

## REFERENCES

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APPENDIX **A**

# UNIQUE COMBINATION SEQUENCE RESULTS

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Unique combinations of the real and imaginary parts of the complex spreading sequences are used as defined by

$$C_{r_1comb} = C_{r_1} - C_{i_1} \quad (\text{A.1})$$

$$C_{i_1comb} = -C_{r_1} - C_{i_1} \quad (\text{A.2})$$

and is shown in Figure A.1. The real and imaginary parts of the root-of-unity filtered complex spreading sequence 1 and 6 of length,  $L = 121$ , and samples per chip,  $spc = 8$ , are depicted in Figures A.1 and A.4, while the real vs. imaginary parts of sequence 1 and 6 are shown in Figures A.2 and A.5, respectively. The power spectral densities (PSD) for sequence 1 and sequence 6 are shown in Figures A.3 and A.6, respectively.

The same for complex spreading sequence 6

$$C_{r_6comb} = C_{r_6} - C_{i_6} \quad (\text{A.3})$$

$$C_{i_6comb} = -C_{r_6} - C_{i_6} \quad (\text{A.4})$$

and is depicted in Figure A.4.

## A.1 AUTOCORRELATION FUNCTION

The sequence  $\{s_k\}$  of length  $L$  has periodic AC function,  $R_{ss}[l]$ , given as:

$$R_{ss}[l] = \sum_{k=0}^{L-1} s[k] \cdot s^*[k+l]_{mod L} \quad (\text{A.5})$$

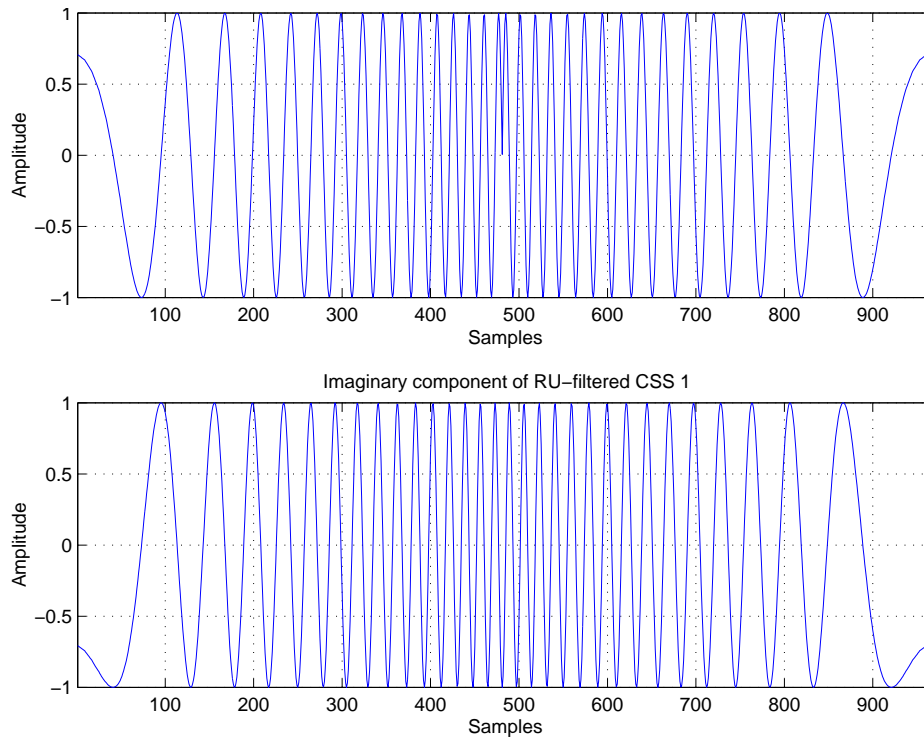


FIGURE A.1: The Real, (a), and Imaginary, (b), part of the unique combination of CSS 1. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

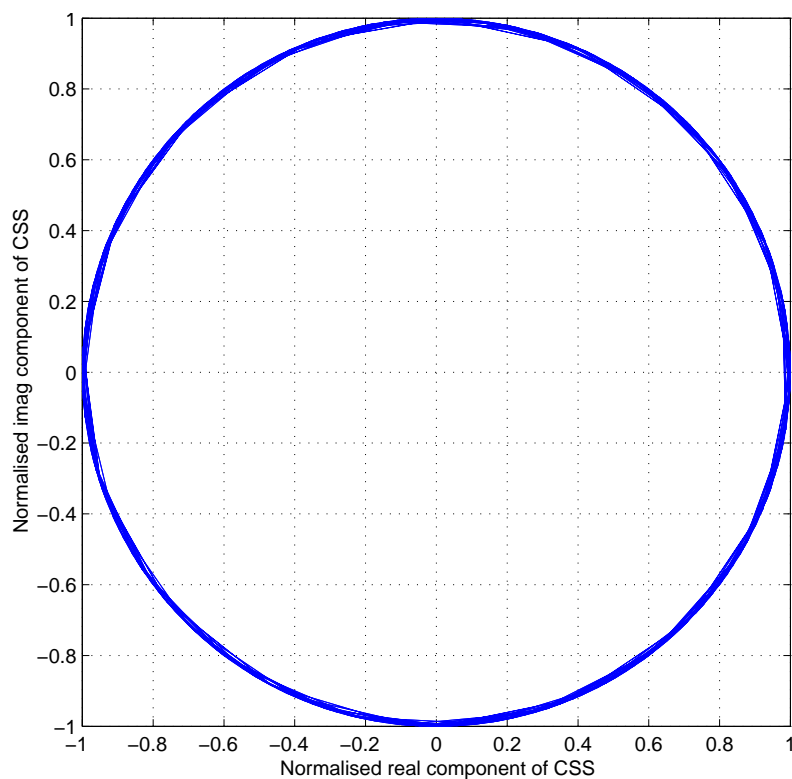


FIGURE A.2: Real vs. Imaginary part of unique combination of complex spreading sequence 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

