

**A MULTI-DIMENSIONAL MEASURE OF  
POVERTY IN SOUTH AFRICA**

*by*

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“Poverty deserves only to be in the museums, where small children can see it in the future and be shocked how we allowed such an inhuman condition to exist for so many people for so long”

Yunus (2006).  
2006 Nobel Peace Winner

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