

# DETERIORATION OF RAILWAY TRACK DUE TO DYNAMIC VEHICLE LOADING AND SPATIALLY VARYING TRACK STIFFNESS

Robert Desmond FRÖHLING

A thesis submitted in partial fulfilment of  
the requirements for the degree of

PHILOSOPHIAE DOCTOR (ENGINEERING)

in the

FACULTY OF ENGINEERING

UNIVERSITY OF PRETORIA, PRETORIA

October 1997

## THESIS SUMMARY

# DETERIORATION OF RAILWAY TRACK DUE TO DYNAMIC VEHICLE LOADING AND SPATIALLY VARYING TRACK STIFFNESS

**Robert Desmond FRÖHLING**

Supervisor: Professor W Ebersöhn  
Co-Supervisor: Doctor H Scheffel  
Department: Civil Engineering  
University: University of Pretoria  
Degree: Philosophiae Doctor (Engineering)

In this thesis a Dynamic and a Static Track Deterioration Prediction Model are developed to predict track deterioration due to dynamic vehicle loading and nonlinear spatially varying track stiffness. The research also contributes to a better understanding of the relationship between spatially varying track stiffness and track deterioration.

Preceding the development of the Track Deterioration Prediction Models, experimental work was done to simultaneously measure the dynamic behaviour of a rail vehicle and the corresponding response of the track. On-track measurements were made as a function of vehicle speed, axle load, track condition, and accumulating traffic. In this process a new technique to measure the dynamic track stiffness was developed.

Track Deterioration Prediction Models were developed systematically to gain a better understanding of the relative influence of vehicle and track parameters. The

dynamic prediction model consists of two elements, an eleven degree-of-freedom dynamic vehicle/track model and a modified track settlement equation, while the static prediction model is based only on the modified settlement equation. The modified settlement equation is based on measurable parameters of the track superstructure, substructure layer properties, the spatial variation of the track stiffness, and the prevailing wheel loading. Using the dynamic interaction between the vehicle and the track, dynamic track loading and differential track settlement are predicted. After validating the model against test results, two applications of the model are given. In the first application void forming is predicted and in the second application the length of a tamping cycle is predicted.

Research presented in this thesis shows that the spatial variation of the track stiffness contributes significantly to track deterioration, both in terms of differential track settlement and increased dynamic vehicle loading. It is thus recommended that track maintenance procedures should be used to reduce the variation of the spatial track stiffness.

**Keywords:** Track deterioration, track stiffness, track settlement, prediction model, dynamic interaction.

## SAMEVATTING VAN PROEFSKRIF

### DETERIORATION OF RAILWAY TRACK DUE TO DYNAMIC VEHICLE LOADING AND SPATIALLY VARYING TRACK STIFFNESS

**Robert Desmond FRÖHLING**

Promotor: Professor W Ebersöhn  
Medepromotor: Doctor H Scheffel  
Departement: Siviele Ingenieurswese  
Universiteit: Universiteit van Pretoria  
Graad: Philosophiae Doctor (Ingenieurswese)

In hierdie proefskrif is 'n Dinamiese en 'n Statiese Spoorbaanagteruitgangvoorspellingsmodel ontwikkel om spoorbaanagteruitgang te voorspel as gevolg van dinamiese voertuigbeladings en nie-liniére afstandgebaseerde variasies in spoorbaanstyfheid. Die navorsing dra ook by tot 'n beter begrip van die verwantskap tussen afstandgebaseerde variasies in spoorbaanstyfhede en spoorbaanagteruitgang.

Voordat met die ontwikkeling van die spoorbaanagteruitgangvoorspellingsmodelle begin is, is eksperimentele werk gedoen om gelyktydig die dinamiese gedrag van die spoorvoertuig en die gepaardgaande reaksie van die spoorbaan te meet. Hierdie meetings is gedoen as 'n funksie van voertuigspoed, asbelasting, spoorbaantoestand, en toenemende verkeer. In dié proses is 'n nuwe tegniek ontwikkel om die dinamiese spoorbaanstyfheid te meet.