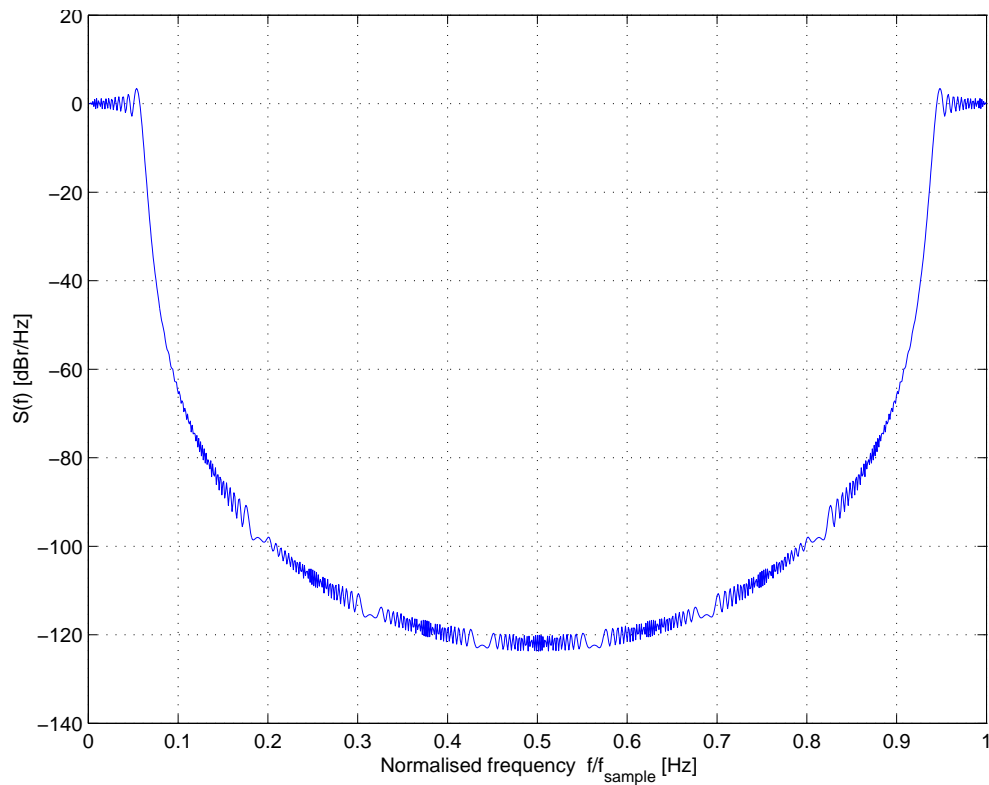


FIGURE A.3: Power spectral density (PSD) of unique combination of complex spreading sequence 1. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

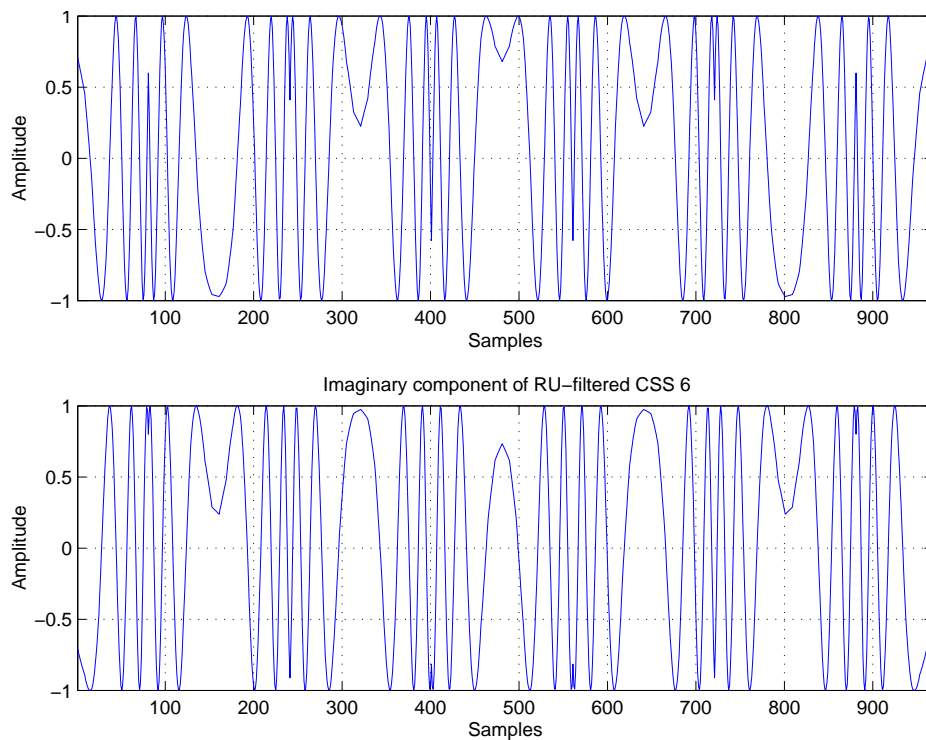


FIGURE A.4: The Real, (a), and Imaginary, (b), part of unique combination of CSS 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

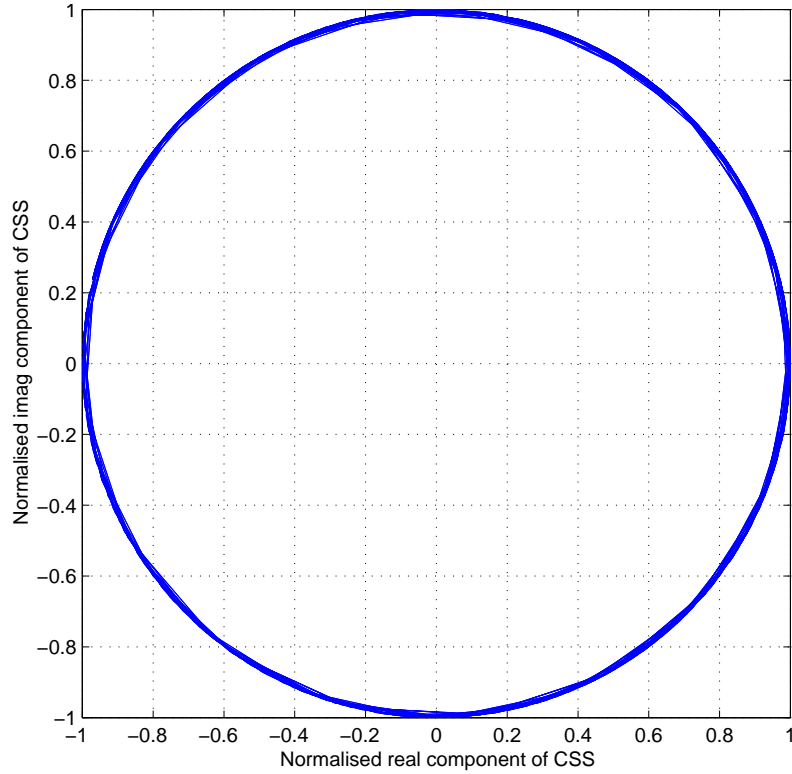


FIGURE A.5: Real vs. Imaginary part of unique combination of complex spreading sequence 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

where \* denotes the complex conjugate, the index  $[k + l]$  is computed modulo  $L$ , and the time shift is  $l$ .

Thus for the ZC sequences, the periodic AC function is:

$$R_{ss}[l] = \sum_{k=0}^{L-1} W_L^{\frac{k(k+1)}{2}} \cdot W_L^{\frac{-(k+l)_{\text{mod } L}((k+l)_{\text{mod } L}+1)}{2}} \quad (\text{A.6})$$

for  $q = 0$  and  $L$  odd.

The periodic AC functions for the ZC sequences 1 and 6, for a length of 121, can be seen in Figures A.7, A.8 and Figures A.9, A.10, respectively.

