

# STRATIFICATION MITIGATION IN THE UPPER TANK OF A NATURAL CIRCULATION LOOP SIMULATING PASSIVE DECAY HEAT REMOVAL IN A POOL TYPE REACTOR

Spaccapaniccia C.\* , Planquart P. and Buchlin J.M.

\*Author for correspondence

Von Karman Institute for Fluid Dynamics,,

Rhode Saint Genese, 1640,

Belgium,

## ABSTRACT

The Belgian nuclear research institute (SCK•CEN) is developing MYRRHA. MYRRHA is a flexible fast spectrum research reactor, conceived as an accelerator driven system (ADS). The configuration of the primary loop is pool-type: the primary coolant and all the primary system components (core and heat exchangers) are contained within the reactor vessel, while the secondary fluid is circulating in the heat exchangers. The primary coolant is Lead Bismuth Eutectic (LBE). After the reactor shut down, in the unlucky event of propeller failures, the primary and secondary loops should be able to remove the decay heat in passive way (Natural Convection). The present study analyses the flow and the temperature distribution in the upper plenum by applying laser imaging techniques in a laboratory scaled water model. A parametric study is proposed to study stratification mitigation strategies by varying the geometry of the buffer tank simulating the upper plenum.

## INTRODUCTION

In a Natural Circulation Loop (NCL) the flow is driven by Archimedes' force and transports heat from a heat source to a heat sink without the aid of mechanical moving parts. Thanks to this, NCLs find applications in many industrial and domestic fields: nuclear reactors core cooling, solar heaters, electronic components cooling, house heaters, etc..

In industrial or domestic heat transport systems, the fluid circulates through hydraulic elements for which pressure drops may be relevant: in these fields a *thermosyphon* loop is most often encountered. A *thermosyphon* loop is a particular case of NCL in which the heat sink is placed at higher level with respect to the heater's thermal centre.

The object of this analysis is the experimental, pool type reactor MYRRHA conceived by the nuclear research institute SCK•CEN. In the pool type reactor, all the thermo-hydraulic elements of the primary loop are submerged in the primary coolant. Figure 1-a sketches the main elements of the primary loop: 1-core, 2-barrar, 3-upper plenum 4-heat exchanger, 5-propellers, 6-lower plenum. The barrel is a perforated cylinder

containing the upper core structure (instrumentation and safety bars).

## NOMENCLATURE

|                 |                       |                                    |
|-----------------|-----------------------|------------------------------------|
| $x$             | [m]                   | Cartesian axis direction           |
| $y$             | [m]                   | Cartesian axis direction           |
| $r$             | [m]                   | radius                             |
| $H$             | [m]                   | Thermal conductivity               |
| $L$             | [m]                   | Volumetric heat generation density |
| $T_h$           | [K]                   | Interfacial thermal resistance     |
| $T_c$           | [K]                   | Temperature                        |
| $p$             | [kg/ms <sup>2</sup> ] | pressure                           |
| $\Delta P_{ch}$ | [kg/ms <sup>2</sup> ] | Characteristic pressure drops      |
| $u$             | [m]                   | Radial velocity                    |
| $v$             | [m/s]                 | Axial velocity                     |
| $V_{ch}$        | [m/s]                 | Characteristic Velocity            |
| $\beta$         | [1/K]                 | Volumetric expansion coefficient   |
| $\alpha$        | [m <sup>2</sup> /s]   | Thermal diffusivity                |
| $g$             | [m/s <sup>2</sup> ]   | Gravity                            |
| $\rho$          | [kg/ m <sup>3</sup> ] | density                            |
| $\nu$           | [m <sup>2</sup> /s]   | Kinematic viscosity                |
| $m_{loop}$      | [kg/ s]               | Loop mass flow                     |
| $\Theta$        | [-]                   | $(T - T_c) / (T_h - T_c)$          |

### Non Dimensional Numbers

|           |     |                                 |
|-----------|-----|---------------------------------|
| $G_{nr}$  | [-] | NCL Grashof number              |
| $G_{r,M}$ | [-] | Reactor Grashof number          |
| $Pr$      | [-] | Prandtl number                  |
| $A_R$     | [-] | Aspect ratio                    |
| $Eu$      | [-] | Euler number for pressure drops |
| $S$       | [-] | Stratification number           |

