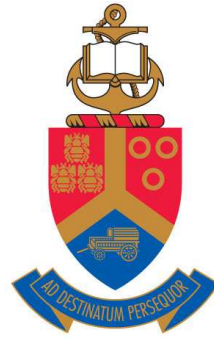




UNIVERSITEIT VAN PRETORIA  
UNIVERSITY OF PRETORIA  
YUNIBESITHI YA PRETORIA



UNIVERSITEIT VAN PRETORIA  
UNIVERSITY OF PRETORIA  
YUNIBESITHI YA PRETORIA

---

# MIMO CHANNEL MODELLING FOR INDOOR WIRELESS COMMUNICATIONS

BTJ MAHARAJ

2007



UNIVERSITEIT VAN PRETORIA  
UNIVERSITY OF PRETORIA  
YUNIBESITHI YA PRETORIA

# MIMO CHANNEL MODELLING FOR INDOOR WIRELESS COMMUNICATIONS

By

**Bodhaswar Tikanath Jugpershad MAHARAJ**

Promotor: Professor Dr L.P. Linde (University of Pretoria, South Africa)

Submitted in partial fulfillment of the requirements for the degree

**Philosophiae Doctor (Electronic)**

in the

Department of Electrical, Electronic & Computer Engineering

in the

School of Engineering

in the

Faculty of Engineering, Built Environment & Information Technology

UNIVERSITY OF PRETORIA

September 2007



# SUMMARY

---

MIMO CHANNEL MODELLING FOR INDOOR WIRELESS COMMUNICATIONS

by

Bodhaswar Tikanath Jugpershad MAHARAJ

Promotor: Professor Dr L.P. Linde (University of Pretoria, South Africa)

Department of Electrical, Electronic & Computer Engineering

Philosophiae Doctor (Electronic)

---

This thesis investigates multiple-input-multiple-output (MIMO) channel modelling for a wideband indoor environment. Initially the theoretical basis of geometric modelling for a typical indoor environment is looked at, and a space-time model is formulated. The transmit and receive antenna correlation is then separated and is expressed in terms of antenna element spacing, the scattering parameter, mean angle of arrival and number of antenna elements employed. These parameters are used to analyze their effect on the capacity for this environment. Then the wideband indoor channel operating at center frequencies of 2.4 GHz and 5.2 GHz is investigated. The concept of MIMO frequency scaling is introduced and applied to the data obtained in the measurement campaign undertaken at the University of Pretoria. Issues of frequency scaling of capacity, spatial correlation and the joint RX/TX double direction channel response for this indoor environment are investigated. The maximum entropy (ME) approach to MIMO channel modelling is investigated and a new basis is developed for the determination of the covariance matrix when only the RX/TX covariance is known. Finally, results comparing this model with the established Kronecker model and its application for the joint RX/TX spatial power spectra, using a beamformer, are evaluated. Conclusions are then drawn and future research opportunities are highlighted.

**Keywords:**

**MIMO channel modelling, frequency scaling, capacity, correlation and maximum entropy.**



# OPSOMMING

---

MIMO CHANNEL MODELLING FOR INDOOR WIRELESS COMMUNICATIONS

deur

Bodhaswar Tikanath Jugpershad MAHARAJ

Promotor: Professor Dr L.P. Linde (University of Pretoria, South Africa)

Departement Elektriese, Elektroniese & Rekenaar Ingenieurswese

Philosophiae Doctor (Elektronies)

---

Veelvuldige-inset-veelvuldige-uitset (VIVU) kanaalmodellering vir 'n wyeband binnemuurse omgewing word in hierdie proefskrif ondersoek. Die teoretiese basis van meetkundige modellering vir 'n tipiese binnemuurse omgewing is aanvanklik ondersoek en 'n ruimte-tyd model is geformuleer. Die stuur- en ontvangsantenna korrelasie is toe geskei en in terme van die antenna elementspasiëring, die verstrooiingsparameter, die gemiddelde aankomshoek en die aantal antenas wat gebruik is, uitgedruk. Hierdie parameters word gebruik om hulle effek op die kapasiteit van die kanaal te bepaal. Die gebruik van 2.4 GHz en 5.2 GHz in die wyeband binnemuurse omgewing is ondersoek. Die konsep van VIVU frekwensieskalering is met behulp van metings by die Universiteit van Pretoria getoets en toegepas. Frekwensieskalering van kapasiteit, ruimtelike korrelasie en die gesamentlike ontvang/stuur dubbelrigtingkanaalrespons is in hierdie omgewing ondersoek. Die maksimum entropie benadering vir VIVU kanaalmodellering is ondersoek en 'n nuwe basis vir die bepaling van die kovariansie matriks wanneer slegs die stuur/ontvang kovariansie bekend is, is ontwikkel. Laastens word resultate van hierdie model met die gevestigde Kronecker model vergelyk. Die toepassing van die gesamentlike stuur/ontvang ruimtelike drywingspektra word met behulp van 'n bundelvormer evalueer. Die studie maak gevolgtrekkings en lig moontlike toekomstige navorsingsgeleenthede uit.