For a sequence  $s_k$  of length  $L$  the aperiodic AC function is defined as:

$$R_{ss}[l] = \int_{-\infty}^{\infty} s[l] \cdot s^*[t + l] dl \quad (\text{A.7})$$

where \* denotes the complex conjugate and the time shift is  $l$ .

In discrete time notation the aperiodic AC function can be expressed as:



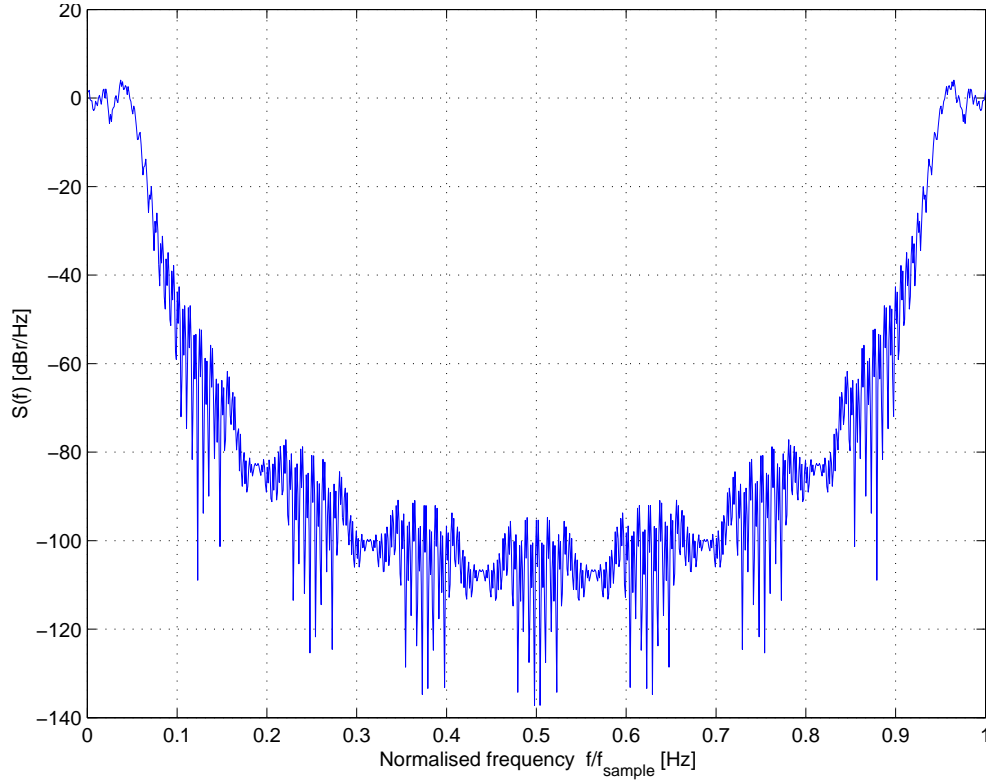


FIGURE A.6: Power spectral density (PSD) of unique combination of complex spreading sequence 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

$$R_{ss}[l] = \begin{cases} \sum_{k=0}^{L-1-l} s[l] \cdot s^*[k+l] & ; 0 \leq l \leq L-1 \\ \sum_{k=0}^{L-1+l} s[k-l] \cdot s^*[k] & ; 1-L \leq l < 0 \\ 0 & ; |l| \geq L \end{cases} \quad (\text{A.8})$$

For ZC sequences the aperiodic AC function is:

$$R_{aa}[l] = \begin{cases} \sum_{k=0}^{L-1-l} W_L^{\frac{k(k+1)}{2}} \cdot W_L^{\frac{-(k+1)(k+l+1)}{2}} & ; 0 \leq l \leq L-1 \\ \sum_{k=0}^{L-1+l} W_L^{\frac{(k-l)(k-l+1)}{2}} \cdot W_L^{\frac{-k(k+l)}{2}} & ; 1-L \leq l < 0 \\ 0 & ; |l| \geq L \end{cases} \quad (\text{A.9})$$

for  $q = 0$  and  $L$  odd.

The aperiodic AC functions for the ZC sequences 1 and 6, for a length of 121, can be seen in Figures A.11, A.12 and Figures A.13, A.14, respectively.

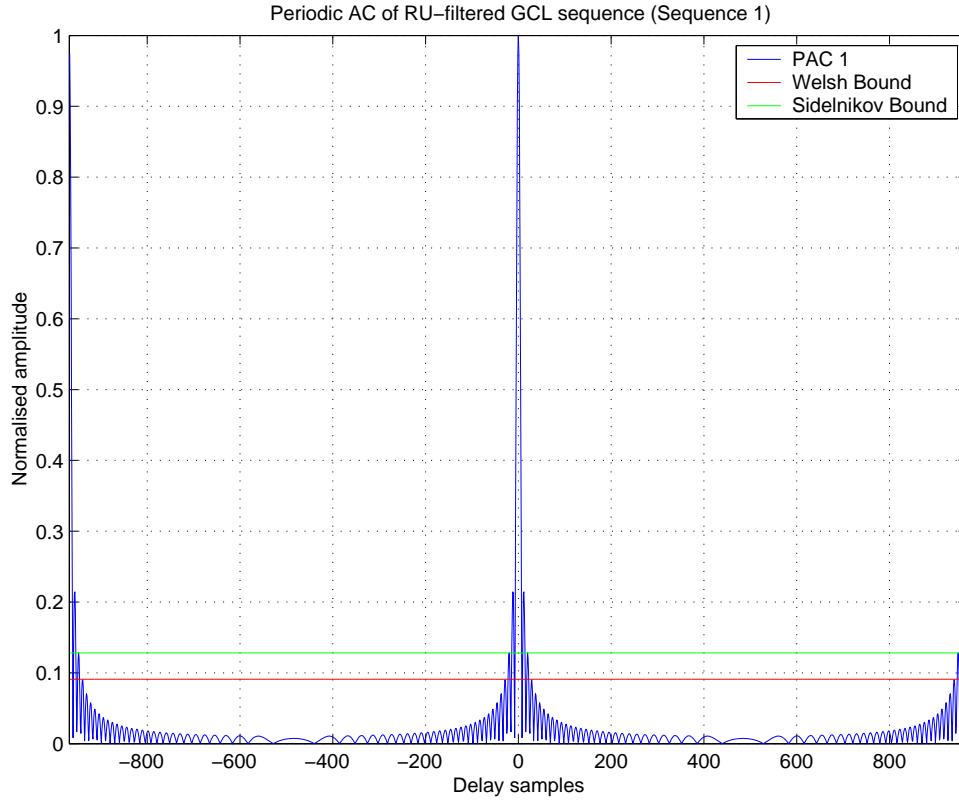


FIGURE A.7: Periodic Auto Correlation (PAC) function of unique combination of complex spreading sequence 1. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

## A.2 CROSSCORRELATION FUNCTION

The CC function shows the correspondence between two signals at different time shifts. The periodic CC function between any two sequences  $s_k$  and  $u_k$ , both of length  $L$ , is defined as:

$$R_{su}[l] = \sum_{k=0}^{L-1} s[k] \cdot u^*[(k+l)_{\text{mod}L}] \quad (\text{A.10})$$

where  $*$  denotes the complex conjugate, the index  $(k+l)$  is computed modulo  $L$ , and the time shift is  $l$ .