### Abbreviations

|            |                            |
|------------|----------------------------|
| <i>LBE</i> | Eutectic Lead Bismuth      |
| <i>NCL</i> | Natural Convection Loop    |
| <i>PIV</i> | Particle Image Velocimetry |
| <i>LIF</i> | Laser Induced Fluorescence |
| <i>TCS</i> | Thermocouples              |
| <i>HE</i>  | Heat Exchangers            |

After a shut down event, the core continues to produce heat by spontaneous decay of radioisotopes. The decay heat is equal to 10% of the nominal power. In the unlucky event of propellers failure, the decay heat should be removed passively by Natural Convection. Thus, the primary loop of the nuclear reactor MYRRHA operating in passive heat removal conditions can be considered an analogous NCL. The NCL under analysis

is a closed, turbulent, single phase *thermosyphon* where the flow is generated by buoyancy forces. Figure 1-b extrapolates and schematizes the NCL starting from a symmetry axis of the pool type reactor. The distance in vertical (y) and horizontal (x) direction between the heating and cooling elements are indicated respectively as H and L. The sketch considers the presence of the upper plenum acting like a buffer tank interposed between core and heat Exchangers (HE).

Few studies exist on NCL provided with a buffer tank. Furthermore, literature concerning this kind of systems usually involves NCLs with constant diameter where the tank's effect is limited to heat storage (Misra et al. [1]) or temperature and flow stabilization (Naveen et al. [2], Misale et al. [3]). It is therefore important to analyze the flow behaviour and temperature distribution inside the buffer tank of the NCL outlined in Figure 1-b.

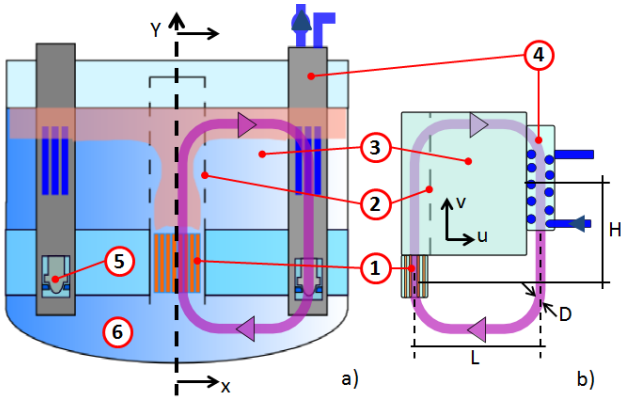


Figure 1 a) main thermal hydraulic elements in the pool type reactor: 1- core, 2-barrel, 3-upper tank, 4- heat exchangers, 5-pumps, 6- lower plenum, b) Simplified NCL system considered for the analysis

In particular, given the buoyancy dominated nature of the flow, thermal stratification is expected to occur in the buffer tank. Stratification and pressure drops in the primary loop are expected to contribute negatively to the NC flow.

The objective of the study was therefore to verify the influence of the geometry of the loop and of the upper vessel on the mass flow. The methodology chosen to address the problem is a parametric study carried out in a 1:8 scaled water model (Aquarium II) of the of the NCL of Figure 1-b. The study consisted in the simultaneous measurement of mass flow, velocity field and temperature field in different buffer tank configurations, using Thermocouples (TCs) and optical imaging techniques such as PIV (Particles Image Velocimetry) and LIF (Laser Induced Fluorescence).

## SCALING AND FACILITY DESCRIPTION

In passive heat removal conditions, a mass flow is established as a consequence of a balance between frictional pressure losses of the hydraulic loop and Archimedes forces induced by the heating and cooling power (Welander [4]). The pressure head generated can be defined as (Todreas [5]):

$$\Delta P_B = \beta \rho (T_h - T_c) g H \quad (4)$$

If the pool geometry is approximated as axial symmetric, the dominating components of velocity are v (vertical) and u (radial) (Figure 1-b). The fluid is incompressible. Under these assumptions and under the hypothesis of equal heat provided and removed, the equations of transport of momentum and energy describing the NCL under analysis are:

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho_0} \frac{\partial p_x}{\partial x} + \nu \frac{\partial^2 u}{\partial x^2} + \nu \frac{\partial^2 u}{\partial y^2} \quad (1)$$

