

- [12] M. T. Ma, *Theory and Application of Antenna Arrays*. New York, N.Y., USA: John Wiley & Sons, 1974.
- [13] M. T. Lo and S. W. Lee, eds., *Antenna Handbook*. New York, N.Y., USA: Van Nostrand Reinhold Corp., 1989.

## References

- [1] A. D. Olver, "Basic properties of antennas," in *The Handbook of Antenna Design* (A. W. Rudge, K. Milne, A. D. Olver, and P. Knight, eds.), vol. 1 and 2, ch. 1, London, UK: Peter Peregrinus Ltd., 2 ed., 1986.
- [2] H. J. Kuno and T. A. Midford, "The evolution of MMIC packaging," in *IEEE AP-S Int. Symp. Digest*, vol. 2, (Ann Arbor, MI, USA), pp. 1005–1008, June 1993.
- [3] N. J. Parsons, "Optical interconnection and packaging for active array antenna," in *IEEE AP-S Int. Symp. Digest*, vol. 2, (Ann Arbor, MI, USA), pp. 1001–1004, June 1993.
- [4] H. R. Fetterman, S. R. Forrest, and D. V. Plant, "Optical controlled phased array radar receivers," in *IEEE AP-S Int. Symp. Digest*, vol. 3, (Ann Arbor, MI, USA), pp. 1523–1525, June 1993.
- [5] R. R. Kunath, "Applications of optics in arrays," in *IEEE AP-S Int. Symp. Digest*, vol. 3, (Ann Arbor, MI, USA), pp. 1526–1529, June 1993.
- [6] J. F. Rose, B. A. Worley, and M. M. Lee, "Antenna patterns for prototype two-dimensional digital beamforming array," in *IEEE AP-S Int. Symp. Digest*, vol. 3, (Ann Arbor, MI, USA), pp. 1544–1547, June 1993.
- [7] G. V. Borgiotti, "Conformal arrays," in *The Handbook of Antenna Design* (A. W. Rudge, K. Milne, A. D. Olver, and P. Knight, eds.), vol. 1 and 2, ch. 11, London, UK: Peter Peregrinus Ltd., 2 ed., 1986.
- [8] R. C. Hansen, ed., *Microwave Scanning Antennas*. Los Altos, CA, USA: Peninsula Publishing, 1985.
- [9] W. L. Stutzman and G. A. Thiele, *Antenna Theory and Design*. New York, N.Y., USA: John Wiley & Sons, 1981.
- [10] R. S. Elliott, *Antenna Theory and Design*. Englewood Cliffs, N.Y., USA: Prentice-Hall, 1981.
- [11] A. W. Rudge, K. Milne, A. D. Olver, and P. Knight, eds., *The Handbook of Antenna Design*, vol. 1 and 2. London, UK: Peter Peregrinus Ltd., 2 ed., 1986.

