

Radiometric calibration framework for ultra-high-resolution UAV-derived orthomosaics for large-scale mapping of invasive alien plants in semi-arid woodlands: *Harrisia pomanensis* as a case study

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Abstract

Orthomosaics derived from consumer grade digital cameras on board unmanned aerial vehicles (UAVs) are increasingly being used for biodiversity monitoring and remote sensing of the environment. To have lasting quantitative value, remotely sensed imagery should be calibrated to physical units of reflectance. Radiometric calibration improves the quality of raw imagery for consistent quantitative analysis and comparison across different calibrated imagery. Moreover, calibrating remotely sensed imagery to units of reflectance improves its usefulness for deriving quantitative biochemical and biophysical metrics. Notwithstanding the existing radiometric calibration procedures for correcting single images, studies on radiometric calibration of UAV-derived orthomosaics remain scarce. In particular, this study presents a cost- and time-efficient radiometric calibration framework for designing calibration targets, checking scene illumination uniformity, converting orthomosaic digital numbers to units of reflectance, and accuracy assessment using in situ mean reflectance measurements (i.e. the average reflectance in a particular waveband). The empirical line method was adopted for the development of radiometric calibration prediction equations using mean reflectance values measured in only one spot within a 97 ha orthomosaic for three wavebands, i.e. red, green and blue of the Sony NEX-7 camera. A scene illumination uniformity check experiment was conducted to establish whether 10 randomly distributed regions within the orthomosaic experienced similar atmospheric and illumination conditions. This methodological framework was tested in a relatively flat terrain semi-arid woodland that is invaded by *Harrisia pomanensis* (the Midnight Lady). The scene illumination uniformity check results showed that at a 95% confidence interval, the prediction equations developed using mean reflectance values measured from only one spot within the scene can be used to calibrate the entire 97 ha RGB orthomosaic. Furthermore, the radiometric calibration accuracy assessment results showed a correlation coefficient r value of 0.977 ($p < 0.01$) between measured and estimated reflectance values with an overall root

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mean square error of 0.063. These findings suggest that given the entire scene being mapped is experiencing similar atmospheric and illumination conditions, then prediction equations developed using mean reflectance values measured in only one spot within the scene can be used to calibrate the entire orthomosaic in semi-arid woodlands. The proposed methodological framework can potentially be tested and adapted for use in large-scale crop mapping and monitoring in precision agriculture, land-use/land-cover classification as well as plant species delimitation, particularly for mapping widespread invasive alien plants such as *H. pomanensis*.

1. Introduction

Orthomosaics derived from consumer grade digital cameras on board unmanned aerial vehicles (UAVs) are increasingly being used for vegetation mapping (Laliberte et al. 2011; Pádua et al. 2017; Bonnet, Lisein, and Lejeune 2017). Recently, the UAV remote-sensing (UAV-RS) approach has been frequently reported as advantageous over spaceborne and traditional airborne remote-sensing approaches due to the resultant high temporal and spatial resolution data as well as the survey cost efficiency associated with this approach (Femondimo et al. 2011; Müllerová et al. 2017; Babapour et al., 2017). Applications of the UAV-RS approach include *inter alia* agriculture (Li et al. 2017), precision agriculture (Primicerio et al. 2012; Gómez-Candón, De Castro, and Lopez-Granados 2014; Rokhmana 2015; Bagheri 2017), land use (Akar 2017), forestry (Thiel and Schmulilius 2017; Torrescan et al. 2017), archaeology (Rinaudo et al. 2012; Fernández-Hernandez González-Aguiler, Rodriguez-Gonzalvez, and Mancera-Taboada 2015), classification of native vegetation (Zhang 2014), and mapping of invasive alien plants (IAPs) (Dvořák et al. 2015; Müllerová et al. 2016; Hill et al. 2017).

UAV-RS imagery are highly influenced by prevailing environmental conditions at the time of data acquisition (Kelcey and Lucieer 2012; Yang et al. 2017). These environmental conditions include the atmospheric composition (e.g. water vapour and aerosols) as well as solar illumination patterns that depend on variations in the earth–sun geometry for different seasons and times of the day (Nguyen et al. 2015; Honkavaara et al. 2017). As a result, images of a target scene acquired by the same sensor on different seasons or times of the day may have different properties (Haghighattalab et al. 2016). On the other hand, images acquired by the same sensor may contain noise due to lens distortions, sensor systematic errors, as well as the variation of the camera sensitivity across the same image (Wang et al. 2006; Hugemann 2010; Del Pozo et al. 2014).

To have lasting quantitative value, it is standard practice to have remotely sensed data calibrated to physical units of reflectance (Smith and Milton 1999). The radiometric calibration process converts image digital numbers (DNs) to at-surface reflectance units so as to enable quantitative analysis across data acquired at different seasons or times of the day as well as by different sensors. Calibrated data sets may be cross compared because while image DNs of a target object change depending on environmental factors such as the incoming irradiance and atmospheric conditions (Honkavaara et al. 2013),

after radiometric calibration, the spectral characterization of an object becomes possible (Kelcey and Lucieer 2012; Crusiol et al. 2017). Moreover, radiometric calibration improves the accuracy of derived vegetation indices as well as biochemical and biophysical parameters (Nguyen et al. 2015). Nevertheless, studies that applied the UAV-RS for IAPs monitoring made use of thematic image classification without either conducting geometric or radiometric calibration (Dvořák et al. 2015; Müllerová et al. 2016; Mafanya et al. 2017). This is because UAV-RS of biological invasions is optimized to be time and cost efficient so as to enable mapping of IAPs at the right phenological stage, at an affordable cost and with a quick turnover (Müllerová et al. 2017; Hill et al. 2017; Tesfamichael et al. 2017). However, monitoring of IAPs could encompass not only qualitative thematic mapping but also quantitative image analysis such as image band mathematics (e.g. vegetation indices) as applied *inter alia* in agriculture (Li et al. 2017), precision agriculture (Honkavaara et al. 2013; Candiago et al. 2015; Sonaa et al. 2016), and forestry (Thiel and Schmullius 2017; Torrescan et al. 2017). Since one of the aims in UAV-RS is cost reduction, a radiometric calibration framework for UAV-based IAPs monitoring ought to be cost and time efficient.