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho_0} \frac{\partial p_y}{\partial y} + \nu \frac{\partial^2 v}{\partial x^2} + \nu \frac{\partial^2 v}{\partial y^2} - g \beta (T_h - T_c) \quad (2)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \frac{\partial^2 v}{\partial x^2} + \alpha \frac{\partial^2 v}{\partial y^2} \quad (3)$$

The following step towards the system scaling is the normalisation of the transport equations. The characteristic lengths chosen for the normalisation of x and y are the quantities H and L as indicated in Figure 1-b.  $T_h$  and  $T_c$  are the hottest and coldest temperature achieved in the NCL (usually at core and HE's exit). The characteristic pressure chosen is the overall pressure drop (friction and local losses) in the hydraulic loop  $\Delta P_{ch}$ , therefore:

$$U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} = -\frac{1}{\rho_0} \frac{\Delta P_{ch}}{V_{ch}^2} \frac{\partial P_y}{\partial Y} + \frac{\nu}{V_{ch} H} \left( \frac{H^2}{L^2} \frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2} \right) - \frac{Hg \beta (T_h - T_c)}{V_{ch}^2} \theta \quad (4)$$

Since in the NCL the buoyant pressure head should balance the pressure drops (Todreas [5]) the expression for the characteristic velocity  $V_{ch}$  can be determined by balancing the pressure term with the buoyant term of Equation 4:

$$\frac{Hg \beta (T_h - T_c)}{V_{ch}^2} = -\frac{1}{\rho_0} \frac{\Delta P_{ch}}{V_{ch}^2} = Eu \Rightarrow V_{ch} = \sqrt{\frac{Hg \beta (T_h - T_c)}{Eu}} \quad (5)$$

where Eu is the Euler number for pressure drops.

In the NCL, flow rate, pressure drops and buoyancy forces are not independent quantities, thus it is not possible to know a priori  $V_{ch}$  and  $\Delta P_{ch}$ .

In the rigorous non-dimensional analysis, in order to escape this problem, the characteristic velocity  $V_{ch}$  (or the characteristic pressure drops  $\Delta P_{ch}$ ) is chosen in order to obtain  $Eu=1$ . For the present case  $Eu=1$  implies  $V_{ch}=(Hg\beta\Delta T)^{0.5}$ .

Replacing the latter expression of  $V_{ch}$  in the normalized equations of momentum and energy we obtain the following non-dimensional equations for the steady state:

$$U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} + \sqrt{\frac{1}{Gr_H}} \left( A_R^2 \frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2} \right) \quad (6)$$

$$U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} = -\frac{\partial P}{\partial Y} + \sqrt{\frac{1}{Gr_H}} \left( A_R^2 \frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2} \right) + \theta \quad (7)$$

$$U \frac{\partial \theta}{\partial X} + V \frac{\partial \theta}{\partial Y} = \sqrt{\frac{1}{Pr \cdot Gr_H}} \left( A_R^2 \frac{\partial^2 \theta}{\partial X^2} + \frac{\partial^2 \theta}{\partial Y^2} \right) \quad (8)$$

where the appearing dimensionless groups are:

$$ND_1 = A_R^2 Gr_H^{-0.5}, \quad ND_2 = A_R^2 (Pr \cdot Gr_H)^{-0.5} \quad (9)$$

Respecting the similarity of both the groups ND1 and ND2 is possible only if the Pr number of the fluids is the same. However this is not feasible when studying a LBE flow with a water facility. The scaling was thus performed trying to respect the  $Gr_H$  number and the geometry as much as possible.

The geometry of a nuclear reactor's primary loop is very complex, especially the reactor's core, and it is unfeasible to reproduce every geometrical detail with a scaled model. However the geometry of the upper plenum can be reproduced accurately. The exact matching of the Grashof number is also unfeasible with a low power water model. However  $Gr_H$  can be relaxed until the flow is in the correct regime (turbulent natural convection for  $Gr_H > 10^9$ ).