## REFERENCES

## REFERENCES

- [12] M. T. Ma, *Theory and Application of Antenna Arrays*. New York, N.Y., USA: John Wiley & Sons, 1974.
- [13] Y. T. Lo and S. W. Lee, eds., *Antenna Handbook*. New York, N.Y., USA: Van Nostrand Reinhold Com., 1988.
- [14] D. A. McNamara, C. W. I. Pistorius, and J. A. G. Malherbe, *Introduction to the Uniform Geometrical Theory of Diffraction*. Boston, MA, USA: Artech House, 1990.
- [15] R. F. Harrington, *Field Computation by Moment Methods*. New York, N.Y., USA: MacMillan, 1968.
- [16] E. A. Wolff, *Antenna Analysis*, ch. 2, pp. 22–23. Boston, MA, USA: Artech House, 1988.
- [17] R. C. Hansen, “Planar arrays,” in *The Handbook of Antenna Design* (A. W. Rudge, A. D. O. K. Milne, and P. Knight, eds.), vol. 1 and 2, ch. 10, London, UK: Peter Peregrinus Ltd., 2 ed., 1986.
- [18] D. R. Rhodes, *Synthesis of Planar Antenna Sources*. London, UK: Clarendon Press, 1974.
- [19] R. S. Elliott, “Array pattern synthesis - Part II: Planar arrays,” *IEEE Antennas Propagat. Soc. Newsletter*, pp. 5–10, April 1986.
- [20] IEEE Std 145-1983, “IEEE standard definitions of terms for antennas,” *IEEE Trans. Antennas and Propagat.*, vol. AP-31, pp. 5–29, June 1983.
- [21] D. K. Cheng, “Optimisation techniques for antenna arrays,” *Proc. IEEE*, vol. 59, pp. 1664–1674, Dec 1971.
- [22] D. A. McNamara, “Quadratic forms for the performance indices of symmetrical and anti-symmetrical linear arrays,” *Electron. Lett.*, vol. 23, pp. 148–149, Feb 1987.
- [23] M. J. Buckley, “Synthesis of shaped beam antenna patterns using implicitly constrained current elements,” *IEEE Trans. Antennas Propagat.*, vol. AP-44, pp. 192–197, Feb 1996.
- [24] O. M. Bucci, G. Mazzarella, and G. Panariello, “Array synthesis with smooth excitation,” in *IEEE AP-S Int. Symp. Digest*, vol. II, (Dallas, Texas, USA), pp. 856–859, May 1990.
- [25] R. C. Hansen, “Linear arrays,” in *The Handbook of Antenna Design* (A. W. Rudge, K. Milne, A. D. Olver, and P. Knight, eds.), vol. 1 and 2, ch. 9, London, UK: Peter Peregrinus Ltd., 2 ed., 1986.
- [26] S. A. Schelkunoff, “A mathematical theory of linear arrays,” *Bell Syst. Tech. J.*, vol. 22, pp. 80–107, 1943.

## REFERENCES

## REFERENCES

- [27] R. C. Hansen, "Measurement distance effects on low sidelobe patterns," *IEEE Trans. Antennas and Propagat.*, vol. AP-32, pp. 591–594, June 1984.
- [28] R. L. Pritchard, "Optimum directivity patterns for linear point arrays," *J. Acoust. Soc. Amer.*, vol. 25, pp. 879–891, Sept 1953.
- [29] Y. T. Lo, S. W. Lee, and Q. H. Lee, "Optimisation of directivity and signal-to-noise ratio of an arbitrary antenna array," *Proc. IEEE*, vol. 54, pp. 1033–1045, Aug 1966.
- [30] C. L. Dolph, "A current distribution for broadside arrays which optimises the relationship between beam width and side-lobe level," *Proc. IRE*, vol. 34, pp. 335–348, June 1946.
- [31] D. Barbiere, "A method of calculating the current distribution of Tschebyscheff arrays," *Proc. IRE*, vol. 40, pp. 78–82, Jan 1952.
- [32] R. J. Stegen, "Excitation coefficients and beamwidths of Tschebyscheff arrays," *Proc. IRE*, vol. 41, pp. 1671–1674, Nov 1953.
- [33] R. J. Stegen, "Gain of Tchebycheff arrays," *IRE Trans. Antennas Propagat.*, vol. AP-8, pp. 629–631, Nov 1960.
- [34] G. J. van der Maas, "A simplified calculation for Dolph-Tchebycheff arrays," *J. Appl. Phys.*, vol. 25, pp. 121–124, Jan 1954.
- [35] A. D. Bresler, "A new algorithm for calculating the current distributions of Dolph-Chebyshev arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-28, pp. 951–952, Nov 1980.
- [36] R. C. Hansen, "The theory of antenna arrays," in *Microwave Scanning Antennas* (R. C. Hansen, ed.), vol. I, ch. 1, Los Altos, CA, USA: Peninsula Publishing, 1985.
- [37] A. T. Villeneuve, "Taylor patterns for discrete arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-32, pp. 1089–1093, Oct 1984.
- [38] R. C. Hansen, "Aperture efficiency of Villeneuve- $\bar{n}$  arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-33, pp. 668–669, June 1985.
- [39] D. A. McNamara, "Generalised Villeneuve  $\bar{n}$ -distribution," *IEE Proc., Pt. H*, vol. 136, pp. 245–249, June 1989.
- [40] D. A. McNamara and E. Botha, "Generalised villeneuve distributions and various definitions of root-mean-square sidelobe levels," *Electron. Lett.*, vol. 29, pp. 989–990, May 1993.
- [41] O. R. Price and R. F. Hyneman, "Distribution function for monopulse antenna difference patterns," *IRE Trans. Antennas Propagat.*, vol. AP-8, pp. 567–576, Nov 1960.

