First-principles studies of SnS₂, MoS₂ and WS₂ stacked van der Waals hetero-multilayers

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Abstract

We present the energetics, structural and electronic properties of SnS₂ monolayer stacked with MoS₂ and WS₂ monolayers making the van der Waals heterolayers using the first-principles methods. The exchange-correlation functionals used are the LDA, GGA functionals as well as the newly developed variants of non local van der Waals (vdW) exchange-correlation functionals, namely vdW-DF-revPBE and vdW-DF2-C09. We also considered the combinations of hetero-layers that involve all the three SnS₂, MoS₂ and WS₂ stacked together. All the investigated hetero-layers have a short decay (offset) of the equilibrium lattice parameters compared to the SnS₂ single layer one. Except for the GGA-PBE functional, all the functionals predict the interlayer distances closer to the previous theoretical and experimental studies. The hetero-layers that have relative low binding energies are indirect band gap semiconductors, while those with dramatically high binding energies are weakly or strongly metallic. This study gave another avenue of altering the energetics and electronic properties of SnS₂ monolayer through vertical stacking with MoS₂ and WS₂. The variation in band gap enables these newly predicted hetero-layers to be suitable candidates for designing novel devices for nanoelectronic and optoelectronic technology, which includes energy storage, photodetectors, thermophotovoltaic.

Keywords: SnS₂, MoS₂, WS₂, van der Waals hetero-layers, Electronic properties, van der Waals exchange-correlation functionals, first-principles

1. Introduction

After the experimental synthesis of the free standing graphene in 2004 [1, 2], the other two dimensional (2D) materials such as hexagonal boron nitride (h-BN), transition metal dichalcogenides (TMDs) [3] such as MoS₂, MoSe₂, WSe₂, WSe₂, etc gained a lot of attention. Amongst of these, the TMDs [3] have become attractive due to their potential practical applications [4, 5] in electronic and opto-electronic devices. These can be possible due to unique physical characters such as indirect or direct large band gaps, reduced dimensionality and great mechanical strength in the TMDs systems [6].

The 2D TMDs materials are layered systems, with the transition metals sandwiched between the chalcogen elements covalently bonded together. For few layered TMDs systems, the bonding along the vertical axis or out of plane is due to the van der Waals interactions (vdW) [7, 8]. The bulk TMDs hexagonal phases present the indirect band gap, whereas they are direct in monolayer phases [8, 9]. Because of the unique crystal structure, high anisotropy and perculiar electronic properties [10, 11, 12], the 2D TMDs become one of the most studied materials in the fundamental research and technological applications. These materials are easily synthesizable through different methods including chemical vapor deposition, chemical, mechanical and electrochemical exfoliation, and are stable at room temperature [10, 11, 13, 14, 15, 16, 17].

Although the TMDs are relatively large band gap systems, the band gap controllability is the major requirement in the nanotechnology applications. To achieve this, modifying the electronic properties of TMDs continues unabated using different methods such as reducing dimensions, intercalation, alloying, creating heterostructures, etc [18]. Recently, the most popular or promising method is the stacking of layers along the vertical axis (vertical heterolayers). This method is practically feasible both experimentally and theoretically [19, 20, 21]. He et al. [9] investigated the stacking effects on the electronic and

optical properties of bilayer TMDs, namely MoS₂, MoSe₂, WS₂ and WSe₂. It has been established that there is a transition from direct-to-indirect band gap going from monolayer to bilayer. It was concluded that the stacked hetero-layers is another promising possibility that can tune the electronic properties of the main material system. Terrones *et al.* [22] demonstrated that a direct band gap ranging from 0.79 eV to 1.16 eV can be achieved in TMDs hetero-bilayers with change in stacking.

The Sn-dichalcogenides have a TMDs-like structure. Recently, the theoretical prediction [23, 24] and experimental synthesis of the SnS₂ monolayers [5, 25, 26] has attracted considerable attention for its promising chances of being exploited in various electronic devices [13, 23, 27, 28, 29, 30]. SnS₂ is an indirect band gap semiconductor over the entire thickness range from bulk to single-layer [24]. With the band gap of about 2.2 eV, SnS₂ showed the attractive visible light photocatalytic activity which makes it the promising materials in photoelectronic devices and solar cells [31, 32]. It displayes interesting charge carrier mobility, mechanical and thermophysical properties, useful in design and the development of new materials [24, 33]. Controlling the electronic properties of SnS₂ through stacking, in particular involving the homo and hetero-layers has been considered lately [34, 35]. In our previous work we have shown, using Density Functional Theory (DFT) calculations, that the stability and electronic properties of the SnS₂ multilayers depend on the stacking sequences [36]. All the SnS₂ multilayer configurations was found to be stable and band gaps tuned with the increase in the number of stacked layers. This study can be extended in the hetero-layer of SnS₂ with others TMDs. Zhang et al. [35] have successfully synthesized SnS₂-MoS₂, SnS₂-WS₂ and WS₂-SnS₂ van der Waals hetero-bilayers using a chemical vapor deposition method at mild temperatures. Theoretical investigations on the electronic properties of these hetero-bilayers was also done [35], and the results confirmed the experiments in altering the electronic properties of the pristine SnS₂ monolayer. The creation of multilayers further alters the electronic properties of the main monolayer structure [35, 37, 38], and could be used to understand the transition from direct to

