EVALUATION OF Bi$_2$O$_3$ AND Sb$_6$O$_{13}$ AS OXIDANTS FOR SILICON FUEL IN TIME DELAY DETONATORS

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Abstract

This study considered bismuth (III) oxide (Bi$_2$O$_3$) and antimony hexatrittecooxide (Sb$_6$O$_{13}$) as potential substitutes for the red lead (Pb$_3$O$_4$) and barium sulphate (BaSO$_4$) oxidants currently used in time delay compositions for detonator assemblies.

Fine silicon powders with a specific surface area of 2 - 10 m$^2$/g were used as fuels. Some experiments were also done with a coarse manganese powder as fuel. Bi$_2$O$_3$ was synthesised by the thermal decomposition of (BiO)$_2$CO$_3$ by heating at 460°C for 15 hours. The yield was near quantitative, i.e. close to the 91.4% expected based on the complete conversion of the carbonate to the oxide. Sb$_6$O$_{13}$ was obtained by heating colloidal antimony pentoxide (Sb$_2$O$_5$) for 8 hours at 315°C. This resulted in a ca. 20% mass loss and yielded a reactive black powder.

In the Si-Bi$_2$O$_3$ system, compositions in the range 5 - 40% by mass Si were ignitable with shock tubing. Burn rates measured in lead tubes varied between 15 and 155 mm/s. This highest burn rate was obtained with 20% silicon. Addition of additives such as KMnO$_4$ and boric oxide had little effect on the burn rate. The fast burning Si-Bi$_2$O$_3$ system is a potential replacement for the commercial Si - red lead system.

The burning rate decreased with increasing compaction of the samples. Burn rate also decreased when the aluminium instead of lead tubes were used. This is attributed to a greater heat loss with the former.

The combustion products were characterised using DTA, FT-IR, XRD and SEM. The results show that the combustion reactions led to reduction of the oxidant to the corresponding metal form.

The Sb$_6$O$_{13}$-Si system requires an initiating composition such as Bi$_2$O$_3$-50%Si (Type 4). It is slow burning and thus a possible replacement for the commercial BaSO$_4$-Si system. The lowest sustainable and reproducible burn rate, in the absence of additives, was 4.8 mm/s. It was achieved using 10% silicon Type 4. Adding small
amounts of fumed silica (<2%) increased the burn rate. This is attributed to better mixing and compaction. However, lower burn rates (~2 mm/s) are possible if more fumed silica is added as inert diluent.

Replacing the silicon fuel with manganese powder gave more exothermic and even slower burning compositions.

**Keywords:** Pyrotechnic time delay compositions, bismuth oxide, antimony hexatridecoxide (Sb$_6$O$_{13}$), silicon.
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I am very proud for my fellow-countrymen. They were very helpful!

Finally, I would like to dedicate this work to my dear mother, my family and my family in law for their prayers and deep love. My deceased father would have been very proud of his son.

For my pretty wife Masele and our brilliant children (Divin, Eternel and Beniciel), it is the crown of my Love.
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<tr>
<td>$C_p$</td>
<td>heat capacity</td>
<td>J/mol.K</td>
</tr>
<tr>
<td>$D$</td>
<td>diffusion coefficient</td>
<td>-</td>
</tr>
<tr>
<td>$E_a$</td>
<td>Arrhenius activation energy</td>
<td>J/mol.K</td>
</tr>
<tr>
<td>$g(n)$</td>
<td>reaction order $n$ and varies between 1 and 2</td>
<td>-</td>
</tr>
<tr>
<td>$G$</td>
<td>Gibbs free energy change</td>
<td>J/mol</td>
</tr>
<tr>
<td>$H$</td>
<td>enthalpy change</td>
<td>J/mol</td>
</tr>
<tr>
<td>$k$</td>
<td>rate constant</td>
<td>1/s</td>
</tr>
<tr>
<td>$k_0$</td>
<td>pre-exponential factor</td>
<td>1/s</td>
</tr>
<tr>
<td>$L$</td>
<td>thickness of the oxide layer</td>
<td>mm</td>
</tr>
<tr>
<td>$P$</td>
<td>pressure</td>
<td>kPa</td>
</tr>
<tr>
<td>$q$</td>
<td>reaction heat</td>
<td>J/mol.s</td>
</tr>
<tr>
<td>$\dot{q}$</td>
<td>rate of heat release</td>
<td>J/mol.s</td>
</tr>
<tr>
<td>$S$</td>
<td>entropy change</td>
<td>J/mol.K</td>
</tr>
<tr>
<td>$t$</td>
<td>time</td>
<td>s</td>
</tr>
<tr>
<td>$T_{ad}$</td>
<td>adiabatic reaction temperature</td>
<td>K</td>
</tr>
<tr>
<td>$T_c$</td>
<td>the maximum temperature of the burning column</td>
<td>K</td>
</tr>
<tr>
<td>$T_{ign}$</td>
<td>critical ignition temperature</td>
<td>K</td>
</tr>
<tr>
<td>$T_m$</td>
<td>melting point</td>
<td>mm/s</td>
</tr>
<tr>
<td>$u$</td>
<td>burn speed</td>
<td>m³/s</td>
</tr>
<tr>
<td>$w$</td>
<td>volume of oxygen</td>
<td>m³</td>
</tr>
<tr>
<td>$x$</td>
<td>degree of conversion</td>
<td>mm</td>
</tr>
<tr>
<td>$Z$</td>
<td>distance in the column of reaction</td>
<td></td>
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### Greek symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Units</th>
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<tr>
<td>$\alpha$</td>
<td>thermal diffusivity</td>
<td>m²/s</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>thermal conductivity</td>
<td>W/m.K</td>
</tr>
<tr>
<td>$\rho$</td>
<td>density</td>
<td>kg/m³</td>
</tr>
<tr>
<td>$\theta$</td>
<td>Bragg angle</td>
<td>-</td>
</tr>
<tr>
<td>$\varsigma$</td>
<td>factor of direction</td>
<td></td>
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### Subscripts

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<td>$Ar$</td>
<td>Arrhenius</td>
</tr>
<tr>
<td>$l$</td>
<td>liquid</td>
</tr>
<tr>
<td>$o$</td>
<td>initial conditions</td>
</tr>
<tr>
<td>$R$</td>
<td>reaction</td>
</tr>
<tr>
<td>$s$</td>
<td>solid</td>
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1. Introduction

1.1 Pyrotechnic time delay systems

Pyrotechnics applications include military and civilian devices such as flares, tracers, signals, smokes, incendiaries and fireworks. Pyrotechnic delay systems are used in detonator assemblies to delay the terminal reaction by a precisely adjustable time interval that is determined by the burning rate of the composition (Ellern, 1968).

A detonator consists of a casing (aluminium tube), an explosive element, an initiator, a delay element, antistatic cap, a shock tube and a grommet (See Figure 1). The explosive element usually contains pentaerythritol tetranitrate (PETN) as the base charge. The initiator typically consists of a lead azide/lead styphnate mixture and is placed on top of the base charge. The delay element consists of a column of deflagrating explosive encased in a lead/aluminium tube. The antistatic cap serves to prevent static ignition and the grommet serves as seal and clamp for the shock tube. The delay composition is ignited by an electric discharge from an electric shock box via a shock tube and the shock cap. The time taken by the combustion wave to travel the length of the deflagrating explosive is called the delay between the initiation impulse and the detonation of the base charge. Delay times ranging from microseconds to a few seconds are generally required.

![Figure 1.1 A typical detonator assembly.](image)

The delay composition is constituted from a fuel and an oxidiser in the solid state. This redox reaction is readily initiated by a temperature impulse. The reaction commences as a self-propagating combustion wave that proceeds along the active
element at a constant velocity. The burning process in pyrotechnic time delays is analogous to the Self-propagating High Temperature Synthesis (SHS) method for ceramics. The latter is used to synthesize high refractory and abrasive compounds, e.g. borides, carbides, nitrides, silicides as monolithic components with desirable structural homogeneity (Munir, 1988).

1.2 Conventional delay composition

Delay elements in Shock Tube detonators are used to provide a delay between the time of ignition (from the spit of a Shock Tube) to the time of initiation of the explosive base charge. Typically delay times may vary from 20 ms to 10 s. This delay time is governed by the type of composition used in the element and the length of the element. Commercial shock tube detonators can have a 1, 2 or 3 element stack depending on their delay. All detonators have a sealing element with a narrow internal bore of pyrotechnic. This composition forms a hot slag once burnt that seals the element column and prevents venting of gases. This is critical in driving the burning front forward in a controlled manner. For the short period delays the sealing unit is the only element in the detonator and it thus acts as the timing element. For delays 150 – 1500 ms, the element stack comprises additional timing elements. For long time delays a starter element is required due to the insensitivity of the compositions used for the timing element. Process constraints restrict the length of the elements between 5 and 25 mm (to be extended to 40mm).

The pyrotechnic composition contains two or more reagents (fuel and oxidant) capable of a highly exothermic, propagating oxidation-reduction reaction. The most commonly used combinations are Si/Pb₃O₄ for short-period delays (SPD) ranging between 0.5 and 1000 ms and Sb/KMnO₄ for long period delays (LPD) between 0,5 and 13 seconds. Silicon is invariably used as the fuel although different grades of different particle size may be used. Burn rate is commonly controlled by the choice of oxidant. Typical oxidants include: red lead (Pb₃O₄), lead dioxide (PbO₂) and barium sulphate (BaSO₄).
1.3 Purpose of the present study

This project is part of a larger research effort with the ultimate objective of developing “green” pyrotechnic delay compositions that:

- Are easy and safe to process into delay elements,
- Burn in a lead or rigid tube within a specific burning speed range (from $\pm 4\text{ms/mm}$ to $\pm 250\text{ms/mm}$),
- Feature highly consistent ignition and burn rate performance (batch variation <2%), and
- Consist of a single fuel in combination with a single oxidant system together with additives for modulating burn rate.

This study considers bismuth oxide and antimony hexatridecoxide as potential replacements for the current lead and barium-based compounds. Lead-based compounds are highly toxic and their use needs to be curtailed. The lead tubes that are currently used will ultimately also have to be replaced (De Vito, 1995).

Bismuth subcarbonate ($\text{(BiO}_2\text{CO}_3$)) and bismuth oxide ($\text{Bi}_2\text{O}_3$) are much less toxic than lead compounds (Kruger et al., 1985). $\text{Bi}_2\text{O}_3$ is formed when $\text{(BiO}_2\text{CO}_3$ is thermally decomposed. It was selected for study because of its potential to replace red lead in millisecond pyrotechnic delay compositions. Attempts were made to increase burn rates in the Si-$\text{Bi}_2\text{O}_3$ system by using additives such as boron, boric oxide and potassium permanganate.

Antimony hexatridecoxide ($\text{Sb}_6\text{O}_{13}$) was investigated as a potential replacement of barium sulphate in long-period delays. It was prepared by an 8-hour thermal decomposition of colloidal antimony pentoxide ($\text{Sb}_2\text{O}_5$) at 315°C. In this case the influence of inert diluent (fumed silica) on the minimal burning rate was considered.

Lead tubes have found widespread use in delay elements owing to their considerable malleability. It allows facile compaction of the powder by a tube rolling process. Environmental concerns are restricting the use of lead-based materials. In future the lead tubes also need to be replaced. Consequently, the use of aluminium and
ceramic (alumina or pyrophillite) rigid delay were investigated. In these the effect of core diameter on the burn rate was determined.
2 Literature Review

2.1 Introduction

Delay elements in shock tube detonators are used to provide a delay between the times of ignition (e.g. from the spit of a shock tube) and initiation of the explosive base charge. The delay element system is an assembly comprising an ignition source, a small-diameter tube containing a compressed composition and an ignition transfer system (Wilson and Hancox, 2001). The type of composition, the dimensions of the element, i.e. its length and diameter, and the material of construction of the tube govern the delay time. A typical pyrotechnic delay composition consists of a fuel and an oxidant in combination with an optional binder. It is capable of an exothermic oxidation-reduction reaction. Following ignition, a combustion wave travels down along the tube at a constant velocity that ensures the transmission of initiation impulse to the detonator in a precisely adjustable time interval.

Preferred delay compositions will burn in an essentially gasless fashion (volume of gas evolved less than 10 cm$^3$/g of mixture (Charsley et al., 1980)) and at a constant predetermined rate. The reaction must be exothermic, self-sustained and self-contained (Conkling, 1996).

2.1.1 Delay elements

A 'delay element' assembly consists of an ignition source, a tube filled with a pressed pyrotechnic composition and an ignition-transfer system (Wilson and Hancox, 2001). The combustion process of the pyrotechnic composition provides the required delay time interval between successive mechanical, electric or explosive events. Typically this ranges from a few tens of milliseconds to several minutes.

Any composition will take a finite time to burn over a given length. However, the requirements of safety, time reproducibility and ignition transfer reliability, particularly in modern military applications, have resulted in the development of specific
formulations known as pyrotechnic delays. Compositions of this type, when consolidated into a tube, burn at reproducible linear rates.

2.1.2 Pyrotechnic delay compositions

Until World War II, black powder was the basis of virtually all delay elements. It provides quite accurate time intervals. Black powder consists essentially of a 75:15:10 KN_3—charcoal—sulphur composition. The drawback is the significant volume of permanent gas formed during combustion (about 300 ml/g of mixture) (Ellern, 1968). Modern weapons require higher performance levels with respect to reliability and reproducibility under a wide range of environmental conditions (pressure, temperature, moisture). This led to the replacement of the gassy delay systems with gasless delays. Actually, the latter are not exactly gasless as they do produce a small amount of permanent gas during combustion. However, they do provide an advantage with respect to greater burn stability: The burn rate is less affected by pressurisation of the burning front. These delay elements provide constant time intervals unaffected by external conditions. Time delays are the same whether the system operates at great depth underwater or in the vacuum of space. Moreover, hermetically sealed delay elements incorporating gasless delays can be stored for long periods without deterioration (Wilson and Hancox, 2001).

Table 2.1. Common oxidants and fuels used in time delay formulations (Krone et al., 1992)

<table>
<thead>
<tr>
<th>Oxidants</th>
<th>Fuels (non metals)</th>
<th>Fuels (metals)</th>
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<tbody>
<tr>
<td>Chlorates</td>
<td>Boron</td>
<td>Aluminium</td>
</tr>
<tr>
<td>Chromates</td>
<td>Carbon</td>
<td>Chromium</td>
</tr>
<tr>
<td>Dichromates</td>
<td>Phosphorus</td>
<td>Iron</td>
</tr>
<tr>
<td>Iodates</td>
<td>Selenium</td>
<td>Magnesium</td>
</tr>
<tr>
<td>Nitrites</td>
<td>Silicon</td>
<td>Manganese</td>
</tr>
<tr>
<td>Oxides</td>
<td>Sulphur</td>
<td>Molybdenum</td>
</tr>
<tr>
<td>Perchlorates</td>
<td></td>
<td>Titanium</td>
</tr>
<tr>
<td>Peroxides</td>
<td></td>
<td>Tungsten</td>
</tr>
<tr>
<td>Permanganates</td>
<td></td>
<td>Zirconium</td>
</tr>
<tr>
<td>Sulphides</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 2.1 lists some of the materials currently used in pyrotechnic delay formulations. Preferably the formulation should be non-hygroscopic; stable during handling and compaction; not affected by temperature; be readily ignitable and react without releasing gases to minimise the effects of pressure on the burn rate. In addition, a relatively low melting point or a polymorphic transition is also beneficial (McLain, 1980).