Na voltooiing van die toetse is die spoorbaanagteruitgangvoorspellingsmodelle ontwikkel. Die ontwikkeling is stapsgewys gedoen om 'n beter begrip van die relatiewe invloed van voertuig- en spoorbaanparameters te ondersoek. Die dinamiese voorspellingsmodel bestaan uit twee komponente, 'n elf vryheidsgraad dinamiese voertuig/spoorbaanmodel en 'n gemodifiseerde vergelyking vir spoorbaanversakking, terwyl die statiese model slegs van die gemodifiseerde vergelyking vir spoorbaanversakking gebruik maak. Die gemodifiseerde vergelyking vir spoorbaanversakking is gebaseer op meetbare parameters van die spoorbaanstruktuur, die eienskappe van die substruktuur, die afstandsgebaseerde variasie van die spoorbaanstyfheid, en die heersende wielbelasting. Deur gebruik te maak van die interaksie tussen die voertuig en die spoorbaan, word die dinamiese wielbelasting en die variërende spoorbaanversakking voorspel. Nadat die modelle geverifeer is teen toetsresultate, is twee toepassings van die model gegee. In die eerste toepassing word die vorming van 'n slapte in the spoorbaan voorspel en in die tweede toepassing word die lengte van 'n onderstopsiklus voorspel.

Die navorsing wat gedoen is toon aan dat die afstandgebaseerde variasie in die styfheid van die spoorbaan beslis bydra tot spoorbaanagteruitgang in terme van variërende spoorbaanversakking en toenemende dinamiese wielbelasting. Meer effektiewe spoorbaanonderhoud behoort dus die afstandsgebaseerde variasie van die spoorbaanstyfheid te verminder.

**Sleutelwoorde:** Spoorbaanagteruitgang, spoorbaanstyfheid, spoorbaanversakking, voorspellingsmodel, dinamiese interaksie.

## ABSTRACT

Title:	Deterioration of railway track due to dynamic vehicle loading and spatially varying track stiffness
Author:	R D Fröhling
Supervisor:	Professor W Ebersöhn
Co-Supervisor:	Doctor H Scheffel
Department:	Civil Engineering
University:	University of Pretoria
Degree:	Philosophiae Doctor (Engineering)

In this thesis a Dynamic and a Static Track Deterioration Prediction Model are developed to predict track deterioration due to dynamic vehicle loading and nonlinear spatially varying track stiffness. The dynamic prediction model consists of an eleven degree-of-freedom dynamic vehicle/track model and a modified track settlement equation, while the static prediction model consists only of the modified track settlement equation.

Preceding the development of the Track Deterioration Prediction Models, experimental work was done to simultaneously measure the dynamic behaviour of a rail vehicle and the corresponding response of the track. On-track measurements were made as a function of vehicle speed, axle load, track condition, and accumulating traffic.

Research presented in this thesis shows that the spatial variation of the track stiffness contributes significantly to track deterioration, both in terms of differential track settlement and increased dynamic vehicle loading. It is thus recommended that track maintenance procedures should be used to reduce the variation of the spatial track stiffness.

## ACKNOWLEDGEMENT

I wish to express my appreciation to the following organisations and persons who made this thesis possible:

- Professor W Ebersöhn, my supervisor, and Doctor H Scheffel, my co-supervisor for their guidance and support.
- The management of Spoornet, and in particular Mr H Tournay, for giving me the opportunity to do and complete the required research work.
- M Howard, C Kayser, H Maree, and M Tomas for their assistance during the extensive on-track tests.
- My wife Elke, and children Conrad and Claudia, for their continuous encouragement and support.

## TABLE OF CONTENTS

	Page
LIST OF FIGURES .....	iv
LIST OF TABLES .....	vii
LIST OF SYMBOLS .....	viii
<b>Chapter</b>	
1 INTRODUCTION .....	1
1.1 Objective .....	2
1.2 Scope .....	2
2 LITERATURE REVIEW .....	5
3 ON-TRACK TESTING .....	9
3.1 Measurements .....	11
3.2 Methodology .....	12
4 TRACK SETTLEMENT MODELLING .....	14
4.1 Assumptions .....	15
4.2 Prediction of Track Settlement .....	15
4.3 Modified Settlement Equation .....	20
5 MODEL OF VEHICLE/TRACK SYSTEM DYNAMICS .....	27
5.1 Track Support Model .....	27
5.2 Track Input .....	32
5.3 Vehicle Model .....	34
5.4 Vehicle/Track Model Development .....	35
5.4.1 Two Degree-of-Freedom Vehicle/Track Model .....	36
5.4.2 Alternative Vehicle/Track Models .....	39
5.4.3 Eleven Degree-of-Freedom Vehicle/Track Model .....	40