indirect band gap observed in the hetero-multilayer systems. The hetero-trilayer of SnS₂ stacked with MoS₂ monolayers should also be plausible, and it will be interesting to examine the band gap variation with the number of hetero-layers. It is interesting to compare the results of standard LDA and GGA functionals [39] with those of the newly developed variants of non-local van der Waals exchange correlation functionals, i.e. vdW-DF-revPBE [40] and vdW-DF2-C09 [41, 42] in such systems. These vdW exchange correlation functionals are known to correctly capture the effects of vdW forces in complex systems, and they are efficient in describing a wide range of systems without too much computational cost [43]. The vdW-DF-revPBE functional generally predicts relatively weak binding energy in the case of stacked nanosheets, but it severely overestimates the interlayer distances [40, 44]. To solve this overestimation, the vdW-DF2-C09 functional has been used, since it has been proved to be suitable for such systems [41, 42, 44].

In the present work, we studied the interlayer interaction energy, structural (in-plane and out of plane) and electronic properties of SnS₂ stacked with MoS₂ and WS₂ nanosheets making van der Waals hetero-bilayers and trilayers using various DFT methods. We considered in more details the hetero-layers that involves the stacking of SnS₂ stacked with MoS₂ and WS₂ nanosheets and compare with previous works on the similar systems. Our results suggest that the newly studied hetero-multilayers can be an effective way for controlling the band gap of SnS₂ nanosheets to meet the requirements of electronic applications at favourable conditions.

This paper is organized as follow: in section II, the details of our computational methods are described. The results of our DFT calculations for SnS_2 , MoS_2 and WS_2 sheets and SnS_2 heterostructures are given in Section II. The conclusion and perspectives are presented in the final section.

2. Computational method

Our first-principles calculations have been performed using QUANTUM ESPRESSO distribution [45] package which uses a plane wave basis set within the pseudopotential approach and periodic boundary conditions. We use the well-known LDA and GGA exchange-correlation functionals, and the newly developed two variants of non-local van der Waals exchange correlation functionals, namely vdW-DF-revPBE and vdW-DF2-C09 which take into account the vdW forces [40, 41, 42]. The Kohn-Sham (KS) orbitals and the charge density are represented using basis sets consisting of the plane waves up to a maximal kinetic energy of 35 Ry and 350 Ry, respectively. The Brillouin zone is sampled using the Monkhorst-Pack scheme [46] with a grid of $7 \times 7 \times 1$ and $10 \times 10 \times 1$ k-points mesh for GGA and LDA functionals respectively. We have used the supercells consisting of 1×1 unit cell, containing 3, 6 and 9 atoms for one, two and three layers respectively. The layers are separated from their periodic images by at least 15 Å of vacuum in order to minimized their image interactions. The parameters of 10⁻⁷ Ry is set for convergence on the total energy in self consistent cycle. The in-plane lattice parameter input is set to the 3.70 Å (the lattice parameter of SnS₂ from GGA functional). All coordinates and lattice constants are allowed to relax. Our preliminary results including spin-orbit interactions have shown no major differences compared to those calculated without spin-orbit interactions. Both the band structures with and without spin-orbit interactions possess nearly equivalent bands spliting at the VBM (valence band maximum) in agreement with [47]. Indeed, the contribution of spin-orbit interaction were excluded in this work.

3. Results and Discussion

In this work, all the calculations were performed on the most stable phase of SnS₂, MoS₂ and WS₂ [8, 25, 48], showing a layered CdI₂-type structure in which the metallic atom is sandwiched between two S atoms in a hexagonal closed packed lattice shown in Figure 1. Using the GGA-PBE functional