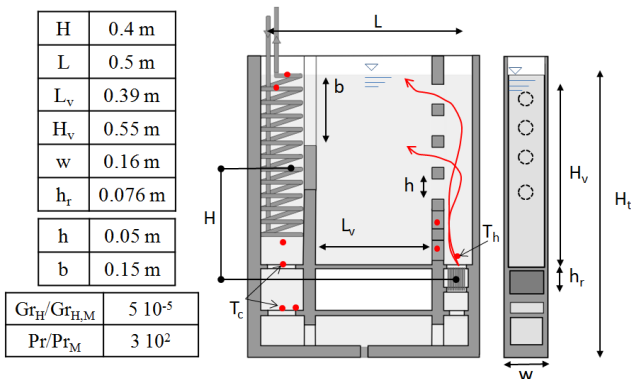


Figure 2: sketch of Aquarium II, the table specifies the characteristic dimensions of the facility and the values of the non dimensional numbers achieved

The resulting model (called AquariumII) and its main dimensions are shown in Figure 2. AquariumII is a 1:8, 2D slab model of the MYRRHA's NCL. The facility is approximately one meter high and 0.8 m wide. The flow circulates in the anticlockwise direction. The main elements of the system are:

- Heater: series of flat electrical resistances (maximum total power =3 kW).
- Barrel Plate: an interchangeable perforated plate with circular holes.
- Buffer Plate: a plate with adjustable height to simulate the Heat Exchangers entrance level.
- Heat Exchanger: a copper spiral in which water cooled by an external refrigerating system is circulating.

The peculiarity of the model is that, differently from the existing water models, the position and the characteristics of each one of these elements can be changed to carry out a parametric study.

The cold leg is accessible through a front window, in order to insert pressure drops elements, in case of necessity.

The buffer tank is provided with four optical accesses (top, bottom, front and side) composed of glass windows.

## EXPERIMENTAL SET UP AND METHOD

Figure 3 shows the reference configuration of Aquarium II and the instrumentation arrangement. The TCs are indicated with red dots.

Water is seeded with a proper concentration of Rhodamine B and with fluorescent tracing particles, for temperature and velocity measurements. An Argon-Ion Laser produces a continuous beam picked at 515 nm. The beam power selected is 2.1 W and it is kept constant during the measurements by the Laser remote control. Since it is necessary to measure the full tank test section (55x39 cm), a rotating mirror was used to scan the test section with the continuous laser beam.

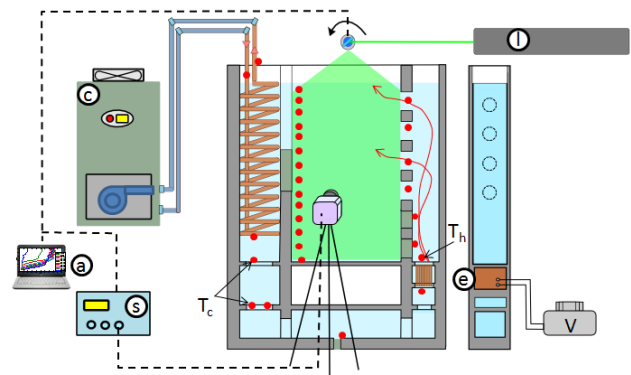


Figure 3 Experimental set up: a) data acquisition system, s) synchronizer, c) chiller, l) Argon-Ion Laser, e) electrical resistances connected to V-voltage generator.  $T_c$  and  $T_h$ : coldest and hottest loop temperature respectively

The laser beam scans a section of the plenum, while the rolling shutter CCD camera, provided with a high pass filter of 550 nm, detects the fluorescent signal for temperature measurements and the fluorescent light emitted by the particles. Each image acquisition occurs when the disk rotating together with the mirror completes a revolution: an opening in the disk activates a sensor that sends a signal to the synchronizer, which activates the camera, triggering the recording of one exposure.

The image acquisition frequency is limited by the rotating mirror speed (41 Hz). The signal triggering the acquisition of the first image also activates the TCs acquisition, which records temperature values simultaneously to the image acquisition but with an independent and higher frequency (70 Hz).

The Rhodamine B concentration used for the LIF experiments is 1.6 mg/litre. The PIV tracers seeding the water are fluorescent polyethylene microspheres of the size of 40  $\mu\text{m}$  with spectrum emission similar to the one of Rhodamine B: in this way a single image will contain information on both temperature (RhB signal) and velocity (particles signal). The concentration of particles is 0.025 g/litre.

