

# **The application of Eulerian laser Doppler vibrometry to the on-line condition monitoring of axial-flow turbomachinery blades**

by

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## **Summary**

The on-line condition monitoring of turbomachinery blades is of utmost importance to ensure the long term health and availability of such machines and as such has been an area of study since the late 1960s. As a result a number of on-line blade vibration measurement techniques are available, each with its own associated advantages and shortcomings. In general, on-blade sensor measurement techniques suffer from sensor lifespan, whereas non-contact techniques usually have measurement bandwidth limitations. One non-contact measurement technique that yields improvements in the area of measurement bandwidth is laser Doppler vibrometry.

This thesis presents results and findings from utilizing laser Doppler vibrometry in an Eulerian fashion (i.e. a fixed reference frame) to measure on-line blade vibrations in axial-flow turbomachinery. With this measurement approach, the laser beam is focussed at a fixed point in space and measurements are available for the periods during which each blade sweeps through the beam. The characteristics of the measurement technique are studied analytically with an Euler-Bernoulli cantilever beam and experimental verification is performed. An approach for the numerical simulation of the measurement technique is then presented.

Associated with the presented measurement technique are the short periods during which each blade is exposed to the laser beam. This characteristic yields traditional frequency domain signal processing techniques unsuitable for providing useful blade health indicators. To obtain frequency domain information from such short signals, it is necessary to employ non-standard signal processing techniques such as non-harmonic Fourier analysis.

Results from experimental testing on a single-blade test rotor at a single rotor speed are presented in the form of phase angle trends obtained with non-harmonic Fourier analysis. Considering the maximum of absolute unwrapped phase angle trends around various reference frequencies, good indicators of blade health deterioration were obtained. These indicators were verified numerically.

To extend the application of this condition monitoring approach, measurements were repeated on a five-blade test rotor at four different rotor speeds. Various damage cases were considered as well as different ELDV measurement positions. Using statistical parameters of the abovementioned indicators as well as time domain parameters, it is shown that with this condition monitoring approach, blade damage can successfully be identified and quantified with the aid of artificial neural networks.

*Keyterms: Laser Doppler vibrometry, Eulerian measurements, Lagrangian measurements, on-line blade vibration, condition monitoring, non-harmonic Fourier analysis, phase angle trends, finite element modelling, artificial neural networks.*

# Die toepassing van Euler laser Doppler vibrometrie op die operasionele toestandsmonitering van aksiaalvloeiturbomasjinerie lemme

deur

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## Opsomming

Die operasionele toestandsmonitering van turbomasjinerie lemme is van uiterste belang met betrekking tot die langtermyn integriteit en beskikbaarheid van hierdie masjiene en is 'n gebied wat al sedert die laat 1960's bestudeer word. Gevolglik is daar 'n aantal operasionele lem-vibrasie meettegnieke beskikbaar, elk met sy eie sterk- en swakpunte. In die algemeen word sensors wat direk op die lemme geïnstalleer word, hoofsaaklik beperk deur sensorleef tyd. Nie-kontak tegnieke aan die ander kant, het gewoonlik meetbandwydte beperkings. 'n Nie-kontak meettegniek wat verbeterings bied op die gebied van meetbandwydte, is laser Doppler vibrometrie.

Hierdie proefskrif bied resultate en bevindings aan ten opsigte van die implementering van laser Doppler vibrometrie in 'n Euler verwysingsraamwerk, ten einde operasionele lem-vibrasies te meet op aksiaalvloeiturbomasjinerie. Met hierdie meetbenadering word die laserstraal gefokus op 'n vaste ruimtelike punt en is metings dan beskikbaar vir die periodes waartydens elke lem deur die laserstraal beweeg. Die eienskappe van die meettegniek word analities bestudeer met behulp van 'n Euler-Bernoulli kantelbalk waarna eksperimentele verifiëring uitgevoer word. 'n Metode om die meettegniek numeries te simuleer word dan aangebied.

Gepaardgaande met hierdie meettegniek is die kort periodes waartydens elke lem blootgestel word aan die laserstraal. Tradisionele seinprosesseringstegnieke is as gevolg daarvan nie geskik om bruikbare lemtoestandsaanwysers te lewer nie. Om frekwensiedomein inligting vanaf sulke kort seine te kry, is dit nodig om van nie-standaard seinprosesseringstegnieke soos nie-harmoniese Fourier analise gebruik te maak.