UAV-RS radiometric calibration poses different challenges to spaceborne and manned aircraft remote sensing. The low flight altitudes of mostly less than 200 m due to some governmental restrictions mean that for the same area of interest there will be more UAV-RS images acquired due to the associated small footprint than there would have been if the data was acquired from a satellite platform or from a piloted aircraft (Grenzdörffer, Engel, and Teichert 2008; Cracknell 2017). This means that it is not feasible to have at-surface *in situ* reflectance calibration measurements for all acquired UAV-derived images as it would be impractical to place enough calibration targets on the ground for this goal. As a result, most radiometric calibration procedures were developed for a single image that is usually an aerial view of the calibration site. For instance, Taylor (2015) successfully demonstrated the process of radiometric calibration of a modified digital single-lens reflex camera using a single image while Kelcey and Lucieer (2012) used a single image to demonstrate the radiometric calibration workflow for a six-band UAV-borne multispectral sensor. Moreover, Wang and Myint (2015) used a single-sample image to demonstrate a simplified empirical line method (ELM) for radiometric calibration of a UAV-derived colour infrared image. Usually, the radiometric calibrated images are then mosaicked to produce a multi-band orthomosaic as done in Clemens (2012). However, based on the successful demonstrations of aforementioned studies, single-image radiometric calibration may become impractical for large-scale UAV-RS vegetation mapping. This is because it is not feasible to have calibration targets and at-surface reflectance measurements for every image captured even for small study areas (Hakala, Suomalainen, and Peltoniemi 2010).

IAPs tend to spread across very large areas (> 90 ha), and this necessitates a radiometric calibration framework for large-scale mapping. For instance, the cactus plant *Harrisia pomanensis* (commonly known as the Midnight Lady) has been detected invading an area of not less than 10,000 ha in Limpopo, South Africa (Mafanya et al. 2017). Following the efforts made in image-by-image radiometric calibration studies (Taylor 2015; Kelcey and Lucieer 2012; Wang and Myint 2015; Crusiol et al. 2017), this study presents a cost- and time-efficient radiometric calibration framework for converting DNPs of UAV-derived orthomosaics to physical units of reflectance for large-scale mapping of

H. pomanensis in flat semi-arid woodlands. Included in the framework are procedures for calibration target design, scene illumination uniformity assessment, prediction equations derivation, and radiometric calibration accuracy assessment using *in situ* at-surface mean reflectance measurements (i.e. the average reflectance in a particular waveband) measured in only one spot within the scene.

2. Vicarious radiometric calibration framework

2.1. Calibration target design

For radiometric calibration, targets that are homogenous and resemble Lambertian properties are highly desirable (Del Pozo et al. 2014). While large homogenous natural targets are usually used for radiometric calibration of satellite imagery, use of artificial targets that are specifically designed for a project is usually made in UAV-RS. This is because coloured artificial targets are easy to transport to the field and can be easily moved to the next study area. Moreover, for the relatively small UAV-RS orthomosaics, compared to satellite RS scenes, it is often difficult to find naturally available pseudo-invariant features. The types of materials used in UAV-RS radiometric calibration target design include plywood (Kelcey and Lucieer 2012), Masonite hardboard (Wang and Myint 2015), polyvinyl chloride (PVC) sheets and canvas (Del Pozo et al. 2014; Crusiol et al. 2017). For radiometric calibration target design, this study made use of the relatively affordable Masonite hardboards for the radiometric calibration target and a reinforced PVC sheet for the check target (Figure 1). The reinforced PVC check target with red, green, blue, black, and white control colours was also placed in the study area for accuracy assessment and error analysis.

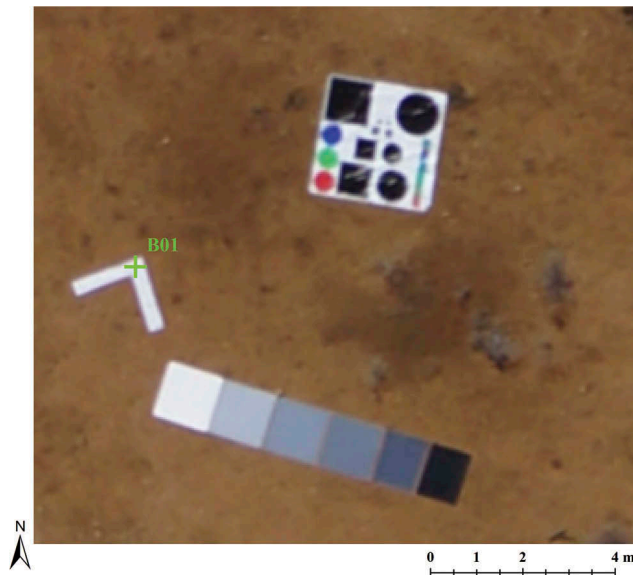


Figure 1. UAV aerial view of the control target (bottom) and check targets (top) taken by the Sony Nex-7 camera on board the UAV flown at a height of 160 m AGL. The L-shaped marker in the middle (B01) was considered to be receiving similar irradiance as the radiometric calibration and check targets due to spatial proximity.

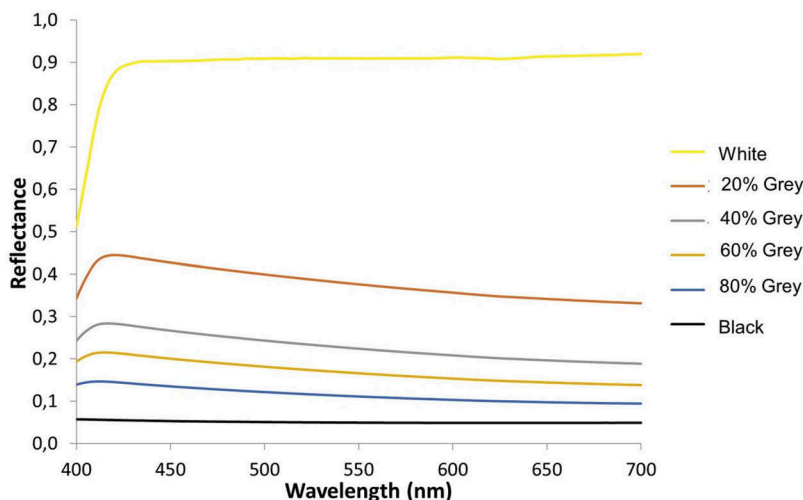


Figure 2. Mean spectral response curves of the Lambertian radiometric calibration targets. The white target (curve shown in yellow) has high reflectance while the black target has low reflectance.

