A SCHEDULING MODEL

FOR

A COAL HANDLING FACILITY

Marinda Swart

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the degree

Master of Engineering (Industrial Engineering)
in the

FACULTY OF ENGINEERING, BUILT ENVIRONMENT
AND INFORMATION TECHNOLOGY

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A SCHEDULING MODEL FOR A COAL HANDLING FACILITY

An operational scheduling model for Sasol Coal Supply

Marinda Swart

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SUMMARY

A scheduling model for a coal handling facility

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Department: Industrial and Systems Engineering

Degree: Master of Engineering (Industrial Engineering)

Keywords: Scheduling; Mixed Integer Non-Linear Programming; MINLP; Coal handling facility; Continuous time representation; Event based scheduling; GAMS; Operational solution time; SOS1 variables; NLP linearization.

Summary:
The objective of this project is to develop an operational scheduling model for Sasol Mining’s coal handling facility, Sasol Coal Supply (referred to as SCS), to optimise daily operations. In this document, the specific scheduling problem at SCS is presented and solved using Mixed Integer Non-Linear Programming (MINLP) continuous time representation techniques.

The most recent MINLP scheduling techniques are presented and applied to an example problem. The assumption is made that the results from the example problem will display trends which will apply to the SCS scheduling problem as well. Based on this assumption, the unit-specific event based continuous time formulation is chosen to apply to the SCS scheduling problem.

The detail mathematical formulation of the SCS scheduling problem, based on the chosen technique, is discussed and the necessary changes presented to customise the formulation for the SCS situation. The results presented show that the first phase model does not solve within 72 hours. A solution time of more than three days is not acceptable for an operational scheduling model in a
dynamic system like SCS.

Various improvement approaches are applied during the second phase of the model development. Special Ordered Sets of Type 1 (SOS1) variables are successfully applied in the model to reduce the amount of binary variables. The time and duration constraints are restructured to simplify the structure of the model. A specific linearization and solution technique is applied to the non-linear equations to ensure reduced model solution times and reliable results.

The improved model for one period solves to optimality within two minutes. This dramatic improvement ensures that the model will be used operationally at SCS to optimise daily operations. The scheduling model is currently being implemented at SCS. Examples of the input variables and output results are presented.

It is concluded that the unit-specific event based MINLP continuous time formulation method, as presented in the literature, is not robust enough to be applied to an operational industrial-sized scheduling problem such as the SCS problem. Customised modifications to the formulation are necessary to ensure that the model solves in a time acceptable for operational use.

However, it is proved that Mixed Integer Non-linear Programming (MINLP) can successfully be applied to optimise the scheduling of an industrial-sized plant such as SCS. Although more research is required to derive robust formulation techniques, the principle of using mathematical methods to optimise operational scheduling in industry can dramatically impact the way plants are operated. The optimisation of daily schedules at SCS by applying the MINLP continuous time scheduling technique, has made a significant contribution to the coal handling industry.

Finally, it can be concluded that the SCS scheduling problem was successfully modelled and the operational scheduling model will add significant value to the Sasol Group.
ACKNOWLEDGEMENTS

I want to give all the honour to my Lord who has given me the insight and perseverance to complete this project successfully.

I also want to sincerely thank the following people for their invaluable contribution in my life:

Cor Swart (husband): For your unconditional love and support for better and for worse.

Professor PS Kruger (supervisor): For many shared life lessons and your continued enthusiasm.

Management at Sasol Mining: For the opportunity and the time you allowed me to complete this project.

Marthi Harmse (Sasol colleague): For your inputs and undying faith in MINLP scheduling.

Professor T Majozi (former Sasol colleague): For your guidance and support throughout this project.