2.2 Solid State Reactions

2.2.1 The solid state

Most solids are crystalline in nature, i.e. they have a homogeneous structure in which the constituent atoms are arranged in a regularly repeated pattern. These repeated units are linked together in different ways: covalent bonds, ionic, metallic, or sometimes hydrogen and Van der Waal’s bonds. The physical properties of a solid depend largely on the bonding forces and the specific crystal structure. With pyrotechnics the crystal habit, i.e. morphology also plays an important role (Kosanke et al., 2000). However, the reactivity of a solid is highly dependent on the presence of imperfections such as lattice defects in the bulk solid (McLain, 1980).

2.2.2 Lattice defects

Some of defects that play a major role in the reactivity of solids are:

a) Inherent defects: These are essentially the Frenkel and Schottky defects, related to interstices and vacant sites in the lattice respectively.

b) Non-stoichiometric defects: It is well known that many chemical compounds deviate from stoichiometry; this is the case with some iron oxides, e.g. Fe$_{1-x}$O, due to the presence of some cation vacancies.

c) Dislocations: These may form as the growing crystal acquires more molecules that do not fit properly into the normal pattern. They are generally located between particle boundaries.

It has also been observed that most reactions of a liquid with a crystal begin at defect locations where bonds have been weakened (McLain, 1980).
2.2.3 Solid-state reactions

Reaction between a metal and a non-metal proceeds by two possible mechanisms: either the non-metal migrates through the product layer to the metal interface, or the metal migrates in the reverse direction. Since the reactant can migrate through the ionic product layer only as ions, electrons must also accompany the ionic migration. It appears obvious that reaction will not take place if the product layer is not capable of conducting electrons (McLain, 1980).

In the course of a solid-solid reaction, different reaction steps such as nucleation, growth, and transfer of matter across phase boundaries (by diffusion) occur. Besides defect thermodynamics, the diffusion theory forms the basis for the explanation of solid-solid reactions (Schmaltzried, 1976).

The role of defects in semi-conductors may be illustrated using the following reaction (McLain, 1980):

$$\text{Ge} + 2 \text{MoO}_3 \rightarrow \text{GeO}_2 + 2 \text{MoO}_2$$

Ge doped with n-type dopant (As and Sb) reacted with MoO$_3$ much faster than Ge doped with p-type dopants (Ga and In). The reactivity of Ge also depended on the concentration of the dopants. Increasing the concentration of the n-type dopants increased the rate of reaction, whereas increasing the concentration of p-type dopants decreased it. This observation is in agreement with the postulate stated below.

An oxidation-reduction reaction necessitates the transfer of electrons and can usefully be compared with semi-conductor activity. The reducing agent is the electron donor and the oxidising agent is the electron acceptor. This is analogous to the activity at an n-p semi-conductor junction where the n-type crystal creates the space charge potential by donating electrons to the p-type crystal. Therefore, an n-type reducing agent (Si doped with As) should be more reactive than a p-type (Si doped with Al) (McLain, 1980).
2.2.4 Solid-liquid reactions

Howlett et al. (1974) have shown that for the B-K$_2$Cr$_2$O$_7$ system, the ignition process is dependent on the transport of matter through a liquid phase. The combustion zone then propagates as a molten front.

Some eutectic oxide compositions have been used to increase the velocity of the wave front. They probably improve the reaction kinetics by increasing the interface between reactants. In these systems the surface tension of the liquid phase is relevant, because it determines the wettability of the granular reactants. Tribelhorn et al. (1995b) noted that the surface tension of Zn at its melting point is high compared to other low melting point metals, i.e. about twice that of Sb and Pb. Therefore, the movement of liquid Zn through pores and channels does not occur readily because the oxidant surfaces are not easily wetted.

2.2.5 Solid-solid and solid-gas reactions

Figure 2.1 illustrates the differences in the burning behaviours of loose and consolidated (compressed or compacted) powders. (Wilson and Hancox, 2001).

(a) Loose composition
Figure 2.1(a) shows a container filled with a loose pyrotechnic composition. An uncontrolled reaction ensues on initiation of the reaction because of the low bulk density of the filling, the travel of combustion products (gases, liquid and thermal radiation) and the added hot air through the voids. This may eventually lead to an explosion because of the confinement imposed by the container.

(b) Consolidated composition
By contrast, as shown in Figure 2.1(b), the compressed sample does not allow much motion for the combustion products through the consolidated column. Combustion is confined to a relatively thin propagation zone known as the ‘burning front’.
Tribelhorn et al. (1995a) showed that pyrotechnic systems differ with respect to their sensitivity to compaction. The burn rate in the Fe/BaO₂ system initially increases with increase in compaction pressure. Increase in compaction pressure increases interparticle contact and this aids solid-solid reactions. At higher compaction pressures the rate decreases again. This suggests that gas transport ahead of the burning front is important. In fact it was concluded that the combustion wave in this iron system is preceded by a flow of oxygen generated by the decomposition of the oxidant.

However, in other systems, e.g. Zn/KMnO₄, the burning rate is decreased by compaction (Tribelhorn et al., 1995b). This behaviour suggests that in this case the reaction rate is determined by solid-gas reactions: Oxidants such as SrO₂ and KMnO₄ decompose without melting to produce oxygen gas and a solid residue.

Increased compaction may decrease the surface accessible to the oxygen gas or
may trap the gas in closed pores. In loose powders the oxygen gas flows is not impeded and burning is fast.

Burning in the Sb/KMnO₄ system also occurs via gaseous intermediates. In this case the O₂ (g) arised from the decomposition of the oxidant and possibly even the Sb₂O₃ reaction product (Beck and Brown, 1986). The Zn /Pb₃O₄ system is even more complex. Here the gas phase contain Zn and Pb vapour as well as O₂ (g) generated by the decomposition of the oxidant.

2.2.6 Reactivity

Chemical reactivity of solids is affected by the degree of lattice vibrations. As temperature rises, crystal atoms or ions vibrate with increasing amplitude about their average positions in the lattice. This can be thought of as the loosening of the bonds holding the solid together. Diffusion is enhanced and the atoms may exchange positions. At a sufficiently high temperature this leads to melting. In addition, at a lower temperature this may induce a transition from one solid state to another, i.e. a phase change.

Tamman used the ratio of the temperature of the solid to its melting point as a rough measure of lattice loosening (Kosanke and Kosanke, 1997). Ionic surface mobility becomes effective at \( T/T_m \approx 0.3 \) and lattice diffusion at \( T/T_m \approx 0.5 \) (McLain, 1980).

Enhanced reactivity is observed near the phase transition temperature, due essentially, to a similar occurrence of lattice disturbances. This is called the 'Hedvall effect' (McLain, 1980).

McLain (1980) lists the following important factors that influence reactivity:

- Deviations from the normal crystallographic or amorphous structure of a substance
- Lattice defects in the form of hereditary structures
- Formation of imperfect structures, e.g. transition from one modification to another on thermal decomposition
- Presence of guest particles in the lattice
• Differences in the crystallographic formation of different surfaces
• Corrosion
• Adsorption and catalysis
• Irradiation by absorbable wavelength
• Changes in the magnetic state
• Changes in the electric state

*Hereditary structures*

The history of the sample and the way in which the mix was crystallised, its impurities and defect content, all influence its further behaviour. For example, sulphate-derived oxide (Fe$_2$O$_3$) is more reactive than Fe$_2$O$_3$ derived from iron oxalate despite the fact that the former had a larger average particle size (McLain, 1980). X-ray powder diffraction patterns revealed that the sulphate-derived Fe$_2$O$_3$ was less crystalline.

*Crystal shape*

The reactivity of KClO$_3$ in match-head formulation decreases as the crystal changes from needles to thin lamellae to near-spherical nodules (McLain, 1980). Kosanke and co-workers (2000) noted the same phenomenon with respect to the effect of particle shape on reactivity. They found that, for the same nominal mesh size, flakes have the greatest reactivity and that they can be raised more quickly to their ignition temperature.

*Mechanically enhanced reactivity*

Milling, pulverising, atomising and grinding are considered to be interesting techniques for breaking down as many atomic bonds as possible before the materials are used in combination with another reactant.

Fracturing a macrocrystal creates new surfaces, edges and corners where the atoms are not bonded as strongly as internal atoms. This enhances the reactivity. Similarly milling enhances reactivity more by introducing lattice deformation and distortions rather than by reducing particle size (McLain, 1980).
Addition of particles – doping

Supersensitive KClO₃: Doping KClO₃ with Cu(ClO₃)₂ made it supersensitive to the extent that its mixtures with sulphur were capable of a spontaneous high-order detonation (McLain, 1980).

Highly reactive Fe₂O₃: Doping by co-crystallisation also makes Fe₂O₃ more reactive (McLain, 1980). The doping was accomplished by growing crystals of CuSO₄·FeSO₄·xH₂O or NiSO₄·FeSO₄·xH₂O in an acidic solution of the salts. The crystals were subsequently decomposed in O₂ at 200 – 250°C to produce Fe₂O₃. This improved the calorific value of a 50:50 Fe₂O₃-Ti mixture.

Reactive NiO: Doping of NiO with LiO₂ and Cr₂O₃ had a positive effect on the reactivity of NiO.

Fluxes
Fluxes are materials that reduce the effective melting temperature of a mixture. They introduce an amount of liquid phase that accelerates the solid-solid reactions.

Presence of water
The role of water vapour as catalyst and accelerator in pyrotechnic reactions is well known. The burning rate and colour of firework star compositions depend markedly on very small changes in the moisture content. A very small amount of 0.1% H₂O (moisture content) seems to be most effective. Above this proportion, it was observed to have an inhibiting effect (McLain, 1980). Moreover, it is well known that the presence of water vapour has a noticeable effect on sintering, structural rearrangement and crystal coarsening of oxides.

These phenomena are ascribed to the chemisorption of water vapour on oxide surfaces and interfaces. This leads, among other things, to an increase in the surface and particle boundary mobility of ions (Ubaldini et al., 2003).
Corrosion inhibition
Chemical treatment to protect powder against corrosion is also a form of inhibition. This process does, therefore, lengthen the life of more reactive materials, including Al, Zn and Mg (McLain, 1980).

2.3 Pyrotechnic ignition and propagation

Kosanke and Kosanke (1997) provide an excellent review of the ignition and propagation processes in pyrotechnics. They describe pyrotechnics as mixtures of fuels, oxidisers and additives that are designed to produce energy on demand in the form of heat, light, sound, etc. Kosanke and Kosanke (1997) define ignition as the initiation of the self-sustained burning of the pyrotechnic material.

2.3.1 Thermodynamics of solid-solid reactions

Gasless pyrotechnic time delays are based on solid-solid oxidation-reduction reactions between an oxide and a metallic or non-metallic element. A unique characteristic of such reactions is the virtually total dependence on a favourable enthalpy change ($\Delta H_R$). The second law of thermodynamics demands, as condition for the spontaneity of a reaction conducted at constant temperature and pressure, that the Gibbs free energy change, $\Delta G_R$, must be negative:

$$\Delta G_R = \Delta H_R - T \Delta S_R$$

The entropy change, $\Delta S_R$, for reactions yielding solid products is usually very small (Spear, 1976). In addition, Kopp's rule states that the sum of the ionic specific heats remains unchanged. Thus, the only way in which $\Delta G_R$ can be large and negative is for $\Delta H_R$ to be negative. Therefore, the reaction must be exothermic.

Ellingham diagrams (Ellingham, 1944) show the variation with temperature of the standard Gibbs free energy of formation ($\Delta G^0$) of the oxides or sulphides of metals and non-metals. They indicate the relative tendencies of the elements to combine
with oxygen or sulphur. This permits rapid evaluation of the reducibility for a specific oxide or sulphide by a given elemental reducing agent. Figure 2.2 shows the Ellingham diagram for selected oxides with oxygen taken a gas at a partial pressure of 1 atm. In this figure the formation of an oxide from its element is written in the following standard form:

\[
\frac{2x}{yz} M_z + O_2 = \frac{2}{y} M_x O_y
\]

![Ellingham diagram for oxides of interest in the present study.](image)

For example for bismuth and silicon the oxidation reactions are:

\[
\begin{align*}
\text{Si} + O_2 &= \text{SiO}_2 \quad \text{(I)} \\
4/3 \text{Bi} + O_2 &= 2/3 \text{Bi}_2\text{O}_3 \quad \text{(II)}
\end{align*}
\]

The reduction of bismuth oxide by silicon is expressed by:

\[
2/3 \text{Bi}_2\text{O}_3 + \text{Si} = 4/3 \text{Bi} + \text{SiO}_2
\]

Note that the net reaction is obtained by adding the "reverse" of the second reaction (II), i.e. in the form of a reduction reaction, to the first reaction (I). Note that O₂ then
appears on both sides and thus cancels out! Thus the difference at a given
temperature between the values of $\Delta G^o$ on the diagram for these two reactions
represents the Gibbs free energy or driving force of the reaction.

The lower down on the diagram the curve for a particular oxide lies, the greater is its
stability and the lower is its reducibility (Ellingham, 1944). In Figure 2.2, for example,
the curve for the formation of the oxide of silicon lies lower than that of bismuth oxide.
This implies a positive tendency for elemental silicon to displace bismuth from its
oxide.

2.3.2 Adiabatic reaction temperature

Consider the following irreversible reaction:

$$A(s) + B(s) \rightarrow C(s)$$

The adiabatic reaction temperature $T_{ad}$ is the maximum temperature to which the
product C, with melting point $T_m$, can be raised as a result of the exothermic heat of
reaction. The adiabatic reaction temperature, for the reaction starting at 298°C, is
calculated as follows (Zuhair, 1988):

a) If $\Delta H_{R,298} < \int_{298}^{T_{ad}} C_p dT$, then $T_{ad} < T_m$ and it can be calculated from:

$$\Delta H_{R,298} = \int_{298}^{T_{ad}} C_p dT$$

(2)

b) If $\Delta H_{R,298} > \int_{298}^{T_{ad}} C_p dT$ then $T_{ad}$ is evaluated from:

$$\Delta H_{R,298} = \int_{298}^{T_m} C_p dT + \Delta H_m + \int_{T_m}^{T_{ad}} C_p dT$$

(3)

Preheating of the reactant mixture will result in a higher $T_{ad}$. 