With regards to the calibration target design, three standard size Masonite hard-boards of 244 cm × 122 cm were painted with 1 mm thick super white and black paints that were further mixed into four colour values of grey (totalling six calibration grey values). The calibration target was designed to form a grey gradient as follows: white, 20% grey, 40% grey, 60% grey, 80% grey and black. The mean spectral signature for each grey value is shown in Figure 2, which demonstrates the Lambertian properties of the created calibration target. The Lambertian properties of the grey gradient painted Masonite calibration target were first tested in a controlled room under an artificial light source, and this material was found to be highly Lambertian in the visible region of the electromagnetic spectrum as also demonstrated by Wang and Myint (2015).

Moreover, white PVC sheets were used to design L-shaped scene illumination uniformity check markers. The white PVC sheets were chosen to design the L-shaped markers due to ease of transportation and visibility in both raw images and the orthomosaic. The L-shaped PVC markers were placed randomly across the scene for orthorectification ground control points (GCPs) surveying and the scene illumination uniformity check experiment. The calibration targets were placed in the study area before the UAV flight and the capturing of their spectral signatures was done before, during, and after the UAV flight. This did not add significant time to the mapping process as the imagery was acquired at noon together with the spectral signatures. Also this was done so as to minimize the differences in solar illumination conditions between image data and *in situ* spectral signatures acquisition. It took almost 43 and 118 min to acquire image data and *in situ* spectral signature measurements, respectively.

2.2. Scene illumination uniformity check

Intuitively, a large-scale vicarious radiometric calibration method using radiometric calibration targets placed in only one region of the study area will require that the prevailing environmental conditions and solar illumination patterns (due to sun elevation angle) across the scene

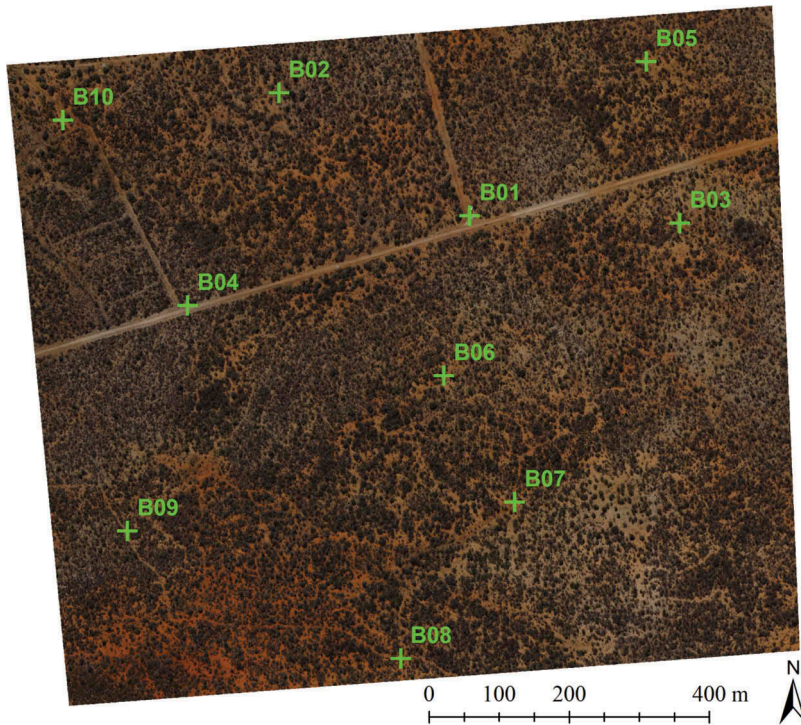


Figure 3. Mapped area showing the distribution of the 10 L-targets B01–B10. The target position is indicated by centres of the green crosses.

be uniform. To check whether the environmental conditions and solar illumination patterns are uniform across the scene, 10 L-shaped PVC markers were placed randomly, across the mapping area in this study (Figure 3). The mean DNs of the L-shaped markers, extracted from raw UAV images, were used to check whether the illumination patterns and prevailing environmental conditions across the scene were the same during image data acquisition, which took about 43 min. Due to the 60% side and 80% forward overlap photo sampling method employed in this study, each of the L-shaped markers appeared in at least five raw images. The ArcGIS 10.4 Spatial Analyst Zonal Statistics tool was used to extract the targets mean pixel DNs from a total of 58 raw images. The B01 marker was considered the reference illumination check maker because it was the closest marker to the radiometric calibration target (Figure 1). A two-sample Student's *t*-test was conducted to check whether the mean DN of the B01 marker, appearing in 6 images, was the same as the mean DNs of the rest of the 9 other markers that appeared in the remainder 52 images. This scene illumination uniformity check experiment was deemed necessary because mean reflectance values measured in only one spot within the scene should be used to calibrate the entire orthomosaic if and only if the entire orthomosaic is experiencing similar atmospheric and illumination conditions.

2.3. Empirical line method

Vicarious radiometric calibration procedures mainly focus on modelling the relationship between image DNs and *in situ* at-surface reflectance values of the calibration targets. In

particular, the ELM is used to obtain image reflectance based on the measured spectral signatures of calibration targets that are placed on the ground (Honkavaara et al. 2013). The ELM calibration prediction equations derived using mean target DNs and mean reflectance per waveband for each colour value of the calibration target were used in this study. These equations were derived using mean DNs and mean reflectance values measured from a target located at a single spot of the study area. For *in situ* spectral measurements, the Analytical Spectral Devices, Inc. FieldSpec 3 Pro calibrated spectro-radiometer was used to take 25 spectral signatures (each spectra was a mean of 10 samples) for all the six grey values of the calibration target. An average of the 25 spectra was taken for each grey value, thus totalling 250 individual measured spectral signatures for each grey value.

To obtain a single *in situ* at-surface reflectance measurement for each grey value on the calibration target, the 1 nm spectral measurements were averaged according to the spectral response curve of the Sony NEX-7 CMOS sensor. Berra et al. (2015) measured the spectral sensitivity of the Sony CMOS using a monochromatic light source and the relative colour channels of the Sony CMOS were found to be approximately 400–490 nm, 491–590 nm, and 591–690 nm for the blue, green, and red colour channels, respectively. The same method was followed to get mean spectral signatures for the coloured PVC check targets. To obtain the mean image DN for each grey value of the calibration target, use of the Zonal Statistics tool within the ArcGIS 10.4 Spatial Analyst extension was made. Considerable care was taken to create polygons that contain only pixels that belong only to that particular grey value.

