

Urea-based moulding compounds for investment casting

By

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ABSTRACT

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Conventional urea-based moulding compounds for investment casting patterns are manufactured using a slow "cooking" process. Nowadays in industrial processes the use of a faster process is highly recommended to increase throughput levels. At the same time, for quality control purposes, the requirements of an investment caster must be met. This study is therefore focused on:

- Finding the appropriate conventional process and conditions to prepare urea-based investment casting moulding compounds.
- Optimising the composition variables to meet the mechanical, thermal, surface, flow and cost properties needed in investment casting.
- Characterising the moulding compounds to meet the requirements of an investment caster by comparing them with an industrial, "cooked" urea-based compound.

Polyvinyl alcohol (PVOH) and ethylene vinyl acetate (EVA) urea-based moulding compounds were prepared using a two-roll mill and a conventional extrusion processes respectively. It was possible to injection mould PVOH urea-based moulding compounds with a urea content of up to 90 wt % which had been compounded using a two-roll mill. Using the conventional extrusion

ii



process, it was also possible to compound and injection mould EVA urea-based moulding compounds containing up to 70 wt % urea.

The effects on composition variables on the properties of the moulding compound were studied and compared to those of the existing "cooked" urea-based moulding compound (Benchmark). The mechanical properties were characterised using the three-point bending test and Charpy impact test. The thermal properties were determined using simultaneous differential thermal analysis and thermogravimetric analysis (SDTA/TGA) and differential scanning calorimeter (DSC). The thermo-mechanical and visco-elastic properties were determined using a dynamic mechanical analyser. A scanning electron microscope was used to study the surface texture of the mouldings.

The EVA urea-based moulding compounds showed two endothermic melting peaks and multiple exothermic crystallisation peaks in the DSC curves. The peak at ca. 55 - 66°C corresponds to the melting of the wax/EVA blend, while the large peak at 130 - 132°C corresponds to the melting of the urea. The DSC heating curve of the PVOH urea-based moulding compounds showed two endothermic peaks. The small peak corresponds to the melting of the wax, while the large peak corresponds to the melting of the urea/PVOH blend.

PVOH urea-based moulding compound had better mechanical properties than the industrial benchmark. The mechanical properties of the EVA urea-based compound were generally lower. The effect of the wax and polymer content on the mechanical properties was as follows:

- Increasing polymer content produced weaker but tougher moulding compounds.
- Increasing wax content improved the strength and stiffness but gave compounds that were less tough.
- Two-way Analysis of Variance (ANOVA) indicated significant polymer-wax interactions.

The urea content determined the stiffness (elastic modulus) of the compounds. PVOH mouldings had superior stiffness compared with the EVA and cooked urea-based mouldings. The Dynamic mechanical analysis (DMA) results confirmed the result obtained from the modulus of elasticity determination in the three-point bending test.



The impact strength increased with an increase in polymer content and reduced with an increase in wax content.

The linear thermal expansion coefficient decreased as the urea content was increased. Measured values (100 to 156×10^{-6} °C) were comparable to those of the benchmark.

The cooked urea-based moulding compound had the lowest melt viscosity at 110°C, as indicated by its melt flow index (MFI). Fluidity increased with the polymer content.

The thermo gravimetric analysis (TGA) results confirmed that both the PVOH and EVA ureabased moulding compounds decomposed readily and left less than 1 wt % ash after combustion.

From the SEM results apparent surface roughness appeared to increase with wax content. The EVA urea-based moulding compound had an irregular surface texture.

Based on the criteria of cost-effectiveness and environmental friendliness, the synthesis of PVOH urea-based patterns is preferable. The use of a conventional extrusion process to prepare PVOH urea-based patterns is recommended.

