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Primary school pre-service teachers' solutions to pattern problem-solving tasks based on three components of creativity

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Education stakeholders and researchers in South Africa have emphasised the need to enhance teachers' creativity through problem-solving tasks. Teachers' creativity entails using new ideas of creative devices to solve problems, implement solutions, and make learning more effective. In the research reported on here, Guilford's theory was used to explore primary school pre-service teachers' solutions to pattern problem-solving tasks based on 3 components of creativity. The data for this research were produced from primary school pre-service teachers' written responses to the pattern problem-solving tasks, and an extract from participants' semi-structured interviews. The research involved a qualitative design using convenient purposive sampling to sample 62 pre-service teachers enrolled for a primary mathematics module at a selected higher education institution. Participants' responses to the written tasks were analysed using content analysis, while the semi-structured interviews were analysed thematically. The result shows that 35 participants were able to draw patterns and express patterns in nth form, while 27 failed to do so. The most common method used to draw a new pattern was counting in 2s and 4s. Furthermore, the result shows that half of the pre-service teachers who participated in the study were not capable of producing varied solutions to pattern tasks. An indication that they did not have the creative potential to prepare learners even after they had been exposed to advanced mathematics content as part of their training process. We recommend that pre-service teacher education programmes should include academic activities that could help pre-service teachers enhance creativity through tasks with divergent thinking.

Keywords: creativity; flexibility; fluency; originality; patterns; pre-service teachers; primary school; problem-solving tasks

Introduction

In a quest for increased teacher enrolment in schools, due to ever-growing demand, developing economies such as South Africa recruit under-qualified teachers that do not possess adequate knowledge of mathematical content and pedagogy to teach mathematics (Deacon, 2016; Ubah & Bansilal, 2018). These under-qualified teachers do not possess the ability to develop learners' creative thinking (Jojo, 2020). As observed by Deacon (2016:25), this leads to a "cycle of mediocrity, where school leavers who were themselves poorly taught are returned to the schools as teachers." This study was conducted in the context of pre-service primary school teachers who found the mathematics content that they were expected to teach after graduation, difficult. Primary school mathematics forms the foundation for mathematical concepts and the main objective of primary mathematics is to help learners understand, make sense of mathematical concepts, and improve on their creativity (Gallant, 2013; Gouws & Dicker, 2011). Education stakeholders and many researchers in South Africa highlight the need for enhanced teacher creativity through problem-solving tasks (South African Institute for Distance Education, 2017).

Vale and Barbosa (2015:103) observe that "creativity begins with curiosity and engages learners in exploration and experimentation-based tasks where they can translate their imagination and originality." Researchers (like Wilkie & Clarke, 2016) have found that understanding and being able to identify patterns allow learners to make educated guesses, assumptions, hypotheses as well as the enhancement of creativity. Research results (Ayllón, Gómez & Ballesta-Claver, 2016:209) have shown that "mathematical problem solving and problem posing are closely related to creativity." Hence, problem-based tasks should be used in mathematics classroom instruction to enhance learners' creativity.

Problem-based tasks usually require creative thinking and recent research (Childcare, 2019; Mendez, 2016) about teaching and learning of mathematics reveal that the development of learners' creativity and mathematical ability could be attributed to the use of patterns in instruction. Moreover, research reveals that learners with a better understanding of patterns tend to perform better in mathematics courses, while learners who are not doing so well in mathematics can substantially increase their scores by training with patterns (Ankowski & Ankowski, 2015). According to Guilford (1975), once learners begin to spot patterns they see them everywhere, not only in the environment but also in daily routines and all kinds of regular behaviour. Mathematics educators must provide prospective teachers with creative ideas for solving mathematical tasks and encourage them to think independently and critically. In this way, primary school pre-service teachers will enhance their creative abilities as well as successfully undertake the same type of tasks, to which they will expose their learners when they start their teaching careers.