6	TRACK DETERIORATION PREDICTION MODELS . . . . .	46
6.1	Dynamic Track Deterioration Prediction Model . . . . .	46
6.2	Static Track Deterioration Prediction Model . . . . .	47
7	MODEL VALIDATION . . . . .	49
7.1	Dynamic Behaviour . . . . .	49
7.2	Track Settlement . . . . .	54
7.3	Assumptions and Simplifications . . . . .	58
8	PREDICTION OF TRACK DETERIORATION . . . . .	61
8.1	Evaluation Criteria . . . . .	61
8.2	Void Forming . . . . .	62
8.3	Tamping Cycle . . . . .	64
9	CONCLUSION . . . . .	66

## APPENDICES

A	LITERATURE REVIEW . . . . .	69
A.1	Problems due to Vehicle/Track Interaction . . . . .	69
A.2	Modelling of the Vehicle/Track System . . . . .	74
A.3	Track Settlement . . . . .	80
B	EXPERIMENTAL WORK . . . . .	84
B.1	Rolling Stock . . . . .	84
B.1.1	Test Trains and Passing Traffic . . . . .	84
B.1.2	CCL-5 Suspension Characteristics . . . . .	86
B.1.3	Vehicle Instrumentation . . . . .	90
B.1.3.1	Purpose and Description . . . . .	91
B.1.3.2	Sample Measurement and Interpretation . . . . .	93
B.2	Infrastructure . . . . .	95
B.2.1	Test Site . . . . .	95
B.2.2	Level Measurements . . . . .	101
B.2.3	Static Track Stiffness Measurements . . . . .	101

B.2.4 Track Instrumentation .....	105
B.2.4.1 Purpose and Description .....	106
B.2.4.2 Sample Measurements and Interpretation .....	110
B.2.5 Dynamic Track Stiffness .....	114
B.3 Test Results .....	116
B.3.1 Influence of Axle Load on Track Behaviour .....	116
B.3.2 Vehicle and Track Performance as a Function of Vehicle Speed	117
B.3.2.1 Dynamic Wheel Load .....	118
B.3.2.2 Vehicle Performance .....	121
B.3.2.3 Dynamic Track Behaviour .....	121
B.3.3 Vehicle and Track Performance Versus Accumulating Traffic ..	124
B.3.3.1 Track Settlement .....	125
B.3.3.2 Track Roughness .....	126
B.3.3.3 Dynamic Wheel Load .....	127
B.3.3.4 Vehicle Suspension Behaviour .....	129
B.3.3.5 Dynamic Track Behaviour .....	129
B.3.3.6 Track Substructure Property .....	132
B.3.4 Void Forming .....	132
C GEOTRACK INPUT AND OUTPUT .....	134
D DYNAMIC MODELLING .....	138
REFERENCES .....	140

## LIST OF FIGURES

Figure		Page
3.1	Instrumented test site .....	10
3.2	Instrumented CCL-5 gondola coal wagon.....	10
4.1	Interactive dynamic settlement methodology .....	16
4.2	Dynamic track settlement model .....	17
4.3	Ballast strain superposition for mixed loading .....	19
4.4	Measured vertical track space curve, differential track settlement, wheel load and track deflection .....	21
4.5	Deviatoric stress versus track stiffness .....	25
5.1	Components of ballasted track .....	29
5.2	Track deflection basin .....	31
5.3	Effective linearised loaded track stiffness .....	33
5.4	Varying static track deflections .....	34
5.5	Two degree-of-freedom vehicle/track model .....	36
5.6	Eleven degree-of-freedom vehicle/track model .....	41
7.1	Wheel load comparison at 30 km/h .....	52
7.2	Wheel load comparison at 70 km/h .....	52
7.3	Displacement across secondary suspension at 30 km/h .....	53
7.4	Displacement across secondary suspension at 70 km/h .....	53
7.5	Average track settlement versus accumulating traffic .....	55
7.6	Measured and predicted track settlement .....	55
7.7	The influence of spatially varying track stiffness on track settlement ..	56
7.8	Measured and predicted track settlement including the STDPM ..	57
8.1	Simulated and measured void forming on the left side of the track ..	63
8.2	Simulated and measured void forming on the right side of the track ..	64
A1	Components of the vehicle/track system .....	78