Thus for the ZC sequence the periodic CC function is:

$$R_{ab}[l] = \sum_{k=0}^{L-1} W_{L_a}^{\frac{k(k+1)}{2}} \cdot W_{L_a}^{\frac{-(k+l)_{\text{mod}L}((k+l)_{\text{mod}L}+1)}{2}} \quad (\text{A.11})$$

for  $q = 0$  and  $L$  odd.

The periodic cross correlation functions between spreading code number 1 and 6 are shown in Figures A.15 and A.16.

The aperiodic CC function between any two sequences  $s_k$  and  $u_k$ , both of length  $L$ , in discrete time notation is defined as:

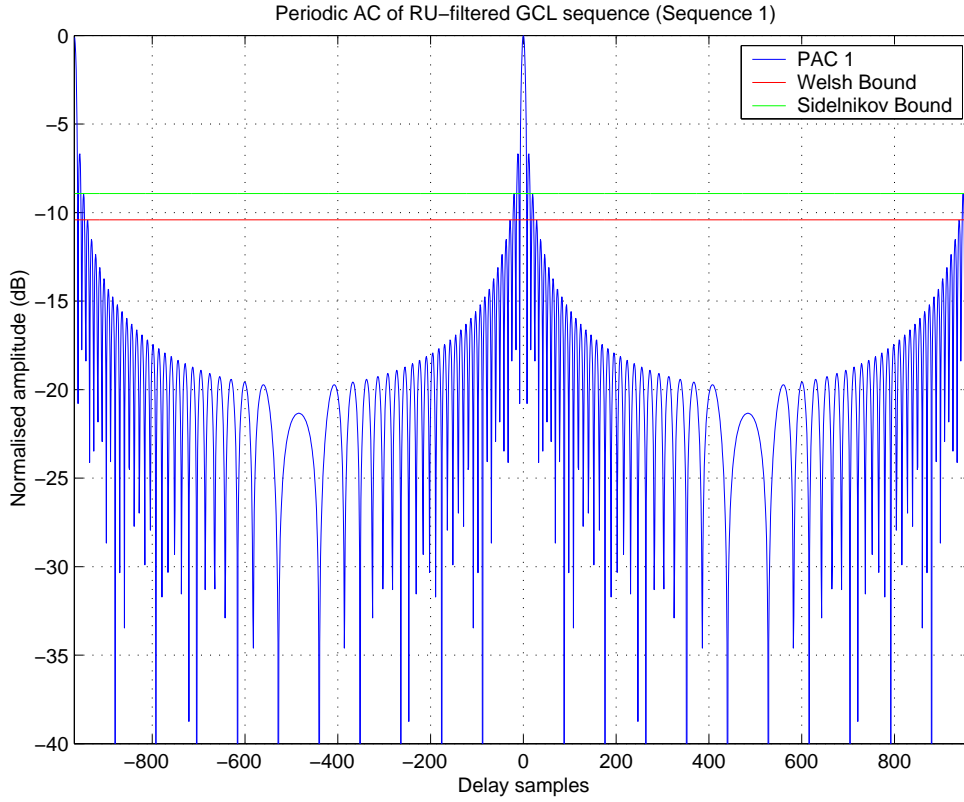


FIGURE A.8: Periodic Auto Correlation (PAC) function of unique combination of complex spreading sequence 1 in decibels. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

$$R_{su}[l] = \begin{cases} \sum_{k=0}^{L-1-l} s[l] \cdot u^*[k+l] & ; 0 \leq l \leq L-1 \\ \sum_{k=0}^{L-1+l} s[k-l] \cdot u^*[k] & ; 1-L \leq l < 0 \\ 0 & ; |l| \geq L \end{cases} \quad (\text{A.12})$$

where \* denotes complex conjugate and the time shift is  $l$ .

For the ZC sequences the aperiodic CC function is

$$R_{ab}[l] = \begin{cases} \sum_{k=0}^{L-1-l} W_{L_a}^{\frac{k(k+1)}{2}} \cdot W_{L_b}^{\frac{-(k+1)(k+l+1)}{2}} & ; 0 \leq l \leq L-1 \\ \sum_{k=0}^{L-1+l} W_{L_a}^{\frac{(k-l)(k-l+1)}{2}} \cdot W_{L_b}^{\frac{-k(k+l)}{2}} & ; 1-L \leq l < 0 \\ 0 & ; |l| \geq L \end{cases} \quad (\text{A.13})$$

The aperiodic cross correlation functions for the ZC sequences are depicted in Figures A.17 and A.18.

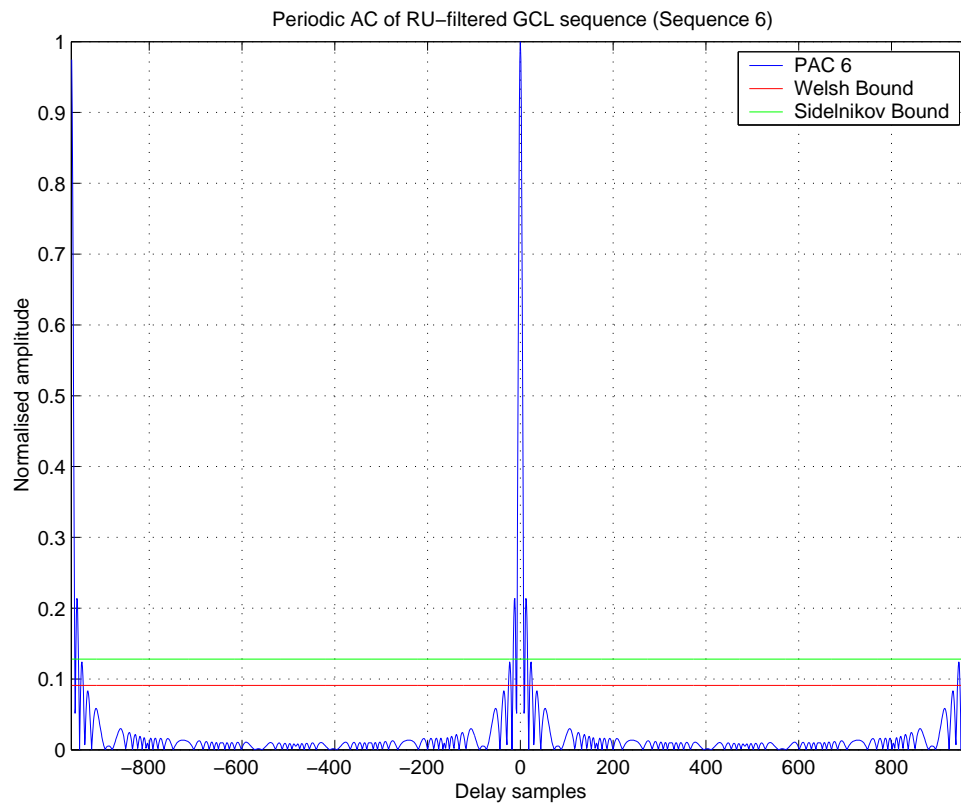


FIGURE A.9: Periodic Auto Correlation (PAC) function of unique combination of complex spreading sequence 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