16
When no phase transition occurs and physical properties can be assumed constant the adiabatic reaction temperature is given by:

\[ T_{ad} = T_o + \frac{\Delta H_R}{c_p} \]  

(4)

2.3.3 Ignition

The combustion of the delay composition starts with the initial process of ignition. Ignition may be defined as the visible appearance of a steady combustion. External factors influencing ignition include the heating rate, the ambient temperature and the size, geometry and nature of the surface of the sample. Thus Pickard (2002) defines the critical ignition temperature, \( T_{ign} \), as the minimum temperature to which a pyrotechnic charge of specified size, shape and boundary constraints must be heated in order to induce thermal runaway.

Figure 2.2 shows a schematic plot of the heat generated versus heat loss as a function of temperature (Kosanke and Kosanke, 1997). The generation of heat initially increases exponentially with temperature. This accords with the Arrhenius temperature dependence of the rate constants for oxidation. However, at higher temperatures the reaction rate becomes diffusion limited and the rate of heat generation tapers off. The rate of heat loss is roughly proportional to the difference in temperature between the flame and the surroundings.

The heat generation and heat loss curves intersect at three locations in the Frank-Kamenetzky plot shown in Figure 2.2. At these temperatures the rate of heat generation balances the rate of heat loss. Point A corresponds to a low temperature oxidation of the fuel. Point C corresponds to the equilibrium combustion temperature. Point B is unstable - at temperatures slightly lower than \( T_B \) the rate of heat loss exceeds the rate of heat generation and the material will cool down to \( T_A \). At temperatures slightly above \( T_B \) the exothermic heat generated will exceed the heat loss and the sample will spontaneously increase in temperature to the steady state flame temperature \( T_C \). Hence \( T_B \) corresponds to the ignition temperature under the test conditions. It is defined as the lowest temperature at which the sample
spontaneously ignites as witnessed by a sustained glow, the appearance of a flame or even an explosion.

![Figure 2.3 Frank-Kamenetzky plot of heat generation and heat loss versus temperature (Kosanke and Kosanke, 1997)](image)

**Figure 2.3** Frank-Kamenetzky plot of heat generation and heat loss versus temperature (Kosanke and Kosanke, 1997)

### 2.3.4 Solid state reactions: the importance of diffusion

Tribelhorn *et al.* (1995c) studied the burning behaviour of Zn/KMnO₄ mixtures in the composition range 30–75% Zn formed at compaction pressure up to 150 MPa. Based on thermal analysis results, they suggested that the Zn diffuses into the solid residue formed during the first stage of KMnO₄ decomposition. An exothermic reaction starting at 520°C was observed and attributed to the reaction of Zn with this ‘K₂MnO₄’ residue (Wilson and Hancox, 2001).

Drennan *et al.* (1992) reported on studies of the combustion of various systems, namely the Mn/BaO₂, Mo/BaO₂, Mn/SrO₂ and Mo/SrO₂ systems, and Tribelhorn *et al.*
(1995a) on the Fe/BaO₂ and Fe/SrO₂ systems. If we referred to the corresponding radii of the different metals and ionic species involved in the combustion, the diffusion via cation vacancies in the oxidant structure should be favoured in the BaO₂ lattice rather than in the SrO₂ lattice. However, for comparable oxidation states, the differences between the behaviour of Mn and Mo based on geometry should be small.

It was also observed after examination of the products from the combustion of Zn/peroxide systems that oxidation of the metals was generally incomplete, probably because of the presence of protective oxide layers (Tribelhorn et al., 1995b).

The above observations lead one to the conclusion that diffusion effects will almost always affect the reaction rate in solids. Diffusion aspect must therefore be taken into account when modelling the solid-state reactions of pyrotechnic compositions.

### 2.3.5 Kinetics of isothermal solid-state reactions

Beretka (1984) provides a critical review of the kinetic equations proposed for isothermal solid-state reactions. He found that Jander’s model for three-dimensional diffusion best describes experimental data:

\[
(1 - (1 - x)^{1/3})^2 = k \, t
\]  

(5)

Here \( x \) is the degree of conversion and \( k \) is an apparent rate constant. In practice, the conversion values of the individual particles vary because of gradients in the temperature and variations in the partial pressure of evolved gas within the sample matrix caused by mass and the heat-transfer phenomena (Koga and Criado, 1998).

### 2.3.6 Apparent kinetic constant

It is conventional to assume that the rate constant \( k \) follows simple Arrhenius kinetics (Laye, 1997):

\[
k = k_o \exp(-E_o / RT)
\]  

(6)
Boddington et al. (1986) advocate evaluation of the activation energy \( E_a \) for pyrotechnics from time-to-ignition data obtained under isothermal conditions. The usual route to determine the activation energy is from the gradient of \( \ln t_{\text{ign}} \) plotted against \( 1/T \), i.e. assuming relationships of the form

\[
t_{\text{ign}} = \exp \left( \frac{E_a}{RT} \right) + C
\]

(7)

Apparent activation energies determined using this method or by using temperature profile analyses yield values about an order of magnitude less than results obtained by thermal analysis (Laye, 1997). Such low activation energies for the pyrotechnic reaction imply that they are controlled by a diffusion mechanism (Boddington et al., 1990). To correct for diffusion effects, Laye (1997) proposed the apparent rate constant should be viewed as a combination of a "true" Arrhenius reaction rate constant and an activated diffusion:

\[
\frac{1}{k} = \frac{1}{k_{\text{Ar}}} + \frac{1}{BT^n}
\]

(8)

The factor \( B \) in equation (7) represents a diffusion coefficient. Equation (7) combines the Arrhenius behaviour at low temperature, which predicts a rapid raise in temperature, with diffusion-controlled behaviour at high temperature, where the rate becomes less dependent on temperature.

2.3.7 Propagation Index

Once the exothermic reaction has been initiated, the temperature will rise rapidly, at least in the neighbourhood of the reaction sites. Such temperature rises can produce phase changes and/or oxidant decompositions, which can significantly alter the mechanisms and the overall course of the reaction. It is now important to establish the degree to which the reaction will be self-sustaining.

Excessive heat loss to the environment is the main reason for failure to propagate through the entire length of the column. This is more likely to occur in small diameter
metal tubes and at low ambient temperatures. The propagation index \((PI)\) provides an indicator for the ability of a gasless delay composition to sustain combustion McLain (1980):

\[
PI = \Delta H / T_c
\]  

(9)

The most effective delay composition is the one with the highest index.

2.3.8 Combustion wave velocity for gasless combustion

Booth (1953) studied the burning of compressed powders in the form of cylindrical rods. He observed that, when ignited at one end, the rate of progression of the reaction zone along the axis is fairly uniform and reproducible for a given powder. This type of behaviour, generally referred to as 'layer-to-layer' burning, is observed only when the reaction is strongly exothermic, i.e. when a considerable amount of heat is evolved in the chemical change (Booth, 1953).

The combustion event in the time delay element is governed by a number of parameters. The thermal diffusivity of the mixture is important as wave propagation depends on repeated re-ignition of adjacent layers along the burning path. Good mixing and adequate inter-particle contact between reactants is required for stable and reproducible burning owing to the low values of the diffusion coefficients (Tribelhorn et al., 1995a).

![Figure 2.4 Schematic of the burning event in a time delay element](image)

Figure 2.4 shows a schematic of the burning event inside a tubular time delay element. The reaction zone is confined to narrow region. Ideally the burning front
propagates along the tube at a constant pace. The objective here is to relate the rate of burning to the physical properties of the pyrotechnic system. Only the simplest theory (Zuhair, 1988; Khaikin and Merzhanov, 1966), that relates the burning speed to the physical properties of the mixture, is considered here. The following simplifications make the problem mathematically tractable (Booth, 1953; Zuhair, 1988):

- Mass diffusion is neglected at the macroscopic level as in solids heat conduction occurs much faster (Tribelhorn et al., 1995a).
- No heat transfer due to radiation.
- The lateral loss heat is negligible.
- The thermal properties and the density are independent of the temperature and the composition.
- Propagation is one-dimensional.
- Constant physical properties (i.e. independent and temperature)
- Phase transformations and heat loss to the environment are ignored.
- Reaction kinetics can be modelled in terms of an exothermic, nth order, solid-state chemical reaction with an Arrhenius-type temperature dependence for the rate constant:

$$\frac{dx}{dt} = k (1 - x)^n$$

(10)

with

$$k = k_0 e^{-E_a/RT}$$

(6)

With the above assumptions the propagation of a combustion wave is described by the one-dimensional energy equation for unsteady heat conduction with a heat source:

$$\rho c_p \frac{\partial T}{\partial t} = \lambda \frac{\partial^2 T}{\partial z^2} + \dot{q}$$

(11)

The rate of heat release is proportional to the rate of reaction and the reaction enthalpy, $\Delta H_R$:

$$\dot{q}_R = \rho \Delta H_R \frac{dx}{dt}$$

(12)
If the burn rate is constant, it is characterised by a combustion wave that travels through the element at a constant pace as shown in Figure 2.5. Under steady state conditions the temperature profile is invariant and it can be expressed in terms of a single variable: $\eta = z - ut$, i.e.

$$T(z, t) = T(\eta) = T(z - ut)$$  \hspace{1cm} (13)

This allows equations (1) and (2) to be transformed into ordinary differential equations:

$$\frac{dx}{d\eta} = -\frac{k}{u}(1 - x)'$$  \hspace{1cm} (14)

$$\rho u c_p \frac{dT}{d\eta} + \lambda \frac{d^2T}{d\eta^2} = u \rho \Delta H \frac{dx}{d\eta}$$  \hspace{1cm} (15)

The boundary conditions are:

$$\begin{align*}
\eta \to -\infty & \quad T = T_c & \quad \frac{dT}{d\eta} = 0 & \quad \eta = 1 \quad \text{(16a)} \\
\eta \to \infty & \quad T = T_o & \quad \frac{dT}{d\eta} = 0 & \quad \eta = 0 \quad \text{(16b)}
\end{align*}$$

Figure 2.5 The combustion wave travels at a velocity $u$ along the solid filling.
Equation (15) can be integrated from $-\infty$ to $\eta$:

$$\rho u c_p (T - T_e) + \lambda \frac{dT}{d\eta} = -u \rho \Delta H_R (1 - x)$$  \hspace{1cm} (17)

Dividing equation (10) by (12) yields:

$$u^2 \frac{dx}{dT} = \frac{\lambda k (1 - x)^n}{\rho c_p (T_e - T) - \rho \Delta H_R (1 - x)}$$  \hspace{1cm} (18)

At this stage the “narrow reaction zone” hypothesis is invoked. It states that the reaction rate is negligible except at $T = T_e$ (Frank-Kamenetski, 1938; Khaikin and Merzhanov, 1966):

$$u^2 \frac{dx}{dT} = \frac{\lambda k (1 - x)^{n-1}}{\rho \Delta H_R}$$  \hspace{1cm} (19)

In principle this equation can be integrated using separation of variables. Unfortunately an analytic solution to the temperature integral is not possible. However, the temperature term can be approximated as follows:

$$k(T) = k_o e^{-E_a RT} \approx k_o e^{-2E_a RT_e} e^{ET_e / RT_e^2}$$  \hspace{1cm} (20)

Note that this approximation matches both the value and the slope of the rate constant $k(T)$ at $T = T_e$. With this substitution the integration can be performed with the result (Frank-Kamenetski, 1938):

$$u = \sqrt{g(n)} \frac{\lambda k_o R T_e^2}{\rho E_a \Delta H_R} \exp \left( -\frac{E_a}{RT_e} \right)$$  \hspace{1cm} (21)

with

$$g(n) = 2 - n$$  \hspace{1cm} (22a)

Equation (22a) is only correct for a zero order reaction where the reaction temperature approaches the adiabatic reaction temperature. For higher order
reactions the reaction rate is also significant at other temperatures. Khaikin and Merzhanov (1966) derived a revised expression for $g(n)$ using the “thin-zone” approximation:

$$g(n) = 2\left[\Gamma\left(\frac{n}{2} + 1\right)\right]^{2-n} \left[\frac{n}{2e}\right]^{n^2/4}$$

(22b)

The plot shown in Figure 2.5 shows that $g(n)$ is close to unity but that it is a decreasing function of the reaction order $n$. The maximum value of $g(n) = 2$ for a zero order reaction.

According to equation (21), the combustion wave temperature, $T_c$, is the most significant variable affecting the burn rate. The reaction temperature can be controlled by adjusting the reagent stoichiometry and by adding inert substances. Equation (21) also suggests that a slow burn speed requires a composition that reacts slowly while releasing a large amount of heat to sustain the thermal wave of reaction.
2.4 Factors affecting the burning rate

Ultimately the intrinsic burning rate of a delay composition is determined by the chemical nature of the ingredients, their relative proportions and the thermo-physical properties of the system. However, apart from those intrinsic to the compositions themselves, a wide range of other factors can influence the burning rate. This includes aspects related to the device into which they are filled and combustion environment itself (Wilson and Hancox, 2001).

2.4.1 Effect of thermal conductivity and density on wave propagation rate

The burning front in a compressed delay composition propagates in a layer-by-layer fashion along the burning path. This requires repeated re-ignition of adjacent layers. According to equation (21) the thermal conductivity and density are the primary physical properties that determine the rate of burning. With all other parameters and properties fixed, it predicts:

\[ u \propto \sqrt{\frac{\lambda}{\rho}} \]  

From this formula it can be deduced that:

- Increasing the thermal conductivity enhances the burning rates, and
- The more loosely the powder is packed, the more rapid is the burning velocity (Booth, 1953).

The last deduction is counter-intuitive! It should be remembered that the model used is based on apparent rate laws and physical constants that are interrelated. It would in general be difficult to separate individual effects.

Adding inert material changes the thermal conductivity of the mixture. Adding low thermal conductivity fillers, e.g. kaolin, reduces the rate of heat transfer through the mix. Conversely, adding thermally conductive fine Cu and Ag powders to gasless delay compositions can significantly increase the rate of burning (McLain, 1980).
2.4.2 Thermochemistry and stoichiometry: The heat of reaction

According to equation (21):

\[
u \propto \sqrt{\frac{T_c^2}{\Delta H_R}} \exp \left( - \frac{E_a}{RT_c} \right)
\]  

(24)

In the absence of phase changes and assuming constant physical properties, equation (4) predicts that

\[T_c \propto T_o + \frac{\Delta H_R}{c_p}
\]

(25)

Equations (25) and (24) indicate that a fuel that produces more heat on oxidation, e.g. boron \((\Delta H_R = 58,96 \text{ kJ/g})\), will react faster than a less exothermic fuel such as silicon \((\Delta H_R = 32,40 \text{ kJ/g})\).