B1	Loading profile of long test train . . . . .	85
B2	Axle load histogram after 13 MGT of traffic . . . . .	86
B3	Axle load histograms for two typical in-service trains . . . . .	86
B4	HS Mk V bogie . . . . .	87
B5	Drawing of a typical three-piece self-steering bogie . . . . .	88
B6	Measured and calculated hysteresis loop for a loaded HS Mk VII bogie . . . . .	90
B7	Test bogie and instrumentation . . . . .	91
B8	Measurements taken on the instrumented bogie . . . . .	94
B9	Details of the track cross section at Sleeper 77 . . . . .	96
B10	Schematic cross section at Sleeper 77 . . . . .	97
B11	Track layout and geometry . . . . .	99
B12	Root Mean Square values of the wheel load at 70 km/h . . . . .	100
B13	Cross sections at test site . . . . .	100
B14	"BSSM" track loading vehicle . . . . .	102
B15	Unloaded and loaded vertical space curve and track deflection due to a 29kN and a 128kN load on the rail . . . . .	103
B16	Track deflection due to vertical loads of 29kN, 49kN, 78kN and 128kN . . . . .	104
B17	Static force-deflection curves . . . . .	105
B18	Layout of test track instrumentation . . . . .	106
B19	Position of shear strain gauges on the rail . . . . .	107
B20	Comparison between wheel load as measured on track and by the load measuring wheelset . . . . .	108
B21	Beam and displacement transducer mounting . . . . .	109
B22	Multi-Depth Deflection Meter Construction . . . . .	110
B23	Measured dynamic track parameters . . . . .	112
B24	Dynamic track stiffness under one wheel . . . . .	112
B25	Track reaction due to a passing locomotive . . . . .	113
B26	Dynamic track stiffness due to a passing locomotive . . . . .	114
B27	Deflection in sub-structure layers . . . . .	114

B28	Dynamic and static track stiffness . . . . .	115
B29	Dynamic track behaviour under varying wheel loads . . . . .	117
B30	Dynamic track stiffness under varying wheel loads . . . . .	118
B31	Influence of vehicle load on track behaviour . . . . .	118
B32	Dynamic wheel loads under the left wheel at various speeds . . . . .	119
B33	Dynamic wheel load as a function of vehicle speed . . . . .	120
B34	Frequency response as a function of vehicle speed . . . . .	122
B35	Vertical displacement across secondary suspension as a function of vehicle speed . . . . .	123
B36	Dynamic track behaviour as a function of vehicle speed . . . . .	124
B37	Average overall track settlement . . . . .	125
B38	Track settlement profiles . . . . .	126
B39	Changes in average track roughness . . . . .	127
B40	Variation of dynamic wheel load with accumulating traffic . . . . .	128
B41	Wheel load as a function of accumulating traffic . . . . .	128
B42	Displacement across secondary suspension as a function of accumulating traffic . . . . .	129
B43	Wheel load, sleeper reaction and sleeper deflection at two different sleepers . . . . .	130
B44	Changes in the dynamic track stiffness due to accumulating traffic . . . . .	131
B45	Differential ballast settlement after 13 MGT . . . . .	133
B46	Dynamic vehicle behaviour including displacement across secondary suspension and dynamic wheel load . . . . .	133
D1	One degree-of-freedom model . . . . .	139

## LIST OF TABLES

Table	Page
7.1      Vehicle and track parameters .....	50
7.2      Dominant wheel load frequencies .....	51
7.3      Wavelength analysis after 2.84 MGT .....	57
7.4      Influence of dynamic wheel load and track stiffness variations on differential track settlement .....	60
8.1      Maintenance history at Km 7 .....	65
A1      Problems concerning vehicle/track interaction .....	70
B1      Track design details .....	95
B2      Ballast properties .....	97
B3      Spoornet track standards .....	98
B4      Modulus of elasticity of substructure layers .....	132