Marinda Swart
October 2004
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<th>Description</th>
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</thead>
<tbody>
<tr>
<td>Cap_sj</td>
<td>capacity of stockpile j</td>
</tr>
<tr>
<td>Cost_i</td>
<td>cost of conveying coal from mine i</td>
</tr>
<tr>
<td>Delta</td>
<td>the size of an interval in the discrete time representation</td>
</tr>
<tr>
<td>Demand</td>
<td>coal demand of factory during time horizon</td>
</tr>
<tr>
<td>Dur_b_{i,p}</td>
<td>duration of conveying coal from mine i to stockpile j if it starts at point p</td>
</tr>
<tr>
<td>Dur_r_{j,p}</td>
<td>duration of reclaiming coal from stockpile j if it starts at point p</td>
</tr>
<tr>
<td>F_{i,p}</td>
<td>any continuous variable (NLP literature study)</td>
</tr>
<tr>
<td>Fmax_{i}</td>
<td>upper limit for the continuous variable $F_{i,p}$ (NLP literature study)</td>
</tr>
<tr>
<td>Fmin_{i}</td>
<td>lower limit for the continuous variable $F_{i,p}$ (NLP literature study)</td>
</tr>
<tr>
<td>G_{i,p}</td>
<td>any continuous variable (NLP literature study)</td>
</tr>
<tr>
<td>Gmax_{i,j}</td>
<td>upper limit for the continuous variable $G_{i,j,p}$ (NLP literature study)</td>
</tr>
<tr>
<td>Gmin_{i,j}</td>
<td>lower limit for the continuous variable $G_{i,j,p}$ (NLP literature study)</td>
</tr>
<tr>
<td>H</td>
<td>scheduling time horizon</td>
</tr>
<tr>
<td>i,ii</td>
<td>set of mines</td>
</tr>
<tr>
<td>Income</td>
<td>income per kt reclaimed (R/kt)</td>
</tr>
<tr>
<td>j</td>
<td>set of stockpiles</td>
</tr>
<tr>
<td>m_{i,p}</td>
<td>a continuous variable substituting the bilinear term (NLP literature study)</td>
</tr>
<tr>
<td>p</td>
<td>set of event points or time-slots</td>
</tr>
<tr>
<td>Q_{i,p}</td>
<td>quantity variable for event i in unit j at point p (SOS1 literature study)</td>
</tr>
<tr>
<td>QQ_{j,p}</td>
<td>SOS1 quantity variable for event i in unit j at point p (SOS1 literature study)</td>
</tr>
<tr>
<td>q_{b_{i,p}}</td>
<td>amount of coal conveyed from mine i to stockpile j at point p</td>
</tr>
<tr>
<td>q_{r_{j,p}}</td>
<td>amount of coal from mine i reclaimed from stockpile j at point p</td>
</tr>
<tr>
<td>q_supply_{i,p}</td>
<td>SOS1 variable: amount of coal supplied from mine i at point p to the set of stockpiles j</td>
</tr>
<tr>
<td>q_stack_{j,p}</td>
<td>SOS1 variable: amount of coal stacked on stockpile j at point p from the set of mines i</td>
</tr>
<tr>
<td>Rate_b_{i}</td>
<td>rate for conveying coal from mine i</td>
</tr>
<tr>
<td>Rate_r_{j}</td>
<td>rate for reclaiming coal from stockpile j</td>
</tr>
<tr>
<td>Ratio1_{i,j,p}</td>
<td>variable to substitute the bilinear terms in NLP linearization</td>
</tr>
<tr>
<td>Ratio2_{i,j,p}</td>
<td>variable to substitute the bilinear terms in NLP linearization</td>
</tr>
<tr>
<td>ST_s_{i,j,p}</td>
<td>amount of coal from mine i on stockpile j at point p</td>
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<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>ST0_sij</td>
<td>starting level of mine i contribution to stockpile j</td>
</tr>
<tr>
<td>Tp</td>
<td>time value of a global event point at point p</td>
</tr>
<tr>
<td>Tk</td>
<td>time value of a global event point at point k (literature study)</td>
</tr>
<tr>
<td>TF_bijp</td>
<td>time value if conveying coal from mine i to stockpile j stops at point p</td>
</tr>
<tr>
<td>TF_rjkp</td>
<td>time value if reclaiming coal from stockpile j stops at point p</td>
</tr>
<tr>
<td>Ts_bijp</td>
<td>time value if conveying coal from mine i to stockpile j starts at point p</td>
</tr>
<tr>
<td>Ts_rjkp</td>
<td>time value if reclaiming coal from stockpile j starts at point p</td>
</tr>
<tr>
<td>wijp</td>
<td>binary variable indicating that coal is conveyed from mine i to stockpile j at point p</td>
</tr>
<tr>
<td>wijkl</td>
<td>four index binary variable to assign stage l of order i to slot k of unit j (literature study)</td>
</tr>
<tr>
<td>Wip</td>
<td>binary variable indicating task i to be done at point p</td>
</tr>
<tr>
<td>xjp</td>
<td>binary variable indicating that coal is reclaimed from stockpile j at point p</td>
</tr>
<tr>
<td>Xijp</td>
<td>binary variable indicating task i to be done in unit j at point p (literature study)</td>
</tr>
<tr>
<td>Xijkk'</td>
<td>binary variable to indicate the task i starting in unit j at time T_k and ending at T_k' (literature study)</td>
</tr>
<tr>
<td>Yjp</td>
<td>binary variable indicating unit j to be used at point p</td>
</tr>
<tr>
<td>yjp</td>
<td>binary variable indicating stacking coal on stockpile j at p</td>
</tr>
<tr>
<td>zmax</td>
<td>objective function variable to maximise profit</td>
</tr>
</tbody>
</table>