Literature Review

The use of patterns is a strategy of 21st-century problem-solving skills. According to Vale, Pimentel, Cabrita, Barbosa and Fonseca (2012:173), the study of patterns “makes it possible to get mathematical ideas as generalization and algebraic thinking where visualization plays an important role.” Similarly, Safitri, Wijayanti and Masriyah (2018) observe that pattern-based tasks have the creative potential to prepare learners for further learning and to enhance their problem-solving skills. Creative ability is a skill that teachers must possess to stimulate the creativity of their learners. Yazgan-Sağ and Emre-Akdoğan (2016) have explored the views and differences that creativity engenders in prospective South African teachers. Their results reveal that prospective mathematics teachers’ creativity was related to the type of instruction presented by the teacher, tasks presented to the learners, and teachers’ approaches to solving problems.

Problem solving is the basis of mathematics because it entails solving tasks not based on procedures (National Council of Teachers of Mathematics [NCTM], 2015). Dunlosky, Rawson, Marsh, Nathan and Willingham (2013) observe that what learners learn is greatly influenced by the tasks given to them by their teachers. Therefore, mathematical tasks must be intellectually challenging for learners, develop different approaches, create ideas, and provide multiple solutions that introduce fundamental mathematical ideas, and enhancement of creativity (NCTM, 2015).

According to Aguilar and Telese (2018:26), “teachers have difficulty in implementing non-routine activities that are open-ended and require reasoning and problem-solving strategies.” Phonapichat, Wongwanich and Sujiva (2014) argue that this difficulty may be because teachers fail to connect real-life situations with mathematical content. They teach learners to memorise procedures in solving problems but do not deeply explain the concepts behind textbook problems (Phonapichat et al., 2014). Therefore, pre-service teachers should possess the mathematical content knowledge for solving non-routine problems as well as the pedagogical knowledge essential for having a positive effect on their learners’ learning (Worrell, Brabeck, Dwyer, Geisinger, Marx, Noell & Pianta, 2014).

According to Liljedahl, Santos-Trigo, Malaspina and Bruder (2016), problem-solving is a prominent research area in mathematics education, aimed at connecting problem-solving processes to students’ enhancement of problem-solving competencies and mathematical ability. Vale et al. (2012) reveal that pre-service teachers’ mathematical creativity and ability were enhanced through pattern problem-solving tasks.

Schrauth’s (2014) qualitative case study on mathematical creativity in middle-grade classes revealed that reasoning, explanation, and use of relevant terminology improved students’ mathematical creativity. Leikin, Leikin and Waisman’s (2017) study on the development of students’ mathematical creativity revealed that the enhancement of creativity in mathematics teachers requires the creation of a “pattern” learning environment.

Patterns can be seen everywhere in our environment and do not always have to be stated in numerical form (NCTM, 2000). Mathematics is a subject that is peculiar with patterns, it involves spatial, numeric, and logical relationships with predictable regularities (Mulligan & Mitchelmore, 2009). The patterns that learners learn at primary school level include recurring patterns (e.g., XYZXYZXYZ), spatial structural patterns (e.g. various geometrical shapes), and increasing patterns (e.g. 5, 10, 15, 20...). Pattern tasks provide learners with the opportunity to observe, verbalise, generalise, and formally translate them.

Obara’s (2019) research on how prospective teachers arrived at generalisations based on patterns revealed that the prospective teachers experienced some difficulties in input-output relationships in a generalisation process. McCrory, Floden, Ferrini-Mundy, Reckase and Senk’s (2012) study revealed that if primary school teachers were not equipped with the knowledge to help learners make the leap from numbers and arithmetic to learning about relationships (patterns), then the learning of mathematical skills could be a challenge.

The literature reviewed for this research reveal a sparsity of research studies on pre-service primary school teachers’ knowledge of how to create, share, and solve mathematical problems through pattern-based activities. The studies also indicate that teachers had difficulty in implementing non-routine classroom activities that involved reasoning and problem solving. Moreover, it has been a challenging task for teachers to develop learners’ creativity in pattern problem-solving tasks. However, most of the empirical studies analysed were on developed economies, with a paucity of research on developing economies like South Africa, hence the need for this research. In this research we used the Guilford framework to explore pre-service primary school teachers’ solutions to two pattern problem-solving tasks based on three components of creativity (fluency, flexibility, and originality).