Stoichiometry can also influence the product spectrum as shown in Table 2.2 for the reaction of silicon with \(\text{PbO}_2\) (McLain, 1980). Such changes can also influence the heat released. This is illustrated in Table 2.3 for the oxidation of manganese metal.

<table>
<thead>
<tr>
<th>% Si</th>
<th>Reactions</th>
<th>Products</th>
</tr>
</thead>
<tbody>
<tr>
<td>2,3</td>
<td>(\text{Si} + 4\text{PbO}_2)</td>
<td>(\text{Pb}_4\text{SiO}_6 + \text{O}_2)</td>
</tr>
<tr>
<td>3,1</td>
<td>(\text{Si} + 3\text{PbO}_2)</td>
<td>(\text{SiO}_2 + 3\text{PbO} + \frac{1}{2} \text{O}_2)</td>
</tr>
<tr>
<td>4,8</td>
<td>(\text{Si} + 2\text{PbO}_2)</td>
<td>(\text{Pb}_2\text{SiO}_4)</td>
</tr>
<tr>
<td>6,0</td>
<td>(2\text{Si} + 3\text{PbO}_2)</td>
<td>(2\text{PbSiO}_3 + \text{Pb})</td>
</tr>
<tr>
<td>8,7</td>
<td>(\text{Si} + \text{PbO}_2)</td>
<td>(\text{SiO}_2 + \text{Pb})</td>
</tr>
<tr>
<td>12,6</td>
<td>(3\text{Si} + 2\text{PbO}_2)</td>
<td>(\text{SiO}_2 + 2\text{SiO} + 2\text{Pb})</td>
</tr>
<tr>
<td>16,1</td>
<td>(2\text{Si} + \text{PbO}_2)</td>
<td>(\text{SiO}_2 + \text{Pb} + \text{Si})</td>
</tr>
<tr>
<td>22,3</td>
<td>(3\text{Si} + \text{PbO}_2)</td>
<td>(\text{Pb} + \text{Si} + 2\text{SiO})</td>
</tr>
</tbody>
</table>

Heat is also removed from the system when a component undergoes a phase change at higher temperature during the combustion process. This has the effect of slowing down the progression of the burning front. Heat loss through the tube walls has a similar effect but is discussed in more detail in Section 2.8.3.
Table 2.3. Effect of reagent stoichiometry on the heat of oxidation of manganese (Wilson and Hancox, 2001)

<table>
<thead>
<tr>
<th>Stoichiometry</th>
<th>$\Delta H_K$, kJ/g</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{Mn}(s) + 0.5 \ O_2(g) \rightarrow \text{MnO}(s)$</td>
<td>5.43</td>
</tr>
<tr>
<td>$\text{Mn}(s) + \ O_2(g) \rightarrow \text{MnO}_2(s)$</td>
<td>5.98</td>
</tr>
<tr>
<td>$2 \ \text{Mn}(s) + 1.5 \ O_2(g) \rightarrow \text{Mn}_2\text{O}_3(s)$</td>
<td>6.07</td>
</tr>
</tbody>
</table>

2.4.3 Effect of gassing

Aldushin et al. (1992) and Norgrove et al. (1991) investigated the case of a steady combustion wave in a porous reacting mass. They considered the effect of gas formation on the combustion wave. Depending on the confinement conditions, the produced gas moves either forward or backward relative to the flame front (Norgrove, 1991). For a sealed element, the ratio of gas flow forwards to gas flow backwards will depend on the confinement conditions and will change as the flame passes along the delay element.

When the gas moves with the combustion wave, it may assist the propagation of the front by means of convective mechanism (Aldushin, 1992). The travelling gas phase pre-heats the system, increases the adiabatic combustion temperature and increases the rate of burning. The overheating of the combustion zone depends on the proportion of gas present in the system, its thermo-chemical properties and its pressure (Bamford and Tipper, 1969). Aldushin et al. (1992) have derived an equation that relates the increase in the adiabatic temperature to the rate of gas convection (backward or forward motion):

$$ T_{ad} = T_0 + \frac{\Delta H_K}{c_p} \left(1 - \xi \frac{\nu c_{p,g}}{c_{p,s}} \right) $$

(26)

For a backward flow of gas through the condensed product, $\xi=0$ and for a flow accompanying the propagation wave, $\xi=1$. 
Zuhair (1988) has shown that if the reacting powder interacts with the gas phase, i.e. oxygen, its partial pressure must be above the characteristic pressure of dissociation of the oxide formed at the ignition temperature.

### 2.4.4 Effect of pressure

The burning rate of most pyrotechnic compositions is expected to increase with pressure according to Vieille’s law (Bamford and Tipper, 1969):

\[
\frac{u}{u_0} = \left(\frac{P}{P_0}\right)^n
\]  

(27)

The constant \( n \) is system specific and typically varies between 0,1 and 0,6. Its value depends on the amount of gas produced during the combustion.

In practice it is found that burning rate initially increases but that it stabilises or even decreases above a certain threshold limit. Consider, for example, the slow burning B/Si/K\(_2\)Cr\(_2\)O\(_7\) (4:5:91) gasless delay formulation used in accurate missile delay detonators. Its burning rate increases sharply with pressure between 0,1 and 0,4 MPa. Thereafter, the burning rate increase is slower. Above about 2 MPa the burning rate is unaffected by pressure (Howlett and May, 1974).

Other examples include the PbO-Si, Pb\(_3\)O\(_4\)-Si and KMnO\(_4\)-Si systems. In all of these the velocity of propagation increases with pressure until a maximum function of composition is reached (McLain, 1980). With the red lead–silicon compositions the burn rate decreases beyond pressures of approximately 6,90 MPa. This effect is attributed to pressure stabilisation of the PbO phase in the reaction mixture (McLain, 1980).

### 2.4.5 Environmental factors

The temperature of the delay column, both prior to and during combustion, also influences the burning rate. For military and aerospace applications, delay elements
must provide an accurate time interval, which is specified to within certain limits over a set environmental temperature range, often between −40 and +60°C (Wilson and Hancox, 2001).

Depending on the formulation, most gasless delay compositions burn about 25% slower at the lower temperature and 25% faster at the higher temperature than they would at room temperature. Gassy delay compositions are less affected by temperature variations (Wilson and Hancox, 2001).

2.5 Formulating pyrotechnic delay compositions

2.5.1 Fuel

<table>
<thead>
<tr>
<th>Fuel</th>
<th>Product oxide</th>
<th>$\Delta H$ (kJ /g fuel)</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>$B_2O_3$</td>
<td>58,9</td>
</tr>
<tr>
<td>C</td>
<td>$CO_2$</td>
<td>32,8</td>
</tr>
<tr>
<td>Si</td>
<td>$SiO_2$</td>
<td>32,4</td>
</tr>
<tr>
<td>Al</td>
<td>$Al_2O_3$</td>
<td>31,1</td>
</tr>
<tr>
<td>Mg</td>
<td>$MgO$</td>
<td>24,7</td>
</tr>
<tr>
<td>Zr</td>
<td>$ZrO_2$</td>
<td>12,0</td>
</tr>
<tr>
<td>Mn</td>
<td>$Mn_3O_4$</td>
<td>8,42</td>
</tr>
<tr>
<td>Fe</td>
<td>$Fe_3O_4$</td>
<td>7,54</td>
</tr>
<tr>
<td>W</td>
<td>$WO_3$</td>
<td>4,59</td>
</tr>
<tr>
<td>Sb</td>
<td>$Sb_2O_3$</td>
<td>2,96</td>
</tr>
</tbody>
</table>

Fuels include metals such as Al, Al/Mg, Cr, Fe, Mg, Zr, W and Zn. Table 2.4 lists the heats of reaction of some metal fuels. Note that fuels are not limited to pure metals and non-metals: alloys such as ferrosilicide ($FeSi_x$) and calcium silicide ($CaSi_2$) (Krone et al., 1992) can also be used. Organic fuels (e.g. sorbitol, hexamethylene tetramine, potassium benzoate, etc.) and some inorganic fuels (C, S, P) generally produce much gas during combustion. This causes pressure build-up that affects the
reaction rate and thus the delay time. As a result, the main charge may be ignited prematurely (Ellern, 1968).

2.5.2 Effect of metal reductant content on burning rate

Usually it is found that the maximum burning rate occurs at a somewhat higher reductant content than does the maximum heat of reaction. This displacement is generally greater for metal reductants such as Fe, Sb and Mn and is smaller for non-metal reductants such as S and C or the metalloids B and Si (McLain, 1980). This phenomenon is associated with the effect of heat transfer on columnar burning.

The slope of the burning rate curve is usually steeper below the maximum than above (percentage reductant above stoichiometry). This is ascribed to the fact that the addition of a good heat conductor, such as a metal or a metalloid, causes departure from the stoichiometry, but may increase the thermal conductivity sufficiently to cause a net increase in the burning rate. In effect, an excess of either oxidant or fuel represents an inert diluent. Excess oxidiser acts like a heat insulator and this retards the burning. In contrast, the excess of a conductive reductant accelerates the burning rate (McLain, 1980).

2.5.3 Silicon as a fuel for pyrotechnic delay composition

Several workers have investigated the behaviour of silicon as fuel (Al-Kazraji and Rees, 1979; Goodfield and Rees, 1985; Yoganarasimhan, 1987). The oxidation of silicon by gaseous oxygen occurs in the temperature range of 990 to 1200°C. The rate of oxidation in wet oxygen atmospheres is faster than in dry oxygen atmospheres. The kinetic of oxidation in wet and dry atmospheres is a function of the partial pressures of H₂O and O₂ respectively (Rugunanan, 1991a).

The oxidation occurs at the Si/SiO₂ interface and O₂ has to diffuse through the oxide layer for the reaction to occur. The layer of SiO₂ that adheres to the silicon particle surface represents a diffusion barrier. If this coating layer is very compact, further oxidation could be inhibited. The rate of oxidation depends on the thickness of the oxide layer. In general a parabolic rate law describes the oxide growth:
\[ AL^2 + BL = t + C \] (28)

Where A, B and C are empirical constants. For thin films (~2nm), the rate of oxide growth is linear:

\[ BL = t + C \] (29)

The oxidation of transition-metal silicides was reported to occur at a faster rate than the oxidation of pure silicon and refractory-metal silicides, possibly owing to higher electron mobility (Rugunanan, 1991a).

### 2.5.4 Oxidisers

The following heavy metal oxides are suitable for used in delay compositions: \( \text{Fe}_2\text{O}_3 \), \( \text{Sb}_2\text{O}_3 \), \( \text{Cu}_2\text{O} \), \( \text{Bi}_2\text{O}_3 \), \( \text{Pb}_3\text{O}_4 \), \( \text{PbO}_2 \), \( \text{ZnO} \), \( \text{MnO}_2 \). A recent trend is to use complex oxides, e.g. \( \text{Cu}_2\text{O.} \text{Sb}_2\text{O}_3 \), \( \text{ZnO.} \text{Sb}_2\text{O}_3 \) or \( \text{BaO.} \text{MoO}_3 \) (Krone et al., 1992). Nitrate, chromate, chlorate and perchlorate salts are used for other pyrotechnic effects (light emissions, signalling smokes, whistling sounds, etc.) (Ellern, 1968). Conkling (1996) discusses factors affecting oxidiser selection. The most important factor is the relative affinity towards oxygen between the metals of the oxidiser and the fuel.

### 2.5.5 Additives

Additives are mixed to the main composition to effect the following: ensure intimate contact between the particles, protect against the environment, premature reaction or to improve mechanical properties. Addition of a third component can alter the burning rate of a binary system. Such additives may be:

- Chemically inert substances
- An additional fuel
- An additional oxidant
- A source of some reactive intermediate.
Suitable agents include:

- **Binders.** Binders are used to maintain the homogeneity of the blended mixture. They also play a minor role as internal lubricants during the compacting phase (Krone et al., 1992). Binders can be organic or inorganic in nature. *Organic binders* include synthetic polymers (polyethylene, polyurethane, polyvinyl chloride and some copolymers), biopolymers (dextrin and starch) and natural resins e.g. gum Arabic and gum acaroid. *Inorganic binders* include gypsum, water glass and bentonite.

- **Formulation aids** include anti-caking agents (pyrogenic SiO₂, Al₂O₃, CaCO₃, MgCO₃) and lubricants (graphite, talc, wax, Teflon, silicone).

- **Catalysts:** Fe₂O₃, CuO.CrO₂, V₂O₅ and MnO₂.

- **Burning rate modifiers:** kieselguhr, diatomaceous earth, fumed silica. Addition of such chemically inert additive may simply reduce fuel/oxidant contact. It may also alter the thermal properties of the system (e.g. additives of high heat capacity may lower the combustion temperature). Inert additives with a low melting point may act as fluxes. Table 2.5 illustrates the use of the inert additive SiO₂ for reducing the burning rate in the Sb/KMnO₄ system.

### Table 2.5. Effect of SiO₂ on the burning rate of a 30:70 Sb:KMnO₄ composition (Beck and Brown, 1986).

<table>
<thead>
<tr>
<th>SiO₂ content, %</th>
<th>0</th>
<th>7</th>
<th>19</th>
</tr>
</thead>
<tbody>
<tr>
<td>Burn speed (mm/s)</td>
<td>1,9</td>
<td>1,6</td>
<td>1,3</td>
</tr>
</tbody>
</table>

2.5.6 *Empirical rules for the design of new mixtures*

McLain (1980) recommended that the following rules of thumb be observed when designing a new pyrotechnic mixture:

- Maximise the burning rate for a given mix by using more than the stochiometric proportion of the reducing agent.

- Decrease the heat of reaction to reduce the burning rate: use a metal that produces less heat or reacts in several different ways depending on its
proportion in the mix (e.g. Mn), or add an inert thermal insulator such as powdered glass, kieselguhr, fuller's earth or fumed silica.

- Use tubes with an inside diameter of 6 mm or larger for mixtures which burn slower than 25 mm/s,
- Do not use tubes made from good heat conductors like brass or copper.
- A mixture with the highest possible propagation index should be used to achieve the desired burn rate.
- The following factors should be kept in mind:
  - The particle size and size distribution of the constituent powders; the size and chemical nature of guest particles; adsorbed gases on the particle surfaces; the loading method and pressure; the mix homogeneity; temperature and type of ignition; the mix type (low gas or gassy) and the humidity during mixing and loading.

### 2.6 Review of Selected Pyrotechnic Delay Compositions

#### 2.6.1 Silicon / lead oxides

Silicon/lead oxide preparations have found widespread application as millisecond time delay systems. These gasless delay compositions were formulated to replace the older fuse materials, which were unreliable under low pressure at high altitudes, e.g. in space research (Al-Kazraji, 1979).