In most studies, a linear relation between image DNs and the at-surface reflectance values is assumed (Karpouzli and Malthus 2003; Staben et al. 2012). When more than two calibration targets are used, the relationship between image DN and reflectance does not have to be assumed to be linear (Smith and Milton 1999). In this study, the mean DNs were regressed with the mean reflectance values and the relationship between image DN and reflectance was found to be exponential for all the three image wavebands as also observed in Wang and Myint (2015). Following the simplified ELM proposed by Wang and Myint (2015), a natural log transformation was performed on all the six mean *in situ* at-surface spectra for each image waveband. The transformation showed that a linear relationship exists between mean image DNs and the mean natural log-transformed reflectance values for each waveband. When the y-intercept of the linear equation is converted back to reflectance, the result is a minimum at-surface reflectance value for that particular image waveband. Therefore, the y-intercept of each waveband is the constant radiometric calibration parameter for that particular waveband. Furthermore, the y-intercept coordinate can be used as an initial point in a Cartesian plane. To derive an ELM prediction equation, another point in the Cartesian coordinate system can be represented by the mean DN and mean at-surface reflectance of the entire calibration target for each image waveband. These two points can then be used to calculate the gradient (m) of the calibration equation as shown in Equation (1):

$$m = \frac{B_y - A_y}{B_x} \quad (1)$$

where A_y is the constant radiometric calibration parameter, B_x is the mean DN of the calibration target, and B_y is the natural log-transformed mean reflectance of the

calibration target (Wang and Myint 2015). The developed ELM prediction equations were used to convert each waveband of the orthomosaic from DNs to reflectance values using the raster calculator in QGIS (Quantum GIS development team 2017). Subsequently, the three image wavebands were stacked together to give a colour RGB image with reflectance values instead of DNs. The radiometric calibration using the raster calculator in QGIS took about 30 min and therefore did not delay the mapping process.

2.4. Radiometric calibration accuracy assessment

The mean reflectance values of the PVC check target with black, blue, green, red, and white colours were used for accuracy assessment. During the acquisition of the *in situ* validation data, 5 spectra (a total of 50 individual spectral signatures) were measured for each check colour. The Zonal Statistics tool in ArcGIS 10.4 was used to get the mean reflectance of each coloured check target for each waveband. There were 6 available mean reflectance values for each coloured check target (i.e. 1 estimated and 1 measured mean value for each waveband thus totalling 24 values). The estimated image mean reflectance values and mean reflectance *in situ* measurements for each coloured target circle or square were then correlated so as to validate the large-scale radiometric calibration method used in this study. Error analysis through root mean square error (RMSE) computations was used to supplement the correlation analysis.

2.5. Radiometric calibration process flow diagram

This framework consists of data acquisition, derived products, and methodological phases (Figure 4). The first acquisition phase is the capture of GCPs that were observed at the randomly distributed L-shaped markers for orthorectification and the scene illumination uniformity check experiment. This is followed by the recording of spectral signatures of the calibration and the check targets. Target spectral signatures were recorded almost contemporary with the UAV flight mission (i.e. the UAV image acquisition phase). Only two final products are derived when using the proposed framework and those are (1) the raw orthomosaic in DNs and (2) the radiometric calibrated orthomosaic in physical units of reflectance. Furthermore, the image processing and statistical methods applicable to this framework are explained in the *H. pomanensis* case study.

3. *H. pomanensis* case study

3.1. Study area

The study area is located near the Alldays town within the Capricon district in the Limpopo province of South Africa (Figure 5). The area is characterized by (1) a semi-arid climate, (2) summer rainfall, and (3) average midday temperatures of 22.3°C and 31.9°C in winter (June–August) and summer (October–February) seasons, respectively (Mzezwa, Mlisi, and Van Rensburg 2010). The rainfall ranges from a few millimetre in winter and could escalate to a maximum of approximately 81 mm in summer (Mzezwa, Mlisi, and Van Rensburg 2010). The 97 ha mapped area is shown in Figure 5(b). The study area is a