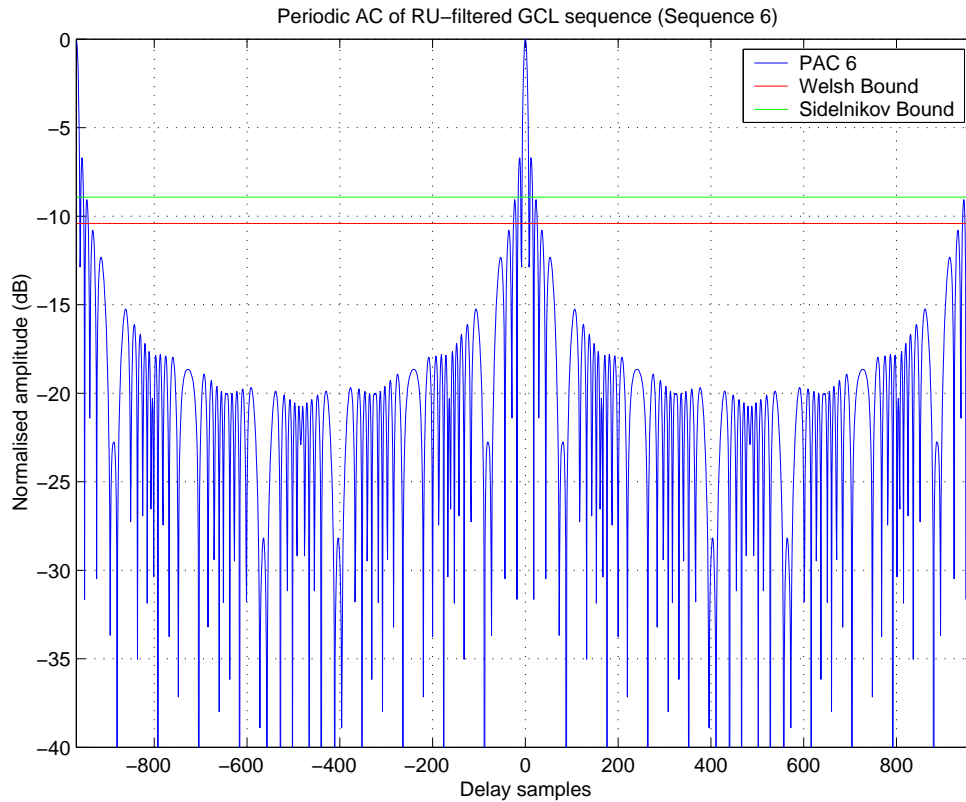


FIGURE A.10: Periodic Auto Correlation (PAC) function of unique combination of complex spreading sequence 6 in decibels. ( $L = 121$ , *RU filtered*,  $spc = 8$ )

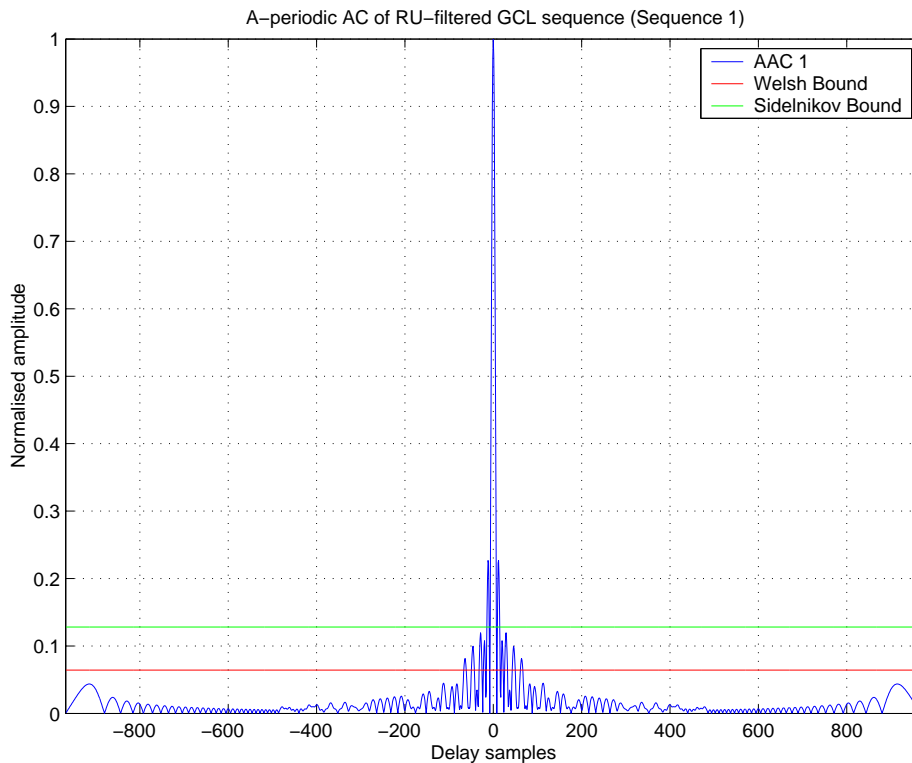


FIGURE A.11: Aperiodic Auto Correlation (AAC) function of unique combination of complex spreading sequence 1. ( $L = 121$ , *RU filtered*,  $spc = 8$ )