Resultate vanaf eksperimentele toetse op 'n enkellem toetsrotor by 'n vaste rotorspoed word aangebied in die vorm van fasehoek grafieke wat verkry is deur nie-harmoniese Fourier analise. Deur die maksimum van die absolute van ontvoude fasehoek grafieke te evalueer, word goeie aanduiders van lemttoestandsverswakking verkry. Die resultate word numeries geverifiëer.

Om hierdie toestandsmoniteringtegniek verder te verifiëer, word die metings herhaal op 'n vyf-lem toetsrotor teen verskillende rotasiesnelhede. Verskeie lemskade gevalle word beskou so wel as verskillende Euler meetposisies. Deur statistiese karakteristieke van die bogenoemde aanduiders asook tyddomein aanduiders te evalueer, word dit bewys dat met hierdie toestandsmoniteringtegniek lemskade suksesvol geïdentifiseer en gekwantifiseer kan word deur gebruik te maak van kunsmatige neurale netwerke.

*Sleuteltermes: Laser Doppler vibrometrie, Euler metings, Lagrange metings, operasionele lemvibrasie, toestandsmonitering, nie-harmoniese Fourier analise, fasehoek grafieke, eindige element modellering, kunsmatige neurale netwerke.*

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*“The fear of the LORD is the beginning of knowledge” (Proverbs 1:7)*



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## **Glossary**

### ***Abbreviations***

<b><u>Abbreviation</u></b>	<b><u>Description</u></b>
AC	Alternating Current
ADC	Analogue to Digital Converter
AIC	Akaike Information Criterion
ANN	Artificial Neural Network
AR	Autoregressive
ARMA	Autoregressive Moving Average
BLEP	Blade Leading Edge Profile
BPF	Blade Pass Frequency
CLSF-IO	Combined Non-Linear Least Squares Frequency Method On Input Output Spectra
CSLDV	Continuous Scanning Laser Doppler Vibrometry
DC	Direct Current
DEN	Denominator
ELDV	Eulerian Laser Doppler Vibrometry
ESPI	Electronic Speckle Pattern Interferometry
EV	Eigenvector
EVR	Eulerian Vibration Response
FBG	Fibre Bragg Grating
FEM	Finite Element Model
FFT	Fast Fourier Transform
FOD	Foreign Object Damage
FPE	Final Prediction Error
FRF	Frequency Response Function
HCF	High Cycle Fatigue
HFA	Harmonic Fourier Analysis
HI	Holographic Interferometry
HP	High Pressure
INVE	Iterative Noise Variance Estimation
LCF	Low Cycle Fatigue
LDV	Laser Doppler Vibrometer / Vibrometry

LP	Low Pressure
LVR	Lagrangian Vibration Response
LVRM	Lagrangian Vibration Response Matrix
MAUPAT	Maximum Absolute Unwrapped Phase Angle Trend
MBLEC	Mean Blade Leading Edge Curve
MDL	Minimum Description Length
MPC	Multi-Point Constraint
MUSIC	Multiple Signal Classification
MW	Megawatt
mW	milliwatt
NExT	Natural Excitation Technique
NHFA	Non-Harmonic Fourier Analysis
NOM	Nominator
ODS	Operational Deflection Shape
PI	Proportional-Integral
PPCRE	Predicted Percent Reconstruction Error
PPR	Pulses-Per-Revolution
PSD	Power Spectral Density
RBVC	Rigid Body Velocity Component
RC	Rotor Circumferential
RMS	Root-Mean-Square
RPM	Revolutions Per Minute
SCC	Stress Corrosion Cracking
SLDV	Scanning Laser Doppler Vibrometer / Vibrometry
SNR	Signal to Noise Ratio
TLDV	Tracking Laser Doppler Vibrometry
TOA	Time-Of-Arrival
UPA	Unwrapped Phase Angle
VI	Virtual Instrument

### ***Symbols***

<b><u>Symbol</u></b>	<b><u>Description</u></b>
A	ELDV measurement position
<i>a</i>	Fourier cosine coefficient