only, we performed the structural optimization of SnS₂, MoS₂ and WS₂ isolated monolayers to calculate the equilibrium in-plane lattice constants, and thereafter their band structures were plotted to examine the electronic properties. Table 1 summarizes the results, and compares them with the available experimental data and previous theoretical results using GGA-PBE functional, and the obtained lattice parameters of 3.70 Å (SnS₂), 3.17 Å (MoS₂) and 3.15 Å (WS_2) are in agreement with these previous works as shown in this table. The calculated in-plane M-S bondlengths are in good agreement with the literature (see table 1). Comparing the lattice constants of these isolated layers, it is noted that the lattice constants of MoS₂ and WS₂ are very close to each other suggesting that if these layers can be stacked on top of each other there should be no issue of lattice mismatch, and this could be the reason of the excessive literature [22, 49, 50, 51, 52, 53, 54, 55, 56, 57]. However, there is notable lattice constants difference between SnS₂ and MoS₂ of 0.53 Å. This suggests that the stacking of SnS₂ layer with MoS₂ layer (SnS₂/MoS₂) vertically would have a lattice mismatch and will not be easily achieved ideally, therefore a special care should be made in the construction of the atomic models. In the experimental study of the synthesis of SnS₂/MoS₂ and SnS₂/WS₂ stacked layers, it was mentioned that there is lattice mismatch of about 15\% along the \vec{a} direction, importantly tolerated by the van der Waals epitaxy [35]. When modeling these type of hetero-layers, it is imperative to use the exchange correlation functionals that can take into account the effects of van der Waals forces.

In Figure 2, we present the calculated band structures of SnS_2 , MoS_2 and WS_2 isolated sheets. The MoS_2 and WS_2 sheets are direct band gap semi-conductors with the valence band maximum (VBM) and the conduction band minimum (CBM) located at the K-high symmetry point, in agreement with the previous studies [8, 49, 23, 58, 59, 60]. The SnS_2 inherently is an indirect band gap with the CBM located at the M-point, while the VBM is seen between the Γ -point and M-point. Table 1 shows the band gap of 1.57 eV, 1.59 eV and 1.75 eV for SnS_2 , MoS_2 and WS_2 isolated sheets respectively, in agreement with the previous DFT studies [8, 49, 23, 58, 59, 60]. Comparing with the experi-

ments [25, 56, 61, 62], our GGA-PBE results show a slight underestimation as expected. For the stacking of SnS_2 with MoS_2 or SnS_2 with WS_2 , it will be interesting to see how their CBM and VBM rearrange and the band gaps change. To investigate which electron orbital states contributes for VBM and CBM, we present the total and partial density of states (Figure 3). It is noted that the VBM and CBM of SnS_2 monolayer are mainly contributed by p-S orbital states, while those of MoS_2 and WS_2 are mainly contributed by d states from Mo and W.

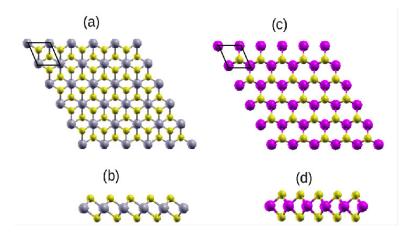


Figure 1 (Color online) The top (a) and side (b) views of $5 \times 5 \times 1$ SnS₂ isolated sheet. The top (c) and side (d) views of $5 \times 5 \times 1$ MoS₂ (resp. WS₂) isolated sheet. The Sn, Mo (resp. W), and S are represented by the gray, purple and yellow spheres respectively. All the calculations were performed on a unit cell delimited by the black lines in (a and c). The 5x5x1 supercell size is used to clearly show the hexagons of the heterostructures.

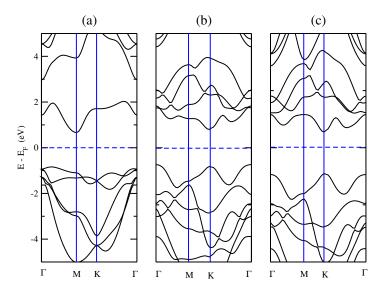


Figure 2 (Color online) The calculated band structure plots of (a) the $\rm SnS_2$, (b) $\rm MoS_2$ and (c) WS₂ isolated layers obtained using the GGA-PBE functional. The Fermi level is set to 0.00 eV.

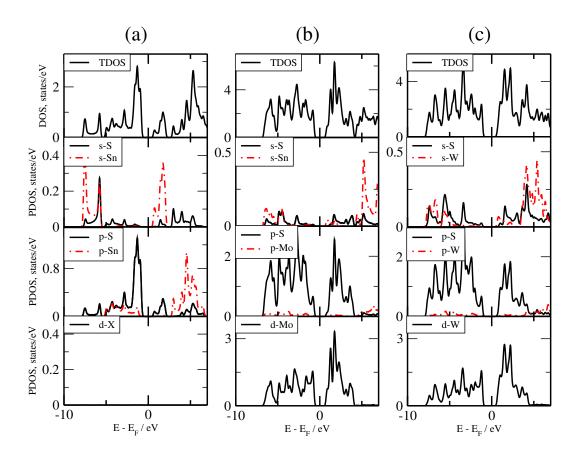


Figure 3 (Color online) The calculated total and partial DOS of (a) SnS_2 , (b) MoS_2 and (c) WS_2 isolated layer systems. The Fermi level is set to 0.00 eV.