### Chapter 3:

- **Bunk_min**  
The minimum level of any bunker
- **Cap_b**  
Capacity of bunker i
- **Cap_strat**  
Capacity of strategic stockpile j
- **CL_sl**  
Limit for strategic stockpile coal contribution to the total amount of coal supplied to the factory at any point p
- **CL_i**  
Limits for source i contribution to the total feed to the factory at any point
- **Cost**  
The handling cost when throwing out and loading back coal at the bunkers or the strategic stockpiles
- **CT_bij**  
Change-over time lost when starting extraction from bunker i to stockpile j
- **CT_rk,kk**  
Change-over time lost when changing the reclaimer position from stockpile k to kk, given there are no stockpiles between k and kk
- **CT_sk,kk**  
Change-over time lost when changing the stacker position from stockpile k to kk
- **Dem_e**  
Coal demand of Eastern factory during time horizon
- **Dem_w**  
Coal demand of Western factory during time horizon
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{Dur}_{bi}p$</td>
<td>duration of extracting coal from bunker $i$ to yard $j$ if it starts at point $p$</td>
</tr>
<tr>
<td>$\text{Dur}_{bl}ip$</td>
<td>duration of loading back coal at bunker $i$ if it starts at point $p$</td>
</tr>
<tr>
<td>$\text{Dur}_{min}$</td>
<td>the minimum duration when coal is extracted from a bunker</td>
</tr>
<tr>
<td>$\text{Dur}_{mi}p$</td>
<td>duration of source $i$ production if production starts at point $p$</td>
</tr>
<tr>
<td>$\text{Dur}_{rjk}p$</td>
<td>duration of reclaiming coal from stockpile $k$, yard $j$ if it starts at point $p$</td>
</tr>
<tr>
<td>$\text{Dur}_{sjk}p$</td>
<td>duration of stacking coal on stockpile $k$, yard $j$ if it starts at point $p$</td>
</tr>
<tr>
<td>$\text{Dur}_{sljk}p$</td>
<td>duration of loading back coal from strategic stockpile $j$ to specific stockpile $k$, if it starts at point $p$</td>
</tr>
<tr>
<td>$H$</td>
<td>scheduling time horizon</td>
</tr>
<tr>
<td>$H_m_r$</td>
<td>end-of-period time value for each period $r$</td>
</tr>
<tr>
<td>$\text{heap}0_{sk}$</td>
<td>starting heap length of stockpile $k$ on yard $j$</td>
</tr>
<tr>
<td>$\text{heap}_{li}jk$</td>
<td>heap length of stockpile $k$, yard $j$, at point $p$</td>
</tr>
<tr>
<td>$HH$</td>
<td>a big value</td>
</tr>
<tr>
<td>$i, ii$</td>
<td>set of sources</td>
</tr>
<tr>
<td>$\text{Income}_{r}$</td>
<td>income per ton reclaimed</td>
</tr>
<tr>
<td>$\text{Income}_{s}$</td>
<td>income per ton stacked</td>
</tr>
<tr>
<td>$j, jj$</td>
<td>set of stockpile yards</td>
</tr>
<tr>
<td>$k, kk$</td>
<td>set of individual stockpiles per yard</td>
</tr>
<tr>
<td>Loaders</td>
<td>the number of front-end loaders available for loading back coal at the bunkers and the strategic stockpiles</td>
</tr>
<tr>
<td>$\text{Max}0_{sk}$</td>
<td>the maximum capacity of a stockpile $k$ on yard $j$</td>
</tr>
<tr>
<td>$\text{Min}_{length}$</td>
<td>the minimum length for any individual stockpile $k$</td>
</tr>
<tr>
<td>$\text{Out}_{bi}p$</td>
<td>amount of coal outside bunker $i$ at point $p$</td>
</tr>
<tr>
<td>$\text{Out}_{0bi}$</td>
<td>starting level of coal outside bunker $i$</td>
</tr>
<tr>
<td>$p$</td>
<td>set of event points</td>
</tr>
<tr>
<td>per$_p$</td>
<td>subset to assign event points to periods</td>
</tr>
<tr>
<td>$\text{Pos}_{rjk}$</td>
<td>reclaimer position tracking variable for stockpile $k$, yard $j$, point $p$</td>
</tr>
<tr>
<td>$\text{Pos}_{0rk}$</td>
<td>starting reclaiming position on stockpile $k$, yard $j$</td>
</tr>
<tr>
<td>$\text{Pos}_{0sk}$</td>
<td>starting stacker position on stockpile $k$, yard $j$</td>
</tr>
<tr>
<td>Prop$_{penalty}$</td>
<td>penalty when coal is bypassed directly to the factory</td>
</tr>
<tr>
<td>$q_{bi}p$</td>
<td>amount of coal extracted from bunker $i$ to yard $j$, point $p$</td>
</tr>
<tr>
<td>$q_{bl}ip$</td>
<td>amount of coal loaded back at bunker $i$ at point $p$</td>
</tr>
<tr>
<td>$q_{bo}ip$</td>
<td>amount of coal thrown out at bunker $i$ at point $p$</td>
</tr>
</tbody>
</table>
### NOMENCLATURE (CONTINUE)