**Si-PbO system**

Al-Kazraji (1979) studied the DTA response of a 30:70 Si: PbO powder mixture in air. He observed three exotherm peaks at 590, 665 and 710°C respectively. The first reaction corresponds to the conversion of PbO to Pb\(_3\)O\(_4\) (red lead) and commences at 350°C (Rugunanan, 1991a):

\[
6 \text{ PbO (s) + O}_2 \text{ (g)} \rightarrow 2 \text{ Pb}_3\text{O}_4 \text{ (s)}
\]

The Pb\(_3\)O\(_4\) reacts with silicon above 540°C and regenerates PbO:
At 665°C more silicon is oxidised by the freshly formed PbO and O₂ (from the atmosphere):

\[
PbO (s) + \frac{1}{2} O₂ (g) + Si \rightarrow Pb (l) + SiO₂ (s)
\]

**Si-PbO₂ system**

DTA analysis of PbO₂ reveals several endotherms corresponding to its step-wise decomposition:

\[
PbO₂ \xrightarrow{435°} PbO_{1.56} \xrightarrow{465°} PbO_{1.43} \xrightarrow{495°} Pb₃O₄ \xrightarrow{573°} PbO
\]

The fifth endotherm observed at ~875°C indicates the melting of PbO (Rugunanan, 1991a).

The observed and calculated heats of reaction Δ\(H_r\) show a maximum near 10.5% Si (McLain, 1980). This suggests that this is the stoichiometric quantity of Si that is required to consume all the oxidiser and it is consistent with the following reaction:

\[
PbO₂ (s) + Si \rightarrow Pb (l) + SiO₂ (s)
\]

The maximum burning rate of Si/PbO₂ mixtures occurs at 35% Si. This burning rate also decreased with increasing particle size (McLain, 1980).

**Si-Pb₃O₄ system**

Al-Kazraji and Rees (1978) investigated the fast pyrotechnic delay composition Si – red lead. Their thermal analysis results revealed three main exothermic peaks: 590, 670, and 760°C. Their observations can be explained in terms of the following sequence of events. The red lead (Pb₃O₄) decomposes above 540°C to yield a solid residue of PbO that reacts readily with silicon. This occurs at the onset of the first exothermic peak (590°C) obtained from DTA:
Pb$_3$O$_4$ (s) $\rightarrow$ 3 PbO(s) + $\frac{1}{2}$ O$_2$ (g) 

2 Pb$_3$O$_4$ (s) + Si(s) $\rightarrow$ SiO$_2$ (s) + 6 PbO (s) 

PbO (s) + Si (s) +$\frac{1}{2}$O$_2$ (g) (from air) $\rightarrow$ Pb (l) + SiO$_2$ (s) 

The reaction corresponding to the second exotherm (665°C) releases more heat and is associated with the oxidation of the molten lead from the previous reaction to lead oxide, which in turn reacts with excess silicon at the onset of 665°C. That produces sufficient heat to raise the temperature for a further reaction to take place in bulk after diffusion through the layer of reaction products formed around the reactants. When the flow was nitrogen, the second reaction was less violent because of the absence of atmospheric oxygen.

The third peak (760°C), smaller than the second and very pronounced for silicon-rich compositions, is possibly due to the reaction between PbO and PbSiO$_2$ (lead silicate) at the melting point of the silicate (Mellor, 1925).

Moghaddam (1981) also investigated the thermal response of Pb$_3$O$_4$/Si systems. He found that the DTA curve in air shows two exothermic peaks at the same temperature ranges found for the PbO/Si reaction.

However, the first exotherm of the Pb$_3$O$_4$ system, larger than the second, is also larger than the first peak of PbO/Si, indicating that the main reaction occurs in this temperature range. It was also observed that the oxygen resulting from the decomposition of Pb$_3$O$_4$ did not react with silicon. The high reactivity of Pb$_3$O$_4$/Si mixtures at lower temperatures is attributed to the presence of highly reactive PbO freshly formed with a larger specific surface area. The highly reactive PbO reacts more readily with silicon, producing burning rates almost three times faster than those of ordinary PbO/Si systems (Moghaddam, 1981).

The maximum burning rate was observed at approximately 30% Si for coarse silicon ($d_{avg}$ ≈ 5 µm) and 15% Si for fine silicon ($d_{avg}$ ≈ 1,9 µm) (Rugunanan, 1991a). In
addition, the composition at which the maximum burning rate occurred did not correspond to the composition of maximum enthalpy (~10%). The maximum burning rate increased (from 16 to 300 mm/s) when the specific surface area of the silicon was increased from 0.08 to 5.36 m²/g (Hedger, 1983).

Moghaddam (1981) suggested that the mechanism for the reaction is essentially the formation of a eutectic of PbO and SiO₂ around 720°C. The PbO and SiO₂ melt at 886 and 1610°C respectively. Thus, the delay time depends on the kinetics of the formation of the eutectic.

2.6.2 Silicon / zirconium / bismuth oxide

Boberg et al. (1997) patented the use of the Si-Bi₂O₃ system in pyrotechnic delay systems. It was found that addition of Zr as co-fuel results in enhanced ignitability and increased burn speed (See Table 2.6). Burn speeds up to 100 mm/s were obtained with Zr contents above 25% (expressed as part of fuel).

![Figure 2.7 The effect of stoichiometry on gas evolution and reaction heat for the Si-Bi₂O₃ system (Brammer et al., 1996)](image)
Figures 2.7 and 2.8 show data obtained by Brammer et al. (1996) for the Si-Bi₂O₃ system. Little gas is produced during combustion. Maximum heat release occurs at about 20% Si.

![Graph showing burn rate vs silicon content](image)

*Figure 2.8 The effect of stoichiometry on the burn rate for the Si-Bi₂O₃ system (Brammer et al., 1996).*

<table>
<thead>
<tr>
<th>Composition*, %</th>
<th>Burning rate (mm/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si</td>
<td>Zr</td>
</tr>
<tr>
<td>-----</td>
<td>-----</td>
</tr>
<tr>
<td>28</td>
<td>5</td>
</tr>
<tr>
<td>30</td>
<td>20</td>
</tr>
<tr>
<td>3</td>
<td>10</td>
</tr>
</tbody>
</table>

*Particle sizes: Silicon: 3 μm; Zirconium: 2 μm; Titanium oxide: < 1 μm; and Bi₂O₃: 5 μm.

### 2.6.3 Silicon / barium sulphate

This system has found much use in long-period delays. The 42% Si composition gives a burning rate of ca. 4.3 mm/s. It has been established that the system burns only when the Si-content of the composition is in the range 33.5–50%, with a specific surface area between 0.45 and 2.36 m²/g for the BaSO₄.
Beck and Flanagan (1992) patented delay compositions consisting of a basic formulation of 45.5% Si/BaSO₄ in combination with 2-10% V₂O₅ as an ingredient acting as a flux. The consolidation was done to a density about 2 g/cm³ in a 22 mm zinc delay element (inner diameter: 3.1 mm, outer diameter: 6.4 mm), containing a 6 mm-long, fast burning igniting sealing composition. Burn rate results are reported in Table 27.

<table>
<thead>
<tr>
<th>V₂O₅ content</th>
<th>%</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Burn rate</td>
<td>mm/s</td>
<td>Failure</td>
<td>4.025</td>
<td>4.05</td>
<td>4.05</td>
</tr>
</tbody>
</table>

Particle surface areas: Silicon: 7 m²/g; BaSO₄: 0.8 m²/g; V₂O₅: very fine.

The melting flux assists the initiation of the Si/BaSO₄ without participating in the main combustion reaction. The content is efficient in the range 1–10% by mass. Above 10% the dilution effect of the inert flux tends to quench the reaction (Beck and Flanagan, 1992).

### 2.6.4 Silicon / boron / potassium dichromate

Charsley and co-workers (1980) showed that in the binary system B/K₂Cr₂O₇, the combustion reaction is self-propagating above a fuel content of 5%. For mixtures prepared from 4% B/K₂Cr₂O₇, the presence of a few percent of silicon is beneficial and indeed is responsible for propagating the combustion.

DTA curves recorded for mixtures of Si/K₂Cr₂O₇ showed an exotherm at approximately 950 K. Such mixtures are more difficult to ignite and self-propagating combustion requires a Si content of more than 15%. The combustion process is recorded as a single exotherm immediately following the onset of dichromate fusion.

The boron in the ternary mixture then burns in a matrix of molten oxidant, which progresses through the burning compositions as a molten front. However, the
determining step of the kinetic mechanism involves the formation of a liquid phase (Howlett and May, 1974).

In B/Si/K$_2$Cr$_2$O$_7$ systems, ignition also occurs immediately after fusion of the oxidant. The boron acts as a trigger by burning with the molten oxidant prior to the combustion of the silicon. The silicon then reacts, as a follow-up reaction.

The ignition temperature of the ternary mixtures is about 660 K. It was observed that the addition of silicon increased the maximum reaction temperature and the rising slope of the temperature profiles (Charsley et al., 1980), and that the addition of 25% Si to 5% B-K$_2$Cr$_2$O$_7$ is critical because further addition decreased the exothermicity.

2.6.5 Zinc / lead oxides

Zinc has a low melting point (420°C) that is readily reached during combustion in Zn/oxidant pyrotechnic systems. Tribelhorn et al. (1995) found that Zn burned in combination with any of the lead oxides (PbO$_2$, Pb$_3$O$_4$ and PbO) over a range of compositions (10–70% Zn). The burning rates varied in the range 2,2–90 mm/s for compositions containing 20 to 50% Zn. However, as the compaction pressure was increased the range of compositions that burned decreased. For example, at a compaction pressure of 55 MPa, only Zn/PbO$_2$ sustained combustion and then only in the range 20–45% Zn. Mixtures of Zn/PbO only burned in loose powder form.

It was observed that compositions with higher percentages of Zn were more gassy and burned more rapidly and violently. The gas should be a mixture of O$_2$ and vapours of Zn and Pb respectively.

Only in the case of Zn/Pb$_3$O$_4$ the oxidant was fully reduced and converted to Pb. The maximum temperatures reached during the combustion of all the Zn/PbO$_2$ or Pb$_3$O$_4$ mixtures were above 1800°C. The Zn/PbO$_2$ combustion residues showed a spongy appearance that indicated gas evolution. These systems were not suitable for use as pyrotechnic delays because of the gassy combustion (Tribelhorn et al., 1995b).
2.6.6 Iron / barium oxides

Tribelhorn et al. (1995) also investigated the formulation variables and the compaction pressure on the behaviour of iron-fuelled binary pyrotechnic systems. Burning rates for the iron/barium oxide system ranged from 2.3 to 39 mm/s reaching a maximum around 30% Fe. The burning rates for compositions compacted at 55 MPa were higher than those for loose compositions. Increasing the compaction pressure beyond 55 MPa led to a decrease in burning rates.

Compaction promotes interparticle contact and hence the rate of solid-solid reactions. When solid-gas reactions are also involved, increased compaction slows the rate of burning as the fuel surface area accessible to the gas is decreased.

The effect of additives and environmental factors was studied using 20% Fe/BaO₂ as the base formulation. Addition of 5% barium hydroxide [Ba(OH)₂] inhibited combustion. Although mixtures containing >15% BaCO₃ supported combustion, its formation on the surfaces of BaO₂ decreased the reactivity of the system.

The presence of even 1% water inhibits the ignition of the composition. This is attributed to the coating of BaO₂ particles with Ba(OH)₂. Such layers apparently inhibit combustion more than having a few separate particles of Ba(OH)₂ interdispersed throughout the mixture. It was also observed that the endothermic decomposition of the hydroxide regenerated water vapour during the combustion and this also affected the combustion rate. Water may have a deleterious effect on the burning rate by corroding the surfaces of the iron particles to form oxides and hydroxides.

The main reactions likely to be involved in combustion of the Fe/BaO₂ system are:

\[
\begin{align*}
2 \text{Fe(s)} + 3 \text{BaO}_2(s) & \rightarrow \text{Fe}_2\text{O}_3(s) + 3 \text{BaO(s)} \\
3 \text{Fe(s)} + 4\text{BaO}_2(s) & \rightarrow \text{Fe}_3\text{O}_4(s) + 4 \text{BaO(s)} \\
\text{Fe(s)} + \text{BaO}_2(s) & \rightarrow \text{FeO(s)} + \text{BaO(s)}
\end{align*}
\]
The reaction order varied with the Fe content of the mixture and ranged from 0.50 to 0.71. The corresponding activation energies observed varied erratically between 7 and 13 kJ/mol. with the Fe ratio. These low apparent activation energies are indicative of diffusion-controlled processes.

2.6.7 Zirconium / iron oxide

Cheng et al. (1984) investigated the use of the Zr/Fe$_2$O$_3$ system as a pyrotechnic delay element. DSC showed a strong exotherm at 395 to 430°C for mixtures containing from 10 to 80% Zr. Cheng et al. (1984) also observed a pre-ignition of reaction in the range of 310–330°C. The overall reaction is:

$$3 \text{Zr} (s) + 2 \text{Fe}_2\text{O}_3 (s) \rightarrow 4\text{Fe} (s) + 3 \text{ZrO}_2 (s)$$

This is a composite of the following two reactions:

$$\text{Zr} (s) + 2 \text{Fe}_2\text{O}_3 (s) \rightarrow \text{ZrO}_2 (s) + 4 \text{FeO} (s) \quad (\Delta H = -1.29 \text{ MJ/kg})$$

$$\text{Zr} (s) + 2 \text{FeO} (s) \rightarrow \text{ZrO}_2 (s) + 2 \text{Fe} (s) \quad (\Delta H = -2.36 \text{ MJ/kg})$$

The nature of the combustion products, identified by XRD analysis, depended on the fuel content of the mixture. See Table 2.8.

<table>
<thead>
<tr>
<th>% Zr in reactants</th>
<th>Identified products</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>ZrO$_2$, Fe, FeO</td>
</tr>
<tr>
<td>50</td>
<td>ZrO$_2$, Fe</td>
</tr>
<tr>
<td>70</td>
<td>ZrO$_2$, ZrFe$_2$</td>
</tr>
</tbody>
</table>

Burning rate and the heat of reaction showed similar trends with respect to the composition dependence. The burning rate did not vary significantly in the Zr content range 48 to 56%. The maximum heat of reaction was obtained with 50% Zr. The compaction pressure had only a slight effect on the burning rate.
2.7 Pyrotechnics processing

It is important in pyrotechnic technology to ensure the homogeneity of the mix as this will result in the regularity, reproducibility and uniformity of the combustion wave motion for a particular composition. Processing also has an effect on the ease of manufacture and loading as well as safety.

