# AN INTEGRATED AND INTELLIGENT METAHEURISTIC FOR CONSTRAINED VEHICLE ROUTING

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#### Summary

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South African metropolitan areas are experiencing rapid growth and requires an increase in network infrastructure. Increased congestion negatively impacts both public and freight transport costs. The concept of *City Logistics* is concerned with the mobility of cities, and entails the process of optimizing urban logistics activities by concerning the social, environmental, economic, financial, and energy impacts of urban freight movement. In a cost-competitive environment, freight transporters often use sophisticated vehicle routing and scheduling applications to improve fleet utilization and reduce the cost of meeting customer demands.

In this thesis, the candidate builds on the observation that vehicle routing and scheduling algorithms are inherent problem specific, with no single algorithm providing a dominant solution to all problem environments. Commercial applications mostly deploy a single algorithm in a multitude of environments which would often be better serviced by various different algorithms.

This thesis algorithmically implements the ability of human decision makers to choose an appropriate solution algorithm when solving scheduling problems. The intent of the routing agent is to classify the problem as representative of a traditional problem set, based on its characteristics, and then to solve the problem with the most appropriate solution algorithm known for the traditional problem set. A not-so-artificially-intelligent-vehicle-routing-agent<sup>TM</sup> is proposed and developed in this thesis. To be considered intelligent, an agent is firstly required to be able to recognize its environment. Fuzzy c-means clustering is employed to analyze the geographic dispersion of the customers (nodes) from an unknown routing problem to determine to which traditional problem set it relates best. Cluster validation is used to classify the routing problem into a traditional problem set.

Once the routing environment is classified, the agent selects an appropriate metaheuristic to solve the complex variant of the Vehicle Routing Problem. Multiple soft time windows, a University of Pretoria etd - Joubert, J W (2007)

heterogeneous fleet, and multiple scheduling are addressed in the presence of time-dependent travel times. A new initial solution heuristic is proposed that exploits the inherent configuration of customer service times through a concept referred to as time window compatibility. A high-quality initial solution is subsequently improved by the Tabu Search metaheuristic through both an adaptive memory, and a self-selection structure.

As an alternative to Tabu Search, a Genetic Algorithm is developed in this thesis. Two new crossover mechanisms are proposed that outperform a number of existing crossover mechanisms. The first proposed mechanism successfully uses the concept of time window compatibility, while the second builds on an idea used from a different sweeping-arc heuristic.

A neural network is employed to assist the intelligent routing agent to choose, based on its knowledge base, between the two metaheuristic algorithms available to solve the unknown problem at hand. The routing agent then not only solves the complex variant of the problem, but adapts to the problem environment by evaluating its decisions, and updating, or reaffirming its knowledge base to ensure improved decisions are made in future.

Keywords: Vehicle routing; fuzzy clustering, time-dependent travel time; metaheuristics

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### Acronyms

**ACO** Ant Colony Optimization

ACS Adapted Combined Savings

AI Artificial Intelligence

**AMD** Absolute Mean Deviation

**AMP** Adaptive Memory Procedure

**ANN** Artificial Neural Network

**ANNs** Artificial Neural Networks

**AOOS** Adapted Optimistic Opportunity Savings

**AROS** Adapted Realistic Opportunity Savings

CMTSP Capacitated Multiple Traveling Salesman Problem

**CS** Combined Savings

**CVRP** Capacitated Vehicle Routing Problem

**CW** Clarke-Wright

**DP** Dynamic Programming

**EER** Enhanced Edge Recombination

**ER** Edge Recombination

**FIFO** First-In-First-Out

**FSMVRP** Fleet Size and Mix Vehicle Routing Problem

FSMVRPTW Fleet Size and Mix Vehicle Routing Problem with Time Windows

**GA** Genetic Algorithm

GIS Geographical Information System

**HVRP** Heterogeneous Fleet Vehicle Routing Problem

**ILP** Integer Linear Program

ITS Intelligent Transportation System

**LP** Linear Programming Problem

MPVRP Multi Period Vehicle Routing Problem

MSE Mean Square Error

MTMCP Multiple Tour Maximum Collection Problem

MTSP Multiple Traveling Salesman Problem

MTVRP Multi-Trip Vehicle Routing Problem

MVRPSP Multi-Vehicle Routing Problem with Split Pick-ups

MX Merged Crossover

OOS Optimistic Opportunity Savings

**PFIH** Push Forward Insertion Heuristic

PMX Partially Matched Crossover

**ROS** Realistic Opportunity Savings

**SA** Simulated Annealing

**SEC** Subtour Elimination Constraints

**SIH** Sequential Insertion Heuristic

**TDTSP** Time Dependent Traveling Salesman Problem

**TDVRP** Time Dependent Vehicle Routing Problem

**TP** Thesis Problem

TS Tabu Search

TSP Traveling Salesman Problem

**TWC** Time Window Compatibility

**TWCM** Time Window Compatibility Matrix

**VFM** Vehicle Fleet Mix problem

VRP Vehicle Routing Problem

**VRPHE** Vehicle Routing Problem with a Heterogeneous fleet of vehicles

**VRPM** Vehicle Routing Problem with Multiple use of vehicles

**VRPMVTTW** Vehicle Routing Problem with Multiple Vehicle Types and Time Windows

**VRPPD** Vehicle Routing Problem with Pickups and Deliveries

**VRPTW** Vehicle Routing Problem with Time Windows