- $q_{m_i^p}$: amount of coal produced by source $i$ at point $p$
- $q_{\text{prop}_{ijp}}$: amount of coal from source $i$ bypassed at yard $j$, point $p$
- $q_{r_{ijkp}}$: amount of coal from source $i$ reclaimed from yard $j$, stockpile $k$ at point $p$
- $q_{r_{sl_{jkp}}}$: amount of coal from strategic stockpile $j$ that were loaded back to stockpile $k$ and reclaimed at point $p$
- $q_{s_{ijkp}}$: amount of coal from source $i$ stacked on yard $j$, stockpile $k$ at point $p$
- $q_{s_{l_{jkp}}}$: amount of coal loaded back from strategic stockpile $j$ to stockpile $k$ at point $p$
- $q_{s_{o_{jp}}}$: amount of coal thrown out at strategic stockpile $j$ at point $p$
- $r$: set of time periods
- $\text{Rate}_{b_{j}}$: maximum rate for conveying coal from bunker $i$
- $\text{Rate}_{bl}$: rate for loading back coal with one front-end loader at the bunkers or the strategic stockpiles
- $\text{Rate}_{f}$: the maximum rate at which one side of the factory can receive coal
- $\text{Rate}_{m_{ir}}$: production rate of source $i$ in period $r$
- $\text{Rate}_{r}$: the maximum rate at which any reclaimer can reclaim
- $\text{Rate}_{s}$: the maximum rate at which any stacker can stack
- $ST_{b_{ip}}$: amount of coal stored in bunker $i$ at point $p$
- $ST_{s_{l_{jkp}}}$: amount of strategic stockpile coal on stockpile $k$, yard $j$, at point $p$
- $ST_{s_{m_{ijkp}}}$: amount of coal from source $i$ on stockpile $k$, yard $j$, at point $p$
- $ST0_{b_{i}}$: starting level of bunker $i$
- $ST0_{s_{l_{jk}}}$: starting level of coal from strategic stockpile $j$ on stockpile $k$
- $ST0_{s_{m_{ijk}}}$: starting level of source $i$ contribution to stockpile $k$ on yard $j$
- $\text{Strat}_{0_{j}}$: starting level of strategic stockpile $j$
- $\text{Strat}_{ip}$: amount of coal on strategic stockpile $j$ at point $p$
- $Tf_{b_{ip}}$: finishing time value if extracting coal from bunker $i$ to yard $j$ stops at point $p$
- $Tf_{bl_{ip}}$: finishing time value if loading back coal at bunker $i$ stops at point $p$
- $Tf_{m_{ip}}$: finishing time value if source $i$ production stops at point $p$
- $Tf_{r_{jkp}}$: finishing time value if reclaiming coal from stockpile $k$, yard $j$ stops at point $p$
- $Tf_{s_{jkp}}$: finishing time value if stacking coal from source $i$ on stockpile $k$, yard $j$ stops at point $p$
- $Tf_{s_{l_{jp}}}$: finishing time value if loading back coal from strategic stockpile $j$ stops at point $p$
- $\text{Tot_length}$: total length of any yard $j$
- $\text{Total}_{e_{p}}$: total feed to the Eastern factory at point $p$
- $\text{Total}_{w_{p}}$: total feed to the Western factory at point $p$
**NOMENCLATURE (CONTINUE)**