3.1. MS_2/SnS_2 (M = Mo, W) hetero-bilayer

Firstly, we examined the properties of WS₂/SnS₂ and MoS₂/SnS₂ stacked hetero-bilayers, using the LDA, GGA-PBE, vdW-DF-revPBE and vdW-DF2-C09 functionals. For both systems, the following stacking sequence was considered; the Sn atoms are directly facing the W or Mo atoms on the adjacent layer, while the S atoms on the top layer directly face the S atoms on the bottom as shown in Figure 4(a). This isolated stacking layers is similar structurally and comparable in energy to the bulk phases of MoS₂ and WS₂ studied by Terrones et al [22].

Table 1: The calculated lattice constants a_0 (Å), bond lengths b_{M-S} (M=Sn, Mo and W) (Å) and the energy band gaps E_g (eV) of the SnS_2 , MoS_2 and WS_2 isolated sheets. These values are compared with the previous DFT studies as well as the available experimental data. The (*) means the value is not available.

Structures		$a_0(\mathring{A})$	$\mathbf{b}_{M-S}(\mathbf{\mathring{A}})$	$E_g(eV)$
SnS_2	This work	3.70	2.60	1.57
	Ref	3.70[23]	2.60 [23]	1.57[23]
	Exp	3.65[25]	2.65[25]	2.23[62]
WS_2	This work	3.15	2.38	1.75
	Ref	3.19[59]	2.43[49]	1.9[60]
	Exp	3.15[61]	*	2.1[56]
MoS_2	This work	3.17	2.37	1.59
	Ref	3.16[8]	2.41[49]	1.60[58]
	Exp	3.15[8]	2.38[8]	1.8[56]

After full geometry optimization, the in-plane lattice constants a_0 , out of plane interlayer spacings d_0 , interlayer binding energies E_b (as the energy needed to keep the stacked layer coupled) and the electronic properties were calculated.

The binding energies E_b are defined as:

$$E_{\rm b} = E_{\rm layers} - iE_{SnS_2} - jE_{MoS_2} - kE_{WS_2} \tag{1}$$

in which E_{layers} , E_{SnS_2} , E_{MoS_2} and E_{WS_2} are the energy of the stacked heterolayers, the energy of a SnS_2 , MoS_2 and WS_2 single layer respectively. Where i=1, 2 and j, k = 0, 1, 2, referring to the number of SnS_2 , MoS_2 and WS_2 layers respectively. According to equation (1), a negative value of E_b corresponds to a strongly coupled hetero-layer, while a positive value corresponds to weakly coupled layers.

From GGA-PBE functionals, we found that for both WS_2/SnS_2 and MoS_2/SnS_2 hetero-bilayers, the value of a_0 is offset compared to the SnS_2 single layer one (see tables 1 and 2). Quantitatively, the in-plane lattice parameter a_0 of WS_2/SnS_2

(resp. MoS₂/SnS₂) hetero-layer is 0.32 Å (resp. 0.37 Å) larger than the SnS₂ single layer one, while it is 0.23 Å (resp. 0.21 Å) lower than the WS₂ (resp. MoS₂) single layer one. This lattice offset is also noted in M-S in-plane bondlengths. Excepted for the vdW-DF-revPBE functional, all other functionals agree with the experimental values in ref [35].

From table 2, all the considered functionals show that the MoS_2/SnS_2 stacked hetero-bilayer has larger d_0 and lower E_b than WS_2/SnS_2 . Apart from the GGA-PBE, all other functionals predict d_0 relatively closer to the experimental and theoretical values [9, 35, 51]. Although, the values of E_b are not negative, this could be due to the lattice mismatch between SnS_2 and WS_2 (resp. MoS_2), observed experimentally by Zhang et al [35]. The small variations in these functionals in predicting the E_b is an indication that the van der Waals interactions are possible but in the very small magnitudes. Although, the MoS_2/SnS_2 bilayer has larger d_0 than WS_2/SnS_2 , its lower E_b could suggests that there is great dipole-dipole interactions between Sn and Mo than between Sn and W.

Figure 5 shows the band structures of (a) MoS₂/SnS₂ and (b) WS₂/SnS₂ hetero-bilayers predicted by all the functionals considered. The plots reveal that the creation of MoS₂/SnS₂ or WS₂/SnS₂ hetero-bilayer rearrange the VBM and CBM of MoS₂, SnS₂ and WS₂ layers, resulting to the indirect band gap semiconductors with the VBM at the Γ -point and CBM located at the K-point. By comparing tables 1 and 2, we observed that the stacking of MoS_2/SnS_2 and WS₂/SnS₂ layers generally reduces the band gaps of the isolated layers, and this for all the functionals used. This reduction in band gap is mainly contributed by the additional d-states coming from Mo (Figure 6(a)) and W (Figure 6(b)) at the VBM. Although the heterostructures are fully relaxed, the noted lattice mismatch could also be the possibility for the band gap reduction. The results presented in this work are for the 1×1 unit cells. For improved results, a large unit cell could be considered in order to reduce the lattice mismatch effects occured when forming the heterostructures from isolated layers that have significant disparity in the lattice parameters $(7 \times 7 \text{ unit cell for MoS}_2 \text{ (resp. WS}_2)$ and 6×6 unit cell for SnS_2).