Theoretical Framework

This research is anchored in Guilford’s Theory of Creativity as a problem-solving technique that improves divergent thinking (Guilford, 1967). In mathematics, creativity is conveyed through the design of non-complicated challenges and the

identification of novel methods of solving mathematical tasks. Presentation of learners with non-routine questions that involve creative thinking, diverse ideas, and multiple answers leads to the enhancement of mathematical thinking (McCrary et al., 2012). If teachers were mathematically competent to analyse their learners' solutions to creatively structured tasks, then the solution could be achieved. For example, instead of the teacher asking, "How do we divide 15 oranges equally among 5 bowls?" with the procedure being unambiguous, the teacher will ask, "How do we divide 15 oranges among several bowls?"; this question has a diverse solution/answer, and the learner will have to consider a variety of alternatives before choosing the right answer (Yee, 2005).

Mann (2006) observes that there is no generally acknowledged description of mathematical creativity because creativity could be expressed in different ways. However, Vale et al. (2012) observe that the accepted definition of creativity involves divergent and convergent thinking. This is in line with Guilford's theory of creativity.

The divergent and convergent thinking aspects of creativity are key characteristics of 21st-century problem-solving skill. Convergent thinking involves obtaining a single response to a problem while divergent thinking involves many possible solutions to a problem. Solving problems by analysing all the likely solutions and identifying the best solution to the problem is referred to as divergent thinking. Divergent thinkers keep their minds open to any possible solutions presented to them and the more prospects they can come up with, the more efficient they become in divergent thinking.

Guilford's main components of creativity are fluency, flexibility, and originality. Fluency involves the ability to quickly come up with many diverse ideas, measured by the total number of ideas generated. Flexibility involves students changing ideas amid solutions. Originality is the proficiency in creating different ideas, which is measured as the number of novel ideas generated. In a regular mathematics classroom, originality is shown when a student explores diverse solutions/answers to a task and then creates a new, different solution/answer. However, Kaufman and Sternberg (2019:59) state that a major limitation on the assessment of students' creativity is the lack of scaled instruments that could be used for a large sample. In problem-solving tasks, fluency, flexibility, and originality could be easily measured in a few samples but scoring is time-consuming, hence not most ideal for classroom use.

Research findings in mathematics education reveal that problem solving is closely related to creativity, and that the creative process develops

during problem solving (Ayllón et al., 2016; Palmér & Van Bommel, 2018). Tasks that promote creativity must be open-ended and teachers should provide their learners with open-ended tasks with diverse alternative solutions rather than closed tasks with a single solution (Siswono, 2008). The study of patterns should involve open-ended problem-solving tasks that could promote diverse mathematical ideas where visualisation plays an important role. Obara (2019) observes that open-ended pattern-based tasks have great creative potential.

It is important to note that for effective learning, teachers should propose mathematical tasks involving learners in a creative way, and teachers should be competent in analysing their learners' diverse solutions to tasks (Palmér & Van Bommel, 2018). Research shows that what learners learn is greatly influenced by the tasks they are given by their teachers (Dunlosky et al., 2013). Therefore, mathematical tasks must be intellectually challenging for learners, must involve different approaches, creative ideas, and provide multiple solutions that introduce fundamental mathematical ideas (NCTM, 2015).

To enhance their mathematical knowledge and ability, teachers must inspire learners to generate diverse solutions to mathematical tasks in a rich learning environment. Problem-solving is at the core of mathematics because it includes solving tasks not based on procedures (NCTM, 2015). Since learners develop creativity if suitable learning prospects are offered by the teachers, then primary school pre-service teachers' training should involve encouraging students to solve mathematical problems that enhance creativity.

Guilford's theory postulates that the enhancement of creativity depends on the ability of the students/learners to visualise varied solutions to a task. This postulation is referred to as divergent thinking. Hence, the relevance of Guilford's theory in this research is based on the interaction of the three components of creativity (fluency, flexibility, and originality) in analysing participants' solutions in two pattern problem-solving tasks.