- $T_{s_{b_{ijp}}}$ starting time value if extracting coal from bunker $i$ to yard $j$ \textit{starts} at point $p$
- $T_{s_{bl_{ip}}}$ starting time value if loading back coal at bunker $i$ \textit{starts} at point $p$
- $T_{s_{m_{ip}}}$ starting time value if source $i$ production \textit{starts} at point $p$
- $T_{s_{r_{jkp}}}$ starting time value if reclaiming coal from stockpile $k$, yard $j$ \textit{starts} at point $p$
- $T_{s_{s_{jkp}}}$ starting time value if stacking coal from source $i$ on stockpile $k$, yard $j$ \textit{starts} at point $p$
- $T_{s_{sl_{jp}}}$ starting time value if loading back coal from strategic stockpile $j$ \textit{starts} at point $p$
- $T_{s0_{m_{r}}}$ starting time value for each period $r$
- $v_{1_{ip}}$ binary variable indicating that coal is thrown out at bunker $i$ at point $p$
- $v_{2_{ip}}$ binary variable indicating that coal is loaded back into bunker $i$ at point $p$
- $w_{ijp}$ binary variable indicating that coal is conveyed from mine $i$ to stockpile $j$ at point $p$
- $w_{w_{jkp}}$ binary variable indicating coal is stacked on yard $j$, stockpile $k$ at point $p$
- $x_{2_{ijp}}$ binary variable indicating that coal is bypassed from mine $i$ to yard $j$, at point $p$
- $x_{kp}$ binary variable indicating coal is reclaimed from yard $j$, stockpile $k$ at point $p$
- $y_{jkp}$ binary variable indicating a new stockpile is created on position $k$, yard $j$, at point $p$
- $z_{1_{jp}}$ binary variable indicating that coal is thrown out at strategic stockpile $j$ at point $p$
- $z_{2_{jp}}$ binary variable indicating that coal is loaded back from strategic stockpile $j$ at point $p$
- $z_{max}$ objective function variable to maximise profit

**CHAPTER 4:**

- $a$ set of options for coal extracted from the bunker
- $b$ set of options for coal conveyed to the stacker
- $B_{blend_{e_{ip}}}$ the variable to substitute the non-linear part in the Eastern blend equation during linearization, represents the blend of the coal loaded back from the strategic stockpiles at a specific point $p$
- $B_{blend_{w_{ip}}}$ the variable to substitute the non-linear part in the Western blend equation during linearization, represents the blend percentage of the coal loaded back from the strategic stockpiles at a specific point $p$
- $B_{blend_{e_{ip}}}$ the variable to substitute the non-linear part in the Eastern blend equation during linearization, represents the blend percentage of a specific mine $i$'s coal at a specific point $p$
- $B_{blend_{w_{ip}}}$ the variable to substitute the non-linear part in the Western blend equation during linearization, represents the blend percentage of a specific mine $i$'s coal at a specific point $p$
<table>
<thead>
<tr>
<th>NOMENCLATURE (CONTINUE)</th>
</tr>
</thead>
</table>