Table 2: The calculated physical properties of the SnS_2 monolayer stacked with MoS_2 and WS_2 monolayers obtained using different exchange correlation functionals. The properties calculated are the lattice parameter a_0 , bondlengths b_{Sn-S} and b_{W-S} , interlayer spacing d_0 , binding energy E_b and band-gap E_g . In the case of three stacked layers, there are two values of d_0 separated by slash.

Stacking		$\operatorname{GGA-PBE}$	PZ(LDA)	vdW-DF-revPBE	vdW-DF2-C09
WS_2/SnS_2	$a_0(\mathring{A})$	3.38	3.29	3.45	3.35
	$\mathbf{b}_{Sn-S/W-S}(\mathbf{\mathring{A}})$	2.51/2.45	2.48/2.39	2.54/2.48	2.50/2.43
	$d_0(\mathring{A})$	6.77	5.94	6.57	5.98
	$E_b(eV/Cell)$	0.882	0.865	0.677	1.338
	$E_g(eV)$	0.56	0.40	0.41	0.58
$ m MoS_2/SnS_2$	$a_0(\mathring{A})$	3.39	3.29	3.45	3.31
	$b_{Sn-S/Mo-S}(\mathring{A})$	2.51/2.45	2.47/2.40	2.54/2.49	2.49/2.41
	$d_0(\mathring{A})$	7.22	6.54	6.88	6.55
	$E_b(eV/Cell)$	0.822	0.753	0.640	0.997
	$E_g(eV)$	0.32	0.53	0.26	0.47
$\mathrm{SnS}_2/\mathrm{WS}_2/\mathrm{SnS}_2$	$a_0(A)$	3.48	3.22	3.54	3.26
	$b_{Sn-S/W-S}(A)$	2.53/2.48	2.50/2.43	2.58/2.52	2.54/2.46
	$d_0(A)$	7.28/6.81	5.74/6.50	6.34/6.80	5.96/6.69
	$E_b(eV/Cell)$	1.146	1.097	0.804	0.855
	$E_g(eV)$				
$\rm SnS_2/MoS_2/SnS_2$	$a_0(A)$	3.49	3.40	3.55	3.45
	$b_{Sn-S/Mo-S}(A)$	2.56/2.48	2.49/2.44	2.57/2.52	2.54/2.47
	$d_0(A)$	6.87/6.88	6.35/6.24	6.81/6.38	6.61/5.96
	$E_b(eV/Cell)$	1.063	0.899	0.678	0.779
	$E_g(eV)$				
$WS_2/SnS_2/WS_2$	$a_0(A)$	3.31	3.21	3.36	3.27
	$b_{Sn-S/W-S}(A)$	2.47/2.42	2.46/2.37	2.51/2.46	2.48/2.41
	$d_0(\mathring{A})$	7.15/6.33	6.61/6.02	6.80/6.53	6.61/6.08
	$E_b(eV/Cell)$	3.199	1.060	2.541	2.903
	$E_g(eV)$	0.63			
$\rm MoS_2/SnS_2/MoS_2$	$a_0(A)$	3.30	3.21	3.38	3.26
	$b_{Sn-S/Mo-S}(A)$	2.49/2.42	2.44/2.38	2.53/2.46	2.50/2.41
	$d_0(\mathring{A})$	6.60/7.01	6.30/6.20	6.21/6.73	6.12/6.53
	$E_b(eV/Cell)$	1.094	0.918	0.732	0.810
	$E_g(eV)$	0.25	0.42	0.48	0.39
$\rm MoS_2/WS_2/SnS_2$	$a_0(A)$	3.31	3.22	3.37	3.26
	$b_{Sn-S/W-S/Mo-S}(\hat{A})$	2.48/2.42/2.42	2.44/2.37/2.38	2.51/2.45/2.46	2.47/2.41/2.41
	$d_0(A)$	6.32/6.28	6.31/6.26	6.32/6.29	6.31/6.26
	$E_b(eV/Cell)$	1.161	1.206	0.977	1.074
	$E_g(eV)$	0.29	0.54	0.21	0.46
$\rm WS_2/MoS_2/SnS_2$	a ₀ (Å)	3.31	3.21	3.36	3.27
	$b_{Sn-S/W-S/Mo-S}(\mathring{A})$	2.51/2.42/2.41	2.44/2.36/2.38	2.53/2.45/2.45	2.49/2.41/2.41
	$d_0(A)$	7.52/6.34	6.34/6.24	6.98/6.46	6.61/6.04
	$E_b(eV/Cell)$	1.160	1.207	0.975	1.075
	$E_g(eV)$	0.32	0.43	0.30	0.37