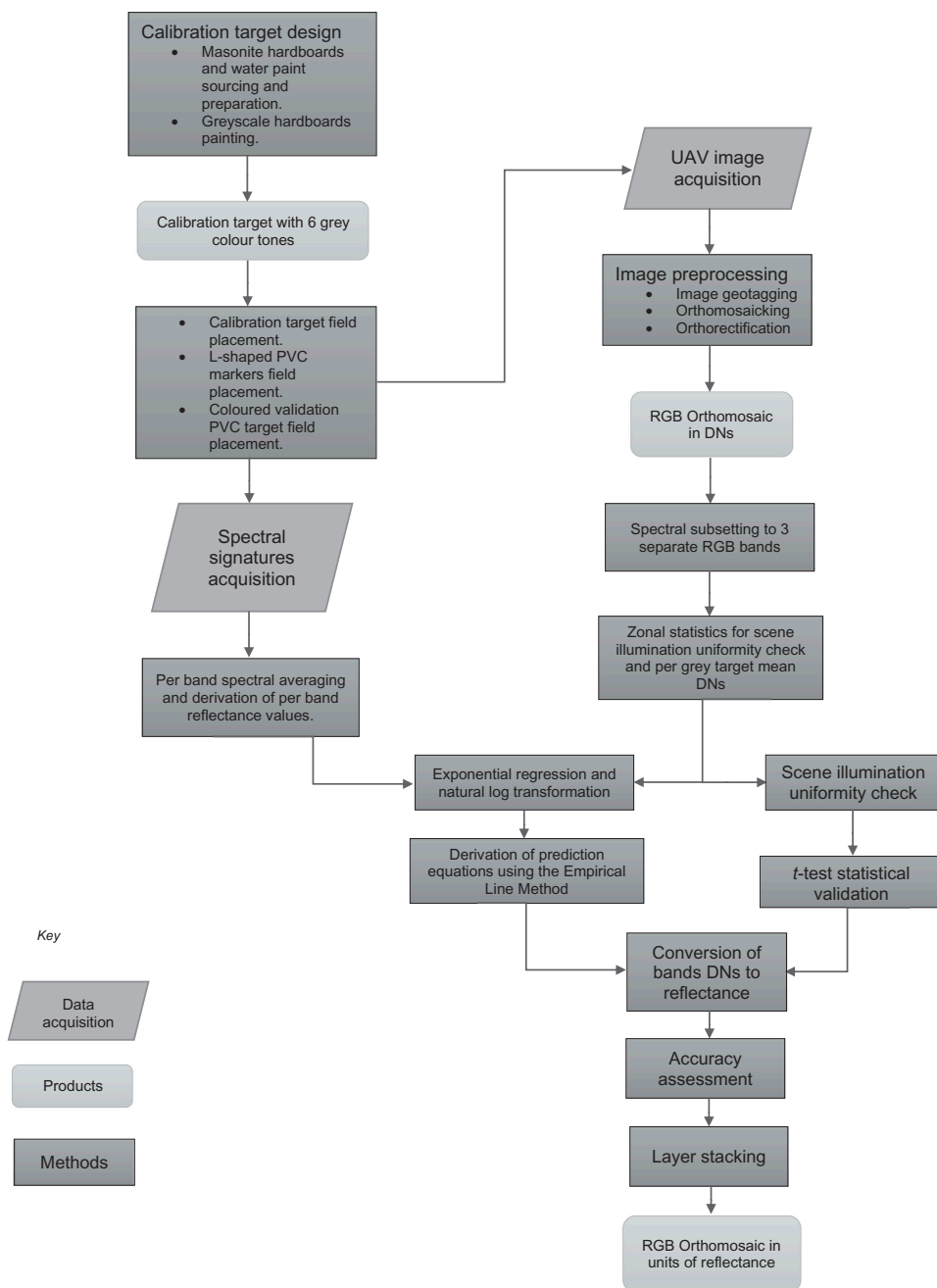


Figure 4. Proposed radiometric calibration framework for large-scale mapping of *H. pomanensis* in semi-arid woodlands using UAV-derived orthomosaics.

relatively flat terrain with orthometric height values ranging from 800 to 817 m. Tree species that occur in this heterogeneous semi-arid woodland include *Commiphora mollis* (velvet-leaved corkwood), *Commiphora neglecta* (green-temmed corkwood), *Commiphora schimperi* (glossy-leaved corkwood), *Commiphora viminea* (zebra-bared

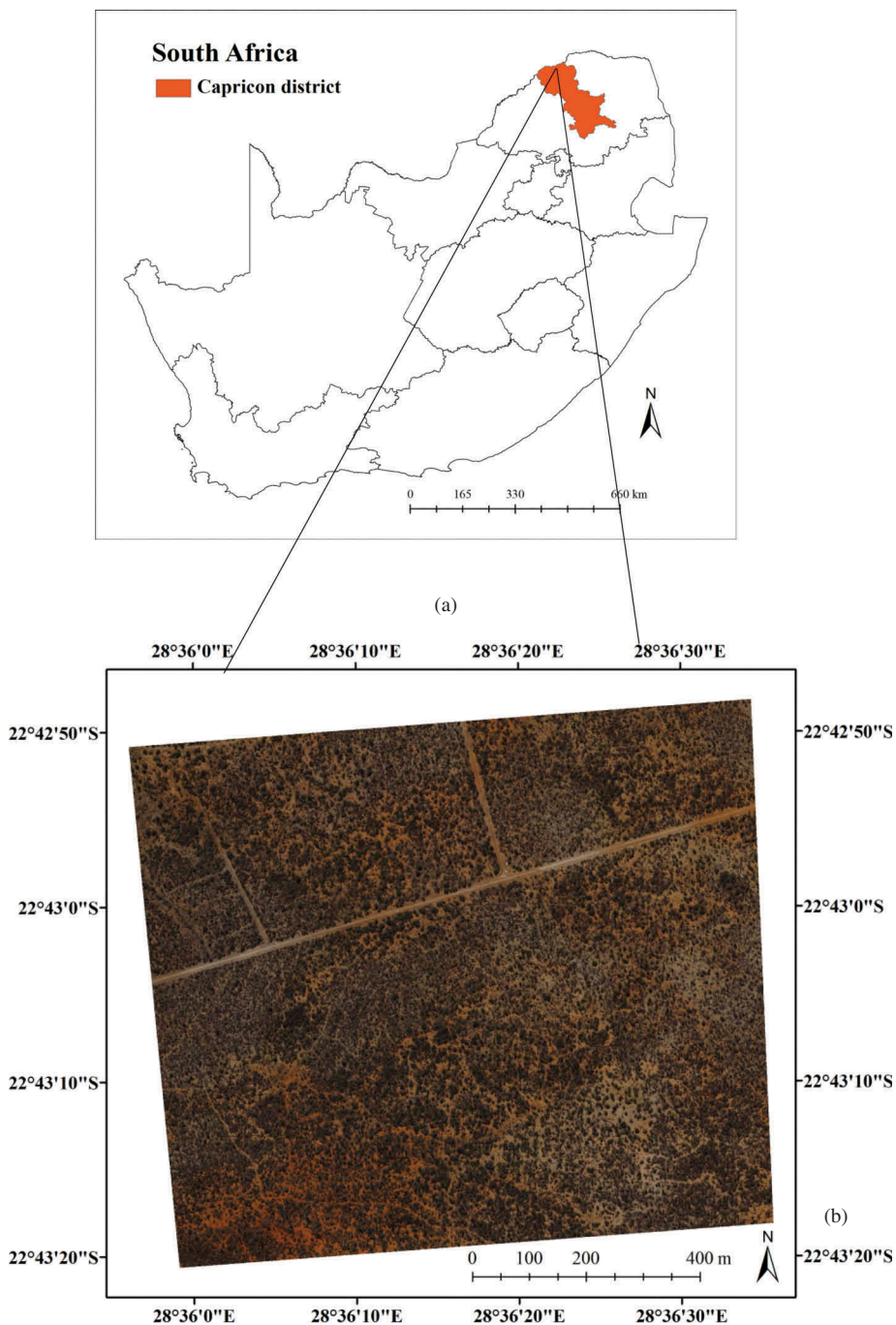


Figure 5. (a) Map of South Africa showing the location of Capricon district within the Limpopo province and (b) a subset of the UAV-derived ultra-high spatial resolution (5 cm) RGB orthomosaic.

corkwood), *Acacia nilotica* (scented pod thorn), *Acacia tortilis* (umbrella thorn), *Acacia nigrescens* (knob thorn), *Acacia robusta* (broad pod robust thorn), *Acacia mellifera* (black thorn), *Balanites maughamii* (green thorn), *Albizia* sp. (false thorn), *Kirkia acuminata*

(white seringa), *Combretum imberde* (leadwood), *Combretum hereroense* (Russet bush willow), *Boscia albitrunca* (shepherd's tree), *Berchemia zeyheri* (red ivory), *Maerua angolensis* (bead bean), *Lannea* sp. (false marula), *Sclerocarya birrea* (marula), and *Opuntia humifusa* (devil's tongue), amongst others (Mafanya et al. 2017). The *H. pomanensis* invasive plant forms dense clusters in the described woodland area and could consequently replace pasture, injure animals, and thus inhibit cropping and grazing (Wilson et al., 2013). *H. pomanensis* is a succulent cactus with jointed spiny fleshy stems and thorny spikes, and when these stems touch the ground, they develop roots and spread. The plant seeds are spread by birds and monkeys that consume the red fruits of the plant. *H. pomanensis* was detected by the South African National Biodiversity Institute: Invasive Species Programme in 2011 as part of ongoing efforts at incursion response planning (Wilson, Panetta, and Lindgren 2016).