Research Question

The research question in this research was: What are primary school pre-service teachers' solutions to pattern problem-solving tasks based on fluency, flexibility, and originality?

Methodology

Research Design

In this research we employed a qualitative research method (in general) and a case study approach (in particular) to explore primary school pre-service teachers' solutions to pattern problem-solving tasks based on fluency, flexibility, and originality. Qualitative research method was chosen because it

permits a detailed analysis of a small number of elements over time (Hsieh & Shannon, 2005).

Sampling

The participants in this study were 62 Bachelors in Education (BEd) pre-service primary school teachers at a South African university. They were purposively selected for the study. They were enrolled in a foundational method course in mathematics as part of the requirement for their qualification. The participants for the interviews were purposively and conveniently sampled to select information-rich cases to answer the research question (Etikan, Musa & Alkassim, 2016).

Ethical Considerations

The University granted us permission to conduct the study. Informed consent was obtained from all the participants to have their scripts analysed, be interviewed, and for the interviews to be audio recorded.

Data Collection

The data for this research were collected from the participants' written solutions to two pattern problem-solving tasks and through semi-structured interviews. The two tasks were part of a formal assessment of the foundation method course. The tasks were intended to probe the students' creative solutions on pattern problem-solving tasks. Two experts in mathematics education validated the written tasks. Four participants (one high achiever, two average achievers, and one lower achiever) were interviewed. The interviews were audio



recorded. The first author conducted and transcribed the interviews word for word while the second author checked the transcriptions. Furthermore, the interviewees were asked to crosscheck the transcriptions of the interviews to ensure the credibility of the data (Korstjens & Moser, 2018).

Data Analysis

An analysis of data entails breaking down the information gathered into elements to obtain responses to the research question (Sauro, 2015). In this research, the data from written tasks were analysed using content analysis (Kondracki, Wellman & Amundson, 2002). The interview data were organised and analysed to get an overview of what was revealed, and the responses were discussed. The analysis was based on Guilford's theory that identified three components of divergent thinking. Firstly, fluency was measured by the number of correct responses obtained by all the participants to the same task; this is a process that Silver (1997) describes as multiple solution tasks. Secondly, flexibility was measured with the number of different solutions that the participants produced. Thirdly, originality was measured by analysing the number of novel responses in the categories identified. In this research, we presented two pattern tasks that required producing various and different responses. Responses derived from each task would determine how creative the participants were. The details of the tasks and the possible responses to the tasks are presented in Table 1 and Figures 1 and 2 respectively.

Tasks

Table 1 Patten problem-solving tasks

<p>Task 1</p> <p>Tinyiko organised a set of objects in her bag, as shown in the diagram below. Show three quickest possible ways of counting them.</p> 
<p>Task 2</p>  <p>a) Draw the next figure b) Write the expression of the nth term</p>

Possible Ways of Counting

The different possible ways of counting the objects

in Task 1 are shown in Figure 1.

$4+4+4+4+4+4+4+4$	$8 \times (2 \times 2)$	$(2 \times 4) \times 4$	$6+6+4+4+6+6$	$2+2+2+2+2+2+2+2+2+2+2+2+2+2+2+2+2+2$

Figure 1 Possible responses to Task 1

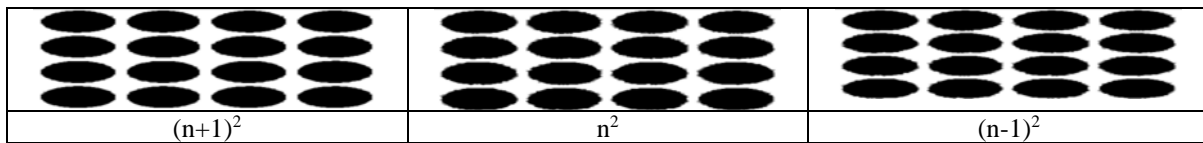


Figure 2 Possible responses to Task 2

Research Results and Discussion

Summary of the Results of the Written Responses

Table 2 presents a summary of the number of ways of counting and the number of participants in each response group.