Keywords:

Urea, wax, ethylene vinyl acetate, polyvinyl alcohol, non-biodegradable pattern, biodegradable pattern, investment casting

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٧



TABLE OF CONTENTS

ABSTR	RACT		11
ACKNO	OWLED	OGMENTS	v
LIST C	F FIG	URES	x
LIST C	F TAB	LES	XV
LIST C)F ABB	REVIATIONS	XVII
		1BOLS	
CHAPI			
		INVESTMENT CASTING	
2.1		DRY OF INVESTMENT CASTING	
2.2		STMENT CASTING PROCESS	
CHAPT	ΓER 3	MOULDING COMPOUNDS FOR INVESTMENT CASTING	6
3.1	Wax	BASED MOULDING COMPOUNDS FOR INVESTMENT CASTING	6
3.3		R MOULDING COMPOUNDS FOR INVESTMENT CASTING	
3.3	PRINC	CIPLES OF COMPOUND FORMULATION	8
3.4	FILLE	RS	9
3.4			
3.4	4.1 Ap	pplications of urea	11
3.4	4.2 Ph	ysical and thermal properties of urea	12
3.5		MERS	
3.5		hylene vinyl acetate	
		lyvinyl alcohol	
3.6		, , , FICISERS	
3.0		vcerol	
	-	echanism of plasticisation	
		ctors influencing plasticisation	
3.7		ICANTS	
3.8		D POLYMERS	23

3.8.1 Filler-polymer interaction	2	27
3.8.2 Factors affecting polymer-fille	r interaction2	28
CHAPTER 4 COMPOUNDING TECHI	NIQUES 3	0
4.1 BATCH MIXERS	3	33
	3	
CHAPTER 5 CHARACTERISATION 1	ECHNIQUES 3	8
5.1 MECHANICAL PROPERTIES	3	38
5.1.1 Three-point bending test		38
5.1.2 Impact testing		39
5.2 DYNAMIC MECHANICAL ANALYSIS PRO	PERTIES4	11
5.3 THERMOMECHANICAL ANALYSIS PROP	ERTIES4	1 5
5.3.1 Thermodilatometry		<i>45</i>
5.3.2 Volumetric expansion		<i>45</i>
5.4 PHYSICAL PROPERTIES OF WAXES	4	15
5.4.1 Melting/softening point		<i>45</i>
5.4.2 Dimensional analysis		46
5.4.3 Density		46
5.5 THERMAL PROPERTIES	4	1 7
5.5.1 Differential scanning calorime	ter (DSC)	<i>47</i>
5.5.2 Thermogravimetric analysis		50
5.6 RHEOMETRY AND MELT FLOW INDEX.	5	50
5.7 IMPLICATIONS FOR THE DEVELOPMEN	T OF A UREA MOULDING COMPOUND5	56
CHAPTER 6 MATERIALS AND SAME	PLE PREPARATION 5	;9
6.1 MATERIALS	5	59
6.2 PVOH UREA-BASED MOULDING COMP	OUNDS6	50
6.2.1 Experimental design	6	50
6.2.2 Sample preparation	6	52
6.3 EVA UREA-BASED MOULDING COMPO	JNDS6	53
6.3.1 Experimental design	6	53
6.3.2 Sample preparation	6	54
6.3.3 Determination of the urea-ace	tamide phase diagram	55

CHAPT	TER 7 CHARACTERISATION OF THE COMPOUNDS	66
7.1	MECHANICAL PROPERTIES	66
7	1.1 Three-point bending test	66
7	1.2 Impact strength	66
7.2	DYNAMIC MECHANICAL ANALYSIS	67
7.3	THERMOMECHANICAL ANALYSIS	67
7.4	THERMAL PROPERTIES	67
7.4	4.1 Differential thermal analysis and thermogravimetric analysis	67
7.4	4.2 Differential scanning calorimetry	67
7.5	MELT FLOW INDEX	68
7.6	SCANNING ELECTRON MICROSCOPY	68
7.7	Density	68
CHAP	TER 8 RESULTS AND DISCUSSION	69
8.1	PROCESS RESULTS	69
8	1.1 Oven	69
8	1.2 Single-screw extruder	69
8	1.3 Two-roll mill	70
8	1.5 Injection-moulding	70
8.2	THERMAL PROPERTIES	70
8.2	2.1 Differential scanning calorimetry	70
8.2	2.2 Vicat softening temperature	82
8.3	MECHANICAL PROPERTIES	83
8	3.1 Charpy impact test	83
8	3.2 Three-point bending test	92
8.4	DYNAMIC MECHANICAL ANALYSIS	122
8.5	THERMAL EXPANSION PROPERTIES	128
8.6	MELT FLOW INDEX	130
8.7	SCANNING ELECTRON MICROSCOPY	133
8.8	Density	135
СНАРТ	TER 9 CONCLUSIONS AND RECOMMENDATIONS	137
REFER	RENCES	142