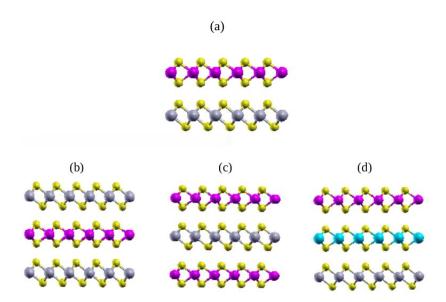


Figure 4 (Color online) The crystal structures of bilayer heterostructure (a) $Mo(W)S_2/SnS_2$. The trilayer heterostructures (b) $SnS_2/Mo(W)S_2/SnS_2$, (c) $Mo(W)S_2/SnS_2/Mo(W)S_2$ and (d) $(W)MoS_2/(Mo)WS_2/SnS_2$. The light green and purple spheres represent the Mo or W atoms.

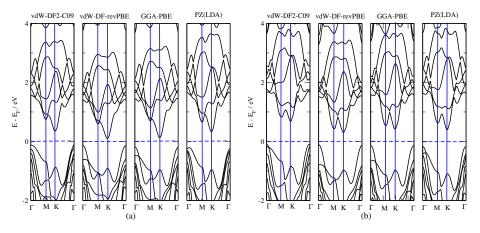


Figure 5 (Color online) The calculated band structure plots of (a) MoS_2/SnS_2 and (b) WS_2/SnS_2 heterostructures obtained using the four different functionals. The Fermi energy is set to 0.00 eV.

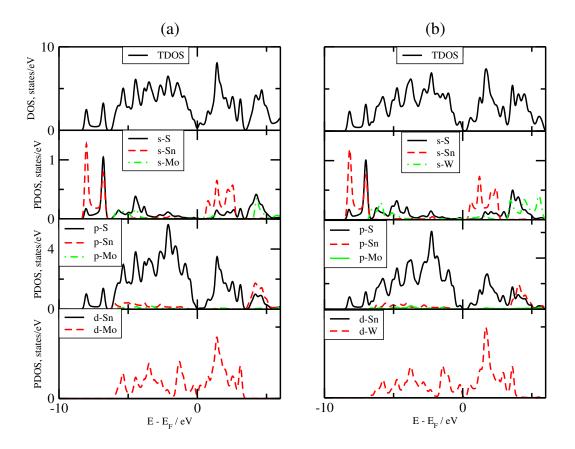


Figure 6 (Color online) The calculated total and partial DOS of (a) MoS_2/SnS_2 and (b) WS_2/SnS_2 systems. The Fermi level is set to 0.00 eV.

3.2. $SnS_2/MS_2/SnS_2$ (M = Mo, W) heterostructures

The hybrid heterostructures consisting of MS_2 sandwiched between two SnS_2 monolayers $(SnS_2/MoS_2/SnS_2$ and $SnS_2/WS_2/SnS_2$ hetero-trilayers) were also studied in this present work (see Figure 4(b)). Similar hybrid study was earlier performed in the case of graphene or Boron nitride sandwiched between MoS_2 layers or between WS_2 layers [63, 64]. Table 2 summarizes the physical properties of the $SnS_2/MoS_2/SnS_2$ and $SnS_2/WS_2/SnS_2$ hetero-trilayers. The values of a_0 are close to those found in the case of hetero-bilayers. As reported in table 2, the Sn-S, Mo-S and W-S bond lengths calculated using all the functionals are approximatively the same for $SnS_2/MoS_2/SnS_2$ as well as for $SnS_2/WS_2/SnS_2$

systems. The calculated d_0 for $SnS_2/WS_2/SnS_2$ hetero-trilayers are shorter between the top layer and the second layer (5.74 Å, 6.34 Å and 5.96 for LDA, vdW-DF-revPBE and vdW-DF2-C09 functionals respectively) than between the second layer and most bottom layer (6.50 Å, 6.80 Å and 6.69 Å for LDA, vdW-DF-revPBE and vdW-DF2-C09 functionals respectively) as presented in table 2. Different scenario is noted in the case of $SnS_2/MoS_2/SnS_2$ where the values of d_0 are almost equal in both interlayer separations. In the two systems, the lowest E_b is obtained using the vdW-DF-revPBE functional (0.678 eV/Cell and 0.804 eV/Cell for $SnS_2/MoS_2/SnS_2$ and $SnS_2/WS_2/SnS_2$ respectively), suggesting that MoS_2 sheet favourably adhere to SnS_2 than WS_2 sheet.