**Sleutelwoorde:**

**VIVU kanaalmodellering, frekwensieskalering, kapasiteit, korrelasie en maksimum entropie.**



UNIVERSITEIT VAN PRETORIA  
UNIVERSITY OF PRETORIA  
YUNIBESITHI YA PRETORIA

**I dedicate this work to**

- The glory of our creator for giving me the intellect, energy and opportunity
- The Jugpershad Jewnath Family - they ventured, struggled and succeed in humility



## ACKNOWLEDGEMENTS

---

I would like to thank

- Professor Louis P. Linde for his support and encouragement
- Professor Jon W. Wallace for his technical guidance, insight and collaborative support
- The National Research Foundation (NRF), Thuthuka Program
- Professor Michael A. Jensen, Brigham Young University, USA
- My wife Pravina, and children Avikar and Akshay TJ



# CONTENTS

CHAPTER ONE - INTRODUCTION	<b>1</b>
1.1 Background and Motivation . . . . .	1
1.2 Author's Contributions and Outputs . . . . .	3
1.2.1 Research Contribution . . . . .	3
1.2.2 Journal Publications . . . . .	4
1.2.3 Conference Proceedings . . . . .	4
1.2.4 Invited Paper . . . . .	5
1.2.5 Additional Contributions . . . . .	5
1.3 Outline of Thesis . . . . .	6
CHAPTER TWO - CHANNEL MODELLING: AN OVERVIEW	<b>8</b>
2.1 MIMO Communication System Model . . . . .	8
2.2 MIMO System Capacity . . . . .	10
2.2.1 Water-Filling Capacity . . . . .	13
2.2.2 Uninformed Transmitter Capacity . . . . .	14
2.2.3 Diversity and Spatial Multiplexing . . . . .	14
2.3 Multipath Characterization . . . . .	15
2.3.1 Beamforming . . . . .	15
2.3.2 Bartlett Beamformer . . . . .	16
2.3.3 Capon Beamformer . . . . .	17
2.3.4 Double-Directional Channel Model . . . . .	18
2.3.5 Ray Tracing . . . . .	19
2.3.6 Geometric Models . . . . .	20
2.4 Conclusion . . . . .	24
CHAPTER THREE - GEOMETRIC MODELLING	<b>25</b>
3.1 Introduction . . . . .	25



3.2	Model Description . . . . .	26
3.3	Model Analysis . . . . .	28
3.4	Results . . . . .	33
3.5	Conclusion . . . . .	38
<b>CHAPTER FOUR - WIDEBAND MIMO MEASUREMENT SYSTEM</b>		<b>39</b>
4.1	Introduction . . . . .	39
4.2	System Overview . . . . .	40
4.3	System Components . . . . .	42
4.3.1	Transmitter Subsystem . . . . .	42
4.3.2	Receiver Subsystem . . . . .	43
4.3.3	Synchronization Module . . . . .	45
4.3.4	Monopole Antennas . . . . .	48
4.4	System Deployment . . . . .	50
4.4.1	Wideband Probing . . . . .	50
4.4.2	Calibration Procedure . . . . .	55
4.4.3	Measurement Environment . . . . .	57
4.4.4	Data Collection . . . . .	59
4.5	Conclusion . . . . .	61
<b>CHAPTER FIVE - DATA ANALYSIS AND MODEL ASSESSMENT</b>		<b>62</b>
5.1	Capacity Modelling . . . . .	65
5.1.1	Introduction . . . . .	65
5.1.2	Model Description . . . . .	65
5.1.3	Results . . . . .	67
5.2	Modelling Spatial Correlation . . . . .	74
5.2.1	Introduction . . . . .	74
5.2.2	Model Description . . . . .	74
5.2.3	Results . . . . .	76
5.3	Double Directional Channel Modelling . . . . .	81
5.3.1	Introduction . . . . .	81
5.3.2	Model Description . . . . .	82
5.3.3	Results . . . . .	83
5.4	Conclusion . . . . .	89





