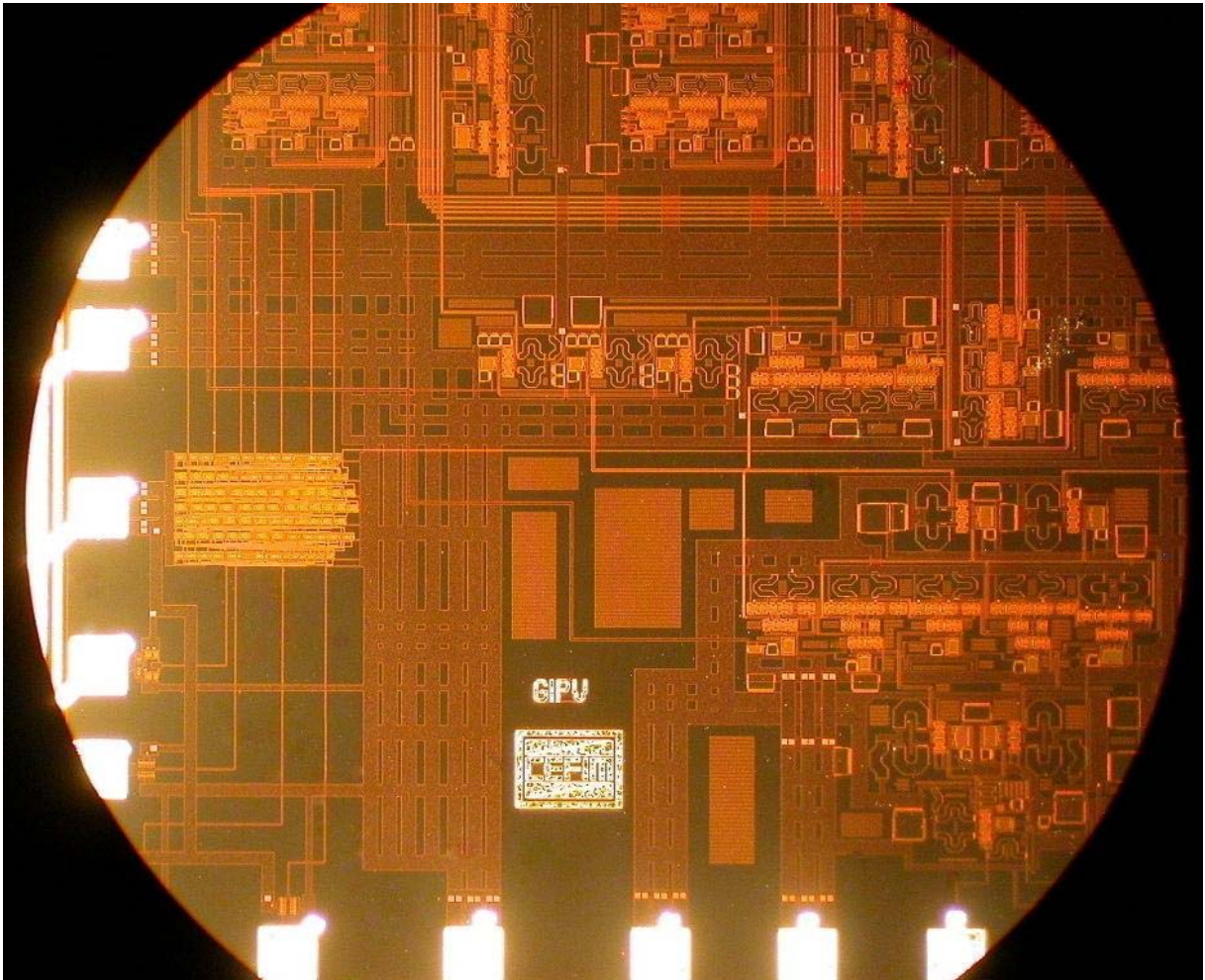


Figure B.2 CMOS control (left) and CML 2/3-prescaler (bottom right)