3.2. Utilized UAV and digital camera

To acquire ultra-high-resolution images (ground sample distance < 5cm) for mapping *H. pomanensis*, utility of a customized UAV with a net weight of 1.5 kg (excluding camera and batteries) and a payload of approximately 5 kg was made (Figure 6). The fundamental components of the utilized UAV included a Global Navigation Satellite System (GNSS) receiver, an Inertial Measurement Unit (IMU) sensor, and a barometer. The UAV was flown at a ground speed of 14 m/s at 160 m above ground level (AGL). The camera mounted on the UAV was the Sony NEX-7, which has a Complementary Metal-Oxide Semiconductor (CMOS) imaging sensor. The Sony NEX-7 is a mirrorless interchangeable lens camera whose sensor format is the Advanced Photo System type-C CMOS. The camera exposure settings were set manually (as opposed to auto-exposure) so as to obtain equally focused images. The camera manual exposure program settings are shown in Table 1 and were established through a set of trial runs before being used



Figure 6. Utilized fixed wing UAV for autonomous image capturing.

Table 1. Manual exposure program of the camera.

Exposure time	1/1000 s
ISO-speed	ISO-100
Focal length	16 mm
Maximum aperture	f/2.96875

in this case study. The resultant 611 24-bit single images had 6000×4000 pixels each with ground coverage of $234 \text{ m} \times 156 \text{ m}$. The camera parameters depend on the prevailing wind speed and flight height and thus should be customized accordingly.

3.3. Image processing

The images, GCPs, and spectral data were acquired on 12 August 2016. This month in particular is naturally known to be the South African late winter season and thus regarded as the most appropriate phenological stage for mapping *H. pomanensis* (Mafanya et al. 2017). This is because the deciduous background vegetation shed leaves while *H. pomanensis* remains evergreen during this season. During image acquisition, the GNSS/IMU system on board the UAV was logging GPS coordinates of each captured image as events that were later used to geotag the raw images using Ardupilot's open source Mission Planner (Osborne 2016). The side and forward overlap were set to 60% and 80%, respectively. This image sampling redundancy is not only critical for providing a basis for checking scene illumination uniformity, as will be demonstrated in this study, but also for generating 3D point clouds, digital surface models (DSMs), and orthomosaics using UAV Structure from Motion (SfM). In particular, SfM is a photogrammetric 3D reconstruction technique that uses overlapping 2D images to create 3D point clouds, DSMs, and orthomosaics. SfM involves three stages, namely (1) feature detection, (2) image matching, and (3) bundle block adjustment (Wang et al. 2014). Furthermore, the proprietary Agisoft Photoscan (Agisoft LLC 2016) software was used for image mosaicking using UAV-SfM. The geotagged raw images were administered into the Agisoft Photoscan photogrammetry package together with 10 GCP points to produce the georectified RGB orthomosaic as done by Coveney and Roberts (2017). SfM does not require camera exterior orientations or interior orientations but the Agisoft lens software was used for lens distortion geometric calibration (Fraser et al. 2016). The 10 GCPs were used to increase the mosaicking speed and image matching accuracy.

3.4. Radiometric calibration results

3.4.1. Scene illumination uniformity check experiment using the Student's *t*-test

Table 2 shows the descriptive statistics used in the two sample Student's *t*-test performed between the mean DN of the reference illumination uniformity check marker

Table 2. Descriptive statistics for reference uniformity check L-shaped markers.

Statistic	B01 marker	B02–B10 markers
Mean DN	223.98	222.62
Variance of DNs	34.63	28.63
STD deviation of DNs	5.88	5.35

(B01) and the other L-shaped markers (B2–B10). In particular, the reference L-shaped marker (B01) had higher variance, standard deviation, and mean pixel DNs than the overall variance, standard deviation, and mean pixel DNs of the other scene illumination uniformity check L-shaped markers. However, the difference of 1.36 between the mean DNs in Table 2 was not found to be statistically significant at the 95% confidence interval ($p < 0.05$). This information can be considered to infer that it is justifiable to calibrate the entire orthomosaic using ELM prediction equations derived from mean reflectance values measured in only one spot within the 97 ha RGB orthomosaic. These results show that the entire scene being mapped is experiencing similar atmospheric and illumination conditions.

3.4.2. Regression of calibration target image mean DNs and mean *in situ* spectral reflectance

A summary of the regression relationships between image DNs and *in situ* reflectance measurements in the red, green, and blue wavebands is presented in Table 3. The regression equations results show that the relationship between image DNs and *in situ* reflectance measurements in all the camera wavebands is exponential (Equations (2)–(4)). An exemplary visual depiction of the exponential relationship for the red waveband is shown in Figure 7. Furthermore, Figure 8 shows that there exists a linear relationship between the natural log transformed reflectance values and image DNs. A similar observation was also found in Wang and Myint (2015). As a result, the y-intercept 3.423 (Figure 8 and Equation (8) in Table 3) can be converted to reflectance (0.033), which represents the minimum at-surface reflectance that the Sony Nex-7 CMOS sensor used in this study can detect in the red waveband colour channel. In addition, the utilized CMOS sensor can detect minimum at-surface reflectance values of 0.032 and 0.029 for the green and blue wavebands, respectively. The minimum at-surface reflectance values for the green and blue wavebands were derived using the constants in Equations (9) and (10).