## REFERENCES

## REFERENCES

- [42] D. A. McNamara, "Optimum monopulse linear array excitations using Zolotarev polynomials," *Electron. Lett.*, vol. 21, pp. 681–682, Aug 1985.
- [43] D. A. McNamara, "Tables of Zolotarev polynomial difference distributions for linear transducer arrays," *J. Acoust. Soc. Am.*, vol. 87, pp. 1336–1339, March 1990.
- [44] D. A. McNamara, "The direct synthesis of optimum difference patterns for discrete linear arrays using Zolotarev distributions," *IEE Proc., Pt. H*, vol. 140, pp. 495–500, Dec 1993.
- [45] D. A. McNamara, "Discrete  $\bar{n}$ -distribution for difference patterns," *Electron. Lett.*, vol. 22, pp. 303–304, March 1986.
- [46] D. A. McNamara, "The performance of Zolotarev and modified-Zolotarev difference pattern array distributions," *IEE Proc., Pt. H*, vol. 140, pp. 495–500, Dec 1993.
- [47] D. A. McNamara, "Excitation providing maximum directivity for difference arrays of discrete elements," *Electron. Lett.*, vol. 23, pp. 780–781, July 1987.
- [48] D. A. McNamara, "Maximisation of the normalised boresight slope of a difference arrays of discrete elements," *Electron. Lett.*, vol. 23, pp. 1158–1160, Oct 1987.
- [49] D. A. McNamara, "Synthesis of sum and difference patterns for two-section monopulse arrays," *IEE Proc., Pt. H*, vol. 135, pp. 371–374, Dec 1988.
- [50] P. M. Woodward, "Method of calculating the field over a plane aperture required to produce a given polar diagram," *J. IEE, Pt. IIIA*, vol. 93, pp. 1554–1558, 1947.
- [51] K. Milne, "Synthesis of power radiation pattern for linear array antennas," *IEE Proc., Pt. H*, vol. 134, pp. 285–296, June 1987.
- [52] R. S. Elliott, "Improved pattern synthesis for equispaced linear arrays," *Alta Frequenza*, vol. 51, pp. 296–300, Nov/Dec 1983.
- [53] R. S. Elliott and G. J. Stern, "A new technique for shaped beam synthesis of equispaced arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-32, pp. 1129–1133, Oct 1984.
- [54] H. J. Orchard, R. S. Elliott, and G. J. Stern, "Optimising the synthesis of shaped beam antenna patterns," *IEE Proc., Pt. H*, vol. 132, pp. 63–68, Feb 1985.
- [55] Y. U. Kim and R. S. Elliott, "Shaped-pattern synthesis using pure real distributions," *IEEE Trans. Antennas and Propagat.*, vol. AP-36, pp. 1645–1649, Nov 1988.
- [56] J. A. Rodriguez, E. Botha, and F. Ares, "Extension of the orchard-elliot synthesis method to pure-real nonsymmetrical-shaped patterns," *IEEE Trans. Antennas Propagat.*, vol. AP-45, pp. 1317–1318, Aug 1997.