Preparation of raw materials

Grinding

A micropulveriser is used to reduce the particle size and to ensure that each batch is prepared in the same way. The standard operating procedure for all inorganic oxidisers is to dry, micropulverise (no more than 2 days before use) and then dry again (McLain, 1980).

Ball milling

Ball mills also serve to reduce the particle size of relatively brittle substances, such as oxidiser salts. It was proved that milling increased the reactivity of the reactants. This change may be the result of the reduction in particle size (increase of specific surface area), the distortion of the structure, the breaking up of agglomerates or, more likely, of stripping the metal particles from inhibiting surface layers (Ellem, 1968). The success of this technique is a function of material properties, such as fragility and hardness. A ball mill or micropulveriser should not be used to mix a flammable pyrotechnic, nor should they be used interchangeably for oxidisers and reductants since small residues of the one can react with the other (McLain, 1980).

Coating

In order to avoid possible surface deterioration of the metal powders, protective coatings are applied. Coating materials such as paraffin, linseed oil, stearic acid and polyvinyl chloride (PVC) may be applied by dipping or spraying (McLain, 1980).

Heat treatment
Heat treatment enhances the uniformity of processed materials by desorption of moisture or other materials that have covered the surface of particulates. For example, PbCrO$_4$ and BaCrO$_4$ are preheated at 400°C before use (McLain, 1980).

The heat treatment of a mixture delay composition requires precautions to avoid ignition. The temperature is therefore kept far below runaway conditions. For example, the fast burning Pb$_3$O$_4$/Si mixture is dried below 70°C.

**Mixing**

Proper mixing eliminates non-uniformities and concentration gradients. This operation is essential to ensure homogeneity of the reaction mixture. Several techniques have been used to achieve the objectives:

**Brush screening**

This is accomplished on a set of brush screeners, similar to flour sifters that are assembled on top of each other. The rotating brushes are usually pulley-driven from a drive shaft connected to a motor (McLain, 1980). They are remotely operated to avoid exposing personnel to the hazards of fire and toxic dust.

**Mechanical mixing – dry**

Different techniques are used for this processing, such as rumbling (the most efficient technique), dough mixers and double-cone blenders. Bladed mixers and ribbon blenders can cause fires (McLain, 1980).

**Mechanical mixing – wet**

Wet mixing process equipment includes:

- Simpson Intensive Muller or Lancaster Mix Muller apparatus, consisting of a central rotating shaft and two wheels with ploughshares inside each wheel. They are used for high viscosity mixtures.
- Sigmoid blade mixer for high-viscosity mixtures.
- Hobart apparatus, usable for mixtures with consistencies ranging from a thin gruel to heavy dough.
- Vibrating screens (McLain, 1980).
Co-precipitation
This is mainly used to produce mixtures with close bonding between the reductant and the oxidant. Examples are:
- The co-precipitation of a B-BaCrO₄ mixture.
- The co-precipitation of Mn-BaCrO₄-PbCrO₄ mixtures as described by McLain (1980).

Co-acervation
In pyrotechnics, co-acervation is a type of co-precipitation that depends on the ability of ethyl alcohol to pre-empt the solvent capacity of water.

Soluble ionic compounds form stable solutions in water because of hydration: the formation of a stable water shell around the ions bonded by ion-dipole interactions. It is the enveloping water layers that prevent re-association and thus stabilise the solution. Ethyl alcohol molecules bond more strongly to the water molecules than do the cations. Consequently, the addition of the alcohol to a water solution of salt strips the ions of their protective coating and causes re-association or precipitation.

This technique has been used in the preparation of Mg-NaNO₃ illuminating flare mixtures and K₂Cr₂O₇-Si-B delay mixtures (McLain, 1980).

Methods of processing highly hazardous mixes
- Wet mixing
  - Polymer precipitation:

This process involves dissolving the polymer in a solvent, adding the dry ingredients and stirring vigorously, then adding a non-solvent to the system to cause precipitation of the mix. The end product is a homogeneously dispersed mix of ingredients uniformly coated with the precipitated polymer. This product does not require screening, which is of special benefit with compositions that are hazardous to screen because of friction sensitivity (McLain, 1980).

Binders for pyrotechnic compositions
Polymeric binders play multiple roles in pyrotechnic compositions and, in general, they contribute towards better mechanical strength and provide moisture-absorption resistance. This latter leads to improved shelf life.

Beck et al. (1986) found that binders also contribute significantly to the performance of composition by lowering the activation energy (ignition temperature) and increasing the combustion temperature and burning rate. Boiled linseed oil (~2%) was added to a 15% Sb (<53\mu m)/ KMnO₄ composition, which does not normally burn. The composition with the binder did burn.

Barton et al. (1982) found that the addition of 2 to 3% of acaroid resin to a mixture of Mg/BaO₂ lowered the ignition temperature by more than 200°C.

Generally, the silicon and red lead system is slurried by the addition of an aqueous solution of carboximethyl cellulose, which acts as a binder. The slurry is stirred thoroughly to ensure even distribution of the two species, and the water is evaporated by placing the slurried composition on a steam-heated copper tray. The binder prevents segregation of Si and Pb₃O₄ (Al-Kazraji and Rees, 1979). It was also observed that the addition of the binder makes the composition sensitive to impact and friction.

**Novel powder-processing techniques**

A major problem in the processing of powdered formulations is agglomeration. This problem can be encountered when one or more of the powdered constituents are:

- Hygroscopic, e.g. ammonium perchlorate or sodium nitrate
- Waxy or oily (TNT or nitroguanidine)
- Unusually shaped, such as needle-type or flake particles.

The agglomeration increases as the particle size decreases and the moisture content increases. The latter leads to caking of the powder. This means that most fine particle powders have to be specially handled in all processing techniques, i.e. drying the powder at elevated temperature, screening to break up or remove agglomerates, and desiccating to prevent moisture uptake (Tulis, 1980).
The milling of hygroscopic materials must be done under conditions of near-absolute dryness. As the particle size is reduced, the surface area increases and moisture absorption becomes extensive. When milled, the waxy materials ‘freeze’ and become sufficiently brittle to fragment (Tulis, 1980).

**Powder conditioning**

Flow-conditioner additives are intensively used to overcome agglomeration problems. These are usually very fine powders of sub-sieve particle size and include various types of silicates, stearates, phosphates, diatomaceous earth, starch, magnesium oxide, talc and fatty amines.

These conditioners proceed in various ways to improve flowability and inhibit agglomeration, e.g.:

- Form a solid barrier between the powder particles, reducing their attractive forces
- Lubricate the solid surfaces, reducing friction between the particles
- Neutralise electrostatic charges (Tulis, 1980).

Colloidal hydrophobic fumed silica, in powder form, is a powerful flow-conditioner additive. Normal silica aerogel is hydrophilic. It can be converted to the hydrophobic state by replacing the surface hydroxyl groups with siloxane groups (Tulis, 1980) by reaction with e.g. hexamethyldisilazane.

The advantages of this flow conditioner are:

- It has an exceedingly light bulk density, about 0.05 g/cc.
- The particle size is about 7 nanometer.
- The conditioner can be premixed before milling and will allow milling of waxy or oily materials.
- The treated powder becomes water repellent, even if initially hygroscopic.
- Low dosage required: Less than one percent, on a mass basis, is often adequate.
- The resultant powder generally has a higher bulk density.
- It is chemically inert, allowing it to be used with sensitive propellants, explosives and pyrotechnics.
The exceptionally high water repellence of powder conditioned with hydrophobic silica is attributed to air entrapment on the surface of the powder particles. One advantage of this technology is associated with the increased bulk density. Because of the better flowability, the particles flow and slip past each other readily so that they compact better (Tulis, 1980).

The addition of 1 to 2% of hydrophobic silica to pyrotechnic mixes proves to be efficient in the milling (Tulis, 1980).

**Powder preparation**
Molecular sieves are used to achieve near-absolute drying of powders. They are crystalline zeolites that have angstrom-sized pores that allow a selective adsorption of polar gases and liquids. Moisture is transferred from the powders to the molecular sieves. This is an equilibrium process. The efficiency of molecular sieves has been demonstrated in the milling of a water-ignitable pyrotechnic composition of B/AgF₂ (Tulis, 1980).

Direct contact of molecular sieves with sensitive materials, such as explosives, must be avoided: The heat of adsorption might be sufficient to cause ignition of sensitive materials (Tulis, 1980).

In certain milling operations, synergism was observed when using a combination of molecular sieves and hydrophobic silica. The former dried the particles and the latter coats their surfaces once fragmented (Tulis, 1980).

### 2.8 Design of pyrotechnic delay elements

#### 2.8.1 Porosity and compaction pressure

The degree of preheating of the reactants in a given system is affected by the forward intrusion of hot combustion products. This, in turn, is partly determined by the porosity of the compacted material. Consolidated compositions exhibit microscopic
voids between the ingredients even when compressed at very high loads. Even at densities approaching the theoretical maximum (TMD), the voids may constitute upward of 2% of the total volume. The reason is that beyond a critical density further displacement of the particles is precluded. The loading pressure for a delay charge is usually around 200–275 MPa (Cheng et al., 1984).

The void volume of a composition depends on the formulation, the physical characteristics of the ingredients such as the size and the shape of the particles; and the presence of substances such as waxes or resins that can deform or flow under pressure (Wilson and Hancox, 2001).

The effect of compaction pressure on the burning rate should be considered when designing a delay element. With the incremental method of filling the delay elements, there will be periodic variations in the degree of compaction. It is believed that the interfaces between the individual increments may cause a momentary slowing of the burning front (Wilson and Hancox, 2001).

2.8.2 Design and manufacturing factors

Design and manufacturing factors that can affect the delay interval produced by a delay element include (Wilson and Hancox, 2001):

- Design of the delay element, e.g. length and diameter of the column
- Density of the column packing
- Type of ignition source used
- Ignition transfer and mechanical strength of the column
- Thermal conductivity of the tube housing the column

Gasless compositions that burn at a rate lower than 3 mm/s tend to be unreliable. This limits the practical time delay to about 25 seconds for a 75 mm stubby.

Delay elements for longer time intervals have been made utilising long, straight lead tubes made by the extrusion technique and pressing them into a flat ‘C’ section or by preparing spirally wound units. In this way time delays of several minutes can be obtained (Wilson and Hancox 2001).
2.8.3 Thermal conductivity of the tube wall

Heat loss through the container walls is essentially dealt with by tubular geometry. The heat flow decreases as the thickness of the tube increases; whereas an increase in the diameter increases the heat loss for a constant wall thickness.

The heat loss will be greater from a tube with high thermal conductivity of the container. The internal tube diameter will have to be kept larger to sustain combustion in a tube of high thermal conductivity, e.g. an aluminium tube. One effect of high heat conductivity along the column wall may be a premature initiation of whatever terminal charge follows the delay column (Ellern, 1968).

Table 2.9 shows the effect of wall thermal conductivity on the burning rate of a specific composition of the Sb-KMnO₄ system. The dramatic decrease in the burning rate in Perspex (polymethylmethacrylate) tubes in an open system is attributed to severe melting and degradation. However, in a closed system the degradation products caused the development of high pressures. This increased the burning rate to approximately 8.2 mm/s and caused a high proportion of tubes to burst.

Table 2.9. Effect of container material on the burning rate of 30% Sb/KMnO₄ in open systems. (Beck et al., 1986)

<table>
<thead>
<tr>
<th>Container material</th>
<th>Burning rate (mm/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Column supported in air</td>
<td>1.9</td>
</tr>
<tr>
<td>Aluminium</td>
<td>2.2</td>
</tr>
<tr>
<td>Polyether imide</td>
<td>2.5</td>
</tr>
<tr>
<td>Perspex</td>
<td>1.3</td>
</tr>
<tr>
<td>Packed in SiO₂</td>
<td>2.4</td>
</tr>
<tr>
<td>Packed in CaCO₃</td>
<td>2.2</td>
</tr>
</tbody>
</table>

The use of heat-resistant polymers (e.g. polycarbonate, PTFE, Kevlar and high-temperature 40% glass-filled polyether imide) did not reduce the quantity of gaseous
degradation products sufficiently to prevent bursting of the detonator tubes. This suggests that polymers are not suitable tube materials for pyrotechnic delays.

Table 2.10 lists the physical properties of potential tube materials.

<table>
<thead>
<tr>
<th>Material</th>
<th>Thermal conductivity (λ) W.m⁻¹.K⁻¹</th>
<th>Density (ρ) 10³ kg.m⁻³</th>
<th>Heat capacity (Cₚ) J.kg⁻¹.K⁻¹</th>
<th>Thermal diffusivity: (α) 10⁻⁶ m².s⁻¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>Al</td>
<td>220</td>
<td>2.7</td>
<td>960</td>
<td>85</td>
</tr>
<tr>
<td>Pb</td>
<td>35.3</td>
<td>11.34</td>
<td>160</td>
<td>19.45</td>
</tr>
<tr>
<td>Stainless steel</td>
<td>15</td>
<td>8.0</td>
<td>500</td>
<td>3.8</td>
</tr>
<tr>
<td>CaSi₂</td>
<td>0.42</td>
<td>2.5</td>
<td>960</td>
<td>2.04</td>
</tr>
<tr>
<td>Si</td>
<td>0.35</td>
<td>2.33</td>
<td>720</td>
<td>3.42</td>
</tr>
<tr>
<td>Al₂O₃</td>
<td>0.22</td>
<td>3.97</td>
<td>780</td>
<td>1.54</td>
</tr>
<tr>
<td>Nylon 6</td>
<td>0.24</td>
<td>1.12</td>
<td>1590</td>
<td>0.13</td>
</tr>
<tr>
<td>Polycarbonate</td>
<td>0.20</td>
<td>1.2</td>
<td>1260</td>
<td>0.13</td>
</tr>
<tr>
<td>Teflon</td>
<td>0.30</td>
<td>2.20</td>
<td>1050</td>
<td>0.13</td>
</tr>
<tr>
<td>Perspex</td>
<td>0.2</td>
<td>1.2</td>
<td>1500</td>
<td>0.11</td>
</tr>
</tbody>
</table>

Some work has been done on the use of ceramic containers (Ellern, 1968). The selection of ceramic bodies rather than metallic ones could have a favourable influence on marginal situations, especially where multiple columns occur in close proximity (Ellern, 1968).
3 Experimental

3.1 Reagents and Apparatus

3.1.1 Reagents

Powdered silicon was supplied by Millrox and obtained via AEL. The three types of silicon used in the present study, are listed in Table 3.1. Manganese powder with a specific surface area of 0,6 m²/g was supplied by Manganese Metal Company (Pty).