APPENDICES		149
APPENDIX A:	PHYSICAL AND CHEMICAL PROPERTIES OF MATERIAL USED	149
APPENDIX B:	SPECIFICATIONS OF PROCESSING AND CHARACTERISATION EQUIPMENT	152
APPENDIX C:	PROCESSING CONDITIONS FOR COMPOUNDING AND INJECTION MOULDING	154
APPENDIX D:	EXPERIMENTAL PROCEDURE FOR PRODUCING COOKED UREA-BASED MOULDING COMPOU	NDS.
		156
APPENDIX E:	PROPERTY VALUES OF COOKED UREA MOULDING COMPOUND (BENCHMARK)	157
APPENDIX F:	MECHANICAL PROPERTY DATA ON UREA MOULDING COMPOUNDS	159
APPENDIX G:	MATLAB SCRIPT FOR PERFORMING TWO-WAY ANOVA	164
APPENDIX H:	EXPERIMENTAL PROCEDURE FOR MEASURING DENSITY USING ARCHIMEDES' PRINCIPLE	170



LIST OF FIGURES

Figure 1:	Investment casting process (Biam, 2004)	5
Figure 2:	Molar volume of urea as a function of temperature (adapted from	13
Figure 3:	Phase diagram for the urea (1) – acetamide (2) system	14
Figure 4:	Polymer volume versus temperature (Sperling, 1992)	16
Figure 5:	Cloud and freezing point for 10% EVA, with different VA	18
Figure 6:	Effect of glycerol on the DSC melting peak temperature of partially	
	hydrolysed PVOH (Jang et al., 2003)	24
Figure 7:	Schematic illustration of the effect of plasticiser addition on the Young's	
	modulus of a polymer	24
Figure 8:	Contact angle when a liquid drops onto a solid surface (Zisman, 1963)	28
Figure 9:	Two types of mixing mechanism: (a) distributive mixing, and	30
Figure 10:	Mixing mechanism: molecular interdiffusion	31
Figure 11:	Schematic representation of the phase dimension of an immiscible fluid	32
Figure 12:	Typical types of twin-screw extruder (Shenoy, 1999)	35
Figure 13:	Three-point bending test set-up (ASTM D790, 1983)	38
Figure 14:	Charpy and impact test set up (Robert, 1985)	40
Figure 15:	Perfectly elastic solid with no phase lag (Menard, 2003)	42
Figure 16:	Purely viscous modulus at a phase angle of exactly 90° (Menard, 2003)	42
Figure 17:	Viscoelastic materials (Menard, 2003)	43
Figure 18:	Heat flow against temperature showing glass transition	48
Figure 19:	Heat flow against temperature showing crystallisation temperature	48
Figure 20:	Heat flow against temperature showing melting temperature	49
Figure 21:	Shear stress vs. rate of shear strain of fluids	50
Figure 22:	The three types of rheometer geometries: (a) concentric cylinder,	53
Figure 23:	Cross-section of a cone-and-plate rheometer	53
Figure 24:	Melt flow indexer	55
Figure 25:	The ternary phase diagram showing compositions explored	61
Figure 26:	Outline of the preparation procedure used to produce the PVOH	63
Figure 27:	Outline of the preparation procedure used to produce the EVA urea	65
Figure 28:	DSC heating curve of pure samples	71
Figure 29:	DSC cooling curve of pure samples	72