B	ELDV measurement position
$b$	Blade number
C	Cosine operator
$c$	Scanning speed
$c_{ref}$	Reference scanning speed
$c_{max}$	Maximum scanning speed
$D_b$	Blade-specific damage level [mm]
$d$	Fourier sine coefficient
$E_j$	$j^{\text{th}}$ modal constant
F	Force
$F_b$	Simulated blade force
$f$	Frequency
$f_{actual}$	Actual frequency
$f_{aliased}$	Aliased frequency
$f_{NQ}$	Nyquist frequency
$f_R$	MAUPAT reference frequency
$f_s$	Sampling frequency
$\Delta f_{min}$	Minimum required ELDV frequency resolution
$\Delta f$	Frequency resolution
G	NHFA signal approximation
$g$	Probe group size
H	Mobility FRF amplitude
$h$	Vector-loop diagram vector number
J	ELDV RMS run-down peak number
$j$	Mode / natural frequency number
$k$	Scanning speed ratio
$l$	Cantilever beam length
$m$	Harmonic number
N	Sample length
$N_k$	Interpolation sample length



$N_{ref}$	Reference sample length
$n$	Sample number
$P_b$	Average nozzle back-pressure waveform
$q_j$	$j^{\text{th}}$ generalized modal coordinate
$\bar{R}_1$	MBLEC offset vector
$\bar{R}_2$	Relative MBLEC measurement position vector
$\bar{R}_3$	Laser orientation vector
$\bar{R}_4$	Laser offset vector
$\bar{R}_5$	Absolute MBLEC measurement position vector
$\bar{R}_h$	Vector-loop diagram vector
$R_h$	$\bar{R}_h$ amplitude
$r$	Angular ELDV measurement radius
$S$	Sine operator
$t$	Time
$t_0$	Zero-based time vector
$t_N$	Sample time span
$\Delta t$	Time increment
$\hat{V}_{L,C_{ref}}$	LVRM
$\hat{V}_{L,W_{ref}}$	Angular LVRM
$v_E$	Eulerian vibration velocity
$\bar{v}_E$	EVR vector
$v_L$	Lagrangian vibration velocity
$\bar{v}_L$	LVR vector
$v_{RB}$	RBVC
$W_j$	$j^{\text{th}}$ characteristic function
$w_E$	Eulerian vibration displacement
$w_L$	Lagrangian vibration displacement
$X$	X-axis

$x_E$	Eulerian measurement position
$x_L$	Lagrangian measurement position
$\Delta x$	Measurement position increment
Y	Y-Axis
$y$	Time signal
Z	Z-axis

### ***Greek symbols***

<u><i>Symbol</i></u>	<u><i>Description</i></u>
$\beta_j$	$j^{\text{th}}$ modal root
$\delta$	$\bar{\varepsilon}$ offset
$\bar{\varepsilon}$	Rotor order vector
$\Phi$	NHFA detected phase angle
$\phi$	Phase angle
$\phi_d$	Damped phase angle
$\eta_h$	$\bar{R}_h$ angle
$\mathcal{G}$	Angular measurement range
$\varphi_E$	Eulerian angular measurement position
$\varphi_L$	Lagrangian angular measurement position
$\mu_b$	Pressure waveform normalization constant
$\theta$	Rotor angle
$\sigma$	Standard deviation
$\sigma_{CORR}$	Correlation coefficient standard deviation
$\sigma_{MAUPAT}$	MAUPAT standard deviation
$\sigma_{RMS}$	RMS standard deviation
$\tilde{\sigma}_{MAUPAT}$	Mean MAUPAT standard deviation
$\tau$	Total signal time span
$\varpi$	Arbitrary frequency
$\varpi_0$	Signal fundamental frequency
$\varpi_{ref}$	NHFA reference frequency
$\Delta \varpi$	Frequency offset



$\Omega_j$	$j^{\text{th}}$ modulation frequency
$\bar{\omega}$	$\omega_1$ estimate vector
$\omega_d$	Damped natural frequency
$\omega_j$	$j^{\text{th}}$ natural frequency
$\omega_1$	Blade first bending mode frequency
$\omega_{1,est}$	$\omega_1$ estimate
$\bar{\Psi}$	Rotation speed vector
$\psi$	Rotor speed
$\psi_{ref}$	Reference rotor speed
$\zeta$	Structural damping coefficient