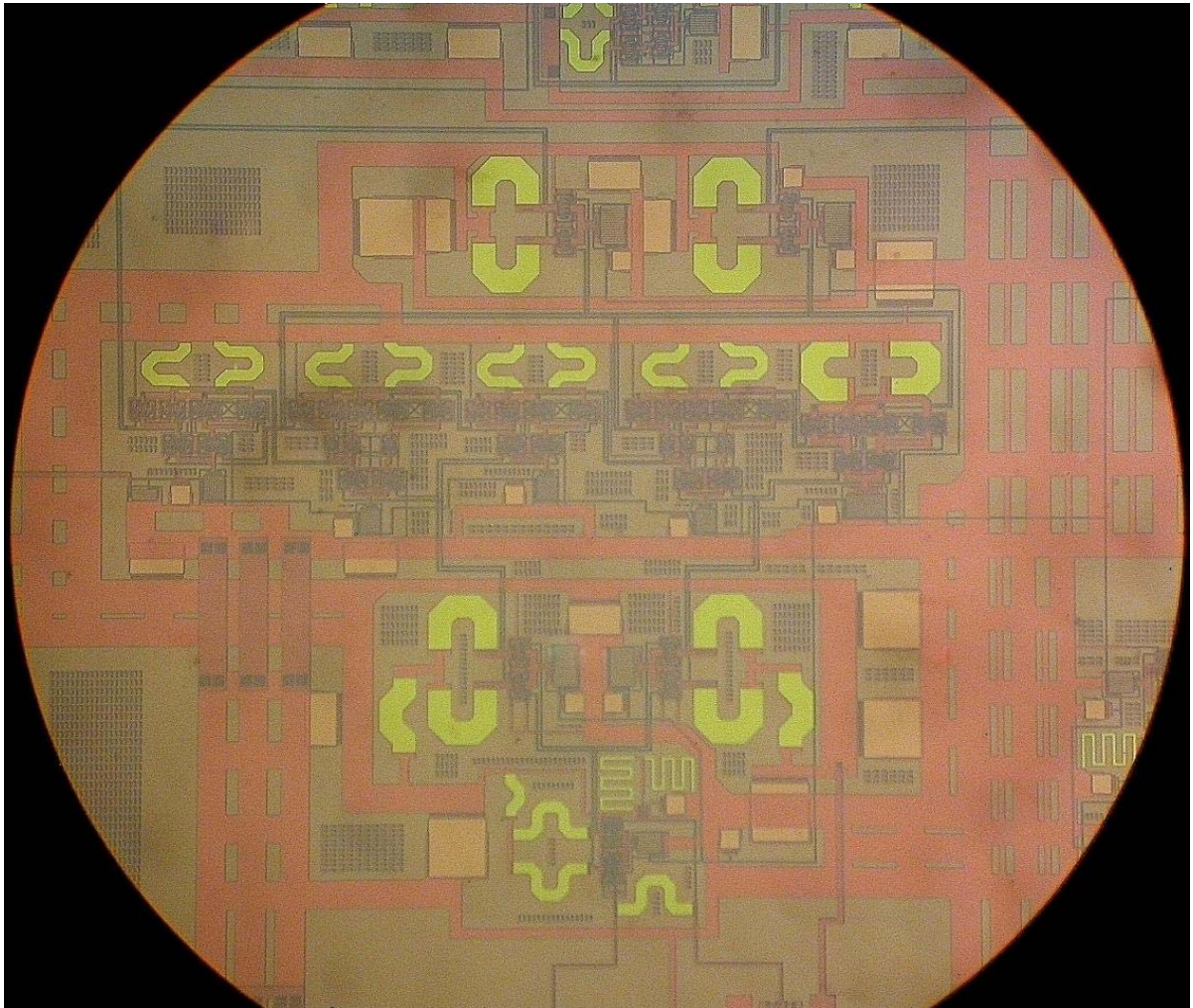


Figure B.3 Zoomed CML 2/3-prescaler