---

5.4.1	Capacity Modelling . . . . .	89
5.4.2	Spatial Correlation . . . . .	89
5.4.3	Double Directional Channel . . . . .	89
<b>CHAPTER SIX - MAXIMUM ENTROPY MODELLING</b>		<b>91</b>
6.1	Introduction . . . . .	91
6.2	Model Description . . . . .	92
6.3	Data Processing . . . . .	95
6.4	Results . . . . .	96
6.5	Conclusion . . . . .	104
<b>CHAPTER SEVEN - CONCLUSION</b>		<b>105</b>
7.1	Summary . . . . .	105
7.2	Future Recommendations . . . . .	107
<b>REFERENCES</b>		<b>108</b>



# LIST OF ABBREVIATIONS

2D	2-Dimensional
A/D	Analogue-to-Digital
AOA	Angle of Arrival
AOD	Angle of Departure
b/s/Hz	Bits per second per Hertz
ccdf	Complementary Cumulative Distribution Function
CIR	Channel Impulse Response
CIRC	Circular Array
COTS	Conventional Off-the-Shelf Components
CSI	Channel State Information
DDCIR	Double Directional Channel Impulse Response
DOA	Direction of Arrival
DOD	Direction of Departure
EVD	Eigenvalue Value Decomposition
EVT1/2	Event 1 or 2
FC	Full Covariance
I/O	Input-Output
IF	Intermediate Frequency
ISM	Industrial Scientific and Medical Bands
KM	Kronecker Model
LIN	Linear Array
LNA	Low Noise Amplifier
LO	Local Oscillator



LOS	Line-Of-Sight
ME	Maximum Entropy
MIMO	Multiple-Input-Multiple-Output
MIO	Multifunction Input-Output
MSE	Mean Square Error
NLOS	Non Line of Sight
PC	Personal Computer
PDF	Probability Distribution Function
RF	Radio Frequency
RX	Receiver
SIMO	Single-Input-Multiple-Output
SISO	Single-Input-Single-Output
SNR	Signal-to-Noise-Ratio
SP8T	Single-Pole-8-Throw
SVD	Singular Value Decomposition
SW	Switch
SYNC	Synchronization Unit
TOA	Time of Arrival
TTL	Transistor-Transistor Logic
TX	Transistor
UCA	Uniform Circular Array
ULA	Uniform Linear Array
UP	University of Pretoria
UPS	Uninterruptible Power Supply
UWB	Ultra-wideband
VIVU	Veelvuldige-Inset-Veevuldige-Uitset
WB	Wideband



# LIST OF FIGURES

2.1	Block diagram of a generic MIMO wireless system . . . . .	9
2.2	Ergodic capacity for a SISO channel vs SNR . . . . .	11
2.3	Comparison of Shannon capacity for SISO and ergodic capacity for Rayleigh fading MIMO Channels. . . . .	13
2.4	Uniform circular 8 element antenna array layout . . . . .	17
3.1	Geometric Model for a 2x2 MIMO channel . . . . .	27
3.2	ccdf versus capacity for varying antenna elements, $n_T = n_R$ . . . . .	34
3.3	ccdf versus capacity for varying antenna spacing, $d=d_{mn}$ . . . . .	35
3.4	ccdf versus capacity for varying scattering parameter, $k$ . . . . .	35
3.5	ccdf versus capacity for varying RX antenna orientation, $\beta$ . . . . .	37
3.6	ccdf versus capacity for varying SNR( $\rho$ ) in dB . . . . .	37
4.1	High level diagram of the wideband MIMO channel sounder . . . . .	41
4.2	High level block diagram of the TX subsystem . . . . .	42
4.3	Transmit RF module . . . . .	43
4.4	High level block diagram of the RX subsystem . . . . .	44
4.5	Block Diagram of the RX subsystem connections . . . . .	44
4.6	Simplified schematic of the SYNC unit . . . . .	46
4.7	Top view of SYNC Unit . . . . .	47
4.8	Reset/Trigger switch allowing simultaneous reset of two SYNC units . . . . .	49
4.9	Front view of SYNC Unit . . . . .	50
4.10	Rubidium frequency standard . . . . .	50
4.11	A 2.4 GHz Monopole antenna . . . . .	51
4.12	2.4 GHz Linear eight element array . . . . .	51
4.13	2.4 GHz Circular eight element array . . . . .	52
4.14	A 5.2 GHz Monopole antenna . . . . .	52
4.15	5.2 GHz Linear eight element array . . . . .	53