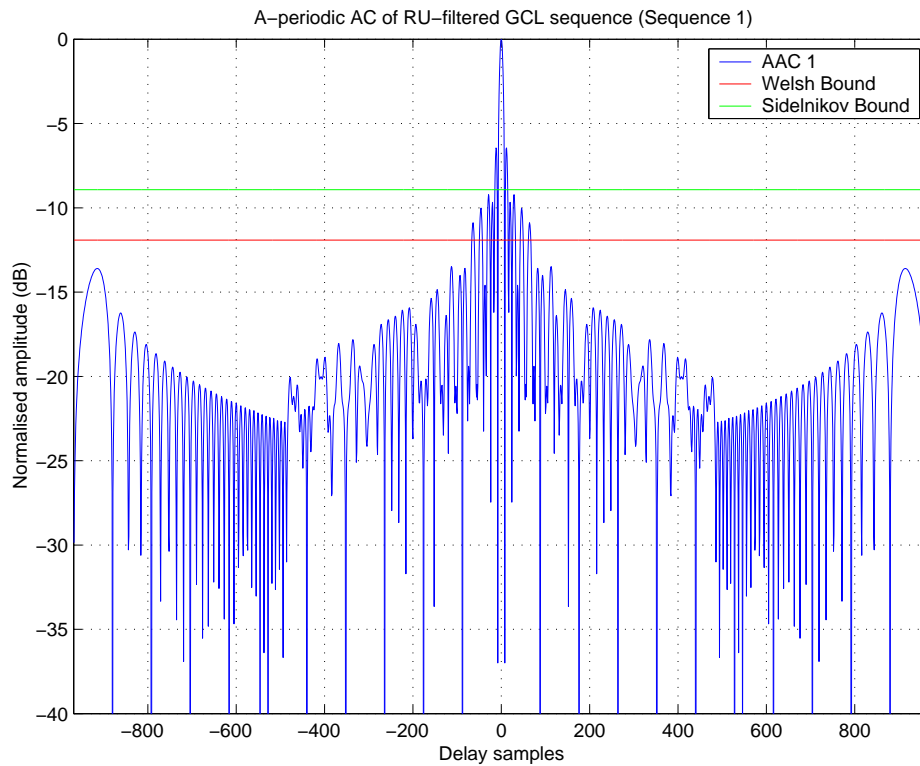


FIGURE A.12: Aperiodic Auto Correlation (AAC) function of unique combination of complex spreading sequence 1 in decibels. ( $L = 121$ , *RU filtered*,  $spc = 8$ )

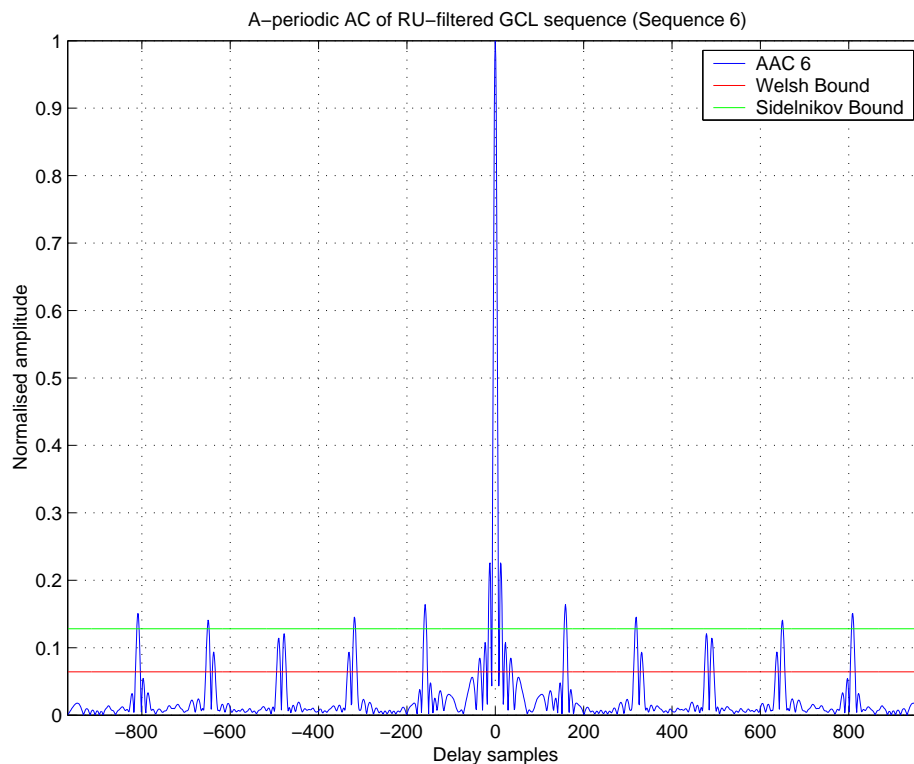


FIGURE A.13: Aperiodic Auto Correlation (AAC) function of unique combination of complex spreading sequence 6. ( $L = 121$ , *RU filtered*,  $spc = 8$ )

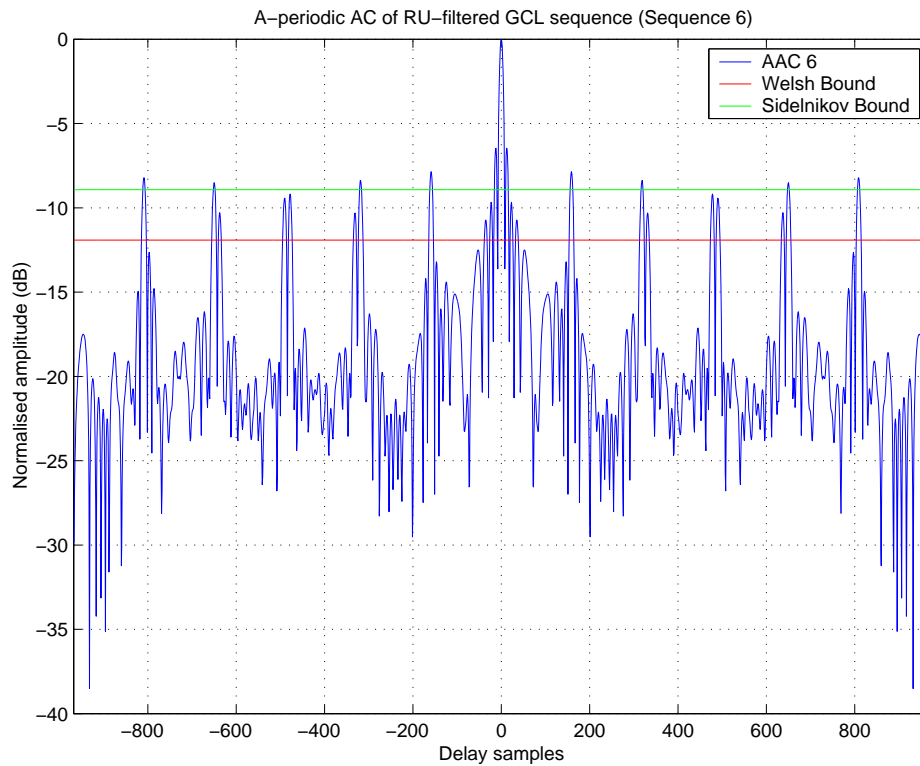


FIGURE A.14: Aperiodic Auto Correlation (AAC) function of unique combination of complex spreading sequence 6 in decibels. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