Table 2 Summary of participants’ responses to Task 1

Quickest number of ways of counting	Correct solutions and responses (fluency)	Correct responses plus varied alternative ways of counting (flexibility)	Correct novel ways of counting different from others (originality)
Three ways of counting	39	18	0
Two ways of counting	3	1	0
One way counting	1	0	0

Table 2 reveals that 39 of the 62 participants provided correct solutions/responses in counting the objects, 18 participants showed correct answers plus a variety of three alternative ways of counting while none of the participants showed original ways of counting. Three participants were able to show only two correct ways of counting, while one participant was flexible in his response, and none used a novel way of counting. Finally, a participant showed only one correct way of counting based on fluency. This is an indication that most of the participants produced the correct solution/answers to the task while few of the participants used different solutions in counting the objects. It is important to note that most students preferred counting in patterns of 2s and 4s. This result reveals that participants were at the fluency and flexibility levels of creativity. These findings are in agreement with Vale et al. (2012) who revealed that fluency and flexibility were statistically significant. However, some of the participants were able to use previous knowledge of counting to enhance their visualisation skills through recognition and reorganisation in the growing pattern problem-solving task. This finding is similar to that of Vale et al. (2012) that pattern tasks promote creativity. However, the finding also supports Vale and Pimental’s (2011) assertion that earlier work on counting tasks in a symbolic setting can enhance creativity.

Table 3 is a summary of the frequency of participants’ correct responses to tasks on the identification of patterns and the general rule that leads to generalisation based on fluency, flexibility, and originality of responses.

Table 3 Summary of participants’ correct responses to Task 2

Responses	Correct solution/response (Fluency)	Correct solution plus diverse alternative responses (Flexibility)	Correct novel responses different from other responses (Originality)
Drawing of next figure	53	9	0
Expression of the nth term	31	4	0

The same analytic approach to the first task was used for analysing participants’ responses to Task 2. All the participants drew the correct pattern of the figure required in task 2; 53 participants were quick in drawing the required pattern, nine participants used a different approach to respond while no participants produced a novel response. However, for the correct expression of the nth term, 31 participants showed a quick response, four participants come up with correct different responses. This is an indication that none of the participants applied deconstructive reasoning (Rivera, 2009). The analysis of Table 3 indicates that half of the participants that were at the creativity level of fluency and flexibility on the drawing of patterns could not express the general rule of the pattern derived.

This finding supports the view of Ubah and Bansilal (2018:860) that “being able to produce the correct answers to questions based on school-level content is just one small part of a mathematics teacher’s task. Beyond that, a teacher should be able to link new content to big ideas in mathematics, to provide unambiguous explanations [of mathematical concepts].”

We suggest that teachers should be trained on how to improve on their originality of ideas that differ from those of other teachers. This observation is in line with Conway (1999) who believes that students should seek varied ideas and original responses to mathematical problems to enhance creativity. The learner who can apply diverse approaches to finding a solution to a task is

the most successful problem solver (Conway, 1999). Based on these observations, we recommend that teacher education programmes need to offer content courses that offer pre-service teachers with prospects of becoming creative thinkers. Future teachers must be trained in a manner that they should implement non-routine mathematical activities that involve reasoning to enhance their learners' creative potential. They need to recognise tasks that promote fluency as well as flexibility and originality which involves a higher-level thinking process.

Results of the Semi-Structured Interviews

The purpose of this was to allow the data from the semi-structured interviews to speak for themselves (Wellington, 2000). The excerpts from the interviews with four participants; Lucky, Shaba, Sam, and James (pseudonyms) are presented here. Excerpts 1 to 3 are from dialogues between the first author (A) and Lucky while excerpts 4 to 6 are from dialogues between the same author and Shaba.