3.4.3. Empirical line calibration equations

The y-intercept value for each linear equation represents the constant calibration parameter in the ELM calibration prediction equation of type:

$$-\ln(y) = m \times (\text{DN}) + C \quad (11)$$

where y represents reflectance, m being the gradient of each image waveband in the derived ELM calibration equation, and C representing the constant calibration parameter (Table 4, Equations (12)–(14)). The derived linear Equations (12)–(14) in Table 4 were used to calibrate the 97 ha RGB orthomosaic image wavebands. Subsequent layer stacking, quantitative analysis, and image classification can thus be performed on the calibrated orthomosaic following the procedures outlined by Mafanya et al. 2017 for mapping *H. pomanensis* from UAV derived ultra-high spatial resolution RGB imagery.

3.4.4. Error analysis between estimated and *in situ* measured reflectance values

To validate the proposed vicarious radiometric calibration methodological framework, reflectance values derived from the calibrated image wavebands were regressed against *in situ* measured reflectance values for the check targets. Results shown in Table 5 present the comparison between mean reflectance values derived from the calibrated

Table 3. Summary of regression relationships for each waveband.

	Red band	Green band	Blue band
Regression equation	$y = 0.032e^{(0.014DN)} \quad (2)$	$y = 0.032e^{(0.013DN)} \quad (3)$	$y = 0.029e^{(0.013DN)} \quad (4)$
Coefficient of determination	$R^2 = 0.99 \quad (p < 0.01) \quad (5)$	$R^2 = 0.99 \quad (p < 0.01) \quad (6)$	$R^2 = 0.98 \quad (p < 0.01) \quad (7)$
Linearized equation	$y = -0.014x + 3.423 \quad (8)$	$y = -0.013x + 3.434 \quad (9)$	$y = -0.013x + 3.518 \quad (10)$

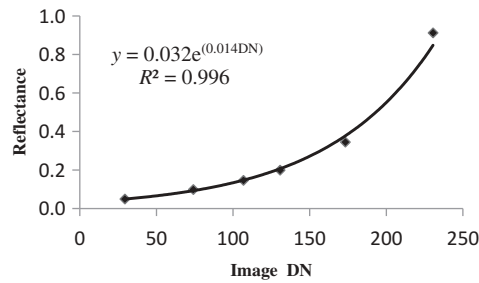


Figure 7. Example of the relationship between image digital numbers and *in situ* at-surface reflectance values for the red waveband.

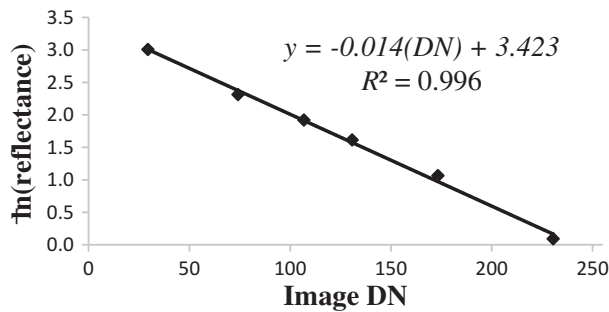


Figure 8. Example of the relationship between natural log-transformed reflectance and *in situ* at-surface reflectance values for the red waveband.

Table 4. Linear calibration equations for the red, green, and blue wavebands.

Image waveband	Radiometric calibration equation
Red	$-\ln(y) = -0.01413 \times (\text{DN}) + 3.423(12)$
Green	$-\ln(y) = -0.01385 \times (\text{DN}) + 3.434(13)$
Blue	$-\ln(y) = -0.01338 \times (\text{DN}) + 3.518(14)$

image wavebands (estimated) and their respective *in situ* at-surface reflectance values (measured) for the black, blue, green, red, and white check targets. There are three data points for each check target representing each waveband. The regression between the reflectance values derived from the calibrated image wavebands and the measured at-surface reflectance values resulted in a correlation coefficient r value of 0.977 ($p < 0.01$) as shown in Figure 9. Furthermore, the RMSE between estimated and measured reflectance values in Table 5, i.e. for all the three wavebands and five check targets, was found to be 0.063, whereas the waveband specific RMSE values were 0.040, 0.048, and 0.089 for the red, green, and blue image wavebands, respectively. The aforementioned strong correlation, coupled with the low overall RMSE, suggests low discrepancies between the *in situ* measured mean reflectance values and the reflectance values derived from the radiometric calibrated image wavebands. In particular, the highest RMSE value of 0.089 reported for the blue waveband could be attributed to the fact that scattering of

Table 5. Comparison between check targets (black, blue, green, red, and white) mean reflectance values and their respective *in situ* at-surface reflectance values.

	Estimated reflectance	Measured reflectance
<i>Black square</i>		
Red	0.046607	0.054228
Green	0.044089	0.049955
Blue	0.041845	0.047642
<i>Blue circle</i>		
Red	0.046601	0.026515
Green	0.062312	0.066245
Blue	0.361492	0.241355
<i>Green circle</i>		
Red	0.088030	0.150555
Green	0.447994	0.362182
Blue	0.132574	0.110585
<i>Red circle</i>		
Red	0.557448	0.521022
Green	0.070380	0.070882
Blue	0.074535	0.053538
<i>White square</i>		
Red	0.709671	0.759841
Green	0.717760	0.782323
Blue	0.658850	0.815857