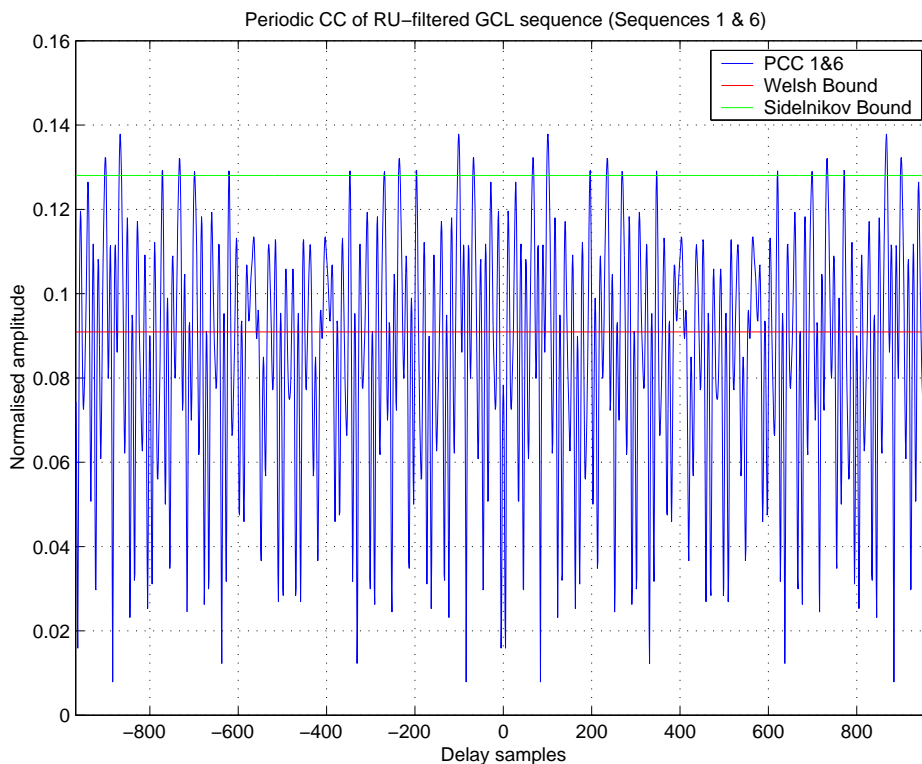


FIGURE A.15: Periodic Cross Correlation(PCC) function between unique combinations of complex spreading sequences 1 and 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

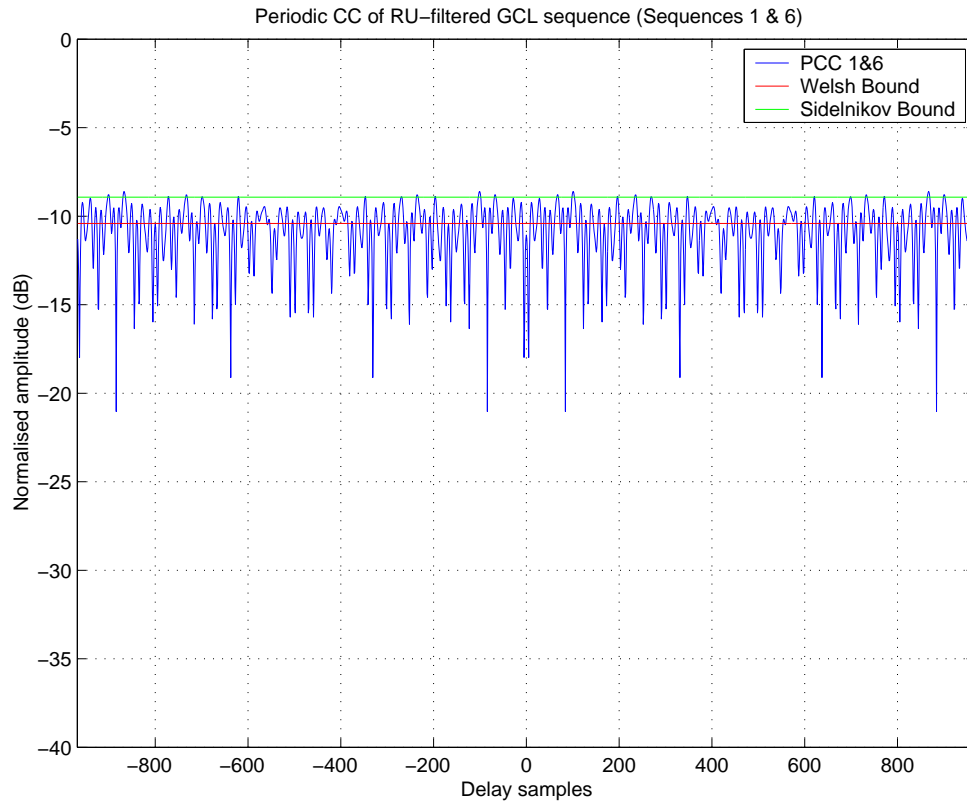


FIGURE A.16: Periodic Cross Correlation(PCC) function between unique combinations of complex spreading sequences 1 and 6 in decibels. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )

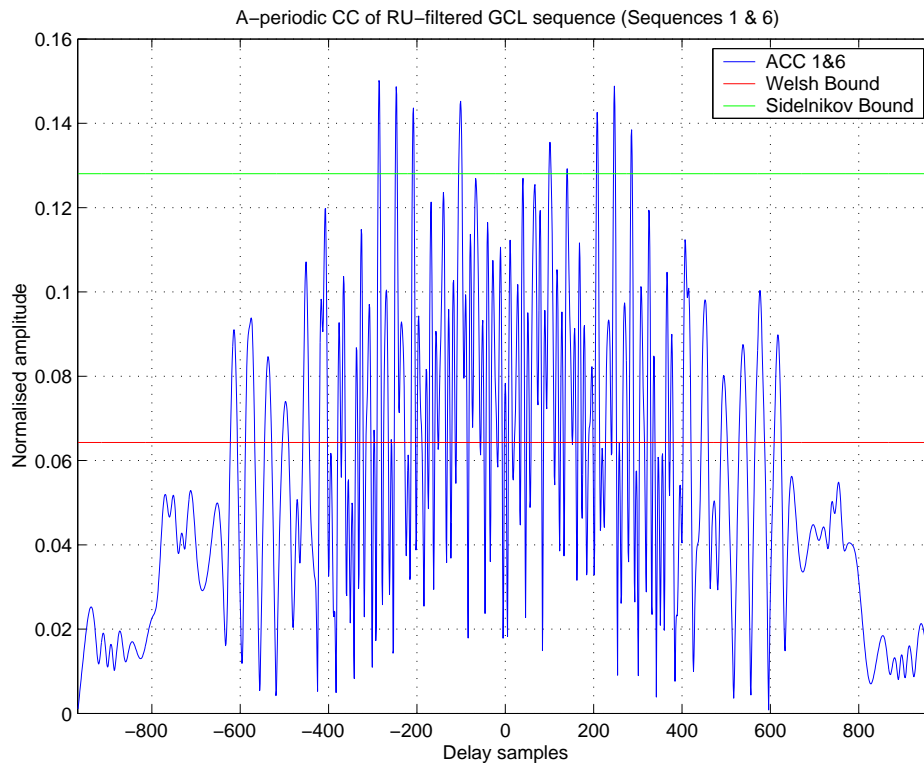


FIGURE A.17: Aperiodic Cross Correlation(PCC) function between unique combinations of complex spreading sequences 1 and 6. ( $L = 121$ ,  $RU$  filtered,  $spc = 8$ )