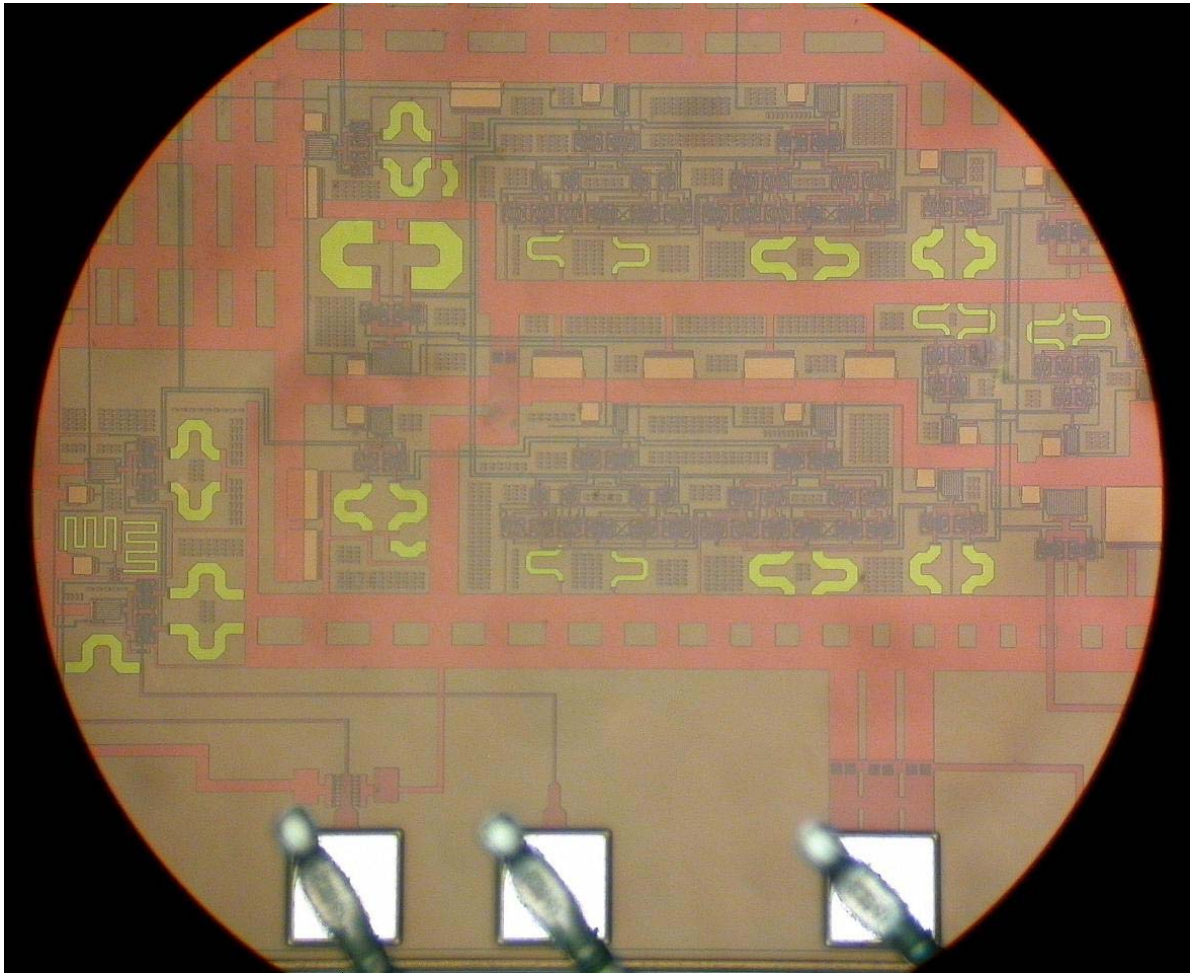


Figure B.4 Zoomed CML PFD (center) and reference clock amplifier (left)