## REFERENCES

## REFERENCES

- [57] F. Ares, A. Vieriro, E. Moreno, and S. R. Rengarajan, "Extension of orchard's pattern synthesis technique for overdetermined systems," *Electromagnetics*, vol. 17, pp. 15–23, Jan/Feb 1997.
- [58] C. J. Bouwkamp and N. G. de Bruyn, "The problem of optimum current distribution," *Philips Res. Rep.*, vol. 1, pp. 135–158, 1945–1946.
- [59] T. T. Taylor, "Design of line-source antennas for narrow beamwidth and low sidelobes," *IRE Trans. Antennas Propagat.*, vol. AP-3, pp. 16–28, Jan 1955.
- [60] R. S. Elliott, "Design of line source antennas for sum patterns with sidelobes of individually arbitrary heights," *IEEE Trans. Antennas Propagat.*, vol. AP-24, pp. 76–83, Jan 1976.
- [61] F. Ares, R. S. Elliott, and E. Moreno, "Optimised synthesis of shaped line-source antenna beams," *Electron. Lett.*, vol. 29, pp. 1136–1137, June 1993.
- [62] E. T. Bayliss, "Design of monopulse antennas for difference patterns with side lobes," *Bell Syst. Tech. J.*, vol. 47, pp. 623–640, 1968.
- [63] R. S. Elliott, "Design of line source antennas for difference patterns with side lobes of individually arbitrary heights," *IEEE Trans. Antennas Propagat.*, vol. AP-24, pp. 310–316, May 1976.
- [64] R. S. Elliott, "On discretizing continuous aperture distributions," *IEEE Trans. Antennas Propagat.*, vol. AP-25, pp. 617–621, Sept 1977.
- [65] S. W. Autrey, "Approximate synthesis of nonseparable design responses for rectangular arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-35, pp. 907–912, Aug 1987.
- [66] C. F. Winter, "Using continuous aperture illuminations discretely," *IEEE Trans. Antennas Propagat.*, vol. AP-25, pp. 695–700, Sept 1977.
- [67] C. F. Winter, "Further discrete optimizations for continuous aperture illumination," *IEEE Trans. Antennas Propagat.*, vol. AP-28, pp. 125–128, Jan 1980.
- [68] W. V. T. Rusch, "The current state of the reflector antenna art," *IEEE Trans. Antennas Propagat.*, vol. AP-32, pp. 313–329, March 1984.
- [69] P. D. Patel and K. K. Chan, "Optimisation of contoured beams for satellite antennas," *IEE Proc., Pt. H*, vol. 132, pp. 400–406, Oct 1985.
- [70] A. R. Cherrette, S. W. Lee, and R. J. Acosta, "A method for producing a shaped contour radiation pattern using a single shaped reflector and a single feed," *IEEE Trans. Antennas Propagat.*, vol. AP-37, pp. 698–706, June 1989.