Figure 4 shows the acquisition time line of the simultaneous temperature and velocity measurements performed. Before the beginning of the test, a reference temperature is recorded by means of TCs and a set of reference images is recorded by the CCD camera.

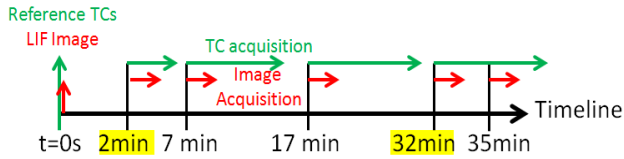


Figure 4 Data acquisition time line.

The TCs measurement covers all the duration of the experiments and it is divided in 5 different recordings. Every image set includes 2400 frames, covering approximately one minute of experiment. In all the tests performed the heat exchanger and the electrical resistances are switched on simultaneously at one minute after the beginning of the experiment.

### Configurations tested

Figure 5 shows the configurations chosen to carry out the parametric study. Configuration 1 was obtained by increasing the free area of the barrel plate through opening all the passages available. Configuration 2 was obtained by shifting the heat exchanger entrance towards the bottom of 15 cm. Configuration 3 was obtained by reducing the area above the heater through the immersion of a triangular full shape.

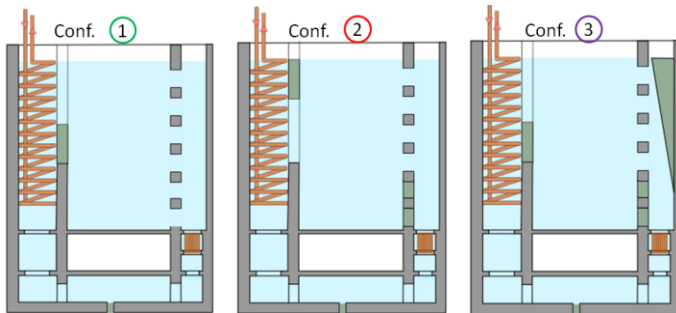


Figure 5: geometry configurations analysed: Conf.1) increased barrel free area, Conf.2) lower HE entrance Conf.3) barrel free area reduction

### PROCESSING OF RESULTS

One camera imaging techniques require a pre-processing of the images in order to separate the signals of the particles and the signal of the background.

Westerweel et al. [6] and Adrian and Westerweel [7] analysed the histogram of a synthetic PIV image. Westerweel et al. found out the background part of a PIV image can be fit by a normal distribution, while Adrian and Westerweel showed that an exponential approximation can be applied to the particles signal, when the background noise is characterized by lower intensity with respect to the particle signal. The intensity levels of an excited solution of water and RhB with a low concentration of dye are lower than the intensity levels of a fluorescent particle which contains the same dye, thanks to the light enhancement due to the Mie scattering. Therefore the threshold separating particles and temperature signal can be found on the image histogram, by approximating it with a Gaussian and an exponential distribution (Figure 6).

The approximation is done iteratively using a guess threshold point, until the point of best fitting is found. The result of the procedure is displayed in the images at the top right of the graph of Figure 6, which shows the image before and after the threshold, where the particle signal is successfully removed.

One of the major problems for a LIF image quality is the appearance of striations forming because of gradient of refractive index. Existing literature (Grafströmming et al. [8], Coolen et al. [9]) suggests to remove geometrical elements like shadow lines by a convolution of the two dimensional Fourier transform of the image with a proper filter.

Once the LIF images are normalized and corrected, a calibration must be used to convert the LIF signal into temperature values. For cases of large facilities like Aquarium II, achieving a uniform temperature in every point of the test section is possible only when the water is at ambient temperature. The calibration is therefore performed by associating the value of normalised intensity measured in small image windows placed nearby the TCs with the temperature measured by the corresponding TC. Figure 7 shows a calibration curve retrieved for five image acquisitions (corresponding to one experiment).