Figure 30:	Effect of increasing the polymer content on the DSC heating curves of the	ne
	PVOH moulding compounds at plasticisation concentrations of (a) 80 ph	r
	and 40 phr	73
Figure 31:	Effect of increasing the wax content on the DSC heating curves of the P	VOH
	moulding compounds at plasticisation concentrations of (a) 80 phr and	
	(b) 40 phr	74
Figure 32:	Effect of increasing the polymer content on the DSC cooling curves of th	ie
	PVOH moulding compounds at plasticisation concentrations of (a) 80 ph	r
	and (b) 40 phr	76
Figure 33:	Effect of increasing the wax content on the DSC cooling curves of PVOH	
	moulding compounds at plasticisation concentrations of (a) 80 phr and ((b)
	40 phr	77
Figure 34:	Effect of increasing the polymer content on the DSC heating curves of the	ne
	EVA moulding compounds	79
Figure 35:	Effect of increasing the wax content on the DSC heating curves of the E	VA
	moulding compounds	79
Figure 36:	Effect of increasing the polymer content on the DSC cooling curves of th	ie
	EVA moulding compounds	80
Figure 37:	Effect of increasing the wax content on the DSC cooling curves of the EV	/A
	moulding compounds	80
Figure 38:	Softening temperature of the PVOH (80 phr glycerol) moulding compour	nds
		83
Figure 39:	Comparison between predicted and experimental Charpy impact strength	h for
	quadratic model fit of the urea-wax-PVOH (80 phr glycerol) compounds	88
Figure 40:	Comparison between predicted and experimental Charpy impact strength	h for
	quadratic model fit of the urea-wax-PVOH (40 phr glycerol) compounds	88
Figure 41:	Comparison between predicted and experimental Charpy impact strengt	h for
	linear model fit of the urea-EVA-wax compounds	89
Figure 42:	Charpy impact strength of the urea-wax-PVOH (80 phr glycerol) compou	ınds
		90
Figure 43:	Charpy impact strength of the urea-wax-PVOH (40 phr glycerol) compou	ınds
		91



Figure 44:	Charpy impact strength of the urea-EVA-wax compounds	91
Figure 45:	Load deflection curve showing the effect of increasing the PVOH content	nt on
	the mechanical properties of the urea-PVOH-based compounds	93
Figure 46:	Load deflection curve showing the effect of increasing the wax content	on
	the mechanical properties of the urea-PVOH-based compounds	94
Figure 47:	Effect of varying EVA content on the load deflection curve of the EVA	
	moulding compounds	94
Figure 48:	Effect of varying wax content on the load deflection curve of the EVA	95
Figure 49:	Comparison between predicted and experimental flexural stress data for	r
	linear model fit of the urea-wax-PVOH (80 phr glycerol) compound	99
Figure 50:	Comparison between predicted and experimental flexural stress for a li	near
	model fit of UP4 data	99
Figure 51:	Comparison between predicted and experimental flexural stress for line	ar
	model fit of urea EVA-wax data	100
Figure 52:	Flexural stress of the urea-wax-PVOH (80 phr glycerol) compound	101
Figure 53:	Flexural stress of the urea-wax-PVOH (40 phr glycerol) compound	102
Figure 54:	Flexural stress of the urea-EVA-wax compound	102
Figure 55:	Comparison between predicted and experimental flexural strain for line	ar
	model fit of the urea-wax-PVOH (80 phr glycerol) compound data	105
Figure 56:	Comparison between predicted and experimental flexural strain for line	ar
	model fit of the urea-wax-PVOH (40 phr glycerol) compound data	105
Figure 57:	Comparison between predicted and experimental flexural strain for line	ar
	model fit of the urea-EVA-wax compound data	106
Figure 58:	Flexural strain of the urea-wax-PVOH (80 phr glycerol) compound	107
Figure 59:	Flexural strain of the urea-wax-PVOH (40 phr glycerol) compound	108
Figure 60:	Flexural strain of the urea-EVA-wax compound	108
Figure 61:	Comparison between predicted and experimental fracture energy for	
	quadratic model fit of the urea-wax-PVOH (80 phr glycerol) compound	data
		111
Figure 62:	Comparison between predicted and experimental fracture energy for	
	quadratic model fit of UP4 data	112