Table 3.1. Specific surface area for different types of silicon

<table>
<thead>
<tr>
<th>Silicon type</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific surface area [m²/g]</td>
<td>2,51</td>
<td>6,30</td>
<td>10,1</td>
</tr>
</tbody>
</table>

Table 3.2. Properties characteristics of bismuth subcarbonate

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>BET Specific Surface Area</td>
<td>m²/g</td>
<td>5-9</td>
</tr>
<tr>
<td>Bulk density</td>
<td>g/cm³</td>
<td>0,4</td>
</tr>
<tr>
<td>Density (theoretical)</td>
<td>g/cm³</td>
<td>6,9-8,3</td>
</tr>
<tr>
<td>Appearance</td>
<td></td>
<td>White</td>
</tr>
<tr>
<td>Particle size (from SEM images)</td>
<td>μm</td>
<td>6</td>
</tr>
<tr>
<td>Nitrate content</td>
<td>%</td>
<td>0,1</td>
</tr>
<tr>
<td>Alkalis and alkaline earth</td>
<td>%</td>
<td>0,3</td>
</tr>
</tbody>
</table>

Adcock Ingram supplied bismuth subcarbonate (Bi₂O₂CO₃) with the properties shown in Table 3.2. Bismuth oxide supplied by Aldrich Chemical Company, Inc., [1304-76-3]. Dry colloidal antimony pentoxide supplied by Nyacol® Nano Technologies, Inc.

Boron [7440-42-8] powder (Merck Cat. No.12070) was used as an energetic fuel additive. Di-boron trioxide [1303-86-2] (Merck Cat. No. 9024721) was used as flux additive. Potassium permanganate [7722-64-7] (Saarchem Cat. No. 504 68 20) used as additional oxidant. Fumed silica Aerosil 200 (supplied by Degussa) was used as inert diluent.
**Synthesis of $\text{Bi}_2\text{O}_3$**

Bismuth sesquioxide can be produced by several paths including the heating at high temperature (750-800°C) of either bismuth metal or bismuth monoxide in air. A similar result is obtained by thermal decomposition of bismuth compounds such as the basic carbonate, the carbonate, the nitrate or the oxalate (Long et al., 1992). The thermal decomposition of bismuth basic carbonate was chosen in this study as the process for the production of the trioxide.

In a typical procedure the heavy bismuth subcarbonate powder weighed into a ceramic crucible and then placed in a convection oven. The temperature was ramped up to 460°C at a rate of 145°C/h and maintained there for 15 hours. Thereafter the product was quenched to room temperature in air as suggested by Levin et al. (1962). To prevent re-carbonation the crucible was covered with a stainless steel lid immediately after removing from the oven.

**Synthesis of $\text{Sb}_6\text{O}_{13}$**

Heating antimony pentoxide ultimately yields antimony trioxide (Mellor, 1933). This transformation proceeds stepwise through a series of intermediates: $\text{Sb}_2\text{O}_3$ (400°C); $\text{Sb}_2\text{O}_4$ (700°C) and $\text{Sb}_2\text{O}_3$ at 900°C (Mellor, 1933). The cubic $\text{Sb}_6\text{O}_{13}$ (antimony hexatratridecoxide) was obtained as follows. The white colloidal $\text{Sb}_2\text{O}_5$ powder was placed in a crucible and covered with a steel lid with a small hole to allow gases to escape. It was then subjected to an 8-hour thermal treatment at 315°C in a convection oven. Thereafter the product was allowed to cool slowly back to room temperature in the oven. This resulted in a dark brown powder. It was characterised by XRD.

**3.2 Sample preparation**

**3.2.1 Preparation of pyrotechnic compositions**

The required quantities of the different ingredients (fuel, oxidant and additives) sufficient to yield 20 g batches were weighed into plastic containers (length = 120
mm and diameter = 80 mm) and blended thoroughly in a tumble mixer for 4 hours. Thereafter the mixture was passed gently through a 125 µm sieve using a soft brush. This process was repeated using the same sieve. In some instances a 53 µm sieve was used during the second brush-mixing. The sieve-brush-mixing operation was done to ensure break-up of agglomerates.

3.2.2 Preparation of delay elements

a. Lead delay elements

The powder mixture was poured into a 165 mm long lead tube with an average inner diameter of 6 mm. The tube wall thickness was between 2 and 3 mm. The tube ends were sealed by crimping with a pair of pliers. The composition in the tube was consolidated and compressed by a rolling operation that reduced the diameter in ten successive steps to 6 mm. A proprietary tube-rolling machine, supplied by AEL, was used for this purpose. During each rolling operation, the sealed tube was passed through a hole with a smaller diameter. This operation yielded a final tube approximately 420 mm long. The external diameter and wall thickness were 6 and 1.5 mm respectively. In this way, good compaction of the powdered delay composition was ensured. The rolled lead tube was then cut to a standard length of 45 mm to form the delay elements.

Where a starter composition was needed, a short increment of the required starter was filled into the top of the core after removing 3 mm of the main composition from the lead tube.

b. Aluminium delay elements

Aluminium delay elements were made by drilling holes through aluminium rods (6 mm ø) cut to a length of 45 mm. These tubes were filled incrementally. The mixture was compacted after adding each increment by inserting a punch and applying controlled compaction pressure that was measured by means of a load-cell device (HBM Komm). For most of the elements prepared in this way, the pressure was set at approximately 42 MPa. A dwell time of about one second was used before
relieving the stress. Thereafter the filled tube is sealed after introduction of different accessories including the anti-static cup, grommet and shock tubing.

---

*Figure 3.1 Apparatus for burning rate determination*
The delay elements were incorporated into a standard non-electric delay detonator assembly for burn-rate testing. First the delay element was placed inside an aluminium tube that was sealed at the other end. A plastic anti-static cup was introduced and pushed against the end of the lead tube followed by a rubber sealing grommet into the aluminium tube. It provided the anchor for the shock tubing. The latter that was inserted until it touched the bottom of the anti-static cup. At this point the free end of the aluminium tube was crimped to complete the assembly and to prevent any relative axial motion of individual elements in the assembly.

A hole (3mm) was drilled at the end of the element body, where a type R (0.38mm in diameter) thermocouple was embedded for measurement of burning rate.
3.2.4 Experimental set-up for burn rate measurements

The burn rates were measured using the experimental set-up shown schematically in Figures 3.1 and 3.2.

3.3 Burning rate measurement

3.3.1 Testing method

The trigger box emits an explosive noise when ignition of shock tube occurs. A sound sensor placed in the box (buffer) records this signal as the starting point for the burn reaction. This signal is transmitted to an electronic system provided with pre-amplification and an amplification circuit which delivers the required signal voltage to the computer.

The end of the burn is detected by means of thermocouple measurements recorded via a computer interface. A Pt-Pt 13% Rh thermocouple (type R) with a diameter of wires equals to 0.38mm, joined by flame, was embedded in the composition through a 3 mm hole in the closed end. The reaction speed was then calculated as the ratio of the length of the element and the burn time-interval. The latter was taken as the time difference between the starting signal (sound signal) and the final thermal signal provided by the thermocouple.

3.3.2 Recording of results.

The thermocouple output was sent via an electronic cold junction compensator to data capture software on an EAGLE PC 30F personal computer. The gain of amplification was varied between 100 and 1000. The signal-to-noise ratio was improved by utilising the digital filter described by Ricco (2004). The sound sensor output, after amplification, was also sent to data capture to get the starting signal.
3.4 Experimental variables

In this investigation the effect of the following variables on the burning rate of the appropriate delay composition was studied:

- Reagent stoichiometry
- Specific surface area of the composition ingredients
- The presence of additional fuels or oxidants
- The effect of diluents
- The nature and design (core size) of the tube materials.

3.5 Characterisation of reagents and combustion products

3.5.1 X-Ray Powder Diffraction Analysis (XRD)

Phase identification was carried out by XRD analysis performed on a Siemens D-501 automated diffractometer Cu Kα (1.5406 Å) operated at 40 kV and 40 mA. This machine is equipped with a divergence slit of 1°, a receiving slit of 0.05°. The sample was scanned from between 3 to 70°, on a 2θ-scale with a counting time of 1.5 s at room temperature.

3.5.2 X-Ray Fluorescence analysis (XRF)

The purity of reagents was determined using a wavelength-dispersive XRF spectrometer (ARL 9400 XP + XRF). The powders were ground in a tungsten carbide milling vessel and roasted at 1000°C for determination of the loss on ignition (LOI). An organic binder (ethyl cellulose) was used during pelletization of samples.

3.5.3 Scanning Electron Microscope (SEM)

Colloidal particles were viewed with a JEOL JSM 6000F cold field emission gun scanning electron microscope at high magnification. Ordinary materials, after gold-
coated, were viewed with a low magnification scanning electron microscope, a JEOL 840 SEM. Images and identification of some phases on residue samples have been obtained thanks to a backscatter JEOL JSM-6300 scanning microscope combined to a NORAN EDS System.

3.5.4 Brunauer-Emmett-Teller analysis (BET)

The specific surface area of different powders was performed with BET (Nova 1000e) under a constant gas flow of nitrogen.

3.5.5 Thermal analysis (DTA/TGA)

A Mettler Toledo A851 simultaneous TGA/SDTA machine was used for the thermal and gravimetric analysis. The TGA and DTA curves were obtained with air or nitrogen as purge gas at a scanning rate of 10°C /min. Experiments were performed in a 70μl alumina crucible with or without lids.

3.5.6 Fourier-Transform Infra Red Spectroscopy (FT-IR)

Bruker IFS 113 spectrometer at low pressures, operated at 32 scans with powder samples in pressed KBr pellets, was used to obtain infrared spectra. The wavelengths were recorded from 3500 to 400 cm⁻¹ in transmission mode of mid-infrared rays.
4 Results and Discussions

4.1 Results

4.1.1 Synthesis of $\text{Bi}_2\text{O}_3$

Bismuth sesquioxide was produced by thermal decomposition of the heavy-type subcarbonate ($\text{Bi}_2\text{O}_2\text{CO}_3$). The latter was kept in a convection oven at 460°C for 15 hours whereafter it was quenched in air. This temperature was chosen on the basis of the thermal behaviour of $\text{Bi}_2\text{O}_2\text{CO}_3$ observed in a TGA scan. See Appendix D: Figure 3. The decomposition reaction is:

$$\text{Bi}_2\text{O}_2\text{CO}_3 \text{ (s)} \rightarrow \text{Bi}_2\text{O}_3 \text{ (s)} + \text{CO}_2 \text{ (g)} \quad (1)$$

Product yields were 91.10 ± 0.2%, i.e. very close to the theoretical expected yield of 91.4%. XRD scans confirmed that the yellow powder obtained as product was the monoclinic phase of $\alpha$-$\text{Bi}_2\text{O}_3$ (See Figure 1 in Appendix A). XRF analysis suggested a purity of 97.8% with CuO and Na$_2$O as the major impurities. The presence of $\text{Bi}_2\text{O}_3$ was also confirmed by FT-IR. The vibration bands at 546.06; 512.70; 443.43 cm$^{-1}$ were in agreement with the pattern for a pure sample of $\text{Bi}_2\text{O}_3$ [1304-76-3] obtained from Aldrich Chemical Company [Figures 1 and 2 in Appendix B].

SEM revealed a spherical dendrite-like morphology where some nodules (1µm) are attached to the ends of a 3µm-long crystal (see Plate 1 in Appendix C). A specific surface area of 0.9 m$^2$/g was obtained by BET analysis. TGA of a 5 mg sample of this $\text{Bi}_2\text{O}_3$ at a scan rate of 10°C/min in nitrogen revealed a large weight loss (95%) at 1100°C. Figure 1 and 2 of appendix D show the TGA curves of pure $\text{Bi}_2\text{O}_3$ and the $\text{Bi}_2\text{O}_3$ produced in this study, respectively.

4.1.2 Synthesis of $\text{Sb}_6\text{O}_{13}$

DTA/TG analysis (at a scan rate of 20°C/min and a constant nitrogen flow maintained at 50 ml/min) of white colloidal $\text{Sb}_2\text{O}_5$ showed an endothermic decomposition at
330°C associated with a weight loss of approximately 17%. The crucible was covered with a lid during the decomposition (see Appendix D: Figure 4).

Based on this observation an 8-hour thermal treatment in convection oven at 315°C was chosen for the preparation of Sb\textsubscript{6}O\textsubscript{13}. This resulted in a mass loss of 19 ± 0.5% and yielded a dark brown powder. XRD confirmed that it was cubic Sb\textsubscript{6}O\textsubscript{13} (antimony hexitratridecoxide) but also showed that Sb\textsubscript{2}O\textsubscript{3} was present as an impurity (see Figure 5 in Appendix A).

When the thermal transformation of the antimony pentoxide was attempted in an uncovered alumina crucible, a brown and yellowish powder mixture corresponding to a poorly defined blend of Sb\textsubscript{6}O\textsubscript{13}, Sb\textsubscript{2}O\textsubscript{3}, and NaSb\textsubscript{5}O\textsubscript{8} was obtained. See XRD data in Figure 4: Appendix A). BET analysis showed that the specific surface area increased from the 4.55 m\textsuperscript{2}/g for the colloidal hydrated pentoxide form to 32.1 m\textsuperscript{2}/g for the final product (Sb\textsubscript{6}O\textsubscript{13}).

The SEM micrographs shown in Appendix C (Plates 2.a and 2.b) reveal the presence of closely packed nanoparticles in a coarse spherical conglomerate (diameter: 15 μm). Figure 5 in Appendix D, shows the TGA measured mass loss of Sb\textsubscript{6}O\textsubscript{13} when heated in nitrogen.

4.1.3 Burning rate

\textit{Sb\textsubscript{6}O\textsubscript{13} – Si systems}

The burn rate measurements for this system were performed using an initiating starter increment (3 mm) based on the Bi\textsubscript{2}O\textsubscript{3} – 50% Si (Type 4) mixture. The following variables affected the burning rate.

Effect of stoichiometry

The reaction between silicon and antimony hexitratridecoxide is described by the following reaction:
Figure 4.1 shows the effect of silicon content on the burn rate. Reaction (II) predicts a stoichiometric composition of 19.4% Si for this mixture. The observed maximum in the burning rate corresponds closely to this value. Note however that the data shows considerable scatter at this composition. A minimum burn rate of 4.8 mm/s was obtained with 10% Si (Type 4). Compositions containing less than 10% Si (Type 4) did not ignite. Above 20% Si (Type 3) the reaction released a considerable amount of heat and gas to the extent that the thermocouple was blown out.

\[ \text{Sb}_6\text{O}_{13} + 13/2 \text{ Si} \rightarrow 6\text{Sb} + 13/2 \text{SiO}_2 \] (II)

*Figure 4.1 Effect of stoichiometry on the burning rate of Si-\text{Sb}_6\text{O}_{13} system.*
Effect of the specific surface area of the fuel (Si)

Figure 4.1 shows that silicon Type 3, with a lower surface area than Type 4, actually burned faster. The reasons for this unexpected result are presently unknown. Note however that this fuel did not sustain the propagation in composition containing less than 20% Si whereas Type 4 did. Compositions containing an even coarser fuel (silicon Type 2) did not ignited at all.