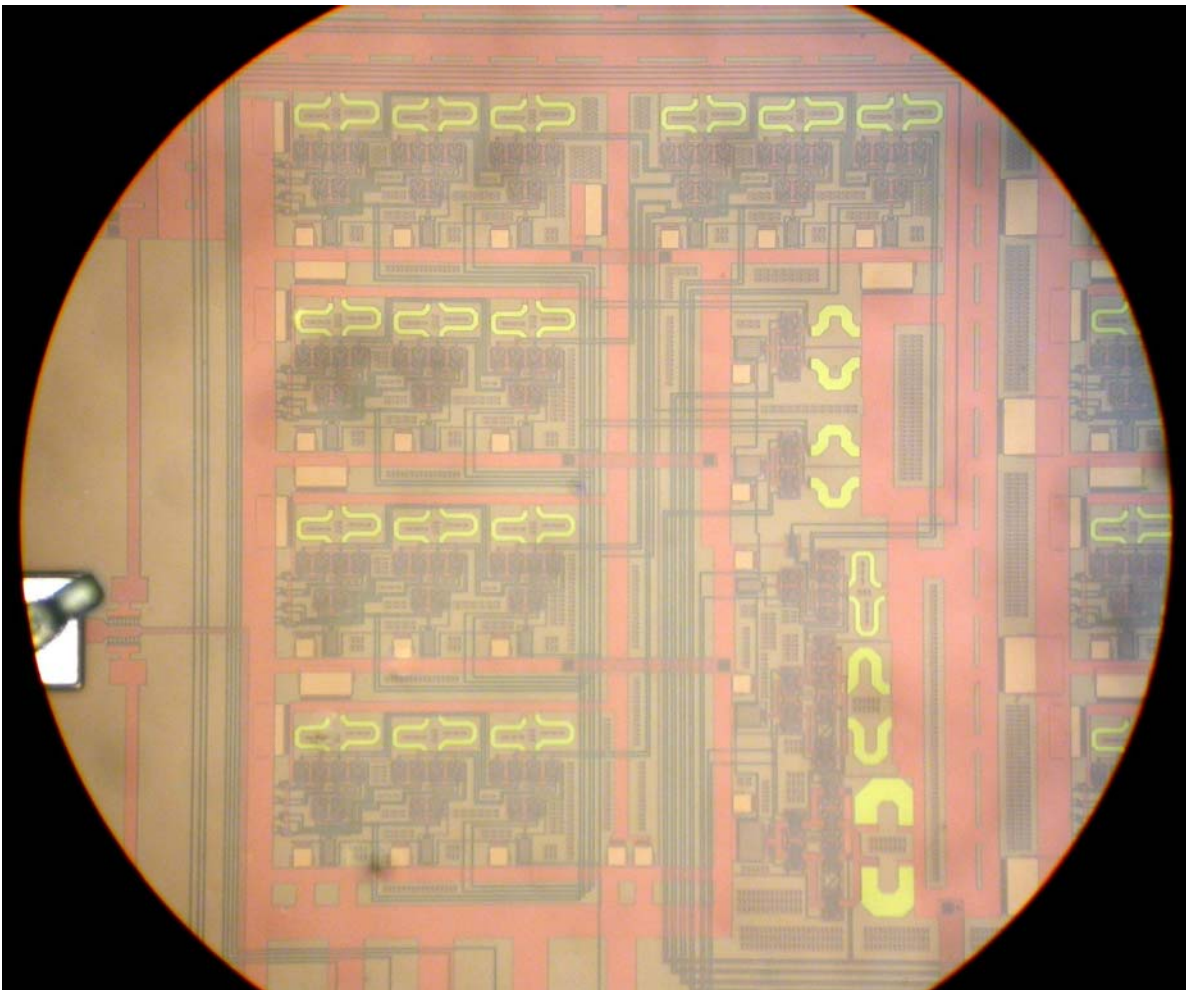


Figure B.5 Zoomed CML 16-1 Multiplexer

## APPENDIX C: TEST GRAPHICAL