## LIST OF SYMBOLS

- $B_{e'}$  : Effective resolution bandwidth
- $b$  : Half distance between the secondary suspension on one bogie
- $b_{cc}$  : Half bogie centre distance
- $C$  : Ballast material constant
- $C_f$  : Foundation modulus
- $C_{slope}$  : Friction wedge stick slope
- $d_i$  : Difference between the elevation at the point of measurement and the mean filtered elevation
- $E$  : Young's modulus
- $F_{ff}$  : Wedge friction force
- $I$  : Rail moment of inertia about its horizontal axis
- $I_1$  : Vehicle body moment of inertia in roll
- $I_2$  : Bogie frame moment of inertia in roll
- $I_p$  : Vehicle body moment of inertia in pitch
- $I_w$  : Wheelset moment of inertia in roll
- $K_1$  : Settlement constant
- $K_2$  : Settlement constant
- $K_3$  : Track stiffness correction factor
- $k$  : General vertical track stiffness
- $k_1$  : Vertical stiffness of secondary suspension
- $k_2$  : Effective linearised vertical track stiffness
- $k_{2i}$  : Calculated track stiffness at a particular sleeper
- $k_{2mi}$  : Measured track stiffness at a particular sleeper
- $k_{2BL}$  : Vertical track stiffness under the left wheel of the trailing wheelset
- $k_{2BR}$  : Vertical track stiffness under the right wheel of the trailing wheelset
- $k_{2FL}$  : Vertical track stiffness under the left wheel of the leading wheelset

$k_{2FR}$	: Vertical track stiffness under the right wheel of the leading wheelset
$k_p$	: Vertical stiffness of primary suspension
$k_{ss}$	: Stiffness of one stabiliser spring
$L_c$	: Characteristic length
$l$	: Half distance between the wheel and rail contact points
$m_1$	: Mass of vehicle body
$m_2$	: Mass of wheel or bogie frame
$m_w$	: Mass of wheelset
$N$	: Number of load cycles
$n$	: Number of measurement in the length of the track under consideration
$n_p$	: Ballast porosity
$P$	: Concentrated force applied to the rail
$P_{dyn}$	: Prevailing dynamic vertical wheel load
$P_{ref}$	: Static reference vertical wheel load
$P_s$	: Static wheel load
$q$	: Vertical force in rail foundation per unit length
$R$	: Track roughness
$T$	: Total measuring time
$u$	: Track modulus
$V$	: Vehicle speed
$x$	: Distance in direction of vehicle travel
$x_{ss}$	: Static deflection of the stabiliser spring from its free height
$y$	: Local deflection of the track support
$y_0$	: Vertical track profile variation
$y_1$	: Vertical displacement of vehicle body
$y_2$	: Vertical displacement of wheel or wheelset
$y_B$	: Vertical displacement of trailing bogie frame
$y_F$	: Vertical displacement of leading bogie frame
$y_s$	: Static track deflection
$y_{BL}$	: Vertical track profile variation under the left wheel of the trailing wheelset

- $y_{BR}$  : Vertical track profile variation under the right wheel of the trailing wheelset
- $y_{FL}$  : Vertical track profile variation under the left wheel of the leading wheelset
- $y_{FR}$  : Vertical track profile variation under the right wheel of the leading wheelset
- $z_B$  : Vertical displacement of trailing wheelsets
- $z_F$  : Vertical displacement of leading wheelsets
- $\Delta P$  : Dynamic wheel load component
- $\alpha$  : Pitching angle of vehicle body
- $\alpha_w$  : Angle of friction wedge
- $\delta$  : Ratio of dynamic wheel load component to static wheel load
- $\epsilon_N$  : Permanent axial strain in ballast after  $N$  cycles
- $\epsilon_1$  : Permanent axial strain in ballast caused by the first load cycle
- $\epsilon_r$  : Normalized standard error
- $\theta$  : Rolling angle of vehicle body
- $\mu$  : Coefficient of friction
- $\rho_1$  : Vertical damping of secondary suspension
- $\rho_{IBL}$  : Vertical damping of the secondary suspension on the left side of the trailing bogie
- $\rho_{IBR}$  : Vertical damping of the secondary suspension on the right side of the trailing bogie
- $\rho_{IFL}$  : Vertical damping of the secondary suspension on the left side of the leading bogie
- $\rho_{IFR}$  : Vertical damping of the secondary suspension on the right side of the leading bogie
- $\rho_2$  : Vertical track damping
- $\rho_P$  : Vertical damping of primary suspension
- $\sigma$  : Local compressive stress on the track support
- $\sigma_1$  : Major principle stress
- $\sigma_3$  : Minor principle stress

$\phi_B$  : Rolling angle of trailing bogie frame

$\phi_F$  : Rolling angle of leading bogie frame

$\omega_B$  : Rolling angle of trailing wheelsets

$\omega_F$  : Rolling angle of leading wheelsets