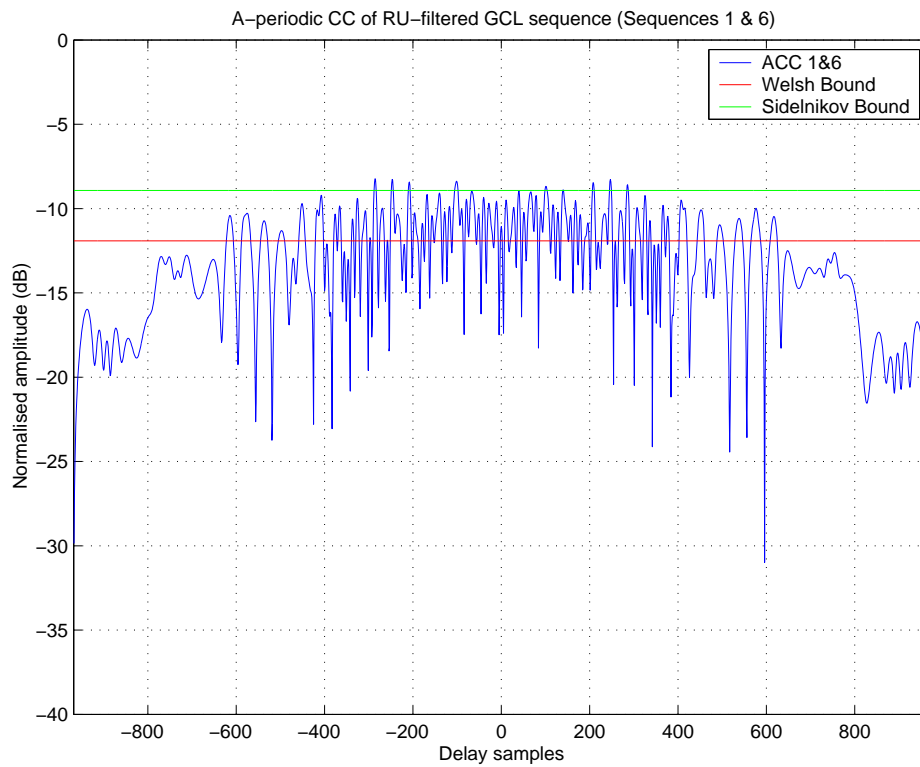


FIGURE A.18: Periodic Cross Correlation(PCC) function between unique combinations of complex spreading sequences 1 and 6 in decibels. ( $L = 121$ , *RU filtered*,  $spc = 8$ )

APPENDIX **B**

**AWARDS RECEIVED DURING  
MASTERS DEGREE**

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- F.E. Marx and L.P. Linde, SABS design institute awards, 1996.
- F.E. Marx, Special Merit Award of the SAIPL, 1996.
- L.P. Linde, D.J. van Wyk, B. Westra, F.E. Marx and W.H. Büttner, SABS design institute awards, 1997.

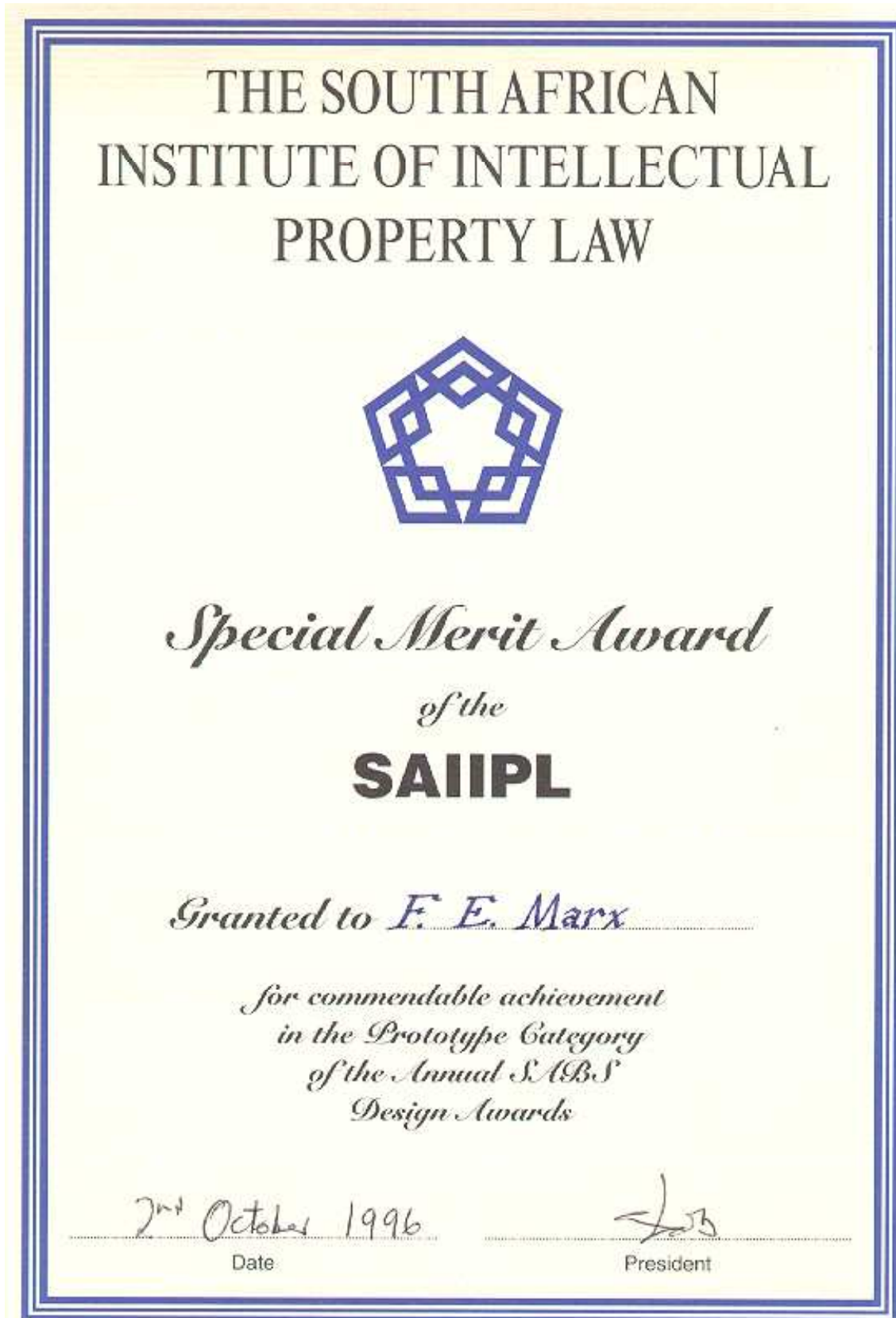


FIGURE B.1: Special Merit Award of the SAIPL