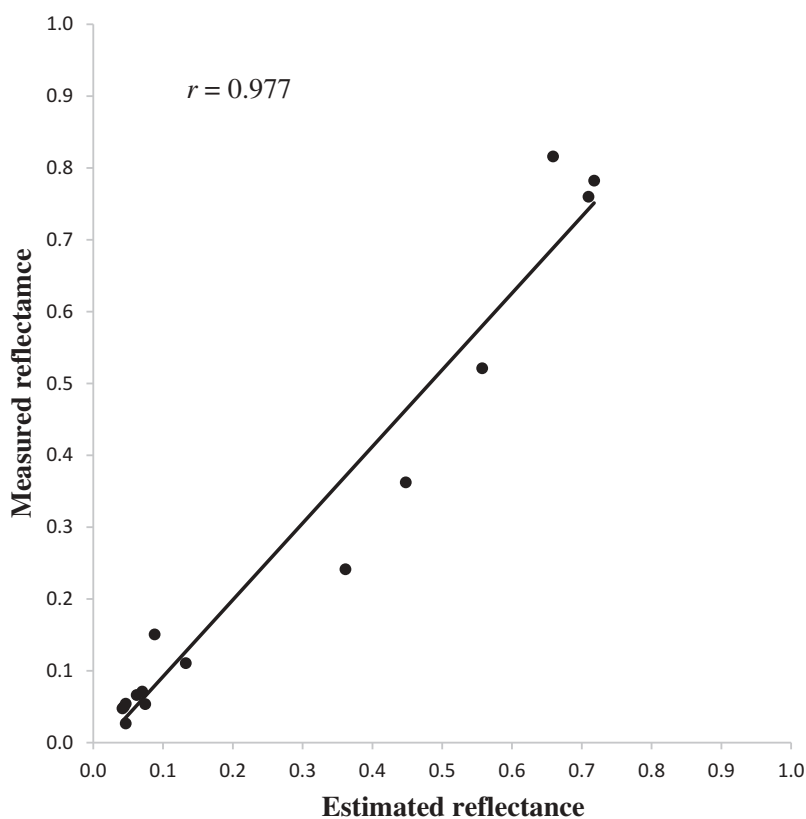


Figure 9. Regression between *in situ* measured reflectance and the reflectance values derived from the calibrated image wavebands ($r = 0.977$).

radiation by the atmosphere is greater at shorter wavelengths (Smith and Milton 1999). Hence, the *in situ* proximally sensed white target mean reflectance of 0.816 is much higher than the remotely sensed mean reflectance of 0.659 in the blue waveband colour channel of the Sony Nex-7 camera. This is because proximal sensing was done at 1 m above the check targets while remotely sensed images were taken at 160 m AGL, meaning radiation interacted with more atmospheric particles in the latter case. In overall, these error analysis and the strong correlation results validate the proposed radiometric calibration framework for applications in flat terrain semi-arid woodlands.

4. Discussion and conclusion

Radiometric calibration methods are usually developed for single-image samples as done in Kelcey and Lucieer (2012), Del Pozo et al. (2014), and Taylor (2015). However, the tendency of IAPs to spread over large areas necessitates the development of vicarious radiometric calibration methods that can be applied on image data spanning large spatial extents and this requires large enough calibration targets. This study demonstrated a radiometric calibration framework for UAV-derived orthomosaics for application in flat semi-arid woodlands. First, it was demonstrated that the relatively affordable Masonite hardboards painted with varying grey values of black and white water paint are highly Lambertian and appropriate for use in calibration target design. This property was observed both in a controlled room with an artificial light source and on the field in the semi-arid woodland study area. The Masonite hardboards of 244 cm × 122 cm were found to be large enough to allow painting of two grey levels in tandem configuration when the UAV is flown at an altitude of less than 160 m AGL. Some studies make use of vinyl sheet canvas to design the greyscale calibration targets as done in Del Pozo et al. (2014), and thus, the target material of choice can be influenced not only by Lambertian properties but also availability, transportability, and ease of use in different environmental settings.

Second, a scene illumination uniformity check method was developed in this study to assess whether the incoming radiant flux is uniform across the orthomosaic. The solar irradiance within the 97 ha study area was found to be uniform, thus indicating that all the 611 images taken by the Sony NEX-7 were acquired under the same environmental conditions. The hypothesis was that under the same environmental conditions the DNs of the same target material should be similar and this was tested at a 95% confidence interval. The difference of 1.36 between the mean DNs of the reference L-target and the other L-targets in Table 2 was found not to be statistically significant at the 95% confidence interval, and from this, it was inferred that it is justifiable to calibrate the entire scene using prediction equations derived using mean reflectance values measured from only a single spot within the mapped area.

Third, this study demonstrated that there exists an exponential relationship between target DNs and their corresponding at-surface mean reflectance values (Equations (2)–(4)). However, in most studies, e.g. in Dean, Warner, and McGraw (2000), Karpouzli and Malthus (2003), Levin, Ben-Dor, and Singer (2009), and Berni et al. (2009), the empirical linear calibration equation were derived by assuming a linear relationship between image DNs and calibration targets *in situ* reflectance values. This assumption is usually made when there is only two calibration targets, e.g. a white and a black target (Smith

and Milton 1999). In this study, this relationship was found to be exponential with coefficient of determination R^2 values greater than 0.98 (Equations (5)–(7)) as found in Wang and Myint (2015). Figure 7 is an example of the observed exponential relationship between image DNs and the mean *in situ* measured reflectance values of the calibration targets. Upon transformation of the exponential equations by taking the natural log, the constant calibration parameters of the empirical linear equations were derived. The three ELM calibration prediction equations were then derived by first computing the gradient of the prediction equation using the calibration target average DN and its average *in situ* reflectance as well as the constant calibration parameter or y-intercepts of the linear equations (Table 4).

Finally, the accuracy of at-surface reflectance values in the calibrated image wavebands was assessed using *in situ* spectral measurements for white, red, green, blue, and black reinforced PVC targets, resulting in a correlation coefficient r 0.96 ($p < 0.01$) and overall RMSE of 0.063. These findings suggest that given the entire scene being mapped is experiencing similar irradiance flux under similar environmental conditions according to the scene illumination uniformity assessment, then radiometric calibration using mean reflectance values measured from only one area of the orthomosaic can be used to calibrate the entire orthomosaic. The proposed framework is not only important for mapping IAPs but also for use in large-scale crop mapping applications in precision agriculture, land-use/land-cover monitoring, as well as vegetation mapping and classification, particularly for mapping widespread IAPs such as *H. pomanensis*. The limitation of this research is that it has no way of showing the largest spatial coverage for which the demonstrated vicarious radiometric calibration framework could be applied. This, however, could also depend on the nature of the environment that is being mapped as well as prevailing weather conditions. Future research objectives could be to apply this framework for areas larger than 200 ha as the developments in UAV and battery technology are increasingly enabling these systems to map larger areas. Most studies that applied UAV-RS for mapping IAPs made use of thematic image classification without conducting either sensor geometric or image radiometric calibration, for instance, Dvořák et al. (2015), Müllerová et al. (2016, 2017), Hill et al. (2017), and Mafanya et al. (2017). Therefore, another future research objective would be to assess whether radiometric calibration improves the image classification accuracy for mapping and detecting various IAPs in different environmental settings. Another important research avenue is quantitative image analysis using radiometric calibrated UAV-RS imagery for improving the estimation of biophysical and biochemical constituents in plants from UAV imagery.

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Author contributions

M.M., P.T., and P.M. conceived the research idea. M.M. and P.T. conducted the data analysis, literature review, tables, figures, and preparation of manuscript. J.B.G.C and T.M. managed the preparation of the manuscript and performed editing.

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