## REFERENCES

## REFERENCES

- [71] W. Bornemann, P. Balling, and W. J. English, "Synthesis of spacecraft array antennas for Intelsat frequency reuse multiple contoured beams," *IEEE Trans. Antennas Propagat.*, vol. AP-33, pp. 1186–1193, Nov 1985.
- [72] G. Mazzarella and G. Panariello, "A projection-based synthesis of non-uniform arrays," in *IEEE AP-S Int. Symp. Digest*, vol. 2, (London, Ontario, Canada), pp. 1164–1167, June 1991.
- [73] A. R. Cherette and D. C. D. Chang, "Phased array contour beam shaping by phase optimisation," in *IEEE AP-S Int. Symp. Digest*, vol. II, (Vancouver, Canada), pp. 475–478, June 1985.
- [74] J. E. Richie and H. N. Kritikos, "Linear program synthesis for direct broadcast satellite phased arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-36, pp. 345–348, March 1988.
- [75] P. Balling, W. Bornemann, and H. H. Viskum, "Reconfigurable contoured beam antenna using fixed sub-beam forming networks," in *IEEE AP-S Int. Symp. Digest*, vol. II, (Syracuse, NY, USA), pp. 510–513, June 1988.
- [76] C. Mangenot, T. Judasz, and P. F. Combes, "Power synthesis of shaped beam antenna patterns," in *IEEE AP-S Int. Symp. Digest*, vol. II, (San Jose, CA, USA), pp. 420–423, June 1989.
- [77] J. E. Richie and H. N. Kritikos, "Preliminary shaped beam synthesis using product function," *IEEE Trans. Antennas Propagat.*, vol. AP-38, pp. 1504–1507, Sept 1990.
- [78] R. S. Elliott and G. J. Stern, "Footprint patterns obtained by planar arrays," *IEE Proc., Pt. H*, vol. 137, pp. 108–112, April 1990.
- [79] R. S. Elliott and G. J. Stern, "Shaped patterns from a continuous planar aperture distribution," *IEE Proc., Pt. H*, vol. 135, pp. 366–370, Dec 1988.
- [80] F. Ares, R. S. Elliott, and E. Moreno, "Design of planar arrays to obtain efficient footprint patterns with an arbitrary footprint boundary," *IEEE Trans. Antennas Propagat.*, vol. AP-42, pp. 1509–1514, Nov 1994.
- [81] F. I. Tseng and D. K. Cheng, "Optimum scannable planar arrays with an invariant side lobe level," *Proc. IEEE*, vol. 56, pp. 1771–1778, Nov 1968.
- [82] Y. V. Baklanov, "Chebyshev distribution of current for a planar array of radiators," *Radio Eng. Electron. Phys. (USSR)*, vol. 11, pp. 640–642, 1966.
- [83] N. Goto, "Nonseparable pattern of planar arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-20, pp. 104–106, Jan 1972.
- [84] N. Goto, "Pattern synthesis of hexagonal planar arrays," *IEEE Trans. Antennas and Propagat.*, vol. AP-20, pp. 479–481, July 1972.

## REFERENCES

## REFERENCES

- [85] Y. U. Kim and R. S. Elliott, "Extensions of the Tseng-Cheng pattern synthesis technique," *J. Electromagn. Waves Applic.*, vol. 2, pp. 255–268, March/April 1988.
- [86] Y. U. Kim, "A transformation technique to produce almost rotationally symmetrical hexagonal array patterns," *J. Electromagn. Waves Applic.*, vol. 4, pp. 359–369, April 1990.
- [87] S. R. Laxpati, "Synthesis of planar arrays based on convolution technique," *Electron. Lett.*, vol. 16, pp. 918–919, Nov 1980.
- [88] S. R. Laxpati and J. P. Shelton, "Theory of null synthesis of planar arrays," in *IEEE AP-S Int. Symp. Digest*, vol. I, (Los Angeles, CA, USA), pp. 40–43, June 1981.
- [89] J. P. Shelton and S. R. Laxpati, "Applications of null synthesis to hexagonal arrays," in *IEEE AP-S Int. Symp. Digest*, vol. I, (Los Angeles, CA, USA), pp. 44–47, June 1981.
- [90] S. R. Laxpati, "Planar array synthesis with prescribed pattern nulls," *IEEE Trans. Antennas Propagat.*, vol. AP-30, pp. 1176–1183, Nov 1982.
- [91] J. P. Shelton and S. R. Laxpati, "Synthesis of hexagonal and square arrays using discrete convolution," *Radio Science*, vol. 19, pp. 1229–1237, Sept/Oct 1984.
- [92] R. M. Mersereau, W. F. G. Mecklenbrauker, and T. F. Quatieri, "McClellan transformations for two-dimensional digital filtering : I - design," *IEEE Trans. Circuits Syst.*, vol. CAS-23, pp. 405–414, July 1976.
- [93] D. A. McNamara and E. Botha, "Transformation-based synthesis technique for planar arrays with contoured beams," *Electron. Lett.*, vol. 27, pp. 1502–1504, Aug. 1991.
- [94] E. Botha and D. A. McNamara, "A contoured beam synthesis technique for planar arrays with quadrantal and centro-symmetry," *IEEE Trans. Antennas Propagat.*, vol. AP-41, pp. 1222–1231, Sept. 1993.
- [95] E. Botha, "Improved synthesis techniques for uniformly-spaced planar arrays," MEng., University of Pretoria, Pretoria, RSA, March 1991.
- [96] T. T. Taylor, "Design of circular apertures for narrow beamwidth and low sidelobes," *IRE Trans. Antennas Propagat.*, vol. AP-8, pp. 17–22, Jan 1960.
- [97] R. C. Hansen, "Circular aperture distribution with one parameter," *Electron. Lett.*, vol. 11, p. 184, April 1975.
- [98] R. C. Hansen, "A one-parameter circular aperture distribution with narrow beamwidth and low sidelobes," *IEEE Trans. Antennas Propagat.*, vol. AP-24, pp. 477–480, July 1976.