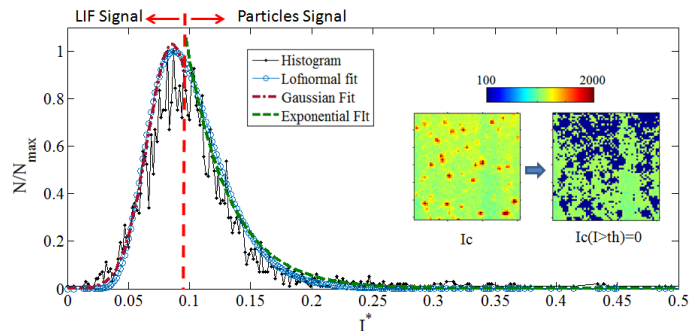


Figure 6 Threshold searching on a PIV-LIF image histogram

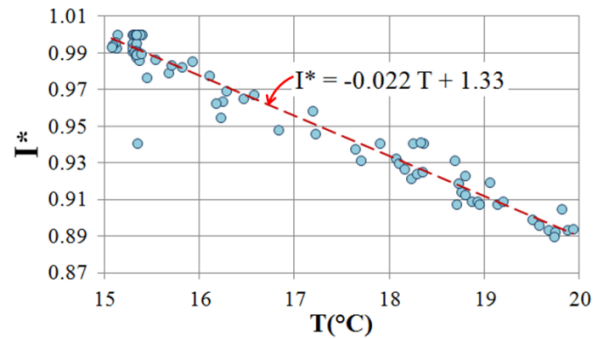


Figure 7 LIF signal-TC signal correlation curve used for calibration

Finally, the parameters of interest allowing to characterize the performance of the loop are loop mass flow and stratification number  $S$ . The loop mass flow was calculated through integration of the velocity profiles measured with PIV at every aperture of the barrel.

$$\dot{m}_{loop} = 2\pi\rho \sum_{i=1}^N \int_0^{h/2} ru(r) dr \quad (10)$$



where  $N$  is the number of barrel holes. The stratification number  $S$  was derived for one line of TCs using the definition of Gandhi et al. [10] (Equation 11).

$$S = \frac{1}{J-1} \sum_{j=1}^{J-1} \frac{T_{j+1} - T_j}{dy} \frac{(J-1)dy}{T_{max} - T_{min}} \quad (11)$$

where  $J$  is the total number of thermocouples,  $T_{max}$  is the maximum temperature measured at the barrel and  $T_{min}$  is the buffer tank lowest temperature.

**RESULTS**

Nevertheless the measurements involved a full transient of the NCL, the velocity and temperature results discussed and compared are the ones obtained at the end of each experiment.

Figure 8 shows Velocity and Temperature fields obtained for the reference configuration at 32 minutes after the beginning of the experiment. We can observe horizontal plumes outgoing from the barrel and forming a central vortex. Smaller scale vortices develops at the boundary layers of the lowest horizontal plumes, as a result of Kelvin-Helmholtz instability occurring at the shear layer between two streams possessing different values of velocity. A colder mass flow re-entering the tank from the heat exchanger is detected by both PIV measurements (Figure 8) and TCs measurements (Figure 10). In this case, the measurements show that the presence of a buffer tank between heater and HE leads to the development of two mass flows: part of the flow completes the loop, passing through HE and heater, another part bypass the main loop and circulates back into the tank.

Both The temperature profile measured with the TC array and the LIF data (Figure 8) show very well the separation between the upper mixing region and the bottom, cold and almost motionless region.

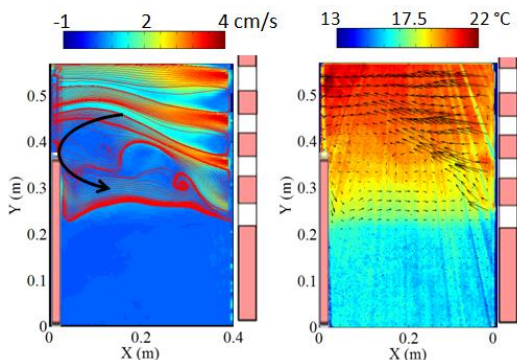


Figure 8 Reference Conf., 32 min after beginning of the test. left-velocity magnitude and streamlines, right-temperature and vector field.

**Effects of increased barrel porosity, Configuration 1**

In Configuration 1 the flow is recalled and en-trained in the plume from the bottommost barrel apertures (Figure 9). The hot flow outgoing from the top of the barrel crosses the tank until the bottom, carrying with him the heat of the warm fluid, and

re-enter partially the plume region. The recirculation involve in this case almost all the tank, improving the thermal mixing, and leads to a more uniform temperature profiles (Figure 10, first graph).