- **Bleedin**\(_e_p\)**: the percentage contribution of coal loaded back from the strategic stockpile in the total amount of coal supplied to the Eastern factory at point \(p\).
- **Bleedin**\(_w_p\)**: the percentage contribution of coal loaded back from the strategic stockpile in the total amount of coal supplied to the Western factory at point \(p\).
- **Blend**\(_e_ip\)**: the percentage contribution of mine \(i\)'s coal in the total amount of coal supplied to the Eastern factory at point \(p\).
- **Blend**\(_w_ip\)**: the percentage contribution of mine \(i\)'s coal in the total amount of coal supplied to the Western factory at point \(p\).
- **Bunk\(_\text{min}\)**: the minimum level of any bunker.
- **Cap\(_{bi}\)**: capacity of bunker \(i\).
- **CL\(_\text{bleedin}\)**: limit for strategic stockpile coal contribution to the total amount of coal supplied to the factory at any point \(p\).
- **CL\(_e_i\)**: blend plan contribution percentage of mine \(i\)'s coal supplied to the Eastern factory.
- **CL\(_w_i\)**: blend plan contribution percentage of mine \(i\)'s coal supplied to the Western factory.
- **Cl\(_\text{bleedin}\)**: blend plan contribution percentage of strategic stockpile coal supplied to the Eastern factory.
- **CL\(_i\)**: limits for source \(i\)'s contribution to the total feed to the factory at any point.
- **CL\(_w\_\text{bleedin}\)**: blend plan contribution percentage of strategic stockpile coal supplied to the Western factory.
- **CT\(_bi\)**: change-over time lost when starting extraction from bunker \(i\) to stockpile \(j\).
- **CT\(_r_{k,kk}\)**: change-over time lost when changing the reclaimer position from stockpile \(k\) to \(kk\), given there are no stockpiles between \(k\) and \(kk\).
- **d**: set of options for coal handling outside a bunker or a strategic stockpile.
- **Dur\(_bl_ip\)**: duration of loading back coal at bunker \(i\) if it starts at point \(p\).
- **Dur\(_\text{min}\)**: the minimum duration when coal is extracted from a bunker.
- **Dur\(_m_ip\)**: duration of source \(i\)'s production if production starts at point \(p\).
- **Dur\(_\text{prop}_{ijp}\)**: duration of the bypass event from mine \(i\) to yard \(j\), starting at point \(p\).
- **Dur\(_r_{kp}\)**: duration of reclaiming coal from stockpile \(k\), yard \(j\) if it starts at point \(p\).
- **Dur\(_r_{jpf}\)**: SOS1 variable to indicate the duration of either an operational event or a maintenance event (set \(f\)) at reclaimer \(j\), point \(p\).
- **Dur\(_\text{rmaint}_{jr}\)**: required reclaimer \(j\)'s maintenance during period \(r\).
- **Dur\(_s_{jpf}\)**: SOS1 variable to indicate the duration of either an operational event or a maintenance event (set \(f\)) at reclaimer \(j\), point \(p\).
event (set f) at stacker j, point p

$\text{Dur}_{\text{smaint}}_{jr}$ required stacker j maintenance during period r

f set of equipment availability options

H scheduling time horizon

HH a big value

i, ii set of sources

$\text{ie}_i$ set of Eastern sources (subset of sources i)

$\text{iw}_i$ set of Western sources (subset of sources i)

j, jj set of stockpile yards

k, kk set of individual stockpiles per yard

Loaders the number of front-end loaders available for loading back coal at the bunkers and the strategic stockpiles

$\text{Max}_{0_s} \text{jk}$ the maximum capacity of a stockpile k on yard j

Out$_b_{ip}$ amount of coal outside bunker i at point p

$\text{Portion}_{1_{ijkp}}$ the variable to substitute the non-linear part in the reclaiming process equation during linearization, represents the layers of a specific mine i's coal

$\text{Portion}_{2_{jkp}}$ the variable to substitute the non-linear part in the reclaiming process equation during linearization, represents the layers of coal loaded back from the strategic stockpile

Pos$_r_{jkp}$ reclaimer position tracking variable for stockpile k, yard j, at point p

Pos$_0_{rjk}$ starting reclaiming position on stockpile k on yard j

q$_{bfel_{ipd}}$ SOS1 variable to ensure that the front-end loaders are used for only one of the handling options d at bunker i, point p

q$_{b_{ipj}}$ SOS1 variable for the amount of coal extracted from bunker i to stockpile yard j at point p, where set j is controlled

q$_{bopt_{ipja}}$ SOS1 variable to ensure that only one of the options a is chosen for the stream of coal extracted from bunker i to stockpile yard j at point p

q$_{e2w_{p\text{ie}}}$ SOS1 variable for the total amount of coal conveyed from the Eastern mines i e to the Western stockpiles at point p, where set ie is controlled

q$_{m_{ip}}$ amount of coal produced by source i at point p

q$_{mopt_{ipc}}$ SOS1 variable to ensure that only one option c is activated for mine i's production at point p

q$_{prop_{ipj}}$ SOS1 variable for the amount of coal bypassed at stockpile yard j from bunker i to at point p, where set j is controlled
NOMENCLATURE (CONTINUE)