Figure 63:	Comparison between predicted and experimental fracture energy for lin	ear	
	model fit of urea-EVA-wax compound data	113	
Figure 64:	Fracture energy of the urea-wax-PVOH (80 phr glycerol) compounds	114	
Figure 65:	Fracture energy of the urea-wax-PVOH (40 phr glycerol) compounds	114	
Figure 66:	Fracture energy of the urea-EVA-wax compounds	115	
Figure 67:	Comparison between the predicted and experimental modulus of elastic	city	
	for quadratic model fit of urea-wax-PVOH (80 phr glycerol) compounds	118	
Figure 68:	Comparison between predicted and experimental modulus of elasticity f	or	
	quadratic model fit of urea-wax-PVOH (40 phr glycerol) compounds	118	
Figure 69:	Comparison between predicted and experimental modulus of elasticity for		
	quadratic model fit of urea EVA-wax compounds	119	
Figure 70:	Modulus of elasticity of the urea-wax-PVOH (80 phr glycerol) compound	ds120	
Figure 71:	Modulus of elasticity of the urea-wax-PVOH (40 phr glycerol) compound	ds121	
Figure 72:	Modulus of elasticity of the urea-EVA-wax compounds	121	
Figure 73:	Effect of increasing the polymer content on the storage modulus versus	the	
	temperature of the urea-PVOH moulding compounds	123	
Figure 74:	Effect of increasing the wax content on the storage modulus versus the	;	
	temperature of the urea-PVOH moulding compounds	123	
Figure 75:	Effect of increasing the polymer content on the damping factor versus t	:he	
	temperature of the urea-PVOH moulding compounds	124	
Figure 76:	Effect of increasing the wax content on the damping factor versus the		
	temperature of the urea-PVOH moulding compounds	124	
Figure 77:	Effect of increasing the polymer content on the storage modulus versus	the	
	temperature of the urea-EVA moulding compounds	125	
Figure 78:	Effect of increasing the wax content on the storage modulus versus the	е	
	temperature of the urea-EVA moulding compounds	125	
Figure 79:	Effect of increasing the polymer content on the damping factor versus t	:he	
	temperature of the urea-EVA moulding compounds	126	
Figure 80:	Effect of increasing the wax content on the damping factor versus the		
	temperature of the urea-EVA moulding compounds	126	
Figure 81:	Thermal expansion coefficients measured at various temperatures for the	ne	
	PVOH (80 phr glycerol) compounds	128	



Figure 82:	Thermal expansion coefficients measured in the temperature range 30 -	40
	°C for the PVOH (40 phr glycerol) compounds	129
Figure 83:	Thermal expansion coefficients measured in the temperature range $30\ $	40
	°C for the EVA moulding compounds	129
Figure 84:	MFI of the urea-wax-PVOH (80 phr glycerol) compounds	131
Figure 85:	MFI of the urea-wax-PVOH (40 phr glycerol) compounds	131
Figure 86:	MFI of the urea-EVA-wax moulding compounds	132
Figure 87:	\ensuremath{SEM} photographs of the surfaces of specimens of the PVOH urea-based	
	moulding compounds: (a) UP8 90:5:5, (b) UP8 85:5:10, (c) UP8 80:5:15	;
	and (d) cooked urea (benchmark)	133
Figure 88:	SEM photographs of the surfaces of specimens of the EVA-urea-based	
	moulding compounds: (a) UE 70:20:10 and (b) UE 80:10:10	134



LIST OF TABLES

Table 1:	Formulation of an investment casting compounding containing polyethylene	
	terephthalate (PET) as filler (Guinn, 2002)	8
Table 2:	Useful properties of fillers in polymers (Gächter & Müller, 1984)	10
Table 3:	Crucial properties of urea (Anon, 1993)	11
Table 4:	Physical properties of polyvinyl alcohol (Finch, 1992)	19
Table 5:	Industrial beneficial properties of glycerol (George, 2004)	20
Table 6:	Chemical, economic and physical properties of hydrocarbon wax	26
Table 7:	Applications and functions of waxes (Horton, 1988)	27
Table 8:	Calculation of material properties by DMA (Menard, 2003)	44
Table 9:	Virgin polymers and their suppliers	59
Table 10:	The compositions explored to make the PVOH urea-based compounds	61
Table 11:	Compositions explored for the synthesis of EVA urea-based compounds	64
Table 12:	Parameters obtained from DSC measurements for investment casting patterns on	the
	large-peak and pure samples	78
Table 13:	Properties obtained from differential thermal analysis of urea peak and EVA/wax	
	blends	81
Table 14:	Two-way ANOVA for Charpy impact strength for the urea-PVOH-wax compound	
	containing 80 phr glycerol	86
Table 15:	Two-way ANOVA for Charpy impact strength for the urea-PVOH-wax compound	
	containing 40 phr glycerol	86
Table 16:	Two-way ANOVA for Charpy impact strength for the urea-EVA-wax compounds	87
Table 17:	Maximum Load and deflection point of PVOH moulding compounds	96
Table 18:	Maximum Load and deflection point of EVA moulding compounds	96
Table 19:	Two-way ANOVA for flexural stress data for the urea-wax-PVOH compound	
	containing 80 phr glycerol	98
Table 20:	Two-way ANOVA for flexural stress data for the urea-wax-PVOH compound	
	containing 40 phr glycerol	98
Table 21:	Two-way ANOVA for flexural stress data for the urea-EVA-wax compounds	98
Table 22:	Two-way ANOVA for flexural strain of the urea-PVOH-wax compound containing 8	30
	phr glycerol	104