A: *Welcome Lucky. You were asked to show the three quickest possible ways to count the objects shown in Task 1. What first comes to your mind with such a question?*

Lucky: *Counting in multiples.*

A: *The question said to provide three quickest ways, can you provide them?*

Lucky: *Different methods mm, I could count them in 2's in 4's and 8's (illustrates on a paper).*

A: *I realise you are the first to get the Task done, how did you quickly get the solution?*

Lucky: *Yes, first, I observe that the total is 32, then from my knowledge of the times table, I recall the factors of 32. Then seeing the way the objects were arranged in a rectangular shape, I re-arranging them in 2's and 4's and 8's to get the total 32.*

Excerpt 1 Dialogue between A and Lucky on Task 1

Lucky's response to Task 1 reveals that he visualised the arrangement in different ways connecting previous knowledge about number relationships and their connections with basic geometric shapes. Lucky's ability to re-arrange the objects through numerical expressions that translate to his thinking and visualisation was his success. The interview continued, where Lucky was asked about his response to Task 2.

A: *Lucky, observing Task 2, how did you respond to the task?*

Lucky: *Looking at the objects, the given pattern has one nut first, followed by four nuts and then six nuts. That means the pattern is 1, 4, 6, and 'x.' Observing the progression you can see that pattern is derived from squares of 1, 2, 3, and 4, etc. So $1^2 = 1$, $2^2 = 4$, $3^2 = 9$ then $4^2 = 16$. Hence 'x' is equal to 16 nuts. The next figure will have four vertical and horizontal nuts receptively to get 16 nuts (sketched the air with his fingers).*

A: *Any other approach to the solution?*

Lucky: *Yes, looking at the sequence, you can see they are increasing in odd numbers; from the first term to the second you have an increase of 3, from the second term to third you have an increase of 5, from the third term to the fourth term is an increase of 7 so the 'x' remains 16 nuts.*

Excerpt 2 Dialogue between A and Lucky on Task 2a

Excerpt 2 reveals that Lucky identified the pattern in a figurative sequence, described it, and produced an argument to support his claims using different representations. A questioned Lucky further about his creative ability to express the n th term rule.

A: *On the same Task 2, could you express the n th rule?*

Lucky: *From the progression that I derived earlier, that is, 1, 4, 6, 16... and the squares were in an arithmetic form that is 1^2 , 2^2 , 3^2 , 4^2 , ... then the n th rule will be $(n+1)^2$ where n takes the values of 0, 1, 2, 3, ... or $(n)^2$ where n takes the values of 1, 2, 3, 4,....*

A: *Did these pattern problem tasks help you to enhance your creativity?*

Lucky: *Yes, the pattern tasks exposed me to ideas that are intellectually challenging and also transformed my ideas about pattern problems to the reality of using creative ideas in providing solutions.*

Excerpt 3 Dialogue between A and Lucky on Task 2b

Lucky was able to write the numerical expressions translating the way of seeing, to make possible the generalisation to distinct terms.

When the participant (Shaba) who showed only one way of counting the objects was probed

during the interview about his performance in the written task, he replied that he “was blank” and preferred using one method to teach such a task. This assertion was revealed in the interview extract below.

A: How did you count the objects shown in Task 1?
 Shaba: They were 32 objects, so I decided to count them in 2s.
 A: Alright, but since you are counting in multiples, think of other multiple ways of counting the objects? Check the factors of 32?
 Shaba: Ok, mmm, what of 4s?
 A: Yes, and what again?
 Shaba: mm, what of 8s?
 A: Very well, the objects could be counted in 2s, 4s, 8s, and 16s.

Excerpt 4 Dialogue between A and Shaba on Task 1

The author spent ample time leading Shaba to identify other ways of counting the objects apart from counting in 2s. With the author’s guidance, Shaba was able to identify two more ways of counting the objects. Shaba’s response to Task 1 revealed that he was unable to generate a great number of ideas. The author went further to probe his response to Task 2.