## REFERENCES

## REFERENCES

- [99] R. S. Elliott, "Design of circular apertures for narrow beamwidth and asymmetric side lobes," *IEEE Trans. Antennas Propagat.*, vol. AP-23, pp. 523–527, July 1975.
- [100] W. D. White, "Circular aperture distribution functions," *IEEE Trans. Antennas Propagat.*, vol. AP-25, pp. 714–716, Sept 1977.
- [101] O. Graham, R. M. Johnson, and R. S. Elliott, "Design of circular apertures for sum patterns with ring side lobes of individually arbitrary heights," *Alta Frequenza*, vol. 47, pp. 21–25, 1978.
- [102] R. F. E. Guy, "General radiation-pattern synthesis technique for array antennas of arbitrary configuration and element type," *IEE Proc. , Pt. H.*, vol. 135, pp. 241–248, Aug 1988.
- [103] A. Ksieinski, "Equivalence between continuous and discrete radiating arrays," *Can. J. of Phys.*, vol. 39, pp. 335–349, 1961.
- [104] W. L. Stutzman and E. L. Coffey, "Radiation pattern synthesis of planar antennas using the iterative soampling method," *IEEE Trans. Antennas Propagat.*, vol. AP-23, pp. 764–769, Nov 1975.
- [105] A. Levi and H. Stark, "Image restoration by the method of generalised projections with application to restoration from magnitude," *J. Opt. Soc. Am., Pt. A.*, vol. 1, pp. 932–943, Sept 1984.
- [106] S. Prasad, "Generalized array pattern synthesis by the method of alternating orthogonal projections," *IEEE Trans. Antennas Propagat.*, vol. AP-28, pp. 328–332, May 1980.
- [107] G. T. Poulton, "Power pattern synthesis using the method of successive projections," in *IEEE AP-S Int. Symp. Digest*, vol. 2, (Philadelphia, PA, USA), pp. 667–670, June 1986.
- [108] G. T. Poulton, "Antenna power pattern synthesis using the method of successive projections," *Electron. Lett.*, vol. 22, pp. 1042–1043, Sept 1986.
- [109] O. M. Bucci, G. Franceschetti, G. Mazzarella, and G. Panariello, "A general projection approach to array synthesis," in *IEEE AP-S Int. Symp. Digest*, vol. I, (San Jose, CA, USA), pp. 146–149, June 1989.
- [110] O. M. Bucci, G. Franceschetti, G. Mazzarella, and G. Panariello, "Intersection approach to array pattern synthesis," *IEE Proc., Pt. H*, vol. 137, pp. 349–357, Dec 1990.
- [111] O. M. Bucci, G. D'Elia, G. Mazzarella, and G. Panariello, "Antenna pattern synthesis: a new general approach," *Proc. IEEE*, vol. 82, pp. 358–371, March 1994.