Formulation:

\[
\text{Sb}_6\text{O}_{13} : \text{Si (Type 4)} = 90:10
\]

Figure 4.2 The effect of diluent fraction on the burning rate of \(\text{Sb}_6\text{O}_{13} - 10\% \text{ Si (Type 4)}\).

Effect of diluents

Figure 4.2 shows the effect of adding the inert diluent, i.e. fumed silica to a composition composed of \(\text{Sb}_6\text{O}_{13}\) with 10% Si (Type 4). Adding small amounts (< 2%) actually improved the burn rate. This may be attributed to the silica acting as a
mixing promoter and a compaction aid. Tulis (1980) proposed this explanation on the basis of theoretical principles. Beyond a 2% addition the burn rate decreases. Surprisingly compositions containing 10% fumed silica (add-on basis) still burned reliably giving a burning rate of 2.3 mm/s.

![Figure 4.3 Effect of the container on the burning rate of Sb₂O₁₃ – Si (Type 4) system.](image)

**Effect of tube material**

Two different tube materials were tested: Lead tubes with standard dimensions (length = 45mm; ID = 2-3 mm; OD 6mm) were prepared by rolling. Aluminium tubes were filled incrementally using a press. The compaction pressure was about 42 MPa applied for about 1 second for each increment. The influence of the nature of the tube is shown in Figure 4.3. Measured burn rates in the lead tubes were about 20-50% faster than those measured with the aluminium tubes.
Figure 4.4 shows that substitution of silicon with a coarse manganese fuel leads to even lower burn rates. Note that only compositions that contain more than 50% Mn ignited and burned in sustained manner.

**Sb₆O₁₃ – Mn system**

Figure 4.4 shows that substitution of silicon with a coarse manganese fuel leads to even lower burn rates. Note that only compositions that contain more than 50% Mn ignited and burned in sustained manner.

**Bi₂O₃ – Si System**

**Effect of silicon specific surface area and reagent stoichiometry**

Figure 4.5 shows the effect of reagent stoichiometry and silicon particle size on burn rate. The coarse silicon (Type 2) only burned in compositions containing >20% Si. Compositions containing the finer fuels burned over the whole concentration range
tested, i.e. 5-40% silicon (Types 3 and 4). A maximum burn rate was achieved at 20% fuel for Si Type 4. This maximum shifted to a somewhat higher silicon concentration for silicon Type 3. The data for Type 4 showed more scatter than Type 3. This probably indicates that homogeneous mixing was more difficult to achieve with the finer silicon.

Visual observation during the burn tests indicated that the compositions that showed high data scatter, e.g. the mixture containing 20% silicon (Type 4) were also gassier. The latter gave an average burn rate of 126.4 mm/s with a standard deviation of 21.5 mm/s. It is speculated that the variability in the performance of gassy systems is due to variable acceleration or deceleration of the front wave, depending on the direction of the gas transport, either forward or backward, depending on the location of leaks. That gas may be produced by the decomposition at high temperature (1100°C) is proven by the TGA curve for Bi₂O₃ shown in Figure 2, Appendix D.
The effect of the additives was determined for the composition containing 25% silicon Type 3. It was chosen because it showed little scatter in burn rate. B₂O₃, with its low melting point (450°C), was expected to play the role of a flux. The boron and the KMnO₄ respectively present the effects of addition of other fuels and oxidants. The results are shown in Figure 4.5 and indicate that these additives had a minor effect on the burn rate at addition levels up to 7%.

The addition of KMnO₄ appears to increase the burn rate when 5% is added. However, at this level the system behaviour becomes very gassy owing to the violent decomposition of KMnO₄. Addition of boron led to the production of even more gas.

Boron oxide (B₂O₃) with its low melting point (450°C) was expected to assist the reaction by generating a liquid phase. Instead it played the role of a retarder at all
compositions. This is attributed to the formation of a glassy phase (Levin and McDaniel, 1962).

![Graph showing the effect of different additives on the burning rate of $\text{Bi}_2\text{O}_3 - 25\% \text{ Si}$ (Type 3).]

**Figure 4.6** Effect of different additives on the burning rate of $\text{Bi}_2\text{O}_3 - 25\% \text{ Si}$ (Type 3).
Figure 4.7 shows the effect of tube wall material on the burn behaviour of the Bi$_2$O$_3$ – Si (Type 4) system. At low silicon concentrations the lead tube yields faster burn rates. However, above 25% silicon the burn rates are not affected by the nature of the tube material.

Effect of tube materials

Figure 4.7 shows the effect of tube wall material on the burn behaviour of the Bi$_2$O$_3$ – Si (Type 4) system. At low silicon concentrations the lead tube yields faster burn rates. However, above 25% silicon the burn rates are not affected by the nature of the tube material.
Figure 4.8 Effect of core diameter of tube on the burning rate of $\text{Bi}_2\text{O}_3$- 30% Si (Type 3) composition.

Effect of core size

Figure 4.8 shows that the burn rate for a 30% Si (Type 3)- $\text{Bi}_2\text{O}_3$ composition in aluminium tubes is not affected by the internal tube diameter when this lies in the range 2 to 5 mm.

Effect of mixing

The higher scatter observed in the burn rates of the $\text{Bi}_2\text{O}_3$ – Si systems containing finer silicon suggested that proper mixing might not have been achieved during the preparation of those samples. It was therefore decided to check the effect of using a finer mesh size during the mixing process. Figure 4.9 shows that burn rates are improved when the 125 μm is substituted with a 53 μm mesh sieve during mixing. A maximum burn rate of 156 mm/s was obtained for the 20% silicon Type 4 composition (standard deviation 11.4%).
EDS spectra taken during SEM analysis of the combustion residue from a 30% Si (Type 4) – Bi$_2$O$_3$ composition showed large peaks indicating the presence of silica and bismuth (see Plate 3a in Appendix C). XRD analysis of the same sample revealed the presence of metallic Bi (rhombohedral) but also the presence of minor amounts of unburned starting material (Bi$_2$O$_3$ and Si). See Figure 6 in Appendix A.

SEM photos showed the presence of a grey mass corresponding to amorphous silica. The bright spots in Plate 3.a, Appendix C, are due to metallic bismuth. Needle-like crystalline deposits were found and identified by EDS as silica. See Plate 4.a and 4.b in Appendix C.

**4.1.4 Identification of reaction products**

**Bi$_2$O$_3$ -Si system**

Figure 4.9 Effect of mixing degree on the burning rate of Bi$_2$O$_3$ - Si (Type 4) system.
The combustion residue of Sb\textsubscript{60}O\textsubscript{13} – 20\% Si (Type 4) from a lead tube were analysed using the SEM – EDS system. The micrographs shown in Plates 5.c and 5.e (Appendix C) reveal the presence of SiO\textsubscript{2} and metallic Sb as the main reaction products. Here too some needle-like crystallites were found at some interfaces and they were also identified to be SiO\textsubscript{2} (Appendix C: Plate 5.a).

XRD patterns revealed the presence of metallic Sb (rhombohedral) and also showed minor peaks due to unreacted Si (Figure 7 in Appendix A). No evidence of crystalline SiO\textsubscript{2} was obtained from the XRD.
5. Conclusion

Antimony hexatridecoxide (Sb$_6$O$_{13}$) and bismuth trioxide were successfully synthesized by controlled thermal decomposition. Sb$_6$O$_{13}$ was obtained by thermal treatment of colloidal antimony pentoxide (Sb$_2$O$_5$) at 315°C for 8 hours. The Bi$_2$O$_3$ was synthesised by heating (BiO)$_2$CO$_3$ at 460°C for 15 hours followed by rapid quenching to room temperature. These compounds were tested as oxidants for silicon in pyrotechnic time delay systems.

Burning rates in the Si (Type 4) – Sb$_6$O$_{13}$ system were carried out using an initiating starter increment (3 mm) based on a 50% Si (Type 4) – Bi$_2$O$_3$ mixture. Experimentally measured rates ranged from ca. 5 to 20 mm/s. The burning rate showed the usual parabolic shape dependence on stoichiometry: A maximum rate was found at 20% Si. The lowest sustainable and reproducible burn rate, in the absence of additives, was 4.8 mm/s (at 10% silicon Type 4). Below this level, the mixtures failed to burn.

The silicon Type 3 presented an unusual situation: Above 20% Si, the propagation of the burning front was faster than for the finer silicon (Type 4). The reasons for this unexpected result are presently unknown. Note however that this fuel did not sustain the propagation for composition containing less than 20% whereas Type 4 did.

Adding inert diluent (fumed silica) to a 10% Si (Type 4) – Sb$_6$O$_{13}$ mix caused a decreased burn rate at high addition levels. Surprisingly, combustion was sustained up to 10% of diluent, yielding a stable burn rate of 2.3 mm/s. This system is a potential replacement of the conventional barium sulphate-silicon system for long-period delays.

Coarse manganese powder was investigated as a potential substitute for silicon as fuel. Sb$_6$O$_{13}$-based compositions sustained combustion in the range 50 to 70% Mn. The burn rates were lower than additive-free silicon-based mixtures.
In the Si-Bi$_2$O$_3$ system, compositions containing 5-40% Si did not require a starter element and were ignitable with shock tubing. The mixture containing 20% silicon Type 4 burned fastest. Unfortunately the measured burn rates showed considerable scatter. This is attributed to the gassy combustion of this system. It is concluded that the fast burning Si-Bi$_2$O$_3$ system is a potential replacement for the commercial Si-red lead system. Before this system can be implemented the problem of reproducibility needs to be solved.

Fuel particle size did affect the burn rate in the Si-Bi$_2$O$_3$ system: Coarse silicon (Type 2) only burned in compositions containing >20% Si. The burn rate did not vary much with the silicon content. Silicon Type 3 compositions showed less scatter in the burn rate. The additives B, B$_2$O$_3$ and KMnO$_4$ showed little effect on the burning rate of a composition containing 25% silicon (Type 3) – Bi$_2$O$_3$ at addition levels up to 7%.

The effect of the material of construction of the delay element tube was also investigated. Measured burn rates in lead tubes were about 20 - 50% faster than equivalent rates measured using aluminium tubes. This accords with the higher thermal conductive aluminium tubes. They yield lower burn rates owing to the greater lateral loss of energy. Varying the core size of aluminium tubes from 2 to 5 mm did not affect the burn rate of a 30% Si (Type 3) – Bi$_2$O$_3$ composition.

Adequate mixing of the ingredients is essential. Its purpose is to break down particle agglomerates and facilitate good mixing, i.e. intimate contact between ingredient particles. The screen mesh size used for brush mixing appears to be an important factor: The burn rate of the 20% Si (Type 4) – Bi$_2$O$_3$ composition increased from 126.4 to 155.5 mm/s when a 125 µm screen was replaced by a 53 µm mesh sieve.

There is still a need for more information on the fundamental physico-chemical properties and reaction kinetics for Si-fuel reacting with either Bi$_2$O$_3$ or Sb$_2$O$_{13}$ as oxidant. It is recommended that a DTA study of the reaction kinetics be done.

The use of ceramic tubes should also be investigated as substitutes for the current lead tubes.
References

Al-Kazraji S.S. and Rees G.J. (1979b). The fast pyrotechnic reaction of silicon and red lead - Heats of reaction and rates of burning. Fuel, 58, 139-143.


Appendix A

Figure 1 XRD pattern of Bi$_2$O$_3$ produced by thermal decomposition of Bi$_2$O$_2$CO$_3$ at 460°C during 15 hours.
Figure 2 XRD pattern of pure Bi$_2$O$_3$
Appendix A

Figure 3 XRD Pattern of the Colloidal Sb$_2$O$_5$. 
Appendix A

Figure 4 XRD pattern of a product resulting from the thermal decomposition of Sb₂O₅ in an uncovered crucible
Figure 5 XRD pattern of \( \text{Sb}_2\text{O}_{13} \) from the thermal decomposition of \( \text{Sb}_2\text{O}_5 \) in a covered crucible.
Figure 6 XRD pattern of a combustion product from the system (Bi$_2$O$_3$-30%Si-type 4)
Figure 7 XRD pattern of a combustion product from the system (Sb₅O₁₃-20%Si -type 4)
Appendix B

![FT-IR Diagram of Pure Bi₂O₃](image)

*Figure 1 FT-IR Diagram of Pure Bi₂O₃.*
Figure 2 FT-IR diagram of Bi$_2$O$_3$ produced from thermal decomposition of Bi$_2$O$_2$CO$_3$ at 460 °C during 15 hours.
Appendix C

Plate 1 SEM micrograph for Bi$_2$O$_3$
Appendix C
2.a

Plate 2.a SEM micrograph for $\text{Sb}_6\text{O}_{13}$. 
Plate 2.b SEM micrograph for a sub-layer $\text{Sb}_8\text{O}_{13}$. 
Plate 3.a SEM micrograph of a residue from the combustion of Bi2O3 – 30% Si (type 4) in open air.

Figure 3.b EDS spectra obtained from a specific point on the glassy mass taken on the micrograph 3a.
Plates 4.a and 4.b SEM micrograph: Residue from the combustion of Bi2O3 – 30% Si (type 4), in confined lead tube.
Figure 4.c EDS spectra from a needle considered on the micrographs 4.a or 4.b.
Appendix C

5.a

Plate 5.a Micrographs for the residue from the combustion of $\text{Sb}_6\text{O}_{13}$ - 20%Si (type 4) in lead tube.

5.b

Figure 5.b EDS spectra for a specific needle selected on the micrograph 5.a.
Plate 5. c Micrographs for the residue from the combustion of $\text{Sb}_6\text{O}_{13} - 20\% \text{Si}$ (type 4) in lead tube.

Figure 5.d EDS spectra done on the body of the hemispherical particle selected on the micrograph 5.c
Plate 5.e Micrographs for the residue from the combustion of $\text{Sb}_6\text{O}_{13}$ - 20$\%$Si (type 4) in lead tube.

Figure 5.f EDS spectra done on the surface of a specific bright particle selected on the micrograph 5.e.
Appendix D

Figure 1 TGA curve of Pure Bi$_2$O$_3$.
Appendix D

Figure 2 TGA curve of Bi$_2$O$_3$ produced from thermal decomposition of Bi$_2$O$_2$CO$_3$ at 460°C during 15 hours.
Appendix D

Figure 3 TGA curve of Bi$_2$O$_2$CO$_3$. 
Appendix D

Figure 4 TGA curve of the colloidal Sb₂O₅.
Figure 5 TGA curve of Sb$_5$O$_{13}$ produced from thermal decomposition of Sb2O5 at 315°C during 8 hours.