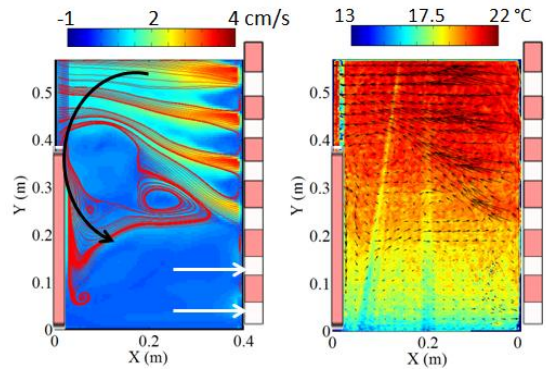


Figure 9 Configuration 1, 32 min after beginning of the test. left-velocity magnitude and streamlines, right-temperature and vector field.

Configuration 1 shows higher values of loop mass flow with respect to other configurations tested (Figure 13), indicating better performances. This is due to the communication between the upper heater warm region and the cold bottom tank region, which yield a stack effect: the difference in temperature between the tank fluid and the fluid above the heater causes a difference of pressure which contributes positively to the mass flow.

**Effects of HE window position, Conf.2**

The measurements performed in the reference configuration and Conf. 2 show that position and shape of the central vortex developing in the buffer tank is strongly influenced by the position of the heat exchanger entrance. The effects of moving the heat exchanger entrance downwards are mostly negative: temperatures achieve higher values in the topmost part of the tank (Figure 10-b). This is due to the increased blockage effect caused by the presence of an obstacle between the upper tank and the heat exchangers. On the other hand, the border between motionless region and the mixing region moves towards the bottom increasing the height of the mixing zone (Figure 11-left) with respect to the reference configuration (Figure 8).

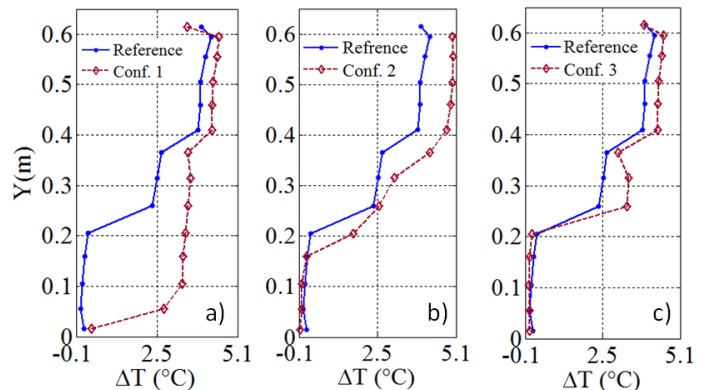


Figure 10 Increase of temperature from the initial, ambient value for the different configurations.

**Effects of blockage in the barrel, Conf.3**

Figure 11-right shows the velocity magnitude field obtained when reducing progressively the barrel free area at 32 minutes after the beginning of the tests. Comparing the field of Figure 11-right with the velocity field of Figure 8, it can be observed that the size of the plume exiting the topmost hole is reduced when the plume passage area in the barrel region is reduced, due to the higher resistance encountered by the hot flow in the barrel region. At the same time, the flow outgoing from the bottommost hole becomes more important. In the reference configuration, the plume outgoing from the bottommost hole merges immediately after the barrel with the buoyant plumes above, while when the passage area is reduced (Configuration 3) this plume in particular assume a horizontal direction and spread further in the tank.

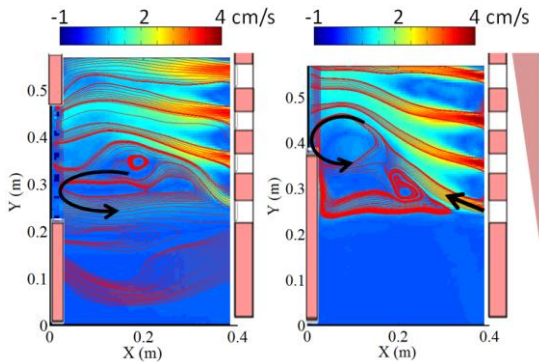


Figure 11 Conf. 2 (left) and Conf. 3 (right) velocity fields and streamlines, 32 min after beginning of the test

Figure 12 shows the velocity profiles measured at the barrel exit for different moments of the experiment for the Reference geometry and Configuration 3. The effect of redistribution of the mass flow in between the holes is clearly visible in the profiles.