USER INTERFACE (GUI)

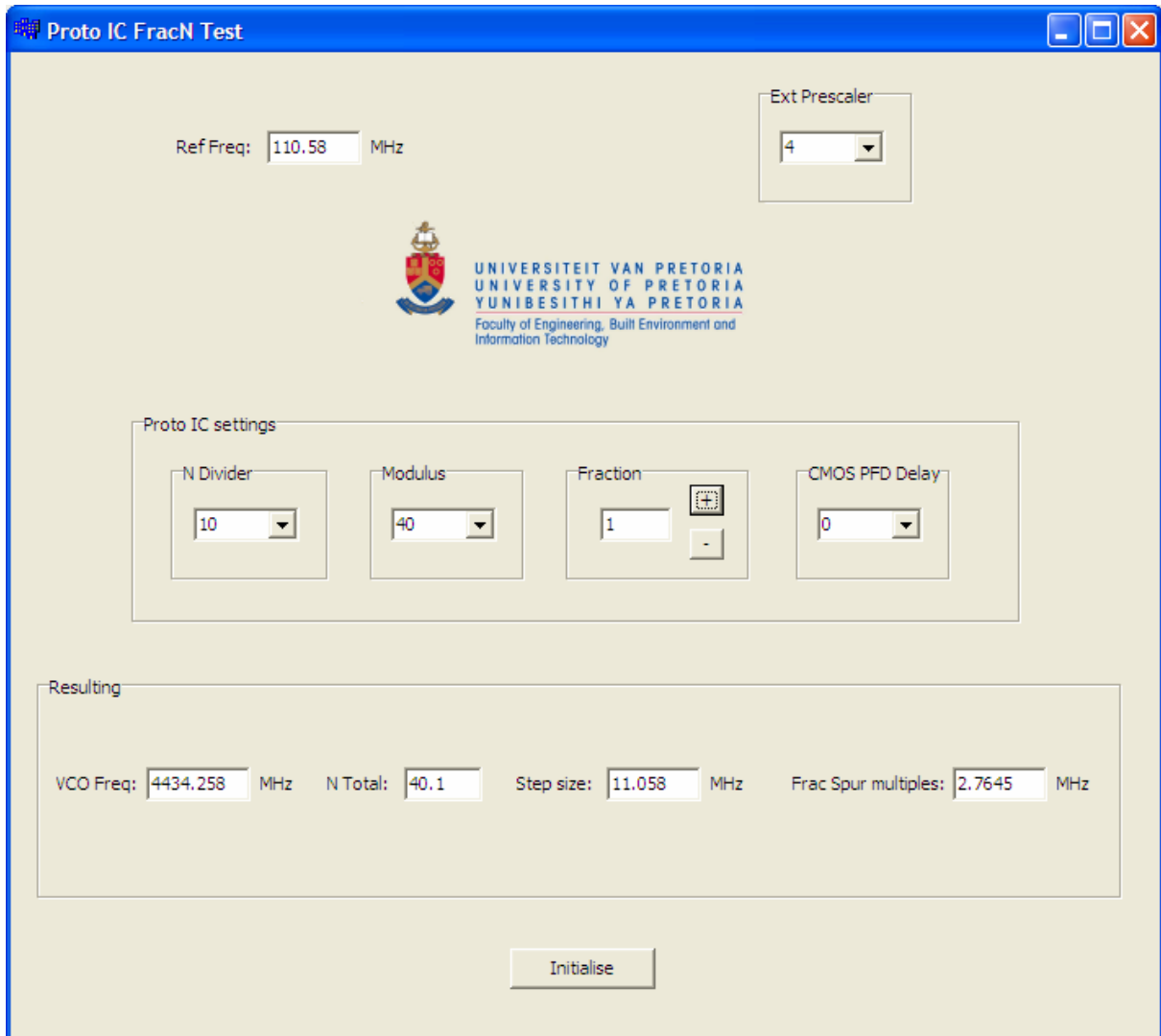


Figure C.1 Test GUI used to control the prototyped IC