The band structures related to $\mathrm{SnS_2/MoS_2/SnS_2}$ and $\mathrm{SnS_2/WS_2/SnS_2}$ heterotrilayers presented in Figure 7, show that an addition of the third layer ($\mathrm{SnS_2}$ layer) to the hetero-bilayer ($\mathrm{SnS_2/MoS_2}$ and $\mathrm{SnS_2/WS_2}$) closes the band gap. For both structures, the VBM and CBM touch the Fermi level at the Γ -Point and the K-point respectively, suggesting a weak metallic character which can be easily altered by external factors such as temperature and pressure. In order to understand the origin of closing the band gap, we calculated the partial density of states (PDOS) for s, p and d orbitals of all the atoms in $\mathrm{SnS_2/MoS_2/SnS_2}$ and $\mathrm{SnS_2/WS_2/SnS_2}$ hetero-layers, and the results are presented in Figures 8(a) and 8(b). In these Figures, one can see that for the two heterostructures, the VBM and CBM at the vicinity of the Fermi level are mainly contributed by the d-W and d-Mo orbitals.

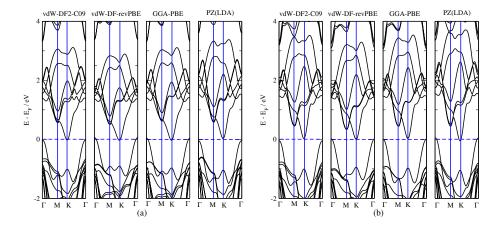


Figure 7 (Color online) The calculated band structure plots of (a) $\rm SnS_2/MoS_2/SnS_2$ and (b) $\rm SnS_2/WS_2/SnS_2$ heterostructures calculated using the four different functionals. The Fermi energy is set to 0.00 eV.

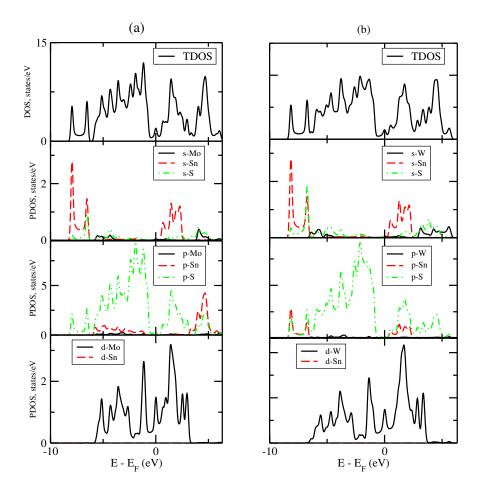


Figure 8 (Color online) The calculated total and partial DOS of (a) $\rm SnS_2/MoS_2/SnS_2$ and (b) $\rm S_2/WS_2/SnS_2$ systems. The Fermi level is set to 0.00 eV.

3.3. $MS_2/SnS_2/MS_2$ (M = Mo, W) heterostructures

The second hybrid hetero-trilayers studied involved MoS_2 or WS_2 layers sandwiching the SnS_2 layer ($MoS_2/SnS_2/MoS_2$ and $WS_2/SnS_2/WS_2$) along the vertical axis as shown in Figure 4(c). The calculated in-plane lattice constant a_0 are similar in the two systems, for each exchange-correlation functional (see table 2). These are the lowest lattice constant compared to the previous heterostructures ($Mo(W)S_2/SnS_2$ and $SnS_2/Mo(W)S_2/SnS_2$). This is the result of the dominance of MoS_2 or WS_2 layers in the hybrid systems. In fact, during

the geometry optimization of the unit cell, the relatively short bondlength b_{W-S} (resp. b_{Mo-S}) in WS₂ (resp. MoS₂) layer reduces the b_{Sn-S} in SnS₂ layer, resulting to a shortest a_0 . Although, the interlayer spacings in MoS₂/SnS₂/MoS₂ and WS₂/SnS₂/WS₂ hetero-trilayers do not deviate much from the previous hetero-trilayers (Mo(W)S₂/SnS₂ and SnS₂/Mo(W)S₂/SnS₂), while the E_b value of WS₂/SnS₂/WS₂ is dramatically very higher than that of MoS₂/SnS₂/MoS₂ as shown in table 2. This suggests that the vertical interaction of Mo with Sn through dipole-dipole is slightly favourable than that of W with Sn, and it could also be more possible to synthesize the MoS₂/SnS₂/MoS₂ than the WS₂/SnS₂/WS₂ system although endothermically. Experimentally, it was reported that these type of systems can be achieved at mild temperatures [35].