## REFERENCES

## REFERENCES

- [112] G. Mazzarella and G. Panariello, "Pattern synthesis of conformal arrays," in *IEEE AP-S Int. Symp. Digest*, vol. 2, (Ann Arbor, DT, USA), pp. 1054–1057, June/July 1993.
- [113] O. M. Bucci, G. D'Elia, and G. Romito, "Power synthesis of conformal arrays by a generalised projection method," *IEE Proc., Pt. H*, vol. 142, pp. 467–471, Dec 1995.
- [114] D. S. Luenberger, *Linear and nonlinear programming*. Addison-Wesley, 1984.
- [115] S. M. Sanzgiri and J. K. Butler, "Constrained optimization of the performance indices of arbitrary array antennas," *IEEE Trans. Antenna Propagat.*, vol. AP-19, pp. 493–498, July 1971.
- [116] G. L. Wilson, "Computer optimization of transducer array patterns," *J. Acoust. Soc. Am.*, vol. 59, pp. 195–203, Jan 1976.
- [117] O. Einarsson, "Optimisation of planar arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-27, pp. 86–92, Jan 1979.
- [118] J. F. DeFord and O. P. Gandhi, "Phase-only synthesis of minimum peak sidelobe patterns for linear and planar arrays," *IEEE Trans. Antennas Propagat.*, vol. AP-36, pp. 191–201, Feb 1988.
- [119] N. H. Farhat and B. Bai, "Phased-array antenna pattern synthesis by simulated annealing," *Proc. IEEE*, vol. 75, pp. 842–844, June 1987.
- [120] F. Ares, S. R. Rengarajan, J. A. F. Lence, A. Trastoy, and E. Moreno, "Synthesis of antenna patterns of circular arc arrays," *Electron. Lett.*, vol. 32, pp. 1845–1846, 26 Sept 1996.
- [121] J. A. Ferreira and F. Ares, "Pattern synthesis of conformal arrays by the simulated annealing technique," *Electron. Lett.*, vol. 33, pp. 1187–1189, 3 July 1997.
- [122] J. H. McClellan, "The design of two-dimensional digital filters by transformations," in *Proc. 7th Annual Princeton Conf. Information Sciences and Systems*, pp. 247–251, 1973.
- [123] M. R. Spiegel, *Mathematical Handbook of Formulas and Tables*. New York, N.Y., USA: McGraw-Hill, 1968.
- [124] D. T. Nguyen and M. N. S. Swamy, "Formulas for parameter scaling in the McClellan transform," *IEEE Trans. Circuits Syst.*, vol. CAS-33, pp. 108–109, Jan 1986.
- [125] Y. Kamp and J. P. Thiran, "Chebyshev approximation for two-dimensional non-recursive digital filters," *IEEE Trans. Circuits Syst.*, vol. CAS-22, pp. 208–218, March 1975.

## REFERENCES

## REFERENCES

- [126] R. M. Mersereau, D. B. Harris, and H. S. Hersey, "An efficient algorithm for the design of equiripple two-dimensional FIR digital filters," in *Proc. IEEE Int. Symp. on Circuits and Systems*, pp. 405–414, April 1975.
- [127] R. S. Elliott, "Synthesis of rectangular planar arrays for sum patterns with ring side lobes of arbitrary topography," *Radio Sci.*, vol. 12, pp. 653–657, 1977.
- [128] E. Botha and D. A. McNamara, "Direct synthesis of near-optimum difference patterns for planar arrays," *Electron. Lett.*, vol. 28, pp. 753–754, April 1992.
- [129] W. H. Kummer, "Basic array theory," *Proc. IEEE*, vol. 80, pp. 127–139, Jan 1992.
- [130] R. W. Gerchberg and W. O. Saxton, "A practical algorithm for the determination of phase from image and diffraction plane pictures," *Optik*, vol. 35, pp. 237–246, 1972.
- [131] D. C. Youla, "Generalized image restoration by the method of alternating orthogonal projections," *IEEE Trans. Circuits Syst.*, vol. CAS-25, pp. 694–702, Sept 1978.
- [132] T. S. Ng, "Generalised array pattern synthesis using the projection matrix," *IEE Proc., Pt. H*, vol. 132, pp. 44–46, Feb 1985.
- [133] T. S. Ng, "Array pattern synthesis by the method of alternating orthogonal projections: the general case," *IEE Proc., Pt. H*, vol. 132, pp. 451–454, Dec 1985.
- [134] D. C. Youla and H. Webb, "Image restoration by the method of projections onto convex sets. part i," *IEEE Trans. Med. Imaging.*, vol. TMI-1, pp. 81–94, 1982.
- [135] H. Elmikati and A. A. Elsohly, "Extensio of projection method to nonuniformly linear antenna arrays," *IEEE Trans. Circuits Syst.*, vol. CAS-31, pp. 801–805, Sept 1984.
- [136] A. Abo-Taleb and M. M. Fahmy, "Design of FIR two-dimensional digital filters by successive projections," *IEEE Trans. Circuits Syst.*, vol. CAS-31, pp. 801–805, Sept 1984.
- [137] G. Franceschetti, G. Mazzarella, and G. Panariello, "Array synthesis with excitation constraints," *IEE Proc., Pt. H*, vol. 135, pp. 400–407, Dec 1988.
- [138] O. M. Bucci, G. D'Elia, G. Mazzarella, and G. Panariello, "Antenna pattern synthesis: a new general approach," *Proc. IEEE*, vol. 82, pp. 358–371, March 1994.
- [139] O. M. Bucci, G. Mazzarella, and G. Panariello, "Reconfigurable array by phase-only control," in *IEEE AP-S Int. Symp. Digest*, vol. I, (San Jose, CA, USA), pp. 142–145, June 1989.
- [140] O. M. Bucci, G. Mazzarella, and G. Panariello, "Reconfigurable arrays by phase-only control," *IEEE Trans. Antennas Propagat.*, vol. AP-39, pp. 919–925, July 1991.