A: Observing Task 2, how did you respond to the Task?
 Shaba: I looked at the objects but could not understand what I was required to do.
 A: The first term was given, followed by the second term, then the third, and you are required to draw the fourth term, so what do you draw?
 Shaba: The first term is 1, the second is 4, the third is 9 then the fourth is 16.
 A: How did you get 16 nuts?
 Shaba: The first nut to the second nuts increased by 3, then second nuts to third nuts increased by 5 then third nuts to fourth nuts will increase by 7. Looking at the odd pattern of 1, 3, 5, 7, next is 9....
 A: This is beautiful. Well-done, Shaba.

Excerpt 5 Dialogue between A and Shaba on Task 2

Shaba’s interview extract in Excerpt 5 reveals that through the guidance of the first author, he identified a pattern in an odd sequence, described it, and produced an argument to support his solution to the task. The author probed further on his creative ability to express the nth term of the pattern.

A: Look at the pattern you have created critically, are the nuts increasing or decreasing?
 Shaba: Yes, it is increasing in odd multiples.
 A: Correct, so how do we express it in general terms?
 Lucky: I have no idea, ma’am.
 A: Alright Shaba, tell us, how do these pattern problem tasks help you to develop creativity?
 Shaba: This interview has transformed my ideas on how to solve pattern problem-based tasks into reality, am grateful ma’am.

Excerpt 6 Dialogue between A and Shaba on Task 2

With guidance from A, Shaba identified the growing sequence of the pattern but could not express the general term of the sequence.

In the dialogue between A and another participant, Sam, the latter stated that he was able to count the objects in Task 1 and drew the next figure as requested in Task 2, but he was unable to state the correct expression of the nth term. With guidance from A, Sam made several fruitless attempts to get the correct expression of the nth term. Another interview with James was a replica of Shaba’s, thus it can be said that the data had attained saturation point (O’Reilly & Parker, 2013). Hence, we were able to conclude from the interviews that most pre-service teachers could not express the general form of the patterns drawn. This submission concurs with Guest, Bunce and Johnson (2006) who note that data saturation can be achieved with a low sample contingent on the proposed sample. Generally, we identified that pattern tasks are intellectually challenging, allow different approaches in solving the tasks, and hence enhance creativity – an indication that pre-service primary mathematics teachers should be exposed to challenging pattern problem-solving tasks which can improve their level of creativity for their future teaching career.

Conclusion and Recommendation

This exploratory research concentrated on the written responses of 62 pre-service teachers to tasks based on the drawing and nth term of patterns. The results show that although 35 participants were able to draw patterns and express patterns in nth form, 27 failed to do so. Furthermore, the results show that out of the three known components of creativity, two of them, fluency and flexibility, were mostly identified in the drawing of patterns than in the expression of a general rule. The major limitation that we encountered was how to measure creativity.

However, we opted to follow the methods of other researchers (Conway, 1999; Silver, 1997) that did not assign a percentage score to each participant, but rather created a group analysis. This suggestion necessitated the need to measure the creativity of the participants through the three components mentioned above.

It was found that most of the participants could not correctly state the general rule of the identified patterns. The findings of this study raise a concern about the need for teacher education programmes to improve pre-service primary school teachers' knowledge of the mathematical concepts that the prospective teachers would teach after their pre-service programmes. This concern seems to be justified in light of the observation by Ubah and Bansilal (2018:861) that "most university programmes focus on developing knowledge of advanced mathematics, ... [having] the assumption that pre-service teachers have developed an understanding of the school mathematics content they need."

However, we could not justify this assumption in this research, hence there is an urgent need for the improvement of prospective teachers' creativity and mathematical knowledge for teaching primary mathematics. The major contribution of this research is that it provided empirical evidence that teachers should implement non-routine tasks that involve reasoning and seek out new and novel ideas to stimulate their learners' creativity. They should provide an enabling problem-solving environment that stimulates creativity and improves the mathematical competence of their learners. From this research we recommended that pre-service primary school teachers should be exposed to diverse academic activities for the development of their qualities and abilities that constitute creativity as part of their training programmes.

Authors' Contribution

The first author conceptualised the study, collected and analysed the data. Both authors wrote the manuscript and reviewed the final manuscript.

Notes

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