Figures 9(a and b) show the band structures of the $MoS_2/SnS_2/MoS_2$ and $WS_2/SnS_2/WS_2$ hetero-trilayer systems. Table 2 shows that the lowest binding energy of the $MoS_2/SnS_2/MoS_2$ hetero-trilayer system has a narrow band gap whose the magnitude depends on the functional used. This magnitude is nearly the same for the MoS_2/SnS_2 (resp. WS_2/SnS_2) hetero-bilayer (see table 2). We can further see the metallic feature in the case of $WS_2/SnS_2/WS_2$ system by all the functionals excepted the LDA functional which predicts the semiconducting character with a band gap of 0.63 eV.

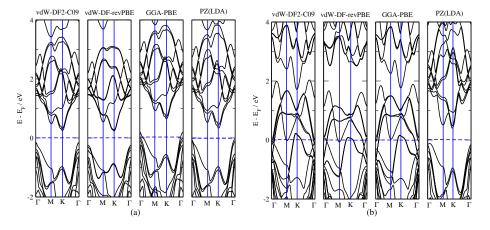


Figure 9 (Color online) The calculated band structures plots of (a) $MoS_2/SnS_2/MoS_2$ and (b) $WS_2/SnS_2/WS_2$ hetero-trilayer obtained using the four different functionals. The

Fermi energy is set to 0.00 eV.

3.4. $W(Mo)S_2/Mo(W)S_2/SnS_2$ heterostructures

Finally, we studied the $\rm MoS_2/WS_2/SnS_2$ and $\rm WS_2/MoS_2/SnS_2$ hetero-trilayer systems which is the combination that was never studied before (see Figure 4(d)). In these hetero-trilayer systems, the value of $\rm a_0$ does not deviate from the previously studied $\rm MoS_2/SnS_2/MoS_2$ and $\rm WS_2/SnS_2/WS_2$ hetero-trilayer systems as shown in table 2. We notice a slight difference in Sn-S bondlength of $\rm MoS_2/WS_2/SnS_2$ compared to $\rm WS_2/MoS_2/SnS_2$ heterostructures while their $\rm E_b$ are almost equal.

The band structures of $WS_2/MoS_2/SnS_2$ and $MoS_2/WS_2/SnS_2$ hetero-trilayer systems are presented in Figures 10 ((a) and (b)). Both systems are narrow indirect band gap semiconductors, with $MoS_2/WS_2/SnS_2$ system having 0.29 eV (GGA), 0.54 eV(LDA), 0.21 eV (vdW-DF-revPBE) and 0.46 eV (vdW-DF2-C09), and $WS_2/MoS_2/SnS_2$ 0.32 eV (GGA), 0.43 eV(LDA), 0.30 eV (vdW-DF-revPBE) and 0.33 eV (vdW-DF2-C09). This study demonstrated the avenue of altering the physical properties of SnS_2 layer through stacking with the MoS_2 and WS_2 layers.

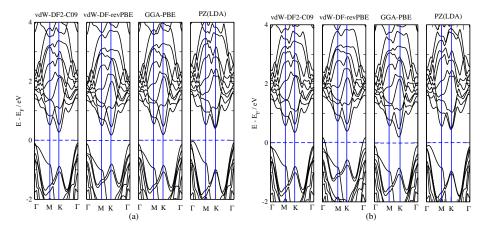


Figure 10 (Color online) The calculated band structure plots of (a) WS₂/MoS₂/SnS₂ and (b) MoS₂/WS₂/SnS₂ systems obtained using the four different functionals. The Fermi level is set to 0.00 eV.

4. Conclusion and perspectives

We have systematically investigated the interlayer interaction, structural and electronic properties of the SnS₂, MoS₂ and WS₂ stacked hetero-layers using first-principles methods. The hetero-layers consist of two or three stacked layers, particulary SnS₂ combined with either MoS₂ or WS₂. We also considered the new combination that involves all the three SnS_2 , MoS_2 and WS_2 stacked together. All the investigated hetero-layers have a short decay (offset) of the equilibrium lattice parameters compared to the SnS₂ single layer one which influences the electronic properties. Apart from the GGA-PBE functional, all other functionals predict the interlayer distances closer to the previous theoretical and experimental studies. The vdW-DF-revPBE functional gives the lowest interlayer binding energies while the GGA-PBE predicts the highest. It was established that the dipole-dipole interactions play a significant role on the energetics of the heterostructures. The hetero-layers that have relative low binding energies are indirect band gap semiconductors, while those of dramatically high binding energies are weakly or strongly metallic. Our newly studied heterolayers are plausible and require further experimental characterization. This study gave another avenue of altering the energetics and electronic properties of SnS₂ monolayer through vertical stacking. The variation in band gap enables these newly predicted hetero-layers to be suitable candidates for designing novel devices for nanoelectronic and optoelectronic technology, which includes energy storage, photodetectors, thermophotovoltaic. In this work, only qualitative effect of different exchange-correlation functionals on the band structure has been study. The quantitative effect can be further investigated by using the hybrid DFT-HSE06 functional known as better to describe accurately the electronic band gap.

Acknowledgments

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