## REFERENCES

## REFERENCES

- [141] B. D. Carlson and D. Willner, "Antenna pattern synthesis using weighted least squares," *IEE Proc., Pt. H*, vol. 139, pp. 11–16, Feb 1992.
- [142] L. I. Vaskelainen, "Iterative least-squares synthesis methods for conformal arrays antennas with optimized polarization and frequency properties," *IEEE Trans. Antennas Propagat.*, vol. AP-45, pp. 1179–1185, July 1997.
- [143] R. Vescovo, "Array factor synthesis for circular antenna arrays," in *IEEE AP-S Int. Symp. Digest*, vol. 3, (Ann Arbor, DT, USA), pp. 1574–1577, June/July 1993.
- [144] R. Vescovo, "Pattern synthesis with null constraints for circular arrays of equally spaced isotropic elements," *IEEE Trans. Antennas Propagat.*, vol. AP-43, pp. 1405–1410, Dec 1995.
- [145] M. J. Rossouw, J. Joubert, and D. A. McNamara, "Thinned arrays using a modified minimum redundancy synthesis technique," *Electron. Lett.*, vol. 33, pp. 826–827, 8 May 1997.
- [146] E. Botha and D. A. McNamara, "Conformal array synthesis using alternating projections, with maximum likelihood estimation used in one of the projection operators," *Electron. Lett.*, vol. 29, pp. 1733–1734, Sept. 1993.

The thinnest arrays can be obtained by the odd case (an odd number of elements along each principal plane) will be discussed in Section A.1 and even case (an even number of elements along each principal plane) in Section A.2. The derivation of the formulas, as well as "ready to implement" algorithms for  $\alpha_{pq}$  and  $\psi_{pq}$  for both cases are supplied. Although it may be possible to write these in what may be considered a more mathematically elegant fashion, such recursive relations are ideally suited to computation.

## A.1 Formulas and Algorithms : The Odd Case

### A.1.1 Computation of $b_p$ and $a_q$

The prototype linear array factor, a summation of cosines weighted by the relative excitations  $a_p$ , can be expressed in a polynomial form, with  $b_p$  the coefficients and  $\cos(\phi_p)$  the variable of the polynomial.

The prototype linear array is a  $2Q+1$  element, uniformly spaced linear array with symmetrical excitation and with inter-element spacing  $a$ . The prototype linear array factor can be in the usual form (3.4) or in a polynomial form (3.6)

$$F_p(t_p) = \sum_{q=0}^{2Q} b_p q! \cos(q\phi_p) = \sum_{q=0}^{2Q} b_p \cos^q \phi_p \quad (A.3)$$