Table 23:	Two-way ANOVA for flexural strain of the urea-PVOH-wax compound containing 40	
	phr glycerol	104
Table 24:	Two-way ANOVA for flexural strain of the urea-EVA-wax compounds	104
Table 25:	: Two-way ANOVA for fracture energy of the urea-PVOH-wax compounds containing	
	80 phr glycerol	110
Table 26:	Two-way ANOVA for fracture energy of the urea-PVOH-wax compounds containing	ng
	40 phr glycerol	110
Table 27:	Two-way ANOVA for Fracture energy urea-EVA-wax compounds	111
Table 28:	Two-way ANOVA for the modulus of elasticity of the urea-PVOH-wax compounds	;
	containing 80 phr glycerol	117
Table 29:	Two-way ANOVA for the modulus of elasticity of the urea-PVOH-wax compounds	3
	containing 40 phr glycerol	117
Table 30:	Two-way ANOVA for the modulus of elasticity of the urea-EVA-wax compounds	117
Table 31:	Theoretical and measured densities of the EVA-urea-based compounds	135
Table 32:	Theoretical and measured densities of the PVOH urea-based compounds	135
Table 33:	Density of the raw materials	135
Table 34:	Properties of the cooked urea moulding compound (benchmark) compared with	
	those of the best PVOH and EVA moulding compounds	140

LIST OF ABBREVIATIONS

ANOVA = Analysis of variance

DMA = dynamic mechanical analysis

DMF = dimethyl formamide

DSC = differential scanning calorimeter

EVA = ethylene vinyl acetate

MFI = melt flow index

PEG = polyethylene glycol

PET = polyethylene terephthalate

PVC = polyvinyl chloride

PVOH = polyvinyl alcohol

phr = parts per hundred of resin

SEM = scanning electron microscope

SDTA = Scanning differential thermal analysis

TGA = thermogravimetric analysis

TMA = thermomechanical analysis

UE = EVA urea-based moulding compound

UF = resin

UP8 = PVOH urea-based moulding compound of plasticisation degree 80

UP4 = PVOH urea-based moulding compound of plasticisation degree 40

VA = vinyl acetate

X: Y: Z = proportion of urea: polymer: wax



LIST OF SYMBOLS

A = weight of the sample in air (g)
B = weight of the sample immersed in water (g)

B = width of beam tested (mm)

c = volumetric fraction of polymer

D = maximum deflection of the centre of the beam

D = depth of beam tested (mm)

E = modulus

 E_B = Young's modulus of bending

 ϵ = strain at time t

 ϵ_0 = strain at a maximum strain

 F_Z = force in the Z direction

H = height

L = liquid phase

 L_S = support span

 L_1 = length at T_1

 L_2 = length at T_2

M = measured torque

 M_D = maximum deflection

 M_1 = maximum load

n = number of components in the blend

 ρ_s = density of the sample (g/cm³)

 ρ_L = density of liquid (g/cm³)

 $\rho_{\rm C}$ = density of the moulding compound

 ρ_i = density of the component

 w_i = weight fraction of component

r = radii of the particles

R = cone radius

S = solid phase

T = time

 ΔT = change in temperature



m = steepest load deflection curve slope

 T_{om} = onset melting temperature

 T_c = crystallisation temperature

T_{oc} = onset crystallisation temperature

 T_g = glass transition temperature

 T_{g1} = glass transition temperature of the polymer

 T_{q2} = glass transition temperature of the plasticizer

U = velocity

V = vapour phase

 V_1 = free volume

 V_o = occupied volume

 W_D = work done

 w_1 = weight fraction of the polymer

 w_2 = weight fraction of the plasticizer

 ω = frequency of oscillation

 W_i = weight fraction of component

 γ = surface tension

 α = coefficient of linear thermal expansion

 Ω = rotational velocity

 Φ = angular displacement; $\beta = \theta - x/2$ (typically 2°-8°)

 θ = cone angle

 σ = stress at time t

 σ_0 = maximum stress

 η = viscosity

 η_{e} = elongation flow

 η_s = shear flow

 $\dot{\gamma}$ = shear rate