$q_{r_{ijp}}$ amount of coal from source $i$ reclaimed from stockpile $k$, yard $j$ at point $p$

$q_{rs_{ljkp}}$ amount of coal from strategic stockpile $j$ that were loaded back to stockpile $k$ and reclaimed at point $p$

$q_{s_{jkp}}$ amount of coal from source $i$ stacked on stockpile $k$, yard $j$ at point $p$

$q_{s_{ljkp}}$ amount of coal loaded back from strategic stockpile $j$ to stockpile $k$ at point $p$

$q_{s_{opt_{ljp}}}$ SOS1 variable to ensure that only one of the options $b$ is chosen for the type of coal conveyed to stacker $j$ at point $p$

$q_{s_{upply_{lpi}}}$ SOS1 variable for the amount of coal supplied to stacker $j$ from bunker $i$ to at point $p$, where set $i$ is controlled

$q_{w_{2e_{p_{iw}}}}$ SOS1 variable for the total amount of coal conveyed from the Western mines $iw$ to the Eastern stockpiles at point $p$, where set $iw$ is controlled

$QQ_{lpi}$ SOS1 quantity variable for event $i$ in unit $j$ at point $p$ (literature study)

$Rate_{-b_j}$ maximum rate for conveying coal from bunker $i$

$Rate_{-bl}$ rate for loading back coal with one front-end loader at the bunkers or the strategic stockpiles

$Rate_{-f}$ the maximum rate at which one side of the factory can receive coal

$Rate_{-m_r}$ production rate of source $i$ in period $r$

$Rate_{-r}$ the maximum rate at which any reclaimer can reclaim

$Rate_{-s}$ the maximum rate at which any stacker can stack

$Ratio_{jlkp}$ the ratio in which the layers on the stockpile is reclaimed during the reclaiming process

$ST_{-b_{ip}}$ amount of coal stored in bunker $i$ at point $p$

$ST_{-s_{ljkp}}$ amount of strategic stockpile coal on stockpile $k$, yard $j$, at point $p$

$ST_{-sm_{ijkp}}$ amount of coal from source $i$ on stockpile $k$, yard $j$, at point $p$

$Strat_{jp}$ amount of coal on strategic stockpile $j$ at point $p$

$Tf_{-b_{ijp}}$ finishing time value if extracting coal from bunker $i$ to yard $j$ stops at point $p$

$Tf_{-bl_{ip}}$ finishing time value if loading back coal at bunker $i$ stops at point $p$

$Tf_{-m_{ip}}$ finishing time value if source $i$ production stops at point $p$

$Tf_{-prop_{ijp}}$ finish time value if coal is bypassed to the factory from mine $i$ at yard $j$, starting at point $(p-1)$

$Tf_{-r_{ijp}}$ finishing time value for any reclaiming event on yard $j$ that started at the previous point $(p-1)$

$Tf_{-s_{ijp}}$ finishing time value for any event involving the stacker on yard $j$ at the previous point $(p-1)$
**NOMENCLATURE (CONTINUE)**

- **Tot_length**
  - total length of any yard \( j \)

- **Total_w_p**
  - total feed to the Western factory at point \( p \)

- **Ts_bl_ip**
  - starting time value if loading back coal at bunker \( i \) starts at point \( p \)

- **Ts_m_ip**
  - starting time value if source \( i \) production starts at point \( p \)

- **Ts_re_p**
  - starting time value for any reclaiming or bypassing event on the Eastern side at point \( p \)

- **Ts_rw_p**
  - starting time value for any reclaiming or bypassing event on the Western side at point \( p \)

- **Ts_sjp**
  - starting time value for any event involving the stacker on yard \( j \) at point \( p \)

- **ww_{jkp}**
  - binary variable indicating coal is stacked on yard \( j \), stockpile \( k \) at point \( p \)

- **x2_{ijp}**
  - binary variable indicating coal is bypassed from mine \( i \) to yard \( j \), at point \( p \)

- **x_{jkp}**
  - binary variable indicating coal is reclaimed from yard \( j \), stockpile \( k \) at point \( p \)

- **z_{max}**
  - objective function variable to be maximised