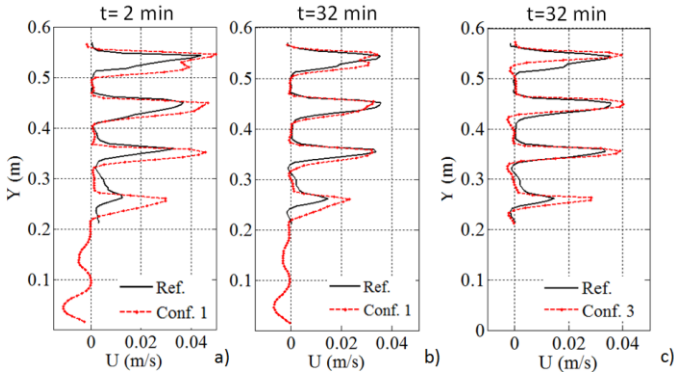


Figure 12 Velocity profiles measured at the barrel exit for Conf.1 (a and b) and Conf. 3 (c) in comparison with the reference configuration

**Summary**

The experimental results obtained for the different configurations tested are summarized in Figure 13 in terms of loop mass flow and stratification number. It can be observed that the highest mass flow is achieved for Configuration 1.

Configuration 1 is also the only case tested in which the mass flow doesn't decrease with the time. The lowest mass flow is obtained for Configuration 3, due to the additional flow resistance introduced by decreasing the barrel area. At the end of the transient, Configuration 1 shows the lowest value of stratification number, as expected from the more uniform temperature profiles illustrated in Figure 10.

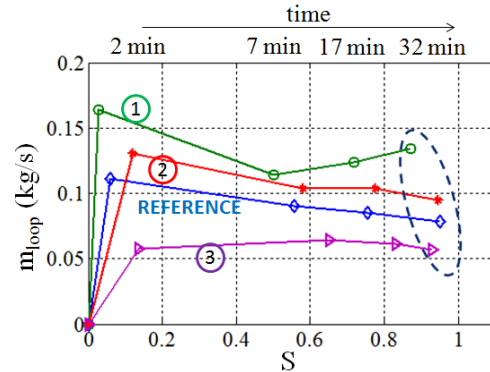


Figure 13 Loop mass flow measured for different configurations along the experiments with S. The dashed circle indicates the values of S achieved

**CONCLUSIONS**

Velocity and temperature measurements with innovative one-camera optical techniques were carried out in the buffer tank of a water NCL simulating passive decay heat removal in a liquid metal pool type reactor. It was observed that the loop mass flow partly completes the loop and partly circulates back in the buffer tank, bypassing the loop.

A parametric study was carried out in order to understand the effect of the buffer tank geometry on the stratification. It was observed that the geometry of the plenum effects the temperature gradients and the value of  $m_{loop}$ .

The lowest values of S and the highest values of  $m_{loop}$  were obtained with Configuration 1. This configuration allows the communication between cold upper plenum and hot barrel duct, yielding to a stack effect. The difference of temperature between these two regions causes a pressure difference which contributes positively to the mass flow. Furthermore, the communication between plenum and barrel duct allows the entrainment of flow in the plume developing right above the heater, reducing the stagnation in the plenum and increasing the mixing. As a result, the plenum temperature profile is more uniform with respect to the reference configuration.

As observed thanks to the measurements carried out in Configuration 3, the progressive reduction of the barrel cross sectional area allows to distribute more uniformly the  $m_{loop}$  between the barrel apertures without affecting sensibly the temperature distribution in the tank.

The flow fields measured in Configuration 2 show that size and position of the convection cell developing at the HE entrance is affected by the heat exchanger window's height and location.

The measurements will serve as a base for validating CFD simulations of the NCL. The simulations will allow more

extensive parametric studies, leading to the optimisation of barrel bottom apertures' size and HE window position.

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