4.16	5.2 GHz Circular eight element array . . . . .	53
4.17	Grid plate layout for fixing monopole antenna array . . . . .	54
4.18	Example of multitone signal plotted versus time and frequency . . . . .	56
4.19	Procedures for system calibration: (a) original measurement setup, (b) single-channel calibration, and (c) direct matrix calibration . . . . .	57
4.20	System constructed and deployed at the University of Pretoria (UP) . . . . .	58
4.21	Measurement scenario in CEFIM at UP . . . . .	59
4.22	Switching sequence for measurements at each location . . . . .	60
4.23	Channel matrix representation . . . . .	60
5.1	Capacity PDF for the MIMO system at 2.4 GHz with different array configurations . . . . .	62
5.2	Capacity PDF for the MIMO system at 5.2 GHz with different array configurations . . . . .	63
5.3	Eigenvalue CDFs for linear arrays at 2.4 GHz and 5.2 GHz . . . . .	64
5.4	Eigenvalue CDFs for circular arrays at 2.4 GHz and 5.2 GHz . . . . .	64
5.5	Capacity versus excitation bandwidth at location 7 for ULA . . . . .	69
5.6	Capacity versus excitation bandwidth at location 9 for ULA . . . . .	69
5.7	Average capacity at each of the measurement locations using ULA . . . . .	70
5.8	Capacity versus excitation bandwidth at location 8 for circular array . . . . .	71
5.9	Capacity versus excitation bandwidth at location 9 for circular array . . . . .	71
5.10	Average capacity at each of the measurement locations in CEFIM . . . . .	73
5.11	Frequency scaling relationship of capacities in WB indoor environment . . . . .	73
5.12	Calculated relative correlation coefficients with curve fit for RX location 4 . . . . .	77
5.13	Calculated relative correlation coefficients with curve fit for RX location 7 . . . . .	77
5.14	Calculated relative correlation coefficients with curve fit for TX location 4 . . . . .	78
5.15	Calculated relative correlation coefficients with curve fit for TX location 8 . . . . .	78
5.16	Relationship of RX decorrelation with respect to frequency scaling . . . . .	80
5.17	Relationship of TX decorrelation with respect to frequency scaling . . . . .	80
5.18	Spatial spectra for Location 4 employing the Bartlett Beamformer . . . . .	84
5.19	Spatial spectra for Location 4 employing the Capon Beamformer . . . . .	84
5.20	Spectral contour for Location 4 employing the Bartlett Beamformer . . . . .	86
5.21	Spectral contour for Location 4 employing the Capon Beamformer . . . . .	86



5.22	Spatial spectra for Location 7 employing the Bartlett Beamformer . . . . .	87
5.23	Spatial spectra for Location 7 employing the Capon Beamformer . . . . .	87
5.24	Spatial spectra for Location 11 employing the Bartlett Beamformer . . . . .	88
5.25	Spatial spectra for Location 11 employing the Capon Beamformer . . . . .	88
6.1	Dominant singular eigenvalues for Location 3 at 2.4 GHz carrier frequency . .	98
6.2	Dominant singular eigenvalues for Location 7 at 2.4 GHz carrier frequency . .	98
6.3	Dominant singular eigenvalues for Location 3 at 5.2 GHz carrier frequency . .	99
6.4	Dominant singular eigenvalues for Location 7 at 5.2 GHz carrier frequency . .	99
6.5	Spatial power spectra for FC and ME at 2.4 GHz at Location 3 . . . . .	100
6.6	Spatial power spectra for FC and ME at 2.4 GHz at Location 7 . . . . .	101
6.7	Spatial power spectra for FC and ME at 5.2 GHz at Location 3 . . . . .	102
6.8	Spatial power spectra for FC and ME at 5.2 GHz at location 7 . . . . .	103



## LIST OF TABLES

4.1	Parameters of the example multitone signal . . . . .	55
5.1	TX/RX Pairwise Average Correlation of Capacity for ULA . . . . .	68
5.2	TX Pairwise Average Correlation of Capacity for UCA . . . . .	72
5.3	RX Pairwise Average Correlation of Capacity for UCA . . . . .	72
5.4	Decorrelation Parameter (b) and Error wrt Wavelength ( $\lambda$ ) at RX . . . . .	79
5.5	Decorrelation Parameter (b) and Error wrt Wavelength ( $\lambda$ ) at TX . . . . .	79
5.6	Correlation coefficient of 2.4 GHz and 5.2 GHz spectra . . . . .	85
6.1	Correlation coefficient of spatial power spectra at 2.4 GHz . . . . .	97
6.2	Correlation coefficient of spatial power spectra at 